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A Bayesian inversion estimate of N₂O emissions for western and central Europe and the assessment of aggregation errors

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A Bayesian inversion approach was used to retrieve temporally and spatially resolved N_2O fluxes for western and central Europe using in-situ atmospheric observations from the tall tower site at Ochsenkopf, Germany (50°01′ N, 11°48′ E). For atmospheric transport, the STILT (Stochastic Time-Inverted Lagrangian Transport) model was employed, which was driven with ECMWF analysis and short term forecast fields. The influence of temporal aggregation error, as well as the choice of spatial and temporal correlation scale length, on the retrieval was investigated using a synthetic dataset consisting of mixing ratios generated for the Ochsenkopf site. We found that if the aggregation error is ignored, then a significant bias error in the retrieved fluxes ensues. However, by estimating this error and projecting it into the observation space, it was possible to avoid bias errors in the retrieved fluxes. Using the real observations from the Ochsenkopf site, N_2O fluxes were retrieved every 7 days for 2007 at 2 by 2 degrees spatial resolution. Emissions of N_2O were strongest during the summer and autumn months, with peak emissions in August and September, while the regions of Benelux and northern United Kingdom had the strongest annual mean emissions.

1 Introduction

The nitrous oxide (N_2O) mixing ratio has been increasing in the atmosphere since the industrial revolution, from 270 ppb in 1750 (Ramaswamy, 2001) to 319 ppb in 2005 (Forster et al., 2007) with a steady growth rate of around 0.26% since the early 1980's. The increase in N_2O is worrisome for two main reasons. First, it is a greenhouse gas; this means that its atmospheric increase translates to an enhancement in radiative forcing of $0.16 \pm 0.02 \, \text{Wm}^{-2}$ (Ramaswamy, 2001) making it currently the fourth most important long-lived greenhouse gas and is predicted to soon overtake CFC's to become the third most important (Forster et al., 2007). Second, it plays an important role in stratospheric ozone destruction (Crutzen, 1974; Nevison and Holland, 1997) and in

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the 21st century is the main ozone-depleting substance and is slowing the recovery of the ozone hole (Ravishankara et al., 2009).

Human activities are the primary cause of the atmospheric N_2O increase. The largest anthropogenic source of N_2O is from the use of N-fertilizers in agriculture (Olivier et al., 1998), which greatly enhances soil N_2O emissions via microbial nitrification and denitrification pathways (e.g. Bremner, 1997). Other important anthropogenic sources of N_2O are fossil fuel combustion and industrial processes, such as adipic and nitric acid production (Olivier et al., 1998). There are also important natural sources of N_2O , the largest of which is from soils under natural vegetation, but the open ocean, coastal upwelling regions, continental shelves, and estuaries are significant sources too (Kroeze et al., 2005; Nevison et al., 2004). Moreover, it is important to note, that as anthropogenic N permeates the nitrogen cycle, the natural emissions of N_2O are also being perturbed (Galloway et al., 2008; Gruber and Galloway, 2008).

There have been few previous top-down estimates of N_2O fluxes using atmospheric observations. On a regional scale, there have been a small number of N_2O emission estimates based on concurrent measurements of N_2O and Radon, where Radon is used to determine the dilution of N_2O emissions in the atmosphere, such as Messager et al. (2008), Biraud et al. (2002) and Schmidt et al. (2001), and one estimate based on an inversion of atmospheric N_2O observations (Manning et al., 2003). Another modelling study by Kort et al. (2008) evaluated emission inventories by comparison of simulated tracer distributions using an atmospheric transport model with aircraft based measurements of N_2O in North America and inferred a scaling of fluxes that was not spatially or temporally resolved. On the global scale, the only inversion estimates are those of Huang et al. (2008), Hirsch et al. (2006) and Prinn et al. (1990) and these have been at low resolution. The shortage of top-down estimates is partly due to the relative scarcity of data but also to problems in the calibration scales used for N_2O measurements by different laboratories, which has made comparisons between stations difficult.

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There have been several recent initiatives that will improve the availability of data as well as make measurements between stations more comparable. In Europe, for example, the establishment of a new network of tall towers under the framework of the CHIOTTO project (Continuous HIgh-precisiOn Tall Tower Observations of greenhouse gases) provides in-situ measurements of N_2O from 7 stations across Europe. Furthermore, these stations participate in regular inter-comparisons, ensuring a uniform scale. These in-situ measurements provide N_2O observations at approximately hourly frequencies making it possible to resolve short-term variability in the atmosphere. The question, however, is how to best incorporate high-resolution measurements into an inversion scheme.

In an ideal inversion, there would be multiple observations of each state variable, in our case the fluxes, at each resolved time-step. In reality, though, a significant portion of the state variables may be undetected by the observations, owing to the fact that there can only ever be a discrete number of measurement sites and the signal observed at these is dependent on the atmospheric circulation. Furthermore, one must make assumptions about the variability of the true fluxes on time-scales shorter than that of the resolved fluxes. To minimise the interval over which these assumptions are made, one can define a higher temporal resolution for the fluxes but there is a trade-off between increasing the temporal resolution and the number of observations available to constrain the fluxes at each time-step. A similar problem occurs when defining the spatial resolution as one assumes that the fluxes within the resolved area are not significantly different from the mean of the area. Errors resulting when such assumptions are invalid are defined as aggregation errors (Kaminski et al., 2001; Peylin et al., 1999).

In some cases the temporal variability of fluxes over certain time intervals can be described and used in the inversion. For example, for CO_2 fluxes, the behaviour on diurnal time-scales can be described and thus the variability on time intervals of less than 1 day do not need to be explicitly solved in the inversion as long as it taken into account (Peylin et al., 2005). However, in the case of N_2O there is no regular pattern to the short-term flux variability, hence the approach used to account for short-term

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variability in CO_2 fluxes is not applicable. Thus the problem remains; on one hand, if high temporal resolution is used, then there are fewer observations available to constrain the fluxes and there are computational limits on how much the resolution may be increased. On the other hand, if lower temporal resolution is used, and if the real short-term variability of the fluxes and their influence on the observations is not accounted for, then a significant risk of temporal aggregation error ensues.

In this paper, we first investigate how high-frequency observations may best be utilized for retrieving N₂O fluxes and how sensitive the inversion is to temporal aggregation errors. This is investigated using synthetic fluxes and mixing ratios but with atmospheric transport determined from meteorological reanalysis data. Secondly, we investigate the potential to use in-situ measurements from the observation site, Ochsenkopf in Germany (50.03° N, 11.81° E), to constrain N₂O emissions and present new estimates. The tall tower observatory is located on the summit of the mountain, Ochsenkopf, in the Fichtelgebirge range, at an elevation of 1022 m. The Fichtelgebirge region is extensively forested and has a low population density (for further details about the site refer to Thompson et al., 2009). It has been shown that air sampled from the highest level on the tower (163 magl), represents the well mixed boundary layer and has a footprint extending over a large part of western and central Europe (Thompson et al., 2009).

The paper is structured as follows. In Sect. 2, we describe the measurements, the atmospheric transport model, STILT, used to describe the relationship between the observations and the fluxes, and provide details on the Bayesian inversion scheme used. The synthetic data, which are used to test the temporal aggregation error, are also described in this section. Section 3.1 covers the results of various tests for the influence of temporal resolution, observational data frequency, and the impact that changes to the prior flux error covariance matrix have on the retrieved fluxes. Finally, in Sect. 3.2, the results of the inversion using the real Ochsenkopf observations are presented and discussed.

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2.1 Measurements

Ochsenkopf has a continuous record of N_2O since mid-2006. N_2O is measured using a Gas Chromatograph (GC), Agilent 6890, equipped with an electron capture detector. The method was largely developed by Worthy et al. (2003) with further improvements by Popa (2008) (details specific to the Ochsenkopf GC set-up can be found in Thompson et al., 2009). Air measurements are made every 16 min and are interspersed with reference measurements. The long-term precision is 0.18 ppb (this is the mean over 2.5 years of the standard deviation of 3 consecutive measurements of a gas standard that is measured daily) and the accuracy is 0.5 ppb. Air is sampled from 3 heights on the tall tower, 23, 90 and 163 m, which are measured on a 3-hourly cycle (note that for the inversion in this paper, we use only the data from the 163 m level).

2.2 Atmospheric transport model

The STILT (Stochastic Time-Inverted Lagrangian Transport) model is used to simulate the transport of air parcels backwards in time from a receptor point, in this case the tall tower, Ochsenkopf (50°01′ N, 11°48′ E). STILT calculates back trajectories from the receptor using wind fields while releasing ensembles of particles, which represent the air parcel. Analysed wind fields are interpolated to the location of each particle and the particles themselves are subject to stochastic perturbations that are parameterised to represent the effects of turbulent transport. The density of particles is used to calculate the surface influence and the footprint (Lin et al., 2003, 2004). This means that in the backward-time run, emissions upstream of the receptor with more particles have a greater contribution to changes in the mixing ratio at the receptor. STILT has already been implemented in a number of regional-scale trace gas experiments (Gerbig et al., 2003a, b; Lin et al., 2004, 2007; Macatangay et al., 2008; Matross et al., 2006; Miller et al., 2008).

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STILT was driven with meteorological data from ECMWF (00:00 and 12:00 analysis fields combined with short-term forecast fields), which have a temporal resolution of 3-hours and a spatial resolution of 1/4 by 1/4 degrees. The STILT model itself has a dynamic resolution, with the finest grid being 1/12 degrees latitude by 1/8 degrees longitude, that increases with the size of the footprint area to reduce computational time as well as preventing under sampling of surface fluxes at times when particles are distributed over large areas (Gerbig et al., 2003a). The model domain was chosen for Europe, extending from 35° N to 62° N and 168° W to 35° E with the Ochsenkopf site approximately in the centre.

2.3 Simulation of N₂O

STILT can be used to advect a tracer to simulate its mixing ratio at a receptor point. The mixing ratio at the receptor located at x_r, y_r, z_r at time t_r is dependent on the footprint, calculated by STILT, and the spatial and temporal distribution of the tracer emissions. The footprint F links the surface emissions to concentration changes at the receptor and is determined by the total time the particle ensemble spends in a column of air with height h at (x_i, y_j, t_m) , normalized by the total number of particles, and has the dimension of concentration divided by flux (i.e. ppb/ μ mol m⁻² s⁻¹) (Lin et al., 2003). The column height h represents the height up to which surface fluxes are mixed at each time-step of the STILT model and is chosen as one half of the mixing height, which is calculated using the modified Richardson number method. The mixing ratio at the receptor $C(x_r, y_r, z_r, t_r)$ is the product of the footprint and the tracer flux at each time step, summed up over the course of the back-trajectory. This is shown in the equation from Gerbig et al. (2006):

$$c(x_{r}, y_{r}, z_{r}, t_{r}) = \sum_{i,j,m} F(x_{r}, y_{r}, z_{r}, t_{r} | x_{i}, y_{j}, t_{m}) \cdot f(x_{i}, y_{j}, t_{m}) + \sum_{i,j,k} c(x_{i}, y_{j}, z_{k}, t_{0})$$
(1)

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where $F(x_r, y_r, z_r, t_r \mid x_i, y_i, t_m)$ is the footprint and relates the flux, $f(x_i, y_i, t_m)$ to the mixing ratio, $c(x_r, y_r, z_r, t_r)$. The last term on the right hand side represents the influence from the mixing ratio at the boundary, $c(x_i, y_i, z_k, t_0)$, that is, when and where the trajectory leaves the model domain. The mixing ratios outside the domain 5 are equal to the background amount in the atmosphere, which is assumed not to be directly affected by local and regional sources.

The back-trajectories were calculated for 10 days going backwards in time. However, only the influence from particles that remained inside the domain was used and for trajectories that left the domain and re-entered it again, only the influence from particles before they left the domain in the first instance was used.

The contribution to the mixing ratios from the lateral boundary can be estimated by coupling the regional model to a global one, or alternatively, by filtering the observations themselves so that what is left are only the instances when they are largely representative of the free-troposphere or 'background' mixing ratio (Wang and Barrett, 2003). For N₂O, however, the global models are either too coarse and/or too uncertain to be used for this purpose and from the observed time-series at Ochsenkopf it is difficult to distinguish periods when the mixing ratio represents the "background", as there is variability occurring on both short and long timescales.

We have, therefore, chosen to use a mixing ratio field derived from the interpolation of the NOAA/ESRL flask data (E. Dlugokencky, personal communication, 2008). For this field, we have only used stations at coastal or high mountain locations to avoid including mixing ratios that have a very strong influence from the near-field. In total, 23 stations from the Northern Hemisphere and tropics were used (see Table 1). Because of missing data and sometimes irregular sampling, all the available data within a 2-week period were averaged for each site. In some cases, only 1 data point was available over the 2-week period and in some instances no data were available. To overcome the problem of missing data, we used a Singular Systems Analysis (SSA) method for gap-filling (Mahecha et al., 2007). In SSA, the frequency components (also known as principle components) of a time-series can be found for datasets that contain

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gaps (Ghil et al., 2001). A new time-series, without gaps, can be reconstructed from these principle components. To generate the "gap-filled" time-series, we fill the missing values in the original time-series with the estimates of these values from the reconstructed time-series. This process can be run iteratively, that is, the principle compo-5 nents of the 'filled' time-series are found and the points in the time-series that were missing in the original data are again filled with the new estimates. The "gap-filled" time-series' at each station were then interpolated over latitude with a resolution of 5 degrees. This interpolated dataset has no longitudinal variation but is an observation based "background" mixing ratio at 2-weekly resolution.

2.4 Bayesian inversion set-up

The N₂O mixing ratio at Ochsenkopf tall tower can be expressed simply in terms of the forward function of the state variables, that is, the atmospheric transport and mixing of the emissions. This function is provided by the surface influence term, $F(x_r, y_r, z_r, t_r)$ x_i , y_i , t_m) from STILT. Thus the forward model can be expressed in matrix form as:

$$c = \mathbf{F} \cdot \mathbf{f} + \mathbf{c}_{\text{bnd}} + \boldsymbol{\varepsilon} \tag{2}$$

where c is the measurement vector containing m observations at the receptor point and **F** is a matrix $(m \times n)$ in which each row is a vector containing the surface influence for each point x_k (where k = 1, ..., n) over the time covered by the back-trajectory corresponding to the measurement with the same row index. In other words, each row of **F** relates the emissions, f, to the mixing ratio in the corresponding row of the measurement vector, c. The second term on the right-hand-side, c_{bnd} , is a vector containing mixing ratios at the lateral boundary corresponding to the time of each observation and ε is a vector containing the model-measurement mismatch. By rearrangement, Eq. 2 can be rewritten as:

$$y = \mathbf{F} \cdot \mathbf{f} + \boldsymbol{\varepsilon} \tag{3}$$

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where y is a vector with each element being the difference between the observed and the boundary mixing ratio, that is $y = c(x_r) - c_{bnd}$ and $\mathbf{F} \cdot \mathbf{f}$ is the forward model. The matrix F is defined according to the resolution of the retrieved fluxes, so that the impact of the flux in each pixel at each resolved time-step is related to the observation via each row of **F**. The assumption is then made that the true fluxes, on which the observations depend, do not change significantly in each pixel during the resolved time interval. This assumption leads to possible temporal aggregation errors, as the correction to the temporal variation in the emissions is aggregated into one emission field for each time-step and thus errors may result in their assignment (Law et al., 2004).

To test the impact of this assumption, we vary the temporal resolution for which the fluxes are retrieved. This corresponds to increasing the number of state variables in f by 1//, where / is the temporal resolution of the resolved fluxes as a fraction of one year, and modifying **F** respectively so that it has the new dimensions of $m \times p$ (where p = n/I). However, there is a trade-off between spatial and temporal resolution; increasing the temporal resolution without decreasing the spatial resolution means an overall increase in the number of state variables, and hence a decrease in the possible constraint on each variable. Therefore, we chose to use a spatial resolution of 2 x 2 degrees, giving n = 299 for our domain.

Depending on the resolution, there may be more state variables than there are observations, that is, p > m, and the problem is under-determined. It is also the case that in some time-steps a number of state variables (fluxes) will not have contributed at all to the mixing ratio at Ochsenkopf as a result of the atmospheric transport. In the Bayesian approach, an under-determined problem is still solvable because of the use of an a priori estimate, which is updated by the information contained in the observations (Enting, 2002; Rodgers, 2000; Tarantola, 2005). Obviously, where no information on a particular state variable is available, no constraint on the a priori estimate is possible. The uncertainty in the a priori estimate, however, must be quantified; this is achieved by a probability density function over the state space. In this study, we assume that it is Gaussian. Similarly, the uncertainty in the observations, that is, the measurement

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error can be quantified as a probability density function over the measurement space. The best estimate of the state vector can then be found from the Bayesian expression:

$$f = f_{\text{prior}} + \mathbf{S}_{\text{prior}} \cdot \mathbf{F}^{\mathsf{T}} (\mathbf{F} \cdot \mathbf{S}_{\text{prior}} \cdot \mathbf{F}^{\mathsf{T}} + \mathbf{S}_{\varepsilon})^{-1} \cdot (\mathbf{y} - \mathbf{F} \cdot \mathbf{f}_{\text{prior}})$$
(4)

where S_{ε} is the error covariance matrix of the measurements and S_{prior} is the error covariance matrix of the a priori estimate. This formulation of the inversion problem does not require finding the inverse of S_{ε} and S_{prior} , thus making it numerically more efficient (the derivation and full description of Eq. 4 is provided by Tarantola et al., 2005). The pseudo-inverse of the matrix $(\mathbf{F} \cdot \mathbf{S}_{\text{prior}} \cdot \mathbf{F}^{\mathsf{T}} + \mathbf{S}_{\varepsilon})^{-1}$ was found using Singular Value Decomposition (SVD) (Press et al., 1992).

An accurate representation of the uncertainty in the a priori emissions is important as erroneous estimates, which have too narrow uncertainty bounds, can lead to estimated emissions that are inconsistent with the atmospheric observations and/or do not correspond to the true emissions patterns (Gerbig et al., 2006; Michalak et al., 2004). The uncertainty in the a priori emission estimates is represented in S_{prior} , which has dimensions $p \times p$. The diagonal elements of \mathbf{S}_{prior} are the squared errors for each of the p state variables and the off-diagonal elements are the correlated errors between them. For the p state variables, we used different errors for the variables corresponding to land and sea fluxes (see Table 2). The correlation was described by an exponential, $\exp(-\Delta d/D - \Delta t/T)$ where Δd is the distance between state variables and Δt is the time interval between variables representing fluxes at the same location but at different points in time. The denominator D is the spatial correlation scale length, and T is the temporal correlation scale length. The choice of D influences how strongly the different state variables are correlated to one another in space. For instance, a long correlation length, D of the order of the domain dimensions, would mean a very strong correlation between state variables and would entail a strong dependence of the inversion on the spatial structure of the a priori emission estimate. On the other hand, a short D of the order of one grid-cell's dimension would mean that the state variables are independent from one another, making the inversion less sensitive to the a priori spatial structure (Kaminski et al., 2001). The drawback of this, however, is that the error reduction on

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each state variable will be small and in the case where the observational constraint is weak there may be errors in the retrieval. The influence of the choice of spatial correlation scale length has been previously investigated with regards to CO_2 (e.g. Gerbig et al., 2006). However, because the pattern of N_2O fluxes do not follow those of CO_2 , we performed an analogous test to that of Gerbig et al. (2006) for N_2O and, additionally, tested the sensitivity of the inversion scheme to the choice of temporal correlation scale length (see Sect. 3.1.2).

The uncertainty in the observations is expressed in the measurement error covariance matrix, \mathbf{S}_{ε} , which is a square matrix of dimensions $m \times m$ with diagonal elements representing the error in each observation and off-diagonal elements representing the correlated errors between observations. The observations used in the inversion, \mathbf{y} , are the differences between the observed mixing ratios and the contribution from advection of the lateral boundary mixing ratios. For this reason, the error in each observation, \mathbf{y}_i , has contributions from the measurement, σ_{meas} , the estimate of the mixing ratio at the boundary, σ_{bnd} , and the transport model, σ_{trans} . The last error component, σ_{trans} , is included to account for imperfections in the transport; this is because the actual mixing ratios may never be exactly determined even if the true emissions field is known. The total error is thus:

$$\sigma_{\varepsilon}^2 = \sigma_{\text{meas}}^2 + \sigma_{\text{trans}}^2 + \sigma_{\text{bnd}}^2 \tag{5}$$

and σ_{ε}^2 is the value of the diagonal elements of \mathbf{S}_{ε} . The measurement, transport and boundary errors are assumed to be correlated over time. The transport error depends significantly on the accuracy of the Planetary Boundary Layer (PBL) height estimate, which varies throughout the day. The degree of correlation between transport errors is represented by an exponential function, $\exp(-\Delta t/A)$ where Δt is the difference in time between measurements and A is the temporal correlation scale length. We assumed that A has a value of 0.5 day based on the temporal development of the PBL. The correlation of the boundary errors was treated in the same way using a temporal correlation scale length, B of 30 days, which is approximately two times the

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2.5 Synthetic data generation

To test the inversion scheme, we generated a synthetic flux dataset of daily varying fluxes with a temporal correlation scale length of 30 days and a spatial correlation scale length of 300 km (see Fig. 1a and b). The synthetic fluxes were generated by adding a spatially and temporally varying offset to each grid-cell of a prior atemporal flux field (we used the GEIA N₂O flux estimates Olivier et al., 1998). The offsets were calculated as the product of the square root of the error covariance matrix, $S_{prior}^{1/2}$ (with $365 \times n$ rows and columns) and a random number vector, r (of length $365 \times n$, with a zero mean and a SD of (1) after the method of Chevallier et al. (2007):

$$f_{\text{syn}} = f_{\text{prior}} + S_{\text{prior}}^{1/2} \cdot \mathbf{r}$$
 (6)

Because S_{prior} is too big to be stored at this temporal resolution, we avoided forming it directly and instead substituted $\mathbf{S}_{\text{prior}}^{1/2}$ in Eq. 6 using the following relationship:

$$\mathbf{S}_{\text{prior}}^{1/2} = \mathbf{S}_{t}^{1/2} \otimes (\mathbf{S}_{s}^{1/2} \cdot (\sigma^{1/2} (\sigma^{1/2})^{\mathsf{T}}))$$
 (7)

 $\mathbf{S}_{\mathrm{prior}}^{1/2}$ can be calculated as the Kronecker product (represented by \otimes) of $\mathbf{S}_{t}^{1/2}$ and $\mathbf{S}_{s}^{1/2} \cdot (\boldsymbol{\sigma}^{1/2}(\boldsymbol{\sigma}^{1/2})^{\mathsf{T}})$, where \mathbf{S}_{t} is the temporal correlation pattern and has dimensions 365×365 and \mathbf{S}_s is the spatial correlation pattern and has dimensions $n \times n$ (both correlations patterns are described by an exponential decay function, see Sect. 2.3), and σ is a vector containing the variances of the fluxes.

We advected the synthetic fluxes with STILT to simulate atmospheric mixing ratios for the Ochsenkopf tall tower, which were used as the observations in the inversion 26085

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tests. In tests B, C and D, we tested the influence that noise and data gaps in the observations has by adding Gaussian distributed noise of 0.1 ppb for each of the measurement, transport and boundary errors (total = 0.3 ppb) with a temporal correlation scale length of 0.5 days for the measurement and transport errors, and 30 days for the boundary errors. Data gaps were introduced following the pattern of gaps in the real observations from the Ochsenkopf tall tower in which about 25% of the data are missing. Figure 2 shows the different time-series' where the "true" mixing ratios (black line) are those generated from the synthetic fluxes (described above). The red line represents the mixing ratios that result from averaging the synthetic fluxes over 7-days, thus the difference between the black and red lines is due to the influence of temporal aggregation in the fluxes, and the blue line shows the influence of adding Gaussian noise to the "true" mixing ratios. In all the inversion tests, we used the GEIA N_2 O flux estimates (Olivier et al., 1998) as the a priori fluxes.

3 Results and discussion

3.1 Synthetic data tests

3.1.1 Reference inversion

The validity of the inversion scheme was tested using the synthetic dataset described in Sect. 2.5. For this test, a temporal resolution of 7 days was used in the state space. The daily varying synthetic fluxes were averaged to this temporal resolution, to avoid aggregation errors, and mixing ratios were generated from the averaged fluxes using the STILT model. Since the same prior was used in the inversion, as was used to create the synthetic fluxes, the only source of error is the difference between the synthetic and the prior fluxes, which is known and is described by the prior error covariance matrix, $\mathbf{S}_{\text{prior}}$. This test was used as a check for internal consistency and as a reference for following tests.

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The performance of this inversion test, and all following tests, were assessed on the basis of the following criteria: (1) the Root Mean Square Error (RMSE) of the retrieved and the synthetic (true) fluxes normalized by the RMSE of the prior and the true fluxes, (2) the reduced chi-squared value, which is equal to two times the cost-function at its minimum divided by the number of observations, and (3) the error reduction over the domain, calculated as $(1-\sigma_{\rm post}/\sigma_{\rm prior})$ where $\sigma_{\rm post}/\sigma_{\rm prior}$ are the posterior/prior flux uncertainties taken as the square-root of the sum of covariances in the posterior/prior error covariance matrices according to Eq. 8, in which case σ_{ii} is an element of $\mathbf{S}_{\rm post}$:

$$\sigma_{\text{post}}^2 = \sum_{i=1,j=1}^N \sigma_{ij}^2 \tag{8}$$

The posterior error covariance matrix, **S**_{post} was calculated according to Eq. 9 (Tarantola, 2005):

$$\mathbf{S}_{\text{post}} = \mathbf{S}_{\text{prior}} - \mathbf{S}_{\text{prior}} \cdot \mathbf{F}^{\mathsf{T}} \cdot (\mathbf{F} \cdot \mathbf{S}_{\text{prior}} \cdot \mathbf{F}^{\mathsf{T}} + \mathbf{S}_{\varepsilon})^{-1} \cdot \mathbf{F} \cdot \mathbf{S}_{\text{prior}}$$
(9)

In this reference test (A in Table 2), the RMSE of the fluxes was reduced by 48% and the reduced chi-square had a value of 0.81. The reduced chi-square can be thought of as the ratio of the actual error to the estimated error, therefore, when all errors are correctly accounted for in the inversion, it has an expected value of 1. In this reference test, the chi-square value is satisfactorily close to 1; this result, and the observed reduction in the RMSE of the fluxes, gives us confidence in the validity of the inversion scheme.

3.1.2 Sensitivity to temporal and spatial error correlations

All following tests in Sect. 3.1 were made using a similar set-up as was used for the reference test but with a few important differences. The synthetic mixing ratios were generated by coupling STILT to the daily varying synthetic fluxes, while in the inversion the flux retrieval is at a temporal resolution of 7 days (unless otherwise stated), therefore they contain a component of temporal aggregation error. Furthermore, the mixing

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ratios were perturbed with Gaussian distributed noise (as described in Sect. 2.5) and data gaps were introduced at the same frequency as in the real observations. Details of each of the parameters used are given in Table 2.

The temporal and spatial correlation scale lengths used in the definition of the prior flux error covariance matrix has important implications for the retrieval (see Sect. 2.5). We tested the influence of changing the temporal correlation of errors in the state space by varying the correlation scale length, T, from 7 to 100 days (B in Table 2). The true value of T, which was used in the generation of the synthetic fluxes, is 30 days, therefore, for any given grid cell, the fluxes in consecutive time-steps will be correlated by $\exp(-7/30) = 0.79$. The minimum in the RMSE of the posterior and true fluxes was found for correlation lengths close to the true value of T (see Fig. 3a). Increasing the correlation length, to example 100 days, means that fluxes in consecutive time-steps would be correlated by 0.93, which is a significant over-estimate of the actual correlation, and hence there is reduction in the freedom to correct the prior temporal variability towards that of the true temporal variability. On the other hand, if the correlation length is under-estimated, then there is too little constraint on the fluxes in different time-steps. Similarly, the error reduction increases with increasing T, since the information used to constrain one time-step has an influence on other time-steps over longer intervals. This means that in the case where T is over-estimated, there is also a corresponding underestimation of the posteriori error and hence an over-estimation of the error reduction. The reduced chi-square value also increases with increasing correlation length, since the actual error (that is between the observed and modeled mixing ratios and between the prior and posteriori fluxes) increases relative to the prescribed error in the inversion set-up.

In an analogous test, the influence of changing the spatial correlation length, D, from 50 to 2000 km was examined (see Fig. 3b). Again, the RMSE is at a minimum for values of D close to the true value (300 km). The reduced chi-square increases for spatial correlation lengths longer than the true length, similar to the result for the test on temporal correlation, as the error between the observed and modeled mixing ratios

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increases. However, using correlation lengths shorter than the true value of D also leads to an increase in the reduced chi-square, as this results in a smaller prior error (in $\mathbf{S}_{\text{prior}}$) and thus a larger ratio of the actual to prescribed errors.

Noteworthy, is the value of the reduced chi-square for the case when T=30 days and and $D=300\,\mathrm{km}$, which has increased from 0.81 in the reference inversion case (Sect. 3.1.1) to 1.56, even though the Gaussian errors in the mixing ratios have been accounted for. This increase is due to the component of temporal aggregation error that arises from inverting mixing ratios, which contain a signal from the daily flux variations, at a 7-day temporal resolution.

3.1.3 Temporal resolution of the resolved fluxes and aggregation errors

The impact of temporal aggregation error was tested by performing inversions with varying flux resolution (C in Table 2). Temporal aggregation errors are incurred when the fluxes are changing significantly from the mean flux over the resolved time interval. Since the observations used in our inversion tests were generated from daily varying fluxes, whereas the retrieved fluxes were resolved only at 7-day and longer intervals, there is a component of aggregation error in all these inversions. The influence of the aggregation error can be seen in the normalized RMSE and reduced chi-square value, which increase with the length of the resolved time interval (see Fig. 4a). This behaviour is similar to that for changing the temporal correlation scale length; one assumes that the fluxes within the resolved time interval have a correlation of 1, compared with the true correlation e.g. at 30 days which is 0.37. However, the correlation between the time intervals decays according to the prescribed function, in our case: $\exp(-\Delta t/T)$. The aggregation error can be projected into the observation space, where it can be thought of as the difference between the true mixing ratios, which would be obtained from the daily varying fluxes, and the mixing ratios that can be obtained from the lower resolution fluxes (e.g. see Fig. 2). Moreover, since increasing the averaging interval results in an additional error, which is not accounted in the observation error covariance matrix, there is an under-estimation of the prior error and thus a corresponding increase in the reduced chi-square value.

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Kaminski et al. (2001) address the problem of spatial aggregation error and proposed an algorithm (based on that of Trampert et Snieder, 1996) for estimating this error based on propagating the information lost by reducing the spatial resolution of the retrieved fluxes (that is with respect to that of the transport model used in the inversion) 5 and projecting this into the measurement space. Although Kaminski et al. (2001) do not discuss temporal aggregation errors, their algorithm can also be applied in the same way to propagate the error induced by reducing the temporal resolution of the inversion. The algorithm involves two steps: (1) calculation of the prior flux uncertainty that is not resolved in the lower resolution model and (2) projection of this uncertainty into the observation space (see the appendix for a detailed description).

We calculated the additional error in the observation space incurred by reducing the temporal resolution of the resolved fluxes from 1 day, coinciding with the variability in the true fluxes, to that used in the inversion. Inversions were performed using the same range of temporal resolutions as in the above test (see Fig. 4b). In contrast to the test that did not account for the aggregation error, the normalized RMSE only increased by approximately 0.1 over the range of temporal resolutions. Furthermore, the reduced chi-square value remained nearly constant over the whole range of resolutions, with all values between 1.08 and 1.10, reflecting the fact that the estimated errors, which included the aggregation error, were close to the actual errors. The magnitude of the aggregation error calculated for the observation space (mean over all observations) was 0.05 ppb and 0.24 ppb for resolutions of 7 and 30 days, respectively, compared with a total observational error (i.e. excluding the aggregation error) of 0.3 ppb, and thus represents a significant contribution to the overall observational error.

3.1.4 Averaging interval of the observations

Another proposed method for dealing with temporal aggregation error, is to average the observations over the same time interval as the retrieved fluxes, and thereby smooth out signals which cannot be represented at the temporal resolution of the model and thus reduce the bias errors (Peylin, 2002). We tested the influence of increasing the averaging interval of the observations up to 240 h (D in Table 2).

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From Fig. 5 it can be seen that averaging in the observation space has a rather complex affect on the retrieval. The best performing inversion, in terms of the RMSE, is that which uses the highest resolution observations. However, there is also a small secondary RMSE minimum at 168 h, which coincides with the averaging interval of the fluxes (7 days). What can be said from this, is that although there is a reduction in the aggregation error when the observations are averaged to remove the short-term variations that cannot be resolved at the temporal resolution of the fluxes, there is an additional error that ensues. This error occurs because the averaged observations are less sensitive to the spatial distribution of the fluxes. However, the reduced chi-square value in this case, is close to 1 for an averaging interval of 168 h. This is because at the longer averaging intervals (>100 h), the RMSE of the prior and retrieved fluxes is at a minimum while there is no change in prior flux error estimate. This shows that the chi-square, although a useful parameter for assessing the inversion, is alone not always a sufficient one. The error reduction also decreases with increasing averaging interval as there are fewer independent observations in the inversion to constrain the fluxes.

3.2 Real observation inversion

3.2.1 N₂O flux estimates

 $\rm N_2O$ fluxes were retrieved for 2007 using the atmospheric mixing ratios observed at the Ochsenkopf tall tower. The inversion set-up was the same as that used in the reference inversion with synthetic data with a few exceptions. For the a priori fluxes we used the IER dataset (http://carboeurope.ier.uni-stuttgart.de) for the anthropogenic fluxes and GEIA for fluxes from the ocean and from soils under natural vegetation, the combination of which we believe is a closer estimate to the true fluxes. However, we kept the same temporal and spatial correlation scale lengths, that is, 30 days and 300 km, respectively, as were used in the reference inversion case. The mixing ratios at the boundaries were taken from the fields of interpolated NOAA flask data as described

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in Sect. 2.3. In the observation space, we used measurements at 3-hourly intervals, each with an uncertainty of 0.5 ppb, which is the quadratic sum of squares of our best estimates of the measurement (0.3 ppb), transport (0.3 ppb), boundary (0.25 ppb), and aggregation errors (0.1 ppb). Using this set-up, we achieved a posterior reduced chisquare value of 1.28, which to some degree indicates an appropriate choice of a priori and measurement uncertainties and covariances.

To verify the posterior fluxes, we compared the mixing ratios generated by coupling the fluxes to the STILT model with the observations at Ochsenkopf, as well as at an independent flask sampling site in the MPI-BGC network, Bialystok (53°13' N, 23°1' E) (see Fig. 6). A significant reduction in the RMSE of the posterior and observed mixing ratios was seen at Ochsenkopf, as well as improvements in the correlation coefficient, normalized standard deviation and regression coefficient (see Table 3). Similarly, at Bialystok, a small improvement in the fit to observations was seen using the posterior fluxes, although there was still an under-estimate of the observed mixing ratios in August and September, owing to the weaker constraint on fluxes in the vicinity of Bialystok from the Ochsenkopf site. In Fig. 6 the contribution to N₂O variability from transport at the domain boundaries is also shown (green line). At each of these sites, the contribution from the boundary defines the trend and seasonal cycle of N₂O, whereas the synoptic variability is predominantly due to effects inside in the domain. Since the boundary mixing ratios are based on observations, errors in boundary mixing ratios are mostly due to transport errors in the STILT model and from the interpolation of the sparse data.

3.2.2 Posterior error

Although only one in-situ measurement site was used in the inversion, substantial error reductions were seen in western and central Europe, between 30 and 65%, with the highest reductions in Germany close to the Ochsenkopf site (see Fig. 7d). The pattern of error reduction closely follows that of the annual mean surface influence function (or footprint) as calculated for Ochsenkopf using STILT (footprint not shown). This result

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is as expected, since the regions that have the strongest influence on the observed mixing ratios, owing to atmospheric transport, will be the best constrained in the inversion, whereas regions that have only a weak influence on the observations are poorly constrained. The spatial extent of the error reduction also depends strongly on the spatial correlation length used in the inversion. We chose to use a correlation length of 300 km; although higher values would have resulted in a greater spread of error reduction, an overestimate of this parameter could lead to wrong assumptions about the correlation of flux errors, and thus, errors in the retrieval.

3.2.3 Temporal variability of fluxes

The observational constraint at Ochsenkopf resulted in a notable reduction in N_2O fluxes, relative to the prior, in February and March for Germany and Poland, which for Germany extended into April. In May, however, this trend reversed and there was a significant increase in fluxes over most of Europe, which was sustained until October. The increase was particularly large in August and September (see Fig. 8).

To better understand what was driving the change in N_2O flux, we looked at the temporal variability of the mean fluxes over 6 regions in Europe (northern France, southern France, northern Germany, southern Germany, United Kingdom, and Poland) and compared these with regional meteorological parameters (see Fig. 8). We performed a linear multiple analysis of variance of the posterior fluxes with the normalized anomalies in temperature, soil moisture and rainfall, where these were calculated using the mean values for each region based on ECMWF analysis fields. Although this approach looks at the integrated influence of these parameters over large regions, some significant correlations were seen; the variance with temperature anomaly was significant for all regions at the 95% confidence level, whereas rainfall was only significant for southern Germany and northern France, and soil moisture was only found to be significant in the UK. We found a positive correlation with temperature anomaly at all sites varying between 0.4 and 0.8 (see Table 4). In southern Germany and northern France, N_2O fluxes were also positively correlated with rainfall. In the UK, N_2O fluxes were

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negatively correlated with soil moisture, a result which can be understood when the soil water filled pore space (WFPS) is considered. N₂O fluxes have been shown to increase with increasing soil moisture up to approximately 80% WFPS, however, above this value N₂O emissions decrease sharply, thus in already very moist soils, increasing soil moisture leads to a decrease in N₂O flux (Freibauer and Kaltschmitt, 2003).

Obviously, human-activities also contribute significantly to variations in N_2O flux. Although it is outside the scope of this study to examine these, we recognise that activities such as the application of N-fertilizer and soil tillage also have a significant impact on N_2O fluxes (Li et al., 1996). N-fertilized applications may contribute to the high emissions seen between April and June, while tillage and harvest may contribute to the high emissions between August and September.

4 Summary and conclusions

In this study, we have firstly examined how high temporal resolution atmospheric measurements of N_2O may be best incorporated into an inversion scheme, while regarding the potential errors that may arise, and secondly retrieved N_2O emissions estimates for 2007 for central and western Europe. By using synthetic datasets with known errors both in the observations and in the fluxes, we explored the influence of temporal and spatial correlation length as well as the temporal resolution of the fluxes. From these tests we find that temporal aggregation of the fluxes can lead to significant errors in the retrieval, if not accounted for. We found for the pseudo-data case, where the true fluxes are varying daily (to which the observations are sensitive), using temporal resolutions of 7-days and longer in the retrieval leads to significant aggregation errors. These errors can be accounted for by increasing the observational error, so that in addition to errors in the transport model, measurements and boundary conditions, the errors resulting from the loss of information by going to a lower resolution model (the aggregation errors) are included. The algorithm of Kaminski et al. (2001) can be used to estimate the aggregation error in the observation space and only requires an

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Using the observations from the tall tower site, Ochsenkopf (50°01′ N, 11°48′ E) we 5 retrieved N₂O fluxes at a 7-day resolution for 2007. The posterior fluxes showed much greater temporal variability than the prior fluxes. Relative to the prior, notable reductions in N₂O fluxes were seen in February and March for Germany and Poland, while in May, a significant increase was seen over most of Europe, which was sustained until October. In particular, large emissions were seen in August and September, which may be due to human activities such as harvest and tillage at this time. Over the whole year and in all regions, we found N₂O fluxes to be significantly correlated (at the 95% confidence level) with temperature anomaly, while correlations with rainfall were only significant for southern Germany and northern France, and correlations with soil moisture were only significant for the UK. The observational constraint had the most impact on the temporal variability of the fluxes, while the annual mean fluxes remained close to those of the prior (see Table 5). Moreover, the mean fluxes found for France, Germany, the UK and Benelux, agreed very well with those found in the inversion of Manning et al. (2003) while substantial increases relative to EDGAR-32FT2000 were seen for France, the UK and Poland (see Table 5).

Appendix A

Description of the algorithm for estimating aggregation errors

We present a description of the algorithm derived by Kaminski et al. (2001) and our method for its calculation. The first step involves defining a projection operator, P_{\perp} that operates in the space of the high-resolution model and projects only the components that are resolved by the low-resolution model:

$$\mathbf{P}_{+} = \Sigma(\boldsymbol{\rho}_{i} \boldsymbol{\rho}_{i}^{\mathsf{T}}) \tag{A1}$$

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$$\mathbf{P}_{-} = \mathbf{I} - \mathbf{P}_{+} \tag{A2}$$

where **I** is the identity matrix. In the second step, the aggregation error covariance matrix, **S**_{agg} is calculated by projecting the error in the flux space into the observation space:

$$\mathbf{S}_{\text{agg}} = \mathbf{F} \cdot \mathbf{P}_{-} \cdot \mathbf{S}_{\text{prior}} \cdot \mathbf{P}_{-}^{\mathsf{T}} \cdot \mathbf{F}^{\mathsf{T}} \tag{A3}$$

where the footprint, \mathbf{F} and prior flux error covariance matrix, \mathbf{S}_{prior} are defined for the high resolution model. Since \mathbf{P}_{-} is too large to be calculated directly (in our case \mathbf{P}_{-} would be a $100\,000\times100\,000$ matrix) we calculate directly the product, $\mathbf{F}\cdot\mathbf{P}_{-}$ (which is approximately $2500\times100\,000$):

$$\mathbf{F} \cdot \mathbf{P}_{-} = \mathbf{F} - \mathbf{F} \cdot \Sigma (\mathbf{p}_{i} \mathbf{p}_{i}^{\mathsf{T}}) \tag{A4}$$

Here, our method departs from that of Kaminski et al. (2001); we calculate the product **F**·**P**₋·**S**_{prior} and thus avoid forming **S**_{prior} directly (using the same method described in Sect. 2.4):

$$\mathbf{F} \cdot \mathbf{P}_{-} \cdot \mathbf{S}_{\text{prior}} = \mathbf{F} \cdot \mathbf{P}_{-} \cdot \mathbf{S}_{t} \otimes (\mathbf{S}_{s} \cdot (\boldsymbol{\sigma}(\boldsymbol{\sigma})^{\mathsf{T}})) \tag{A5}$$

and lastly S_{agg} is calculated according to Eq. A6, which is equivalent to A3:

$$\mathbf{S}_{\text{agg}} = \mathbf{F} \cdot \mathbf{P}_{-} \cdot \mathbf{S}_{\text{prior}} \cdot (\mathbf{F} \cdot \mathbf{P}_{-})^{\text{T}}$$
(A6)

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Table 1. Northern Hemisphere stations used in the interpolation for the background mixing ratio.

Station	Coordinates	Station	Coordinates
Alert, Canada, ALT	82.5° N, 62.5° W, 200 m	Mace Head, Ireland, MHD	53.3° N, 9.9° W, 25 m
Ascension Isl., ASC	7.5° S, 14.4° W, 54 m	Sand Isl., USA, MID	28.2° N, 177.4° W, 3.7 m
Terceira, Azores, AZR	38.8° N, 27.4° W, 40 m	Mauna Loa, Hawaii, MLO	19.5° N, 155.6° W, 3397 m
Baltic Sea, Poland, BAL	55.4° N, 17.2° E, 3 m	Niwot Ridge, USA, NWR	40.0° N, 105.6° W, 3050 m
Barrow, Alaska, BRW	71.3° N, 156.6° W, 11 m	Pallas, Finland, PAL	68.0° N, 24.1° E, 560 m
Bermuda, BME	32.4° N, 64.4° W, 30 m	Ragged Pt, Barbados, RPB	13.2° N, 59.4° W, 45 m
Cold Bay, Alaska, CBA	55.2° N, 162.7° W, 25 m	Shemya Isl., Alaska, SHM	52.7° N, 174.1° E, 40 m
Christmas Isl., CHR	1.7° N, 157.2° W, 3 m	Ocean Stn, Norway, STM	66.0° N, 2.0° E, 0 m
Mariana Isl., GMI	13.4° N, 144.8° E, 1 m	Summit, Greenland, SUM	72.6°, 38.5° W, 3238 m
Iceland, ICE	63.3° N, 20.3° W, 118 m	Mt. Waliguan, China, WLG	36.3° N, 100.9° E, 3810 m
Tenerife, IZO	28.3° N, 16.5° W, 2360 m	Ny-Alesund, Sweden, ZEP	78.9° N, 11.9° E, 475 m
Kumukahi, Hawaii, KUM	19.5° N, 154.8° W, 3 m		

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Table 2. Summary of the inversion tests and the parameters used.

	symbol	unit	Α	В	С	D
true flux temporal variability		days	7	1	1	1
observation averaging interval		hours	3	3	3	3-240
time-step length		days	7	7	7-30	7
measurement error	σ_{meas}	ppb	0.001	0.1	0.1	0.1
transport error	σ_{tran}	ppb	0	0.1	0.1	0.1
boundary error	σ_{bnd}	ppb	0	0.1	0.1	0.1
measurement error scale length	M	days	0	0.5	0.5	0.5
transport error scale length	Α	days	0	0.5	0.5	0.5
boundary error scale length	В	days	0	30	30	30
prior flux error for land fluxes	σ_{land}	%	100	100	100	100
prior flux error for sea fluxes	$\sigma_{\rm sea}$	μmolm ² s ⁻¹	1e-06	1e-06	1e-06	1e-06
prior flux spatial scale length	D	km	300	50-2000	300	300
prior flux temporal scale length	Τ	days	30	7–30	30	30

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Table 3. Comparison of prior and posterior mixing ratios at Ochsenkopf and Bialystok.

		RMSE (ppb)	R^2	normalized SD	regression coefficient
Ochsenkopf	prior	0.526	0.444	0.827	0.754
	posterior	0.268	0.866	0.896	0.866
Bialystok	prior	1.134	0.158	0.794	0.573
	posterior	0.883	0.373	0.660	0.521

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Table 4. Analysis of variance of N₂O fluxes with temperature, soil moisture and rainfall.

	temperature	soil moisture	rainfall
southern France	0.54	N.S.	N.S.
northern France	0.63	N.S.	0.42
United Kingdom	0.43	-0.51	N.S.
southern Germany	0.80	N.S.	0.70
northern Germany	0.57	N.S.	N.S.
Poland	0.71	N.S.	N.S.

N.S. = Not Significant (at the 95% confidence level).

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Table 5. Comparison of annual mean N_2O emissions for five European countries in units of $Gg-N_2O/y$.

	posterior ¹	prior ²	EDGAR ³	Manning et al.4
France	260 ± 144	214	139	271, (252–287)
Germany	225 ± 135	242	238	247, (220–274)
United Kingdom	150 ± 87	111	79	121, (107-134)
Benelux	72 ± 44	78	98	101, (81–146)
Poland	151 ± 116	144	77	not given

^{1.} The total uncertainties were calculated by integrating the posterior uncertainty in each grid-cell over the land surface area (where the grid-cell uncertainty was calculated according to Eq. 8);

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^{2.} the prior used in this study included the anthropogenic emissions of IER (http://carboeurope.ier.uni-stuttgart.de) and the natural soil and ocean emissions of GEIA (Olivier et al., 1998) with uncertainties of 100%;

^{3.} EDGAR-32FT2000 (anthropogenic emissions only) with a nominal uncertainty of 100% (Olivier et al., 2005);

^{4.} uncertainty range given inside parentheses (Manning et al., 2003).

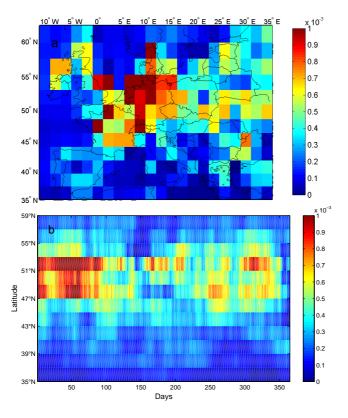


Fig. 1. The synthetic N₂O flux dataset that is used to generate the pseudo-observations. The synthetic fluxes contain spatially and temporally correlated errors according to the specifications of the prior error covariance matrix S_{prior} : (a) the annual mean flux and (b) the zonal mean flux, both in units of μ mol m⁻² s⁻¹.

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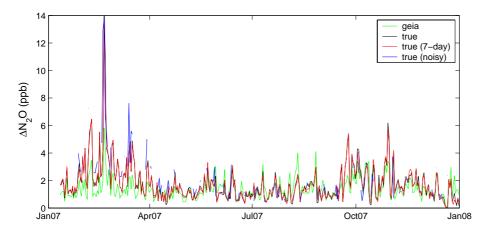


Fig. 2. Daily averaged mixing ratios generated using the forward STILT model coupled to the following flux maps: GEIA (green), true with daily variation (black), true averaged over 7-days (red), and true with added Gaussian distributed noise and data gaps (blue).

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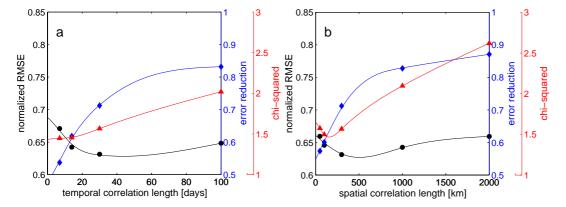


Fig. 3. The influence of changing the correlation scale lengths, used in the definition of the prior flux error covariance matrix, on the Root Mean Square Error (RMSE) of the posterior and true fluxes (black), the error reduction (blue) and the reduced chi-square value (red), for **(a)** changing the temporal correlation scale length and **(b)** changing the spatial correlation scale length. All these figures show the results of inversions using synthetic mixing ratios with data gaps and added Gaussian noise.

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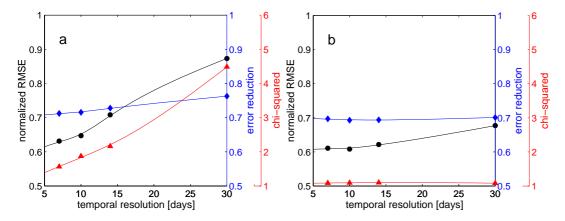


Fig. 4. Analysis of the impact that temporal resolution in the state space has on the retrieval. Shown is the influence on RMSE of the posterior and true fluxes (black), error reduction (blue) and the reduced chi-square value (red) for two cases **(a)** using errors in the observation space with contributions from only transport, measurement and boundary errors and **(b)** including in addition the estimated aggregation error for each temporal resolution.

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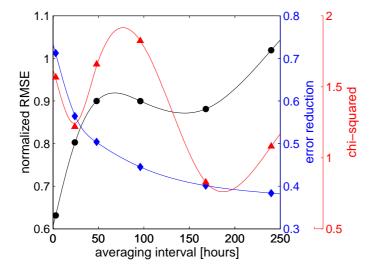


Fig. 5. The influence that changing temporal resolution in the observation space has on the retrieval (using a fixed resolution in the state space of 7-days). Shown is the impact on the RMSE of the posterior and true fluxes (black filled circles), error reduction (blue) and the reduced chi-square value (red). (The lines are cubic-spline fits to the data).

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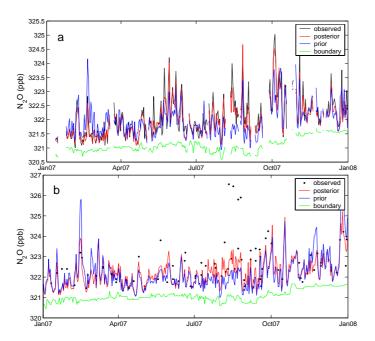


Fig. 6. Comparison of the observed (black), posterior (red), prior (blue) and boundary mixing ratios (green). The boundary mixing ratio is the mixing ratio at the receptor that would be seen in the absence of any fluxes inside the domain, in other words, it is the N_2O that is transported from the domain boundaries to the measurement site. Mixing ratios are shown for **(a)** the Ochsenkopf tall tower, and **(b)** for the MPI flask site Bialystok (53°13′ N, 23°1′ E).

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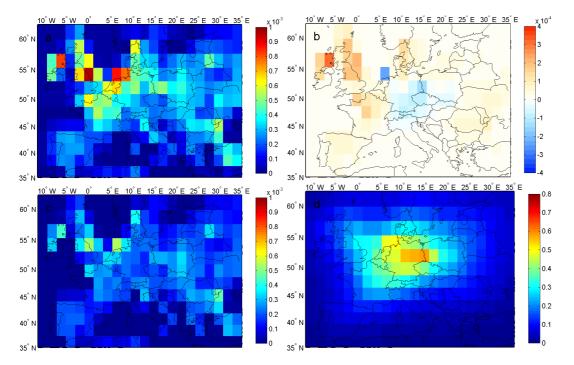


Fig. 7. Inversion results using the observed N₂O mixing ratio at Ochsenkopf: (a) annual mean posterior N₂O flux, (b) annual mean difference between the posterior and prior N₂O flux, (c) posterior error for the annual mean flux, and (d) error reduction calculated as $1-\sigma_{\text{post}}/\sigma_{\text{prior}}$. All fluxes are in units of umol m⁻² s⁻¹.



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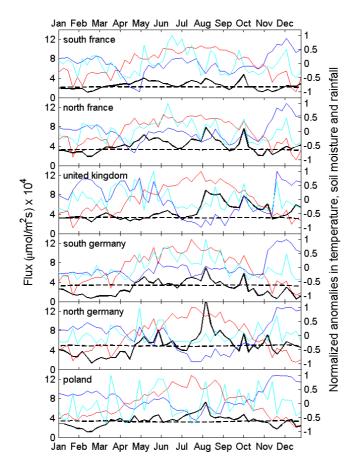


Fig. 8. Temporal variability of the total posterior (black solid) and prior (black dashed) N₂O flux for 6 regions in Europe compared with the normalized anomalies in mean temperature (red), soil moisture (blue) and rainfall (cyan) for each region in 2007.

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