Microstructure Mechanics Dislocation dynamics

Dierk Raabe

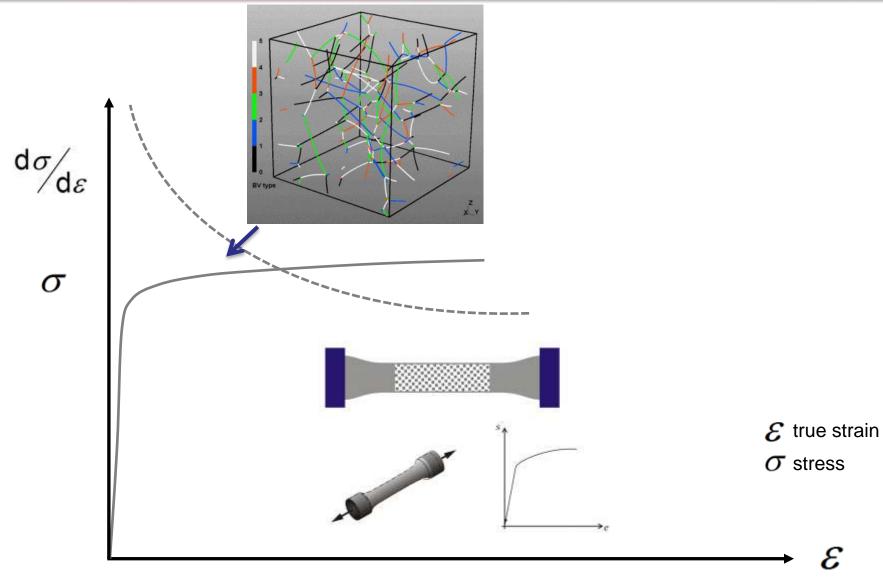


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Class 2013

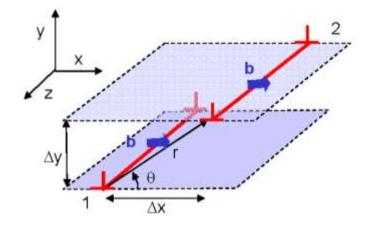
Dislocations and strain hardening





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Dislocation 2 "feels" the stress field of dislocation 1 (and vice versa).

Peach-Koehler Force

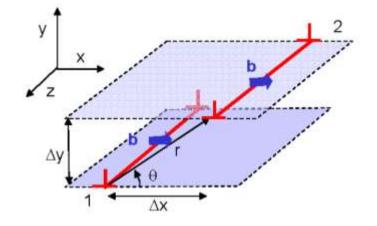
$$\vec{F}_{1\to 2} = \left(\underline{\underline{\sigma}}^{1\to 2} \ \vec{b}_2\right) \times \vec{t}_2$$

 σ_{xy} – produces glide force

 σ_{xx} – produces *climb* force

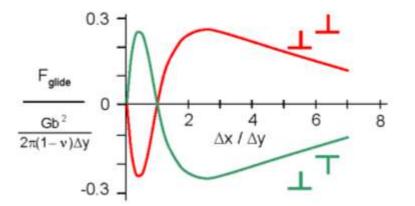
Forces among edge dislocations





So glide force, resolved onto the slip plane, is:

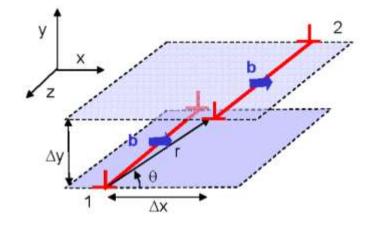
$$F_{glide} = \frac{Gb^2}{2\pi(1-\nu)} \frac{\Delta x(\Delta x^2 - \Delta y^2)}{\left(\Delta x^2 + \Delta y^2\right)^2}$$

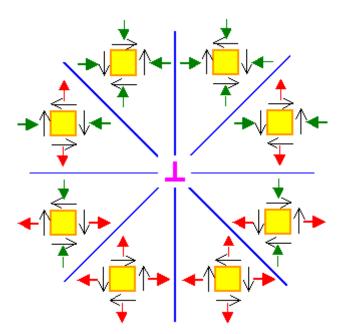


$$\begin{split} \sigma_{xx} &= -\mathsf{D}\, y \, \frac{3 \Delta x^2 + \Delta y^2}{\left(\Delta x^2 + \Delta y^2\right)^2}, \quad \text{with}: \quad \mathsf{D} = \frac{\mathsf{G}\mathsf{b}}{2\pi(1-\nu)} \\ \sigma_{xy} &= \sigma_{yx} = \mathsf{D}\, \Delta x \, \frac{\Delta x^2 - \Delta y^2}{\left(\Delta x^2 + \Delta y^2\right)^2} \end{split}$$

Forces among edge dislocations

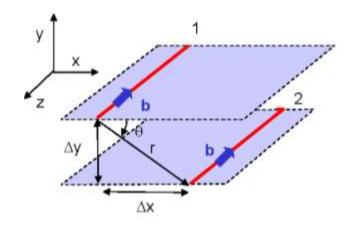






$$\begin{split} \sigma_{xx} &= -\mathsf{D}\, y \frac{3 \Delta x^2 + \Delta y^2}{\left(\Delta x^2 + \Delta y^2\right)^2}, \quad \text{with}: \ \ \mathsf{D} = \frac{\mathsf{G}\mathsf{b}}{2\pi(1-\nu)} \\ \sigma_{xy} &= \sigma_{yx} = \mathsf{D}\, \Delta x \frac{\Delta x^2 - \Delta y^2}{\left(\Delta x^2 + \Delta y^2\right)^2} \end{split}$$





Dislocation 2 "feels" the stress field of dislocation 1 (and vice versa).

$$\sigma_{\theta z} = \sigma_{z\theta} = \frac{Gb}{2\pi r}$$

So force on dislocation 2 from dislocation 1 is:

$$F = \frac{Gb^2}{2\pi r}$$

... but this force acts in the radial direction.

Force on dislocation 2 from dislocation 1, resolved onto the glide plane is:

$$F_{res} = \frac{Gb^2}{2\pi r} \cos\theta$$

Alternatively, we can use the stress field expressed in Cartesian co-ordinates:

$$\sigma_{xx} = \sigma_{yy} = \sigma_{zz} = \sigma_{xy} = \sigma_{yx} = 0$$

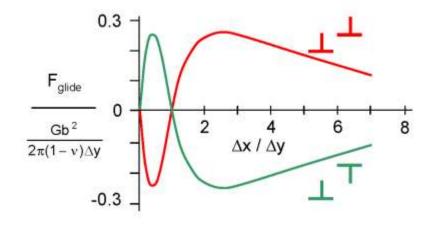
$$\sigma_{xz} = -\frac{Gb}{2\pi} \frac{\Delta y}{\Delta x^2 + \Delta y^2} = -\frac{Gb}{2\pi} \frac{\sin \theta}{r}$$

$$\sigma_{yz} = \frac{Gb}{2\pi} \frac{\Delta x}{\Delta x^2 + \Delta y^2} = \frac{Gb}{2\pi} \frac{\cos \theta}{r}$$

Note that the shear stress acting to shear atoms paralle to **b** above and below the glide plane is σ_{yz} .

$$F_{res} = \sigma_{yz}b = \frac{Gb^2}{2\pi r}\cos\theta = \frac{Gb^2}{2\pi}\frac{\Delta x}{\Delta x^2 + \Delta y^2}$$



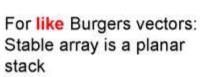


For like Burgers vectors: $\Delta x = \pm \Delta y$: unstable equilibrium $\Delta x = 0$: stable equilibrium

For opposite Burgers vectors: $\Delta x = \pm \Delta y$: stable equilibrium $\Delta x = 0$: unstable equilibrium

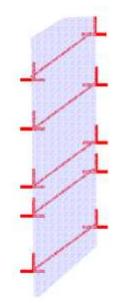
For a set of "opposite" Burgers vectors:

There are a large number of possible stable arrangements.



A low angle tilt boundary.

This arrangement has a strong long-range stress field.



"Taylor lattice"

"Dipole dispersion"

These stable arrangements have minimal *long*range stress fields.

Calculate the mutual forces for the following dislocation configurations:

2 parallel edge dislocations (same glide plane)
parallel edge and screw dislocations (same glide plane)
2 parallel screw dislocations (same glide plane)
2 parallel edge dislocations (above each other)
2 anti-parallel edge dislocations (same glide plane)

Write program:

store: stress fields of 2D infinite screw and edge dislocations (along z axis) enter: position (x,y) and Burgers vector b of second dislocation (place first dislocation in origing)

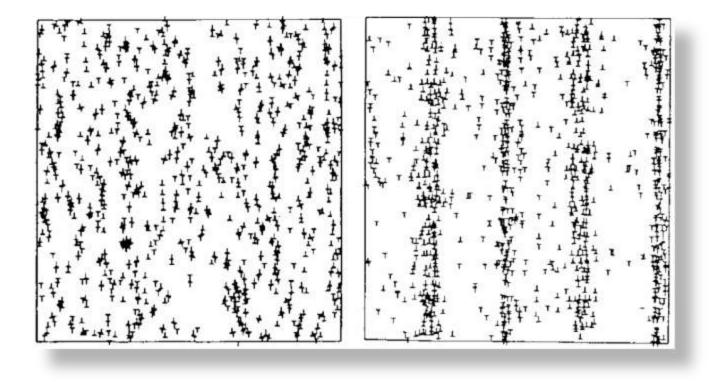


Statistical Dislocation Dynamics



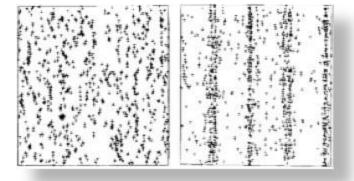


2D - view parallel to dislocation line





2D – view parallel to dislocation line



Some questions:

Difference between edge and screw dislocations?

How to do multiplication?

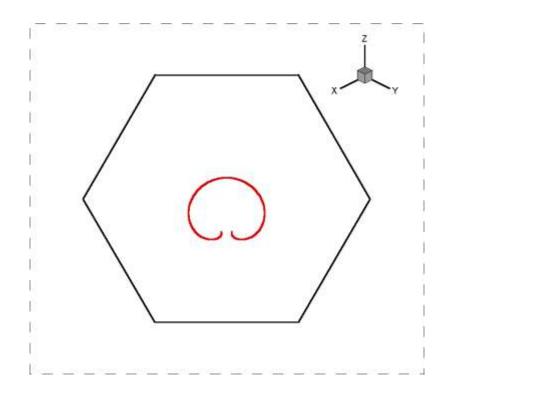
Dislocation bow-out?

Annihilation?

Climbing?



2D - view into the glide plane





2D – view into the glide plane

Some questions:

Difference between edge and screw dislocations?

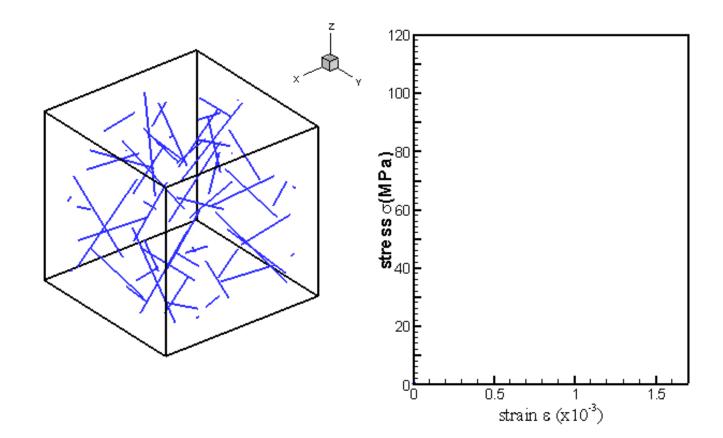
Cross-slip?

Cutting?

Jog-drag?

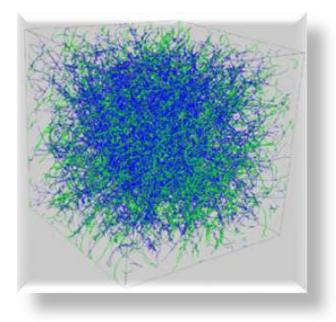


3D: DDD (discrete dislocation dynamics)





Full 3D segment treatment



Some questions:

Difference between edge and screw dislocations?

Junctions?

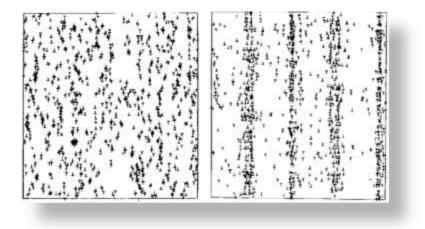
Cutting?

Cores of the dislocations?

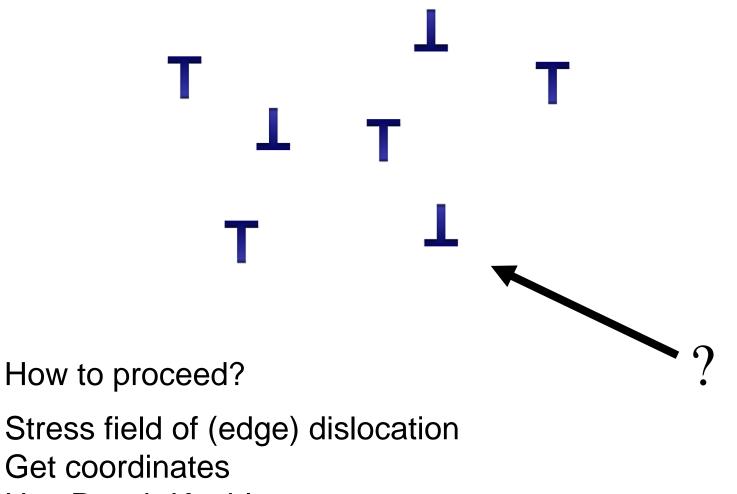


2D – view parallel to dislocation line

Principle procedure







Use Peach Koehler

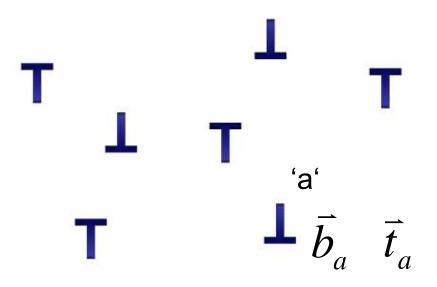
Move it

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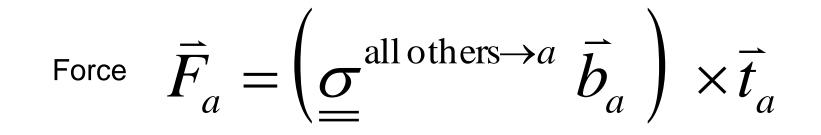


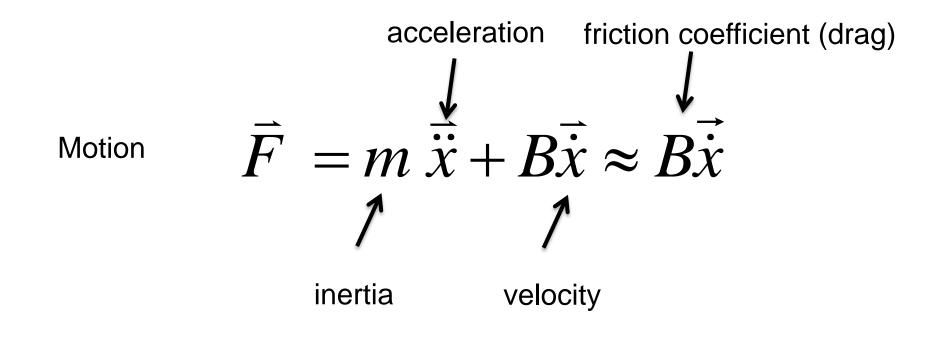
Force
$$\vec{F}_a = \left(\underline{\sigma}^{\text{all others} \to a} \vec{b}_a\right) \times \vec{t}_a$$

Force on dislocation 'a' by all others











Equilibrium of forces

$$\sum \vec{F}_i = 0$$

$$\sum \vec{F}_i = B\vec{x} + \vec{F}_a = 0$$

$$\vec{F}_a = \left(\underline{\sigma}^{\text{alle} \to a} \ \vec{b}_a \right) \times \vec{t}_a$$



Equilibrium of forces

$$\sum F = 0$$

$$F_{disloc} + F_{self force} + F_{extern} + F_{therm} + F_{viscous} + F_{obstacle} + F_{Peierls} + F_{osmotic} + F_{image} + F_{inertia}$$

$$F_{disloc}$$
: elastic – other dislocations

*F*_{extern}: external

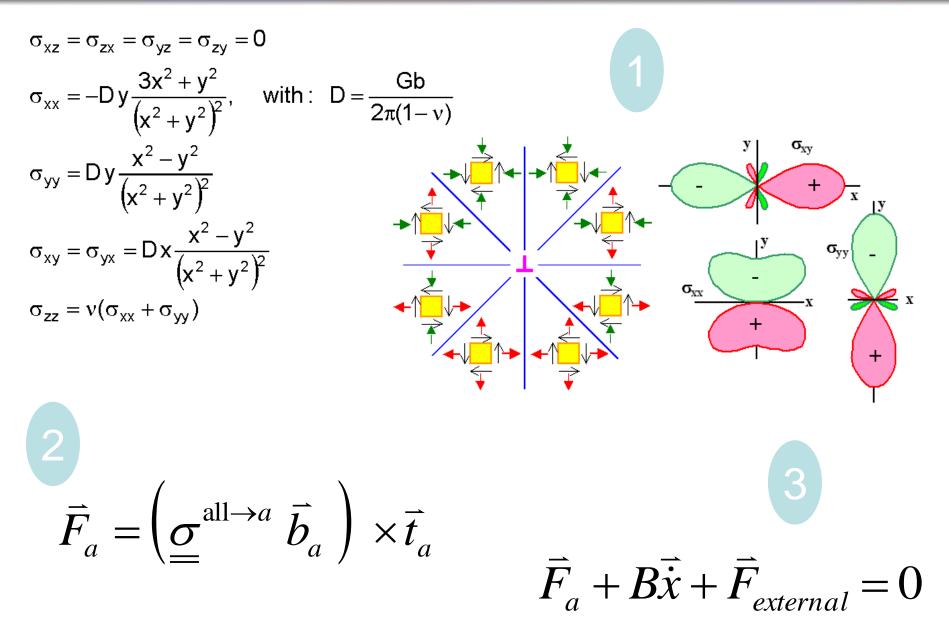
*F*_{obstacle}: obstacle

*F*_{osmotic}: chemical forces

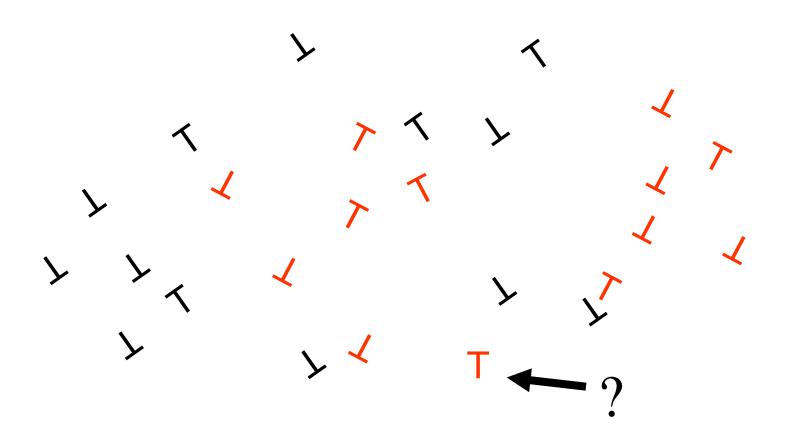
F_{image}: surface forces

Example of Discrete Dislocation Dynamics in 2D









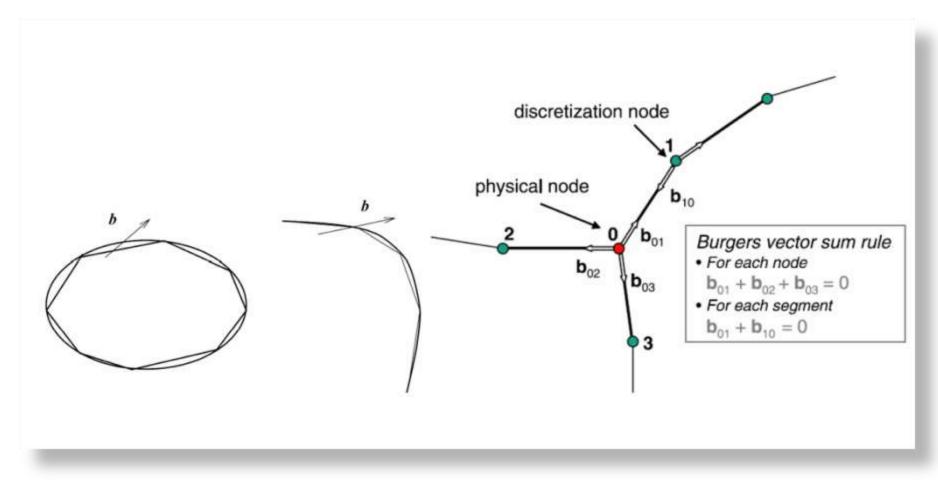


▼ ← ?

- 1) Calculate stress field of machine and of all other dislocations at position of T
- 2) Use Peach-Koehler equation to get force on dislocation
- 3) Integrate with very small time step (explicit) viscous eq. of motion

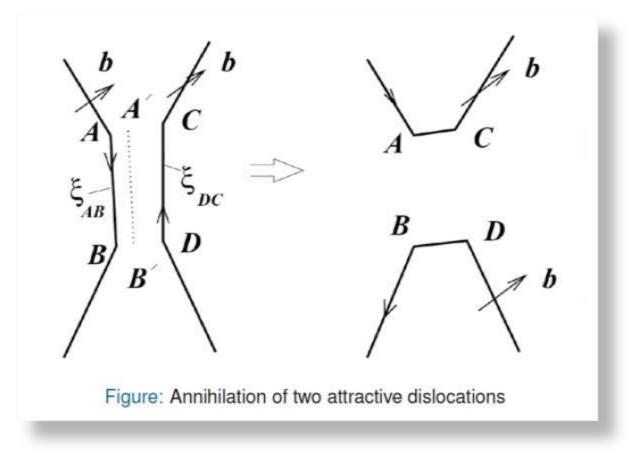


3D segments and node construction





Annihilation events





Jog formation

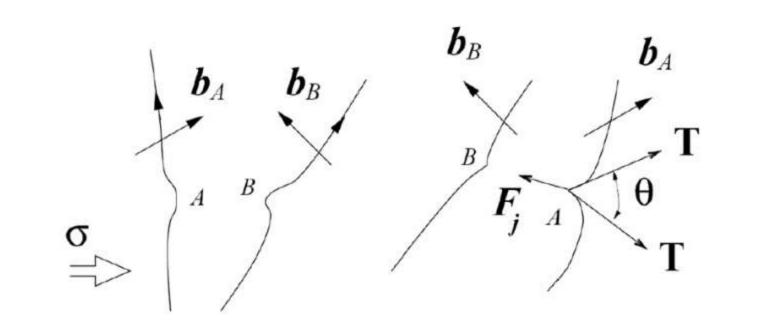


Figure: Jogs are formed when the angle between two attractive dislocations in different planes becomes less than a critical angle θ_c^{jog}

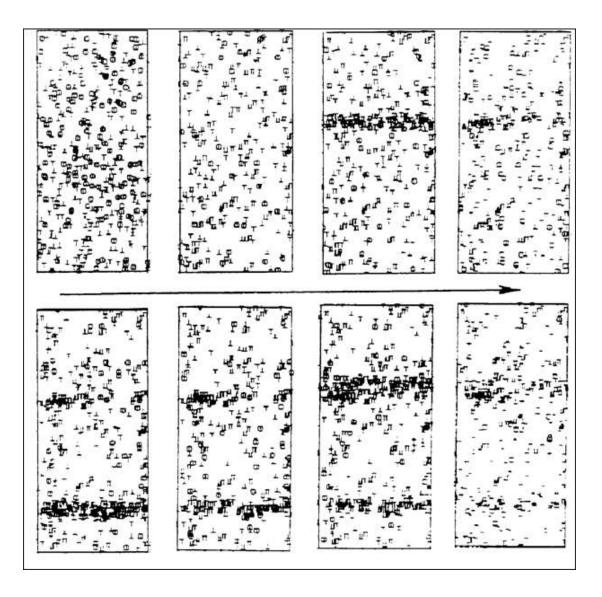


Examples

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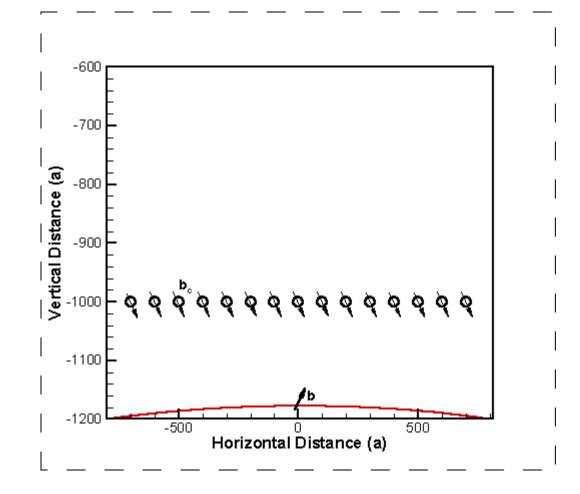
Example of Discrete Dislocation Dynamics in 2D



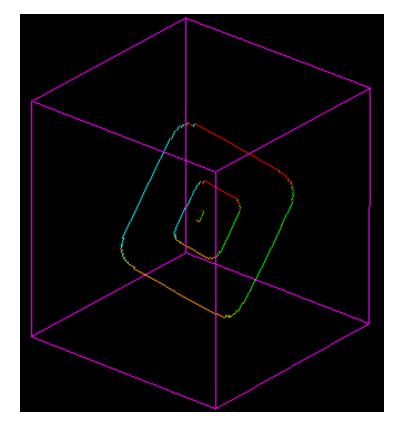


Example of Discrete Dislocation Dynamics in 2D



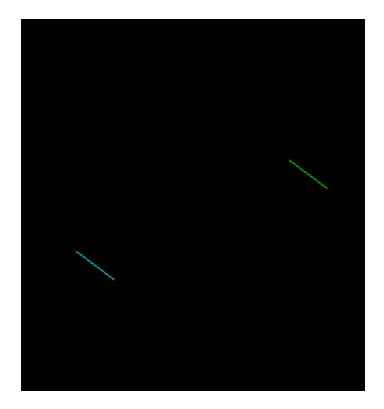




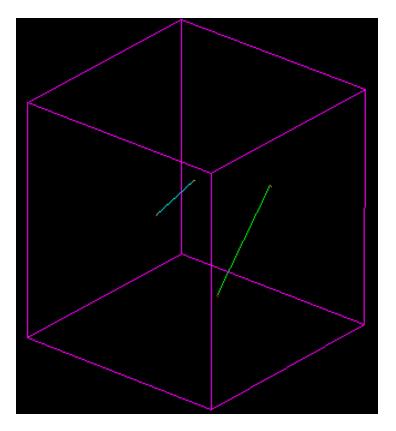


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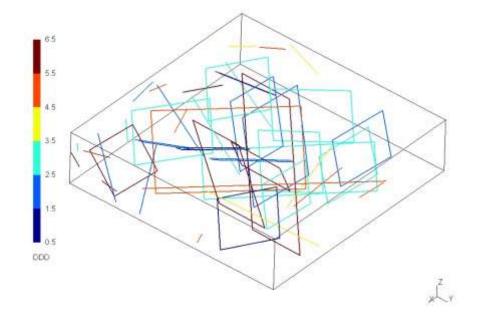






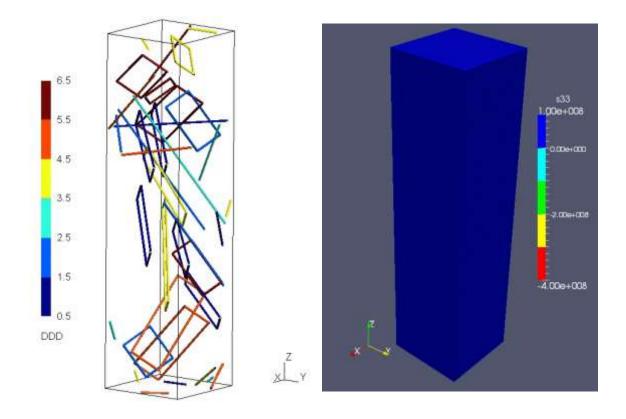
Example of Discrete Dislocation Dynamics in 3D



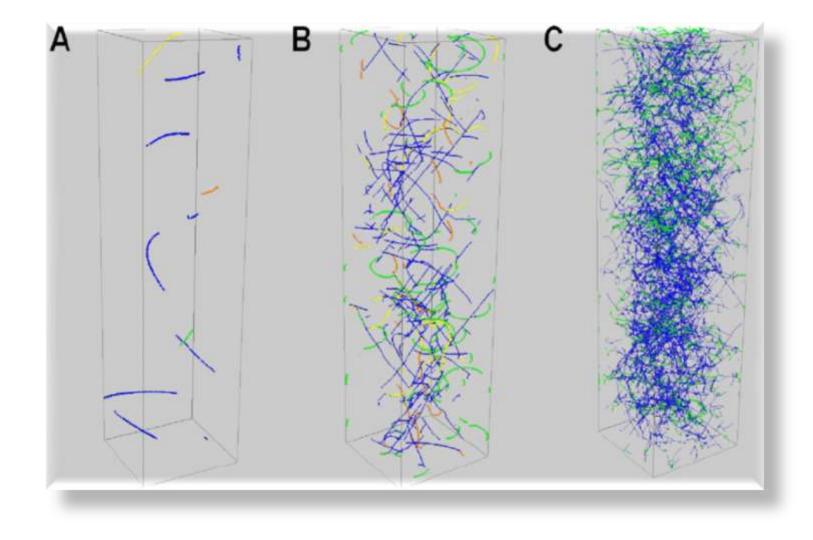


Example of Discrete Dislocation Dynamics in 3D

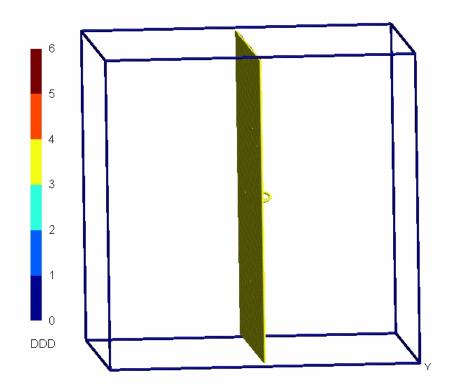




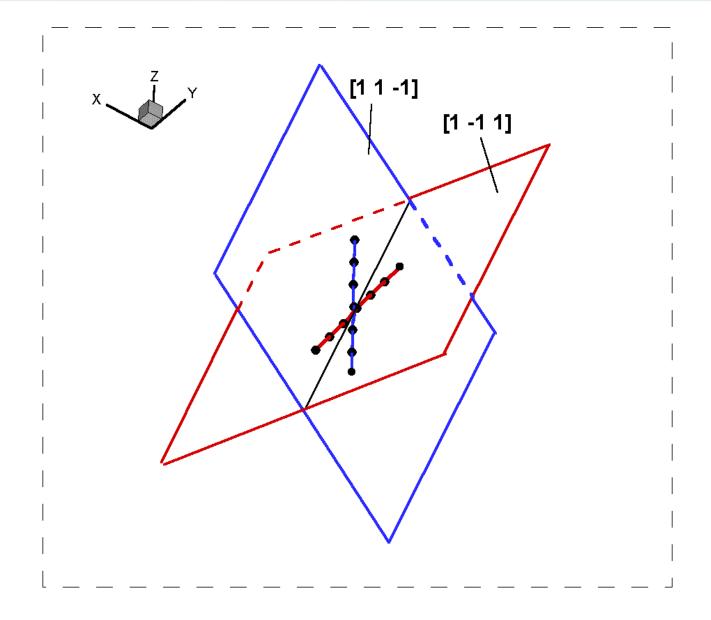




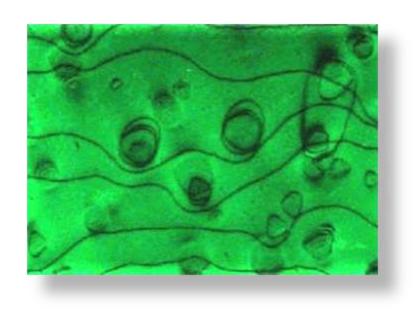


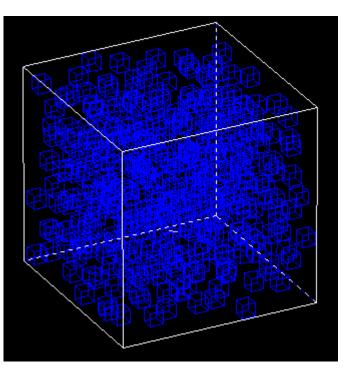




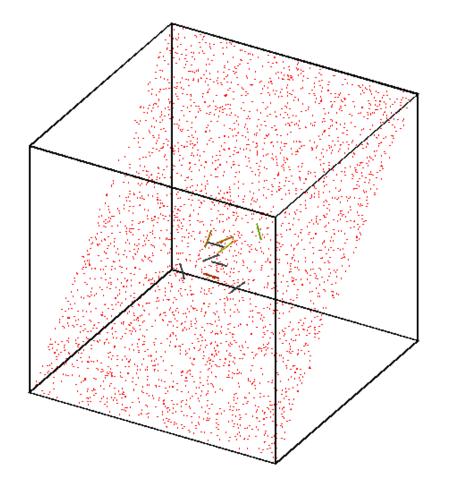


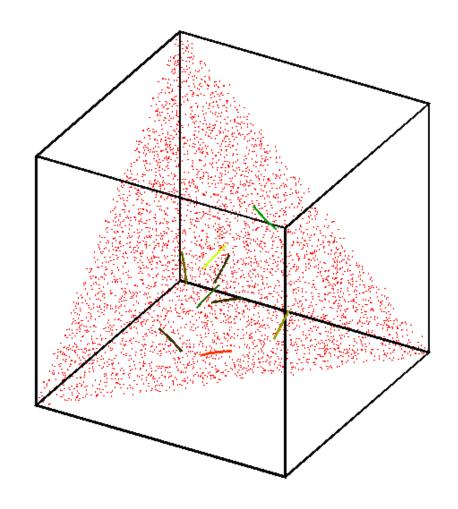




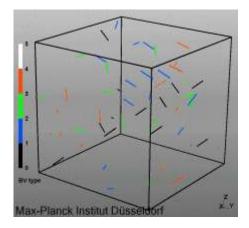


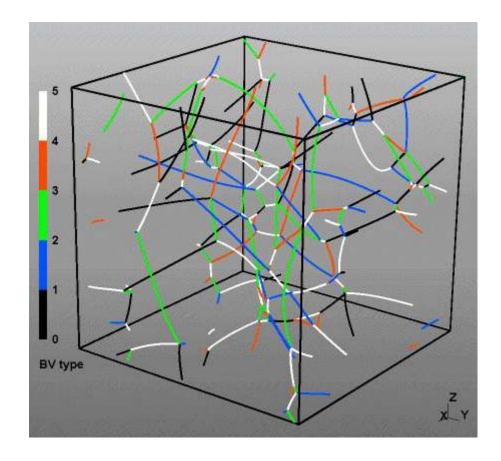






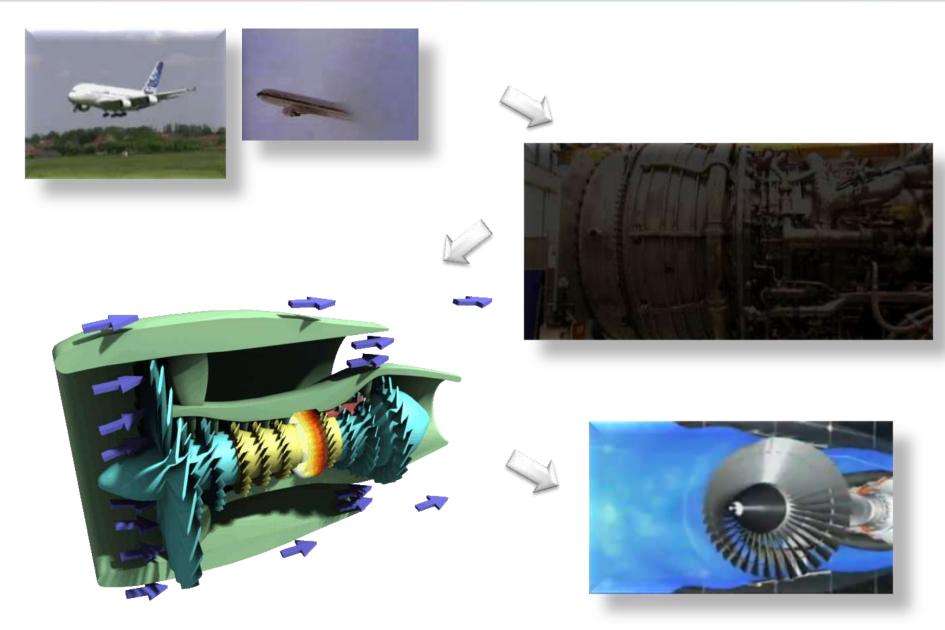






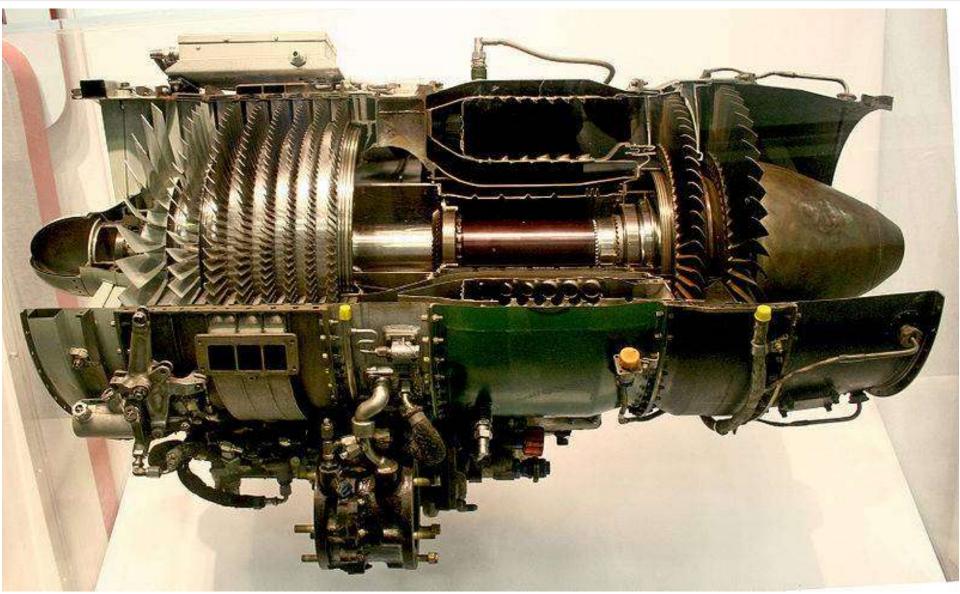
Example of Discrete Dislocation Dynamics in 3D: superalloys





Example of Discrete Dislocation Dynamics in 3D: superalloys



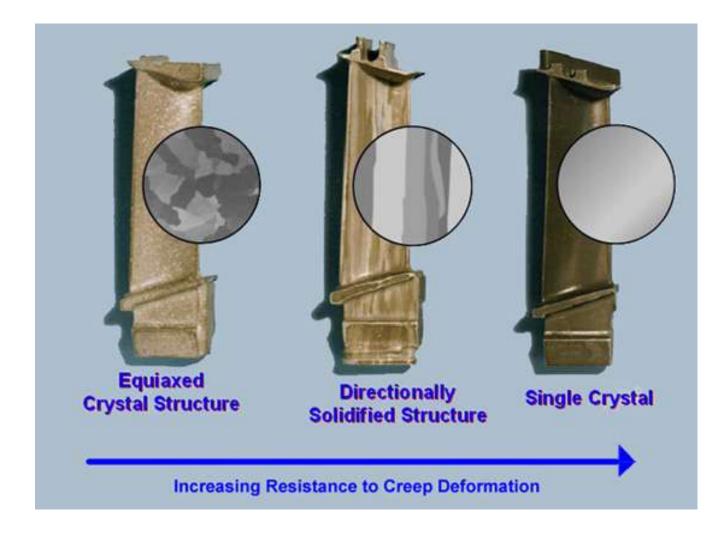


courtesy: Pratt and Whitney

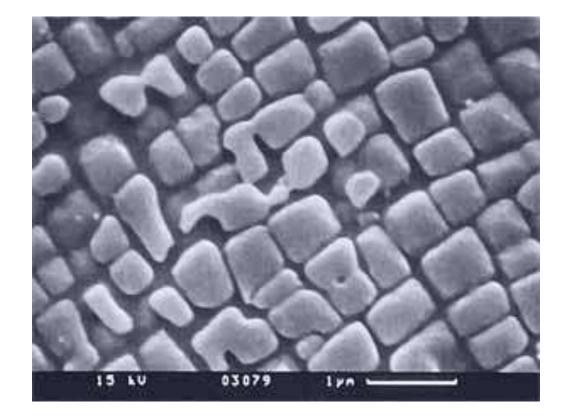




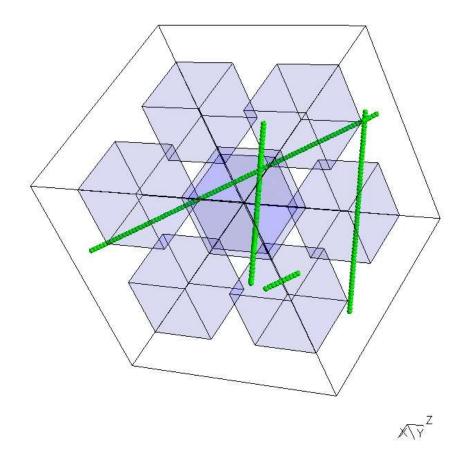


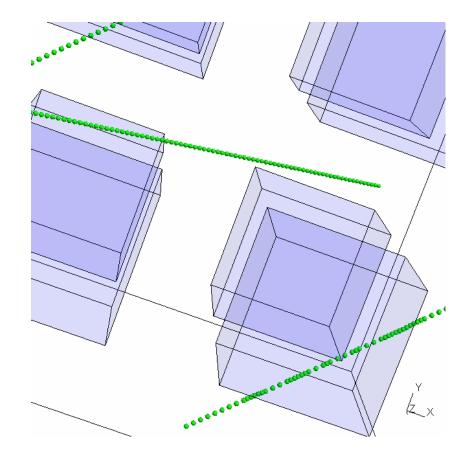




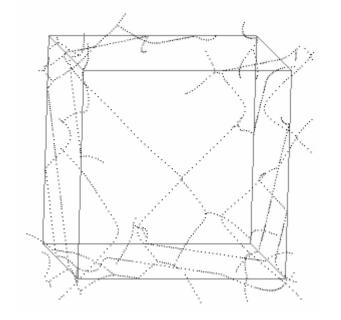




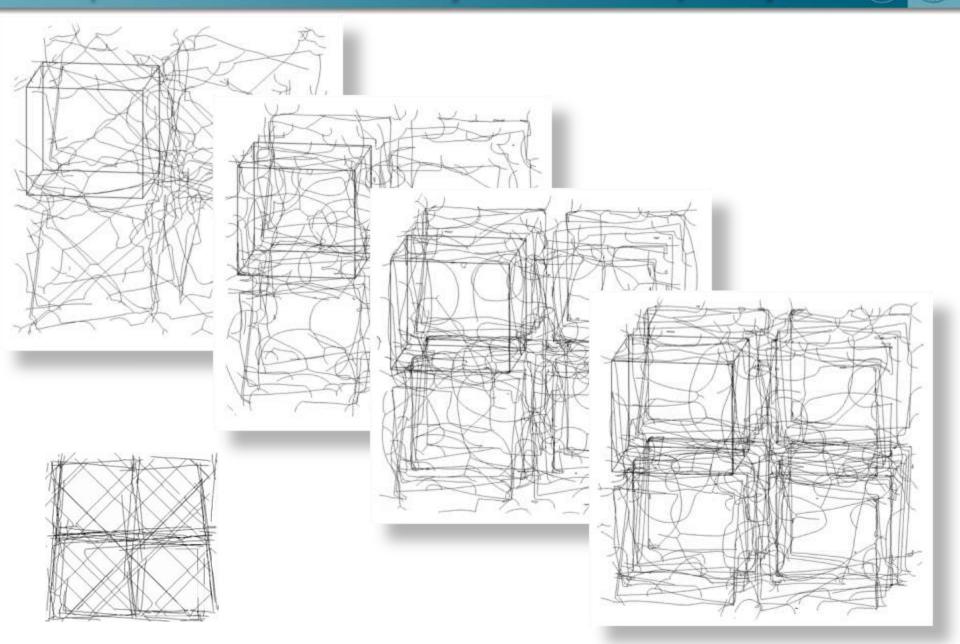






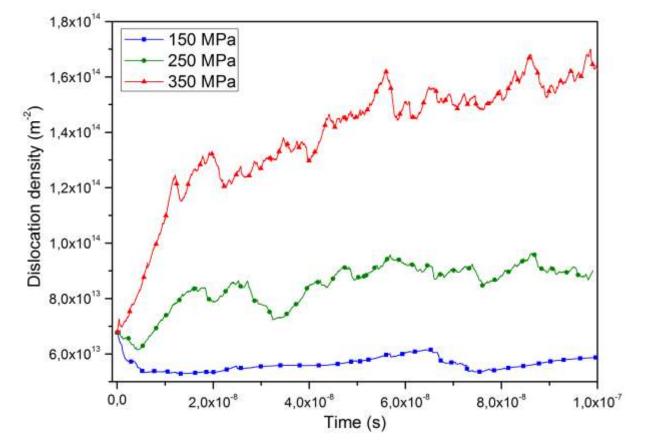


Example of Discrete Dislocation Dynamics in 3D: superalloys



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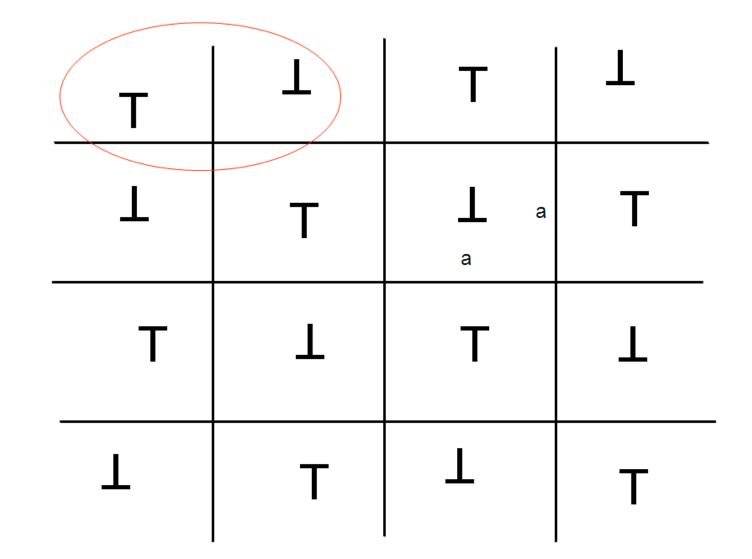
WHY Statistical Dislocation Dynamics ?

- kinetic equation of state
- structure evolution
- coupling to continuum kinematics



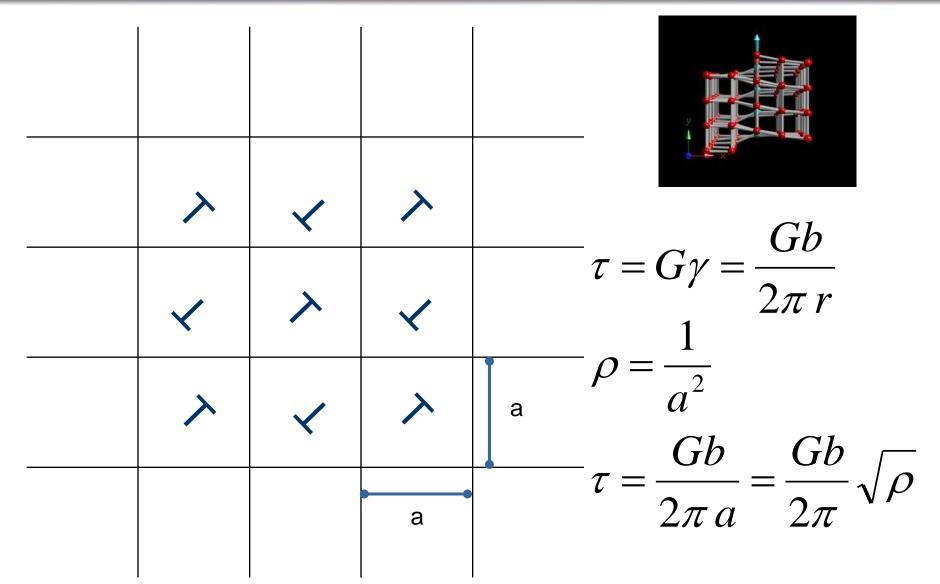
Statistical Dislocation Dynamics





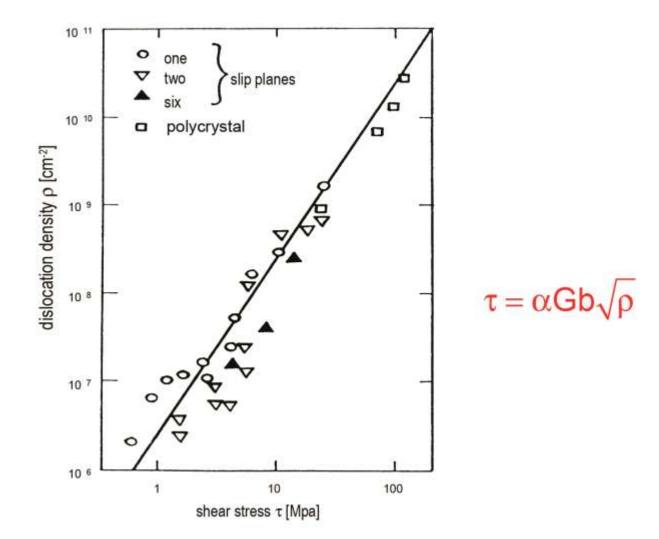
Statistical Dislocation Dynamics











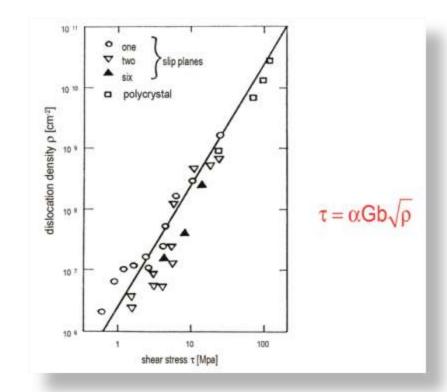
Statistical Dislocation Dynamics



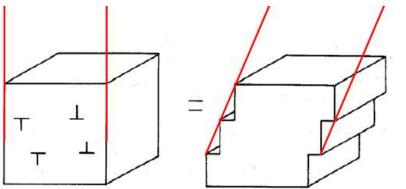
kinetics: collective dislocation behaviour

- kinetic equation of state
- structure evolution

$$\frac{d\rho}{d\gamma} = A\rho^+ + B\rho^-$$



• coupling to imposed shape change



$$\dot{\gamma} = \frac{\mathrm{d}\gamma}{\mathrm{d}t} = n\frac{\mathrm{d}x}{X}\frac{b}{Z}\frac{1}{\mathrm{d}t} = \rho_{\mathrm{m}}bv$$