Impurity ion density measurements at the plasma edge of ASDEX Upgrade using lithium beam charge exchange spectroscopy

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Abstract

The method of lithium beam charge exchange spectroscopy is used to determine the density of C^{6+} and He^{2+} impurity ions at the edge of the ASDEX Upgrade tokamak plasma. Spectrally resolved measurements are used. l-level resolved atomic capture cross sections are corrected for collisional mixing. The absolute calibration relies on simultaneous beam emission spectroscopy. Together with detailed beam attenuation modelling, impurity ion densities can be measured with good accuracy.

I. INTRODUCTION

The H-mode regime is the choice for next step tokamak devices. It is characterised by the existence of a steep gradient region at the plasma edge, forming a so-called edge pedestal. Temperature values at the pedestal top determine the temperatures that can be reached in the plasma centre due to the self similarity of core temperature profiles¹. As the physics in the pedestal region is not yet fully understood, a lot of effort has been devoted to the development of edge profile measurements with sufficient spatial resolution at ASDEX Upgrade². By measuring the impurity ion density profiles, a better understanding of the processes which determine energy and particle transport in the pedestal region can be gained.

Along with edge Thomson scattering³ and multichannel FM reflectometry⁴, the Lithium beam is a tool particularly appropriate to probe the plasma edge^{5,6,7}. At ASDEX Upgrade a fast 20-70 keV diagnostic Lithium beam is used to measure the electron density⁸ and the ion temperature⁹ at the plasma edge. While the electron density is determined from the emitted Li I (2s-2p) light, the ion temperature is derived from the line width of light emitted by impurity ions after charge exchange, i.e. electron capture from the Lithium beam donor atoms. With both installed Li-beam systems an accurate calibration of the charge exchange signal is achievable¹⁰. In this work we use the spectrally resolved charge exchange signal rather than the spectrally integrated signal. This is mandatory for the measurement of He²⁺ ion densities because of the large background signal from the cold He⁺ ions. Moreover, we show that only careful handling of the necessary atomic data in a plasma environment yield accurate impurity ion density profiles in the outer pedestal region.

In the following we give a brief description of the experimental setup followed by a detailed explanation of the calibration procedure. Then the atomic data which were prepared for this work and are now implemented in the ADAS database are compared to experimental values where possible. The influence of the plasma environment on emission cross sections is demonstrated. Subsequently, all error sources are discussed and quantified and finally some results are shown for specific plasma discharges.

II. EXPERIMENTAL SETUP

The experimental setup of the neutral lithium beam diagnostics installed at ASDEX Upgrade has been described in detail elsewhere ^{8,9}. In the following, only a short description is given, to facilitate

comprehension. The isotopically pure 7 Li ions are extracted from a β -eucryptite emitter, accelerated to the chosen energy and subsequently neutralised via charge exchange in a sodium vapour cell. In the measurements presented here, the Lithium beam energy was always set to 40 keV, optimising the charge exchange cross sections and neutralisation efficiency but compromising beam penetration into the plasma. With these settings the beam delivers a neutral beam equivalent current of about 2.2 mA within a diameter of 10-15 mm. The beam is chopped by means of horizontal deflection plates positioned between ion source and neutraliser cell with a beam on:off cycle of 60:20 ms.

A schematic view of the position of the lithium beam and its optical systems is shown in figure 0^{11} . The horizontal beam enters the plasma 32.6 cm above the tokamak midplane. The radial region of about 20 cm is observed by two optical systems: (i) The Li-IXS (Lithium beam impact excitation spectroscopy) system with a top down view images the region onto 35 fibres coupled to filter photomultiplier arrangements. The Li I (2s-2p) emission ($\lambda = 670.8$ nm) is recorded with a spatial resolution of 5 mm and a temporal resolution of 200 µs. (ii) The Li-CXS optical system images the beam-plasma interaction region from below onto an array of 56 fibres, each covering a 5 mm diameter spot. Of these fibres 10 are chosen dependent on the actual plasma edge position and are connected to the 0.75m Czerny-Turner spectrometer, equipped with a 1200 l/mm grating and a fast, back-illuminated frame-transfer CCD camera (Roper Scientific MicroMax: 512BFT). The camera was set up to record these 10 channels in frame-transfer mode with a temporal resolution of 7.8 ms. In the course of this work, a second similar system was installed, so that 16 radial positions can be recorded simultaneously with the new setup. The number of radial channels per CCD was reduced and the temporal resolution increased to 4 ms. The active charge exchange signal emitted in the small volume defined by the intersection of the respective line of sight and the Lithium beam is determined by subtraction of an averaged background of the temporally neighbouring 'beam off'-measurements from the 'beam on'-measurements. The data are subsequently fit with a Gaussian to determine the ion temperature.

Figure 2 a and b show measured spectra of the C VI (7-8) charge exchange line at 529.2 nm and the He II (3-4) charge exchange line at 468.7 nm, respectively. The data were taken in ELMy H-mode plasma discharges. While the errors of the measured spectra are equally distributed across the C VI line, there is a clear error maximum in the centre of the He II line due to the very large but spectrally narrow He II background radiation. In figure 2b it can clearly be seen that in the region of the large error bars the data are not statistically distributed within the range of these error bars. This is due to the nature of the background, namely He⁺ density fluctuations during or following ELMs. These

fluctuations lead to strongly varying intensities of the cold He II background line and subsequently to the observed pixel-to-pixel correlated noise.

In this case the Gaussian fit to the error weighted data is dominantly determined by the wide wings yielding an accurate result for the otherwise undetermined line centre. Consequently the fitting parameters are used to calculate the spectrally integrated charge exchange signal S_Z^{CCD} .

III. ABSOLUTE CALIBRATION

This signal S_Z^{CCD} is the locally emitted intensity multiplied by an absolute calibration factor C_Z^{CCD} . The intensity depends on the impurity ion density n_Z , the charge exchange emission rate $\langle \sigma v_{Li} \rangle$ and the Lithium beam density n_{Li} . The signal can be written as

$$S_{Z}^{CCD} = C_{Z}^{CCD} v_{Li} n_{Z} n_{Li} \sigma_{\lambda}^{eff}$$
(1)

where $\sigma_{\lambda}^{\text{ eff}}$ is the beam weighted effective emission cross section

$$\sigma_{\lambda}^{\text{eff}} = \sum_{nl} N_{\text{Li}}(nl) \, \sigma_{\lambda}^{\text{eff}}(nl) \tag{2}$$

Here $N_{Li}(nl)$ is the relative occupation number of Li(nl) atoms in the beam, which is calculated by the beam attenuation code and is temporally and spatially dependant on the plasma electron density and temperature. $\sigma_{\lambda}^{eff}(nl)$ denotes the effective emission cross section in a plasma environment after electron capture from a lithium atom in the state nl (see also next chapter).

Determination of the Lithium beam density and of the calibration factor is not necessary in this setup, because the Li I (2s-2p) emission is monitored on every plasma discharge with the Lithium beam IXS (impact excitation spectroscopy) system used to measure the edge electron density⁸. The signal S_{2p} that is collected by a filter-photomultiplier arrangement can be written as $S_{2p}^{PM} = C_{2p}^{PM} n_{Li} N_{2p} \tau^{-1}$, with C_{2p}^{PM} the absolute calibration factor for this optical system, n_{Li} the local particle density in the neutral beam, N_{2p} the relative occupation of the 2p level and $1/\tau$ the transition probability of the Li I (2s-2p) transition.

For every spatial position of the charge exchange system the relation of the calibration factors C_{2p}^{CCD}/C_{2p}^{PM} is determined by setting the spectrometer to the Li(2s-2p) transition line at 670.8 nm and comparing the signals S_{2p}^{CCD} and S_{2p}^{PM} :

$$S_{2p}^{PM} / S_{2p}^{CCD} = C_{2p}^{PM} / C_{2p}^{CCD}.$$
 (3)

The impurity ion density can now be derived from

$$n_Z = S_Z^{CCD}/S_{2p}^{PM} C_{2p}^{PM}/C_{2p}^{CCD} C_{2p}^{CCD}/C_Z^{CCD} N_{2p}/(v_{Li} \tau \sigma_{\lambda}^{eff}). \tag{4}$$

Here the first term consists of the two measured signals on the CXS system and the IXS system, the second term is the measured relative response of the two systems to the Li I (2s-2p) transition, the third term is the relative response of the spectrometer system at the two different wavelengths which was accurately determined using an absolutely calibrated light source. The last term is composed of the constants v_{Li} , τ and σ_{λ}^{eff} as well as the relative occupation number of the Li(2p) level, N_{2p} . The latter can be determined in two ways: (i) it is routinely calculated during the evaluation procedure of the Li-IXS diagnostic, and (ii) it can be calculated in a forward calculation of the beam-attenuation code with the measured electron density and temperature profiles as input. For both methods the routinely used and well tested Lithium beam attenuation code is used 12. It consists of a system of coupled differential equations for the occupation numbers N_{nl} of the Lithium beam, taking into account excitation and de-excitation processes of Li atoms due to collisions with electrons, protons and impurities. Ionisation, charge exchange processes and radiative transitions are also included.

IV. ATOMIC DATA

In order to determine the (n,l)-resolved charge exchange cross sections in collisions of Li atoms with C⁶⁺, calculations using the classical trajectory Monte Carlo (CTMC) method¹³ have been performed. This procedure involves numerically solving Hamilton's equations for a three-body system interacting solely via the Coulomb interaction. Numerous trajectories are integrated to emulate a mono-energetic beam of incident ions and to produce statistically reliable electron capture cross sections. A detailed description of the applied methods can be found in reference [14].

Atomic orbital close coupling calculations¹⁵ (AOCC) for He²⁺ colliding with Lithium atoms in various initial states (2s,3s,2p,3p,3d) have been performed using a single set of basis states. The expansion includes travelling atomic orbitals on the He²⁺ centre (n-shells 1 - 6) and Li I states up to Li(5g). The latter states have been obtained by diagonalisation of the atomic Hamiltonian with a model potential. In addition to bound states pseudo-states on both centres are included which improve the convergence behaviour and represent ionisation. Altogether, the expansion consists of 87 states on the He centre and 49 on Li. From these calculations partial cross sections for charge exchange into He II(nl) (n=1-6) have been derived in an energy range of 1.5 - 20 keV/amu. The accuracy is 5-10% for cross sections > 10^{-15} cm² and 30-40% for those < 10^{-16} cm².

The determined state selective electron capture cross sections were written in the ADAS adf01 file format and thus made available for use with the ADAS program package¹⁶. The Atomic Data and Analysis Structure (ADAS) is a collection of codes and data for modelling the radiative properties of ions and electrons in plasmas (http://adas.phys.strath.ac.uk/). The code ADAS308 used in this work calculates effective emission cross sections taking into account all relevant effects occurring in a plasma environment (*l*-level mixing and cascade contributions applying branching ratios) for given relative velocities between Li atoms and impurity ions.

A comparison of the calculated emission cross sections without l-mixing (no plasma environment) with available measurements is shown in figure 0. The data sets for the He^{2+} , C^{6+} + Li(2s) collisions measured at the Kernfysisch Versneller Instituut ¹⁷, ¹⁸ are both consistently lower than the calculated values, the data measured by Aumayr et al. ¹⁹ for He^{2+} + Li(2s) agree very well with the calculated ones. The agreement between calculated and measured data for collisions with the Li(2s) ground state justifies a high confidence in the data for excited initial Li(nl) states.

The importance of collisional mixing for the determination of effective emission cross sections was shown for charge exchange with deuterium neutral beams²⁰. In the case of the Lithium beam edge diagnostic, it is even more important to take into account collisional mixing, because the plasma parameters change rapidly across the plasma edge. In figure 4 an example is given of the radial variation of the C VI effective emission cross section for discharge #18055 at t = 3 - 5 s. The electron density and temperature profiles (fig. 4a) show the characteristic steep gradients of an H-mode. In figure 4b and 4c for C^{6+} and He^{2+} , respectively, the effective emission cross sections $\sigma_{\lambda}^{eff}(2s)$ and $\sigma_{\lambda}^{eff}(2p)$ as calculated by the ADAS routine for the given electron and temperature profiles are plotted versus a normalised radius (ρ_{pol} is normalised to poloidal flux, ρ_{pol} =1 indicates separatrix position). Also indicated (dotted lines) are emission cross sections for no 1-mixing scenarios (upper

boundary) as well as emission cross sections calculated under the assumption of complete collisional mixing (fully mixed, i.e. statistical population of states immediately after electron capture, lower boundary) for electron capture from Li(2s). It can clearly be seen that the correct treatment of l-level mixing in the cross sections has a strong impact on the determination of impurity ion densities. For the case of carbon, at ρ_{pol} =0.9, the calculated emission cross sections are reduced as compared to the no l-mixing emission cross sections by factors 1.6 and 2.7 for electron capture from Li(2s) and Li(2p), respectively. For Helium the reduction factors are somewhat smaller, 1.14 and 1.94, which is due to the fact that the upper level of the C VI line radiation consists of more l-levels (n=8) than that of the He II transition (n=4). Moreover, the radial change in emission cross section in the observed region has a direct influence on the measured impurity ion density gradient.

V. ERRORS

As the impurity ion densities are derived from a number of separate input data, the determination of an absolute error is not trivial. The main input data are: the CCD measurements of the charge exchange signal, the absolute calibration factors derived from cross calibration with the IXS system, the effective emission cross sections and the calculated Li-beam composition from the attenuation code. In the following we point out potential error sources and quantify them where possible.

As already shown in section II. the statistical errors of the averaged and background corrected data taken by the CCD are used as weights for the fitting routine (see figure 2). With the resulting fitting parameters the spectrally integrated charge exchange signal is calculated and with the corresponding errors of the fitting parameters a statistical error can be determined. For the spectra shown in figure 2 the signal is calculated to be 249 +/-18 (7%) counts and 1559 +/-162 (10.4%) counts for the C VI and the He II line, respectively, which are typical statistical errors of the measurements. In the case of helium, for plasma temperatures below 80 eV the statistical errors from the Gauss fit become too large for a reasonable impurity ion density evaluation.

The relative calibration between IXS and CXS system is accurate to less than 4%, but it must be ensured that there is no cross talk between CXS channels at all wavelengths used. Moreover, the beam position must be monitored carefully, as the upper optical system collects light from a wider spot normal to the beam direction than the lower system. To detect a relative shift in the horizontal plane between the upper and the lower optical system, two fibres from the lower optical system are permanently connected to additional filter-photomultiplier detectors monitoring the Li I (2s-2p)

resonance line. If the monitored beam position is stable from one plasma discharge to the next, one reference measurement (spectrometer set to Li I at 670.8 nm) per experimental day is sufficient.

Atomic data have estimated errors up to 10% for processes with a relevant contribution to the signal. Those charge exchange cross sections with larger errors are generally smaller than 10^{-16} cm² and either occur in collisions of highly excited Li(n*l*) or the electrons are captured into final n-states that are far away from the observed transition. In both cases the contribution to the measured signal and thus to the resulting error is very small (< 1%).

Treatment of collisional mixing has not been verified experimentally up to now, so that an error estimate cannot be given.

The assumption of just one collision energy rather than integrating over a Gauss distribution of the impurity ion energies is justified as long as the Li-beam energy is much higher than the impurity ion energy. With a maximum temperature of 1200 eV in the observed plasma edge region the velocity of a He²⁺ ion is 0.3 keV/amu compared to 5.7 keV/amu for a 40 keV Lithium beam. Even if the Li-beam energy is varied between 35 and 45 keV, the total effective emission cross section (weighted with the Li-beam composition) changes by less than 3% for given electron density and temperature profiles. Finally, the calculated composition and attenuation of the Li-beam is accurate to less than 5% for n < 4, as could be demonstrated by the comparison of calculated and experimentally determined radial profiles of the most relevant excited states Li(2p) and Li(3d)¹².

Taking all errors into account (except from collisional mixing) a systematic error of 20% has to be added to the statistical errors from the measurements. The latter stems from the photon statistics of the charge exchange measurements and the subsequent fit to the measured data. The error variation depends mainly on the impurity ion density and the local current density of the Lithium beam.

VI. RESULTS IN EXAMPLES

Figure 5 shows the C⁶⁺ density profile of discharge #18055 as measured by the Lithium charge exchange system together with the edge portion of the profile measured with the core charge exchange system²¹. The plasma discharge is an H-mode with a plasma current of 0.8 MA, a central line averaged density of 5.5 10¹⁹ m⁻³, and heated with 5 MW neutral beam injection. The plasma parameters were chosen to obtain an ELMy H-mode with low ELM frequency, so that the CCD camera frames which contain an ELM can be disregarded for the evaluation of the ion temperature. For the edge system, the C⁶⁺ densities are evaluated with three different cross sections: no collisional mixing taken into account, full collisional mixing over the whole radial length and collisional mixing

calculated with the ADAS package with the measured electron density and temperature profiles as input. Clearly, there is a large difference not only in the absolute values of the density but also in the resulting edge gradient, demonstrating the importance of a proper treatment of collisional mixing. The carbon concentration (n_{C6+}/n_e) is 0.7 +/- 0.1 % at normalised radii $\rho_{pol} = 0.9 - 0.95$. In discharge #18053, a similar H-mode discharge with a slightly higher central line averaged density of 6.3 10^{19} m⁻³, a He²⁺ concentration (n_{He2+}/n_e) of 25 +/- 4% was measured at $\rho_{pol} = 0.9 - 0.95$.

The He²⁺ densities were also measured in ohmic discharges in ASDEX Upgrade. The selected discharge, only 27 plasma discharges (3rd day) after wall boronisation, was carried out early in the morning, immediately after a 10 minute glow discharge in helium, a routine machine conditioning procedure at the beginning of an experimental day. A line integrated density of 3.8 10^{19} m⁻³ with no additional heating characterises the later part of the discharge, which is kept constant for two seconds. Figure 6 shows the electron and ion temperature profiles, the electron density profile, and the measured He²⁺ ion density for discharge #20463 for the constant phase from 3.5 to 5.0 s. In such low density discharges a typical concentration ($n_{\text{He2+}}/n_{\text{e}}$) of around 12-15% He²⁺ can be observed at a major radius between R=2.09 and 2.13 m corresponding to a normalised poloidal radius ρ_{pol} of 0.91 and 0.99. In an earlier part from 1.7 to 2.3 s the discharge has an even lower line averaged density of 2.5 10^{19} m⁻³. Here the concentration rises to 20%, indicating that the He²⁺ impurity ion density stays approximately constant for both density steps ($n_{\text{He2+}}$ = 4-5 10^{18} m⁻³).

VII. CONCLUSIONS

The method of lithium beam charge exchange spectroscopy has been refined in this work, especially for the density measurement of C^{6+} and He^{2+} impurity ions at the plasma edge of the ASDEX Upgrade tokamak. Absolute calibration is achieved by simultaneous beam emission spectroscopy. The atomic data for electron capture from various initial Li states into nl-resolved final states of C^{5+} and He^{+} have been added to the ADAS data base.

For the correct determination of the impurity ion density gradient at the plasma edge it is important to include collisional mixing when calculating emission cross sections. The C^{6+} concentration (n_{C6+}/n_e) can be determined with high accuracy and is at present < 1%. The quality of the He^{2+} ion density data is excellent in low density discharges, because fitting to the spectrally resolved data allows the determination of the line centre which is dominated by spectrally narrow He II background radiation. After boronisation, a He concentration (n_{He2+}/n_e) between 12 and 20% is found in low density ohmic

discharges. Impurity ion densities can be measured in H-modes in between ELMs by disregarding CCD camera frames which contain ELM induced signals.

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FIGURES

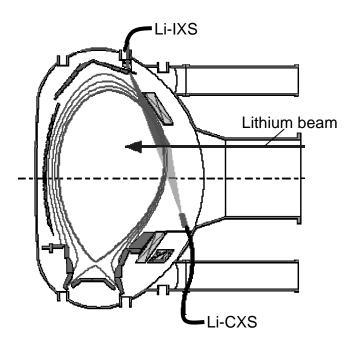


Figure 1: Toroidal cross section of ASDEX Upgrade with the position of the lithium beam and the two optical heads, one looking from above (Li-IXS) and the other from below (Li-CXS) on the beam.

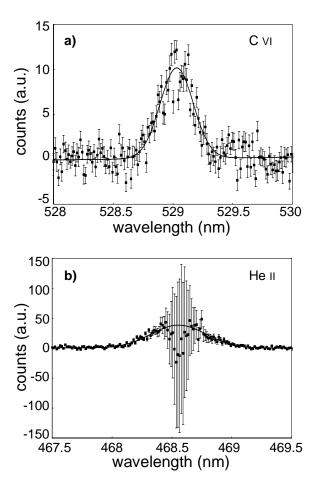


Figure 2: H-mode charge exchange spectra of a) carbon (#18055, t=3-5s, $T_i = 770$ eV, $\rho_{pol} = 0.97$) and b) helium (#18053, t=3.5-4.2s, $T_i = 950$ eV, $\rho_{pol} = 0.97$). Helium background radiation is much stronger due to ELMs and recycling from the vessel walls but restricted to a narrow spectral range. Thus, error bars (including correlated noise, see text) are large in the central wavelength region. C VI background radiation affects the whole line width.

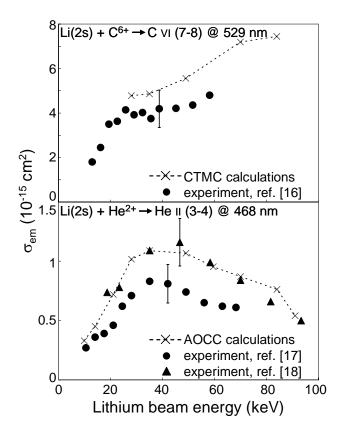


Figure 3: Comparison of calculated and measured emission cross sections for Li(2s) colliding with a) C^{6+} and b) He^{2+} .

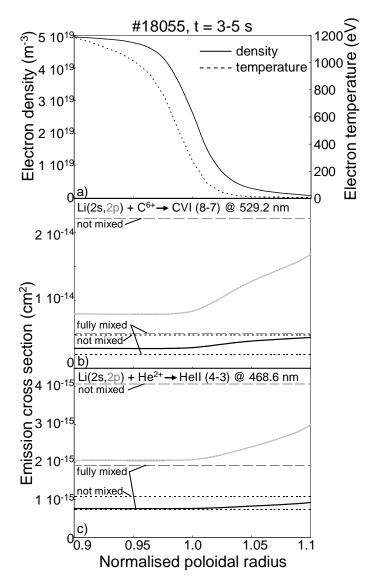


Figure 4: a) Electron density and temperature profiles for H-mode discharge #18055 at t=3-5 s. These profiles are used to calculate emission cross sections for b) C⁶⁺ at 529 nm and c) He²⁺ at 468 nm. The black solid lines denote capture from the Li(2s) ground state, the grey solid lines denote capture from the Li(2p) excited state. Also indicated are emission cross sections calculated with no collisional *l*-level mixing (upper boundary) as well as emission cross sections with full collisional *l*-level mixing (lower boundary).

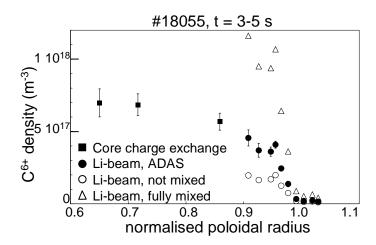


Figure 5: C⁶⁺ ion density profiles are shown for the H-mode discharge #18055 at t= 3-5 s. The full square symbols denote measurements from the core charge exchange system. The full circular symbols represent the Lithium beam measurements evaluated with emission cross sections calculated with the ADAS package and taking into account *l*-level mixing. The open symbols show the same measured data but evaluated without *l*-level mixing (circles) or full (i.e. statistical occupation) *l*-level mixing (triangles).

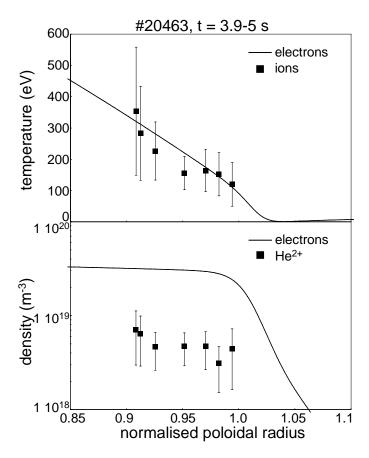


Figure 6: Electron and ion temperatures (upper graph) as well as electron and He^{2+} densities (lower graph) are shown for the standard ohmic discharge #20463 averaged over the time period t=3.9-5 s.

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