Characterization of optical systems for the ALPS II experiment

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Abstract: ALPS II is a light shining through a wall style experiment that will use the principle of resonant enhancement to boost the conversion and reconversion probabilities of photons to relativistic WISPs. This will require the use of long baseline low-loss optical cavities. Very high power build up factors in the cavities must be achieved in order to reach the design sensitivity of ALPS II. This necessitates a number of different sophisticated optical and control systems to maintain the resonance and ensure maximal coupling between the laser and the cavity. In this paper we report on the results of the characterization of these optical systems with a 20 m cavity and discuss the results in the context of ALPS II.

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1. Introduction

Long baseline, low-loss optical cavities are used in a number of different applications including gravitational wave detectors [1] and magnetic vacuum birefringence experiments [2]. In addition to being essential to these projects, optical cavities can also be used to improve the sensitivity of Light-Shining-through-Wall (LSW) experiments [3–5].

These experiments are designed to detect theoretically proposed and astrophysically motivated weakly-interacting-sub-eV-particles (WISP) [6]. This experimental approach is characterized by shining a light source at an opaque wall. Before the wall some photons will convert to WISPs and these WISPs will traverse the wall into the regeneration side of the experiment [7]. There, the WISPs will reconvert to photons which are measured with a single photon detection scheme. Optical cavities have been used before the wall to increase the number of photons creating WISPs, such as in the Any Light Particle Search I (ALPS I). A cavity can also be used after the wall to increase the probability that WISPs will reconvert to photons. The cavities before and after the wall will be referred to as the production cavity and the regeneration cavity, respectively. LSW experiments typically include dipole magnets in their design to search for axion-like particles.

ALPS II [8] is a second generation LSW experiment currently being prepared at DESY in Hamburg. It will consist of a production and a regeneration cavity each with a length of 100 m. Each of the cavity Eigenmodes will pass through a string of 5 T superconducting dipoles that form 88 m of magnetic length. The design sensitivity of ALPS II will surpass current limits for the detection of axion-like particles by three orders of magnitude set by other experiments of its kind [9–11].

The cavities on both sides of the wall must maintain their resonance condition such that they can sustain 95% of their designed power buildup for an extended period of time to ensure that the experiment meets its sensitivity goals. This requires a number of different controlled optical systems. Our goal for ALPS II is that the control systems described in this paper are individually capable of suppressing their respective noise sources such that they do not reduce the power buildup in the cavities by more than 1%. The optical technologies and the frequency and alignment control schemes were tested using an optical cavity with a length of 20 m in an attempt to meet these goals for the ALPS II power noise. Furthermore, an in-depth characterization of the optical losses, control loop couplings, and environmental noise sources is required to understand and probe the stability and robustness of the setup.

With a length of 100 m the ALPS II production cavity will be set up in a nearly semi-confocal configuration using a 250 m radius of curvature in-coupling mirror and a flat out-coupling mirror. The Eigenmode of the cavity will have a waist at the out-coupling mirror with a radius of 6.4 mm while the beam radius of Eigenmode at the in-coupling mirror will be 8.3 mm. The cavity will be over-coupled and have a designed power buildup factor of 5000 giving it a finesse of 8000. This will allow the cavity to achieve 150 kW of circulating power. With a free spectral range of 1.5 MHz the linewidth of the cavity will be 185 Hz.

In this article we report on the progress of these efforts. Section 2 describes the optical setup
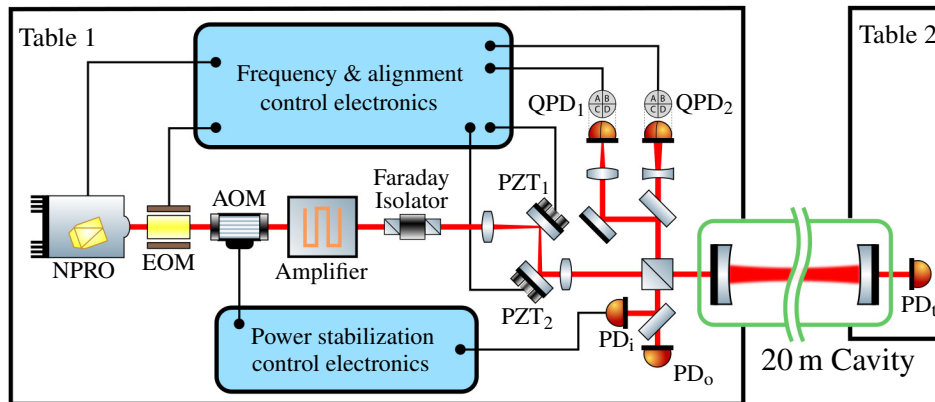
Fig. 1. Diagram of the current optical setup with control electronics for the frequency stabilization, automatic alignment, and power stabilization. An NPRO laser provides the beam which is modulated with EOM and AOM, and then amplified to an output power of 35W. A fraction of this light is incident on the 20 m cavity. The photodetectors QPD_1 and QPD_2 in reflection of the cavity are used to generate the PDH and automatic alignment error signals. The PDH error signal is fed back to a PZT on the NPRO crystal as well as a heater that actuates the crystal temperature. The automatic alignment error signals are sent to the alignment PZTs which are located at the same Gouy phase position as their corresponding photodetectors. This is displayed by PZT_1 and QPD_1 both occupying a waist position while PZT_2 and QPD_2 are both located at a far field position in the beam. A power stabilization scheme uses the AOM as an actuator with the sensing performed by PD_i. PD_o measures the out-of-loop power noise. The cavity mirrors are located on separate tables and the vacuum system is shown in green. PD_t measures the power noise in transmission of the cavity.

of this test experiment. The experimental results are presented and discussed in Section 3 and conclusions are drawn in Section 4.

2. Setup

The setup consists of a 20 m optical cavity with the mirrors on two separate optical tables as shown in Fig. 1. The cavity mirrors are two inches in diameter with a radius of curvature of 23.2 ± 0.5 m giving the cavity a nearly confocal configuration. The transmissivity of the mirrors was measured to be 878 ± 2 ppm. The resonant Eigenmode of the cavity that is used for stabilizing the laser frequency is the Hermite-Gauss U_{00} mode defined in [12]. It has a beam waist of 1.97 ± 0.02 mm and a mode radius of 2.62 ± 0.01 mm at the cavity mirrors. For a loss free cavity the calculated finesse is 3577 ± 8 and the linewidth is 2097 ± 5 Hz. This corresponds to a storage time of 151.8 ± 0.3 μs.

A vacuum system houses the two cavity mirrors and the measurements were taken at a pressure of $5 \cdot 10^{-5}$ mbar. A dedicated lab hosts the 20 m vacuum envelope and the optical tables in a clean environment.

The laser system consists of a non-planar-ring-oscillator (NPRO) master laser and a $Nd:YVO_4$ amplifier [13]. To avoid thermal effects in this experiment we inject only 50 mW of power into the cavity. The laser, developed for the LIGO gravitational wave detector, delivers a single frequency beam with a high fundamental mode content.

The laser frequency is stabilized to a resonance of the cavity using the Pound Drever Hall (PDH) frequency stabilization technique [14, 15]. The required phase modulation at 2.5 MHz is created with an Electro Optic Modulator (EOM). For frequency actuation the control loop uses a Piezo (PZT) actuator mounted to the NPRO crystal for fast frequency correction and

the temperature of the NPRO crystal to stabilize long term frequency drifts. The control loop operates with unity gain frequencies up to 55 kHz.

In addition, an automatic alignment system was built using the quadrant photodetectors QPD_1 and QPD_2 to do differential wavefront sensing in order to maintain the alignment of the injected beam with respect to the cavity Eigenmode [16]. The actuation is done with the two axes alignment piezo mirrors PZT_1 and PZT_2 (see Fig. 1). We were able to realize unity gain frequencies of 170 Hz actuating on PZT_2 and 15 Hz actuating on PZT_1.

The photodetector PD_i is used as a sensor for the power stabilization while the Acoustic Optic Modulator (AOM) is used as an actuator for the control loop. The out-of-loop photodetector PD_o measures the resulting power noise at a pick off in front of the cavity. We achieved a unity gain frequency of 1 kHz with a suppression of 60 dB at 10 Hz. The photodetector PD_t on table 2 measures the light transmitted through the cavity.

3. Measurements

ALPS II aims to achieve high power buildup factors of the optical cavities as well as 95% spatial overlap between their Eigenmodes and the mode of the laser. Therefore, the characterization and mitigation of losses in the cavity and a high visibility is essential.

The visibility of the cavity, which refers to the ratio of power reflected from the incoupling mirror on and off resonance, was found to be greater than 95%. This indicates that the higher order spatial mode content and mode mismatch of the input beam is less than 5%.

Two independent methods are used to accurately measure the internal cavity losses. The first method measures the pole frequency of the cavities low-pass filter property [17]. The linewidth is equal to twice the pole frequency and a high finesse corresponds to a high power build up factor in the cavity. This measurement reveals a linewidth of 2460 ± 20 Hz in vacuum and 2370 ± 70 Hz in air which corresponds to a finesse of 3050 ± 20 and 3170 ± 90, respectively.

The second method measured the cavity storage time by observing the exponential decay of the light leaking from the output mirror of the cavity after the input power is instantaneously reduced [18]. The cavity storage time ($\tau_{storage}$) is 134 ± 10 µs for the in air case leading to a finesse of 3160 ± 240. Thus, the two results agree very well.

This corresponds to a measurement of 230 ± 50 ppm internal losses within the cavity for the pole frequency measurement in air. The pole frequency measurement in vacuum yields internal losses of 300 ± 20 ppm. The additional losses could potentially be explained by scattering on point defects, dust, or the micro-roughness of the mirror surfaces. The intracavity losses appear to have some dependence on the location of the Eigenmode on the cavity mirrors. Further investigations of this are required.

The frequency stabilization scheme is very robust. Long term drifts are compensated by the automatic alignment and the feedback to the temperature of the NPRO. The range for the latter is up to 30 GHz corresponding to cavity length changes of 2 mm. A stable resonance condition was maintained for more than 48 hours before the control loop was manually disengaged.

The optical systems for the current setup are evaluated by measuring their ability to suppress the relative power noise in transmission of the cavity. Suppressing this noise while minimizing the amount of light reflected from the input mirror ensures that there is maximum power circulating inside the cavity. We investigated three noise sources which contribute to the cavity transmission power noise. These are the differential frequency noise between the laser and the cavity resonance, the alignment noise between the input beam and the cavity Eigenmode, and the power noise of the laser. The following sections detail measurements of all three noise sources and project them in terms of their contribution to the relative power noise in transmission of the cavity.
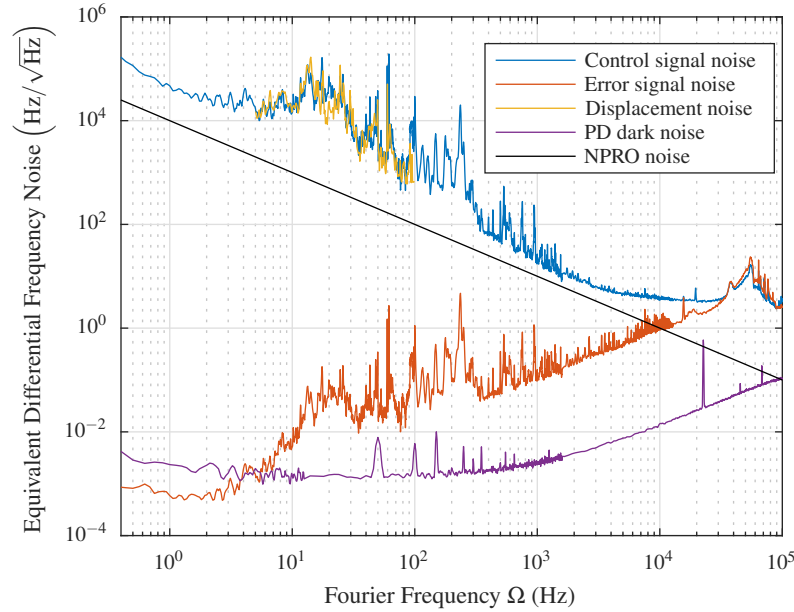
Fig. 2. Spectral densities of the control and error signals of the frequency stabilization control loop calibrated in terms of differential frequency noise are shown in blue and orange respectively. A non-coincident geophone measurement of the differential displacement noise between the optical tables is plotted in yellow. This measurement represents the length noise of the cavity due to ground motion. The electronic noise of the PDH sensing is shown in purple and a typical trace of the NPRO frequency noise is plotted in black [19].

3.1. *Cavity frequency noise*

Figure 2 shows spectra of the electronic noise at various points of the frequency control electronics. These spectra are calibrated as equivalent differential frequency noise which refers to the difference between the resonant frequency of the cavity and the frequency of the laser. We will refer to this as the differential frequency. The blue curve is the control signal that is sent to the laser piezo to stabilize its frequency with respect to the cavity. When expressed as frequency noise below the unity gain frequency of the control system this gives the differential frequency fluctuation of the uncontrolled system (free running).

The orange curve is the spectrum of the measured noise at the error point of the control electronics divided by the cavities transfer function. This division is required to calibrate the error point noise in terms of differential frequency noise. Therefore the orange curve represents an in-loop measurement of the differential frequency noise with suppression from the frequency stabilization control scheme. The system was able to reach a unity gain frequency up to 55 kHz before becoming unstable. At 20 Hz we have roughly six orders of magnitude suppression of the free running noise.

The yellow curve is a measurement of the differential displacement noise from two Mark Products L-4C geophones placed on tables 1 and 2 and oriented in the direction of the optical axis of the cavity. The differential displacement noise measured by the geophones is calibrated to differential frequency noise in the cavity with Eq. (1).

$$\frac{\Delta f}{f} = \frac{\Delta L}{L} \tag{1}$$

Here Δf is the frequency change of the cavity resonance due a displacement ΔL between the mirrors of the cavity. f is the laser frequency and L distance between the cavity mirrors.

Figure 2 shows that the control signal noise closely follows the seismic noise from 5 Hz to 100 Hz. This demonstrates that in this region the displacement noise between the mirrors couples to the differential frequency noise. Differences between these two curves can be attributed to the fact that these measurements were not performed coincidentally. Differential displacement noise dominates the RMS for frequencies below 400 Hz.

The black line is a representation of the typical frequency noise of a free running NPRO laser like the one we are using [19]. As Fig. 2 shows, NPRO noise is the dominating noise source from 400 Hz to 10 kHz. Above 10 kHz the control signal noise is elevated by the limited phase margin of the control electronics.

The purple curve is a measurement of the error signal noise divided by the cavity transfer function when the laser system is turned off. This shows the effect of photodetector dark noise on the frequency stabilization scheme and represents a lower limit on the possible suppression of the frequency noise.

The coupling between the differential frequency noise and the power noise in transmission of the cavity is not linear. Therefore an analysis of the RMS of the differential frequency noise in terms of the cavity linewidth is insufficient for projecting the transmitted power noise. To perform this projection we model the remaining phase noise as if it were caused by the laser. This is done by solving Eq. (2) with the measured error signal representing the differential phase $\phi(t)$ [20].

$$E_{\text{cav}}(t) = \sqrt{R_1 R_2 (1-l)} E_{\text{cav}}(t-\tau) + \sqrt{T_1} E_{\text{in}}(t) \cdot e^{-i\phi(t)} \tag{2}$$

Here $E_{\text{cav}}(t)$ gives the field circulating inside the cavity. It is clearly dependent on phase and amplitude of the input field $E_{\text{in}}(t)$. There is no phase term in $E_{\text{cav}}(t-\tau)$ since the cavity is assumed to be on resonance. R_1 and R_2 are the power reflectivities of the in and out-coupling mirrors, while T_1 is the power transmissivity of the in-coupling mirror. τ is the light travel time for one round trip through the cavity and l represents the extra losses inside the cavity. This equation was solved iteratively using a time series of the error signal noise calibrated in terms of phase. The spectra of the projected differential frequency noise contribution to the power noise in transmission of the cavity is shown in Fig. 3.

It is important to note that a small offset in the error signal will increase the coupling from differential frequency noise to power noise in transmission of the cavity. Therefore we minimized the linear component of the coupling before the measurement.

3.2.   Pointing noise

Small misalignments between the Eigenmode of the cavity and the input beam can be expressed as the latter having a small amount of power in the Hermite-Gauss U_{01} and U_{10} modes defined by the cavities Eigenmode basis. Previous works have chosen to quantify this in terms of the parameter ϵ by writing the input laser as a superposition of the spatial eigenmodes of the cavity as shown in Eq. (3) [16].

$$U_{\text{in}} \approx A[U_{00} + \epsilon_x U_{01} + \epsilon_y U_{10}] \tag{3}$$

Here ϵ represents the relative field amplitude of the U_{01} or U_{10} modes with U_{01} corresponding to a horizontal misalignment and the U_{10} to a vertical misalignment. For small values of $|\epsilon|$ Eq. (4) gives an expression for A.

$$A = 1 - \frac{1}{2}|\epsilon|^2 \tag{4}$$

Equations 3 and 4 show that the power noise in the U_{00} mode of the cavity is given by $|A|^2$ which simplifies to $1 - \epsilon$ for $|\epsilon| \ll 1$. This is the case when the system is aligned and the automatic alignment control is engaged. Consequently, higher order terms of ϵ are not considered. The

contribution of higher order modes to the power noise in transmission of the cavity is also not considered as it will be significantly less than that of the U_{10} and U_{01} modes in this case.

In addition to having vertical and horizontal components, ϵ also has real and imaginary parts as shown in Eq. (5) for the x component.

$$\epsilon_x = \frac{\delta x}{w_o} + i\frac{\delta\phi_x}{\theta_o} \tag{5}$$

The real part of ϵ_x describes the relative lateral displacement between the waist positions of the modes. δx is the lateral offset between the parallel optical axes of the modes and w_o is the beam radius at the waist. The imaginary part of ϵ_x gives the angular misalignment of the two beams. $\delta\phi_x$ is the angular mismatch between the optical axes while θ_o is the divergence half angle of the beams. PZT_1 is located at a waist position and actuates on the imaginary part of ϵ while PZT_2 is located in the far field of the laser beam and actuates on the real part of ϵ.

The contribution of pointing fluctuations to power noise in transmission of the cavity was projected by measuring the real and imaginary parts of the vertical and horizontal components of ϵ. This measurement was performed by taking coincident time series of the error point of each of the four automatic alignment channels.

The error point of each of these channels was calibrated in terms of ϵ by engaging the automatic alignment control system and introducing a single frequency sinusoid to the error point along with an additional voltage offset. The spectrum of the power noise in transmission of the cavity as a function of the amplitude of the sinusoid was then measured to determine ϵ.

The sum of the squares of the four calibrated time series was filtered by the cavity transfer function to produce the time series of the projected pointing noise contribution to power noise in transmission of the cavity. The spectra of this projection is displayed in yellow Fig. 3 as the projected laser pointing noise.

3.3. Power noise

The laser power noise spectrum is measured with the out-of-loop photodetector PD_o. The performance is currently limited by the electronic noise of the in-loop photodetector below a Fourier frequency of 500 Hz. However, peaks in the power noise spectrum which dominate the free running RMS noise are suppressed by the control loop. The contribution of the intrinsic power noise of the input beam to the power noise in transmission of the cavity can be found by multiplying the laser's power noise spectral density by the transfer function of the cavity as shown in Fig. 3.

3.4. Relative power noise in transmission of the cavity

Figure 3 shows a plot of the relative power noise in transmission of the cavity along with projections of the three noise sources we investigated. These are the differential frequency and pointing noise of the input beam with respect to the cavity Eigenmode and the power noise of the input beam. The total RMS of the measured transmission power noise spectrum is 4.0×10^{-4}. The three projections have a total RMS of 3.5×10^{-4}, 5×10^{-5}, and 1.3×10^{-4}, for the projections of the differential frequency noise, pointing noise, and input beam power noise respectively. Therefore all three of these control systems meet the 1% power noise goal described in Section 1 by better than a factor of twenty. The RMS of sum of the three noise projections is 3.8×10^{-4}. Thus we can attribute 95% of the RMS of the cavity transmission power noise to these three noise sources.

The spectrum of the power noise in transmission of the cavity has three regions with distinct features. A low frequency region below 20 Hz where the noise increases as the frequency decreases, a middle region from 20 Hz to 2 kHz in which the spectrum is relatively flat, and a high frequency region above 2 kHz at which point the noise rolls off with a f^{-1} slope. The
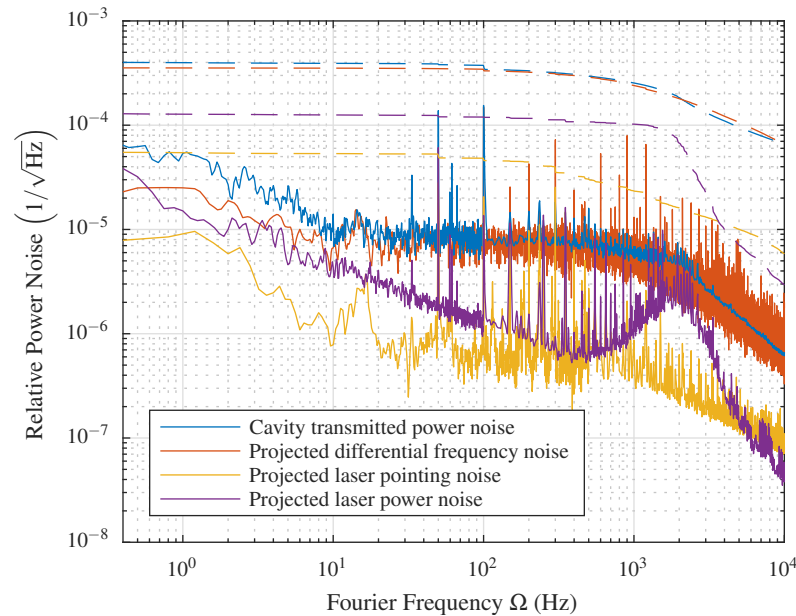
Fig. 3. Noncoincidently measured linear spectral densities of the relative power noise in transmission of the cavity along with projections of the transmitted power noise due to differential frequency, pointing, and input beam power noise. The dashed lines denote the integrated RMS of each of the spectral densities.

broadband noise below 20 Hz is responsible for 3% of the RMS and the peaks at 100 Hz and 50 Hz are responsible for 8% and 2% of the RMS respectively. The noise above 100 Hz accounts for 85% of the RMS.

The projected differential frequency noise accounts for 90% of the RMS power noise in transmission of the cavity. The spectrum of this projection closely follows the shape of the measured transmission power noise. A broad peak at 15 Hz can be seen clearly in the projection as well as in the measured power noise. Our calculations suggest that the 5% of cavity transmission RMS power noise that is unaccounted for by the projections sets the maximum DC frequency offset between the cavity resonance and the laser at 7.5 Hz.

As Fig. 3 shows, the spectrum of the projected pointing noise is significantly below the measured power noise spectrum in transmission of the cavity. The automatic alignment system suppresses the transmitted power noise in two ways. First, by compensating for relative pointing fluctuations between the Eigenmode of the cavity and the input beam and second by reducing the coupling of pointing noise to transmitted power noise by maintaining the ideal alignment between the input beam and the cavity Eigenmode. Since only 5% of the current RMS of the measured cavity power noise is unaccounted for we assume that any offset in $|\epsilon|$ must be less than 0.02.

4. Conclusions and implications for ALPS II

These results demonstrate that in the given environment we can stabilize a laser to a long baseline cavity with a finesse above 3000 for extended periods of time while coupling more than 95% of the incident light into the cavity. The frequency stabilization scheme, automatic-alignment controls, and input power stabilization all work together to suppress the RMS power noise of the light in transmission of the cavity. These systems were able to reduce the RMS to 0.04% of the power transmitted through the cavity and meet their respective goals for ALPS II. The

current measured losses would limit the power buildup factor for the ALPS II production cavity. Therefore, further work must be done to characterize and mitigate the extra losses in the cavity.

We assume that the pointing noise is predominately from the input beam and we do not believe it will significantly change for ALPS II. Therefore, this noise is not expected to prevent the production cavity from maintaining its required circulating power. The larger Eigenmode of ALPS II will actually suppress the impact of pointing noise from the input optics on the real part of ϵ. Using a cavity with a larger mode, however also means that the divergence angle will be smaller and therefore the input pointing noise will have a larger effect on the imaginary part of ϵ. Still, the divergence angle will only decrease by a factor of 3.5 so the automatic alignment system should be able to reduce this noise enough to ensure that we can sustain the necessary circulating power in the production cavity.

We can also estimate the impact of displacement noise in the production cavity of ALPS II with the projected differential frequency noise derived in Section 3.4. The ALPS II production cavity is designed to have a smaller linewidth compared to the 20 m cavity. This is due to the fact that it is longer and will use a highly reflective out-coupling mirror in a non-impedance matched configuration. As Eq. (1) shows, changes in the cavities resonant frequency due to seismic noise will scale inversely with the length of the cavity just as the cavity linewidth does. Therefore, the coupling from displacement noise to power noise in transmission of the cavity is unaffected by changes in the cavity length. Furthermore, seismic noise measurements reveal a similar environment for the 20 m cavity lab and the ALPS II site. While the differential displacement noise in ALPS II will have less common mode rejection due to the longer cavity length, this will occur at low enough frequencies that the frequency stabilization control loop should be able to compensate for it.

Using a highly reflective out-coupling mirror will also lead to some reduction in the linewidth that will increase the coupling of displacement noise to the transmitted power noise. Still, we do not anticipate that a change in the cavity finesse by a factor of 2.7 will be substantial enough to prevent the cavity from meeting its requirements on circulating power.

The coupling between frequency noise in the NPRO and the transmitted power noise will increase for a longer cavity. Despite this we expect that the passive filter property of the cavity should ensure that transmitted power noise still meets its requirements. This indicates that it should be possible to maintain a stable resonance condition for the ALPS II production cavity.