

Direct detection of fermion dark matter in the radiative seesaw model

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Abstract

We consider the scenario in the radiative seesaw model where the dark matter particle is the lightest Z_2 -odd fermion. We identify the regions of the parameter space of the model compatible with neutrino oscillation data, with the upper limits from rare charged lepton decays and with the observed dark matter abundance via thermal freeze-out, and we compute the dark matter scattering cross section with nuclei via the one-loop exchange of a photon, a Z^0 -boson or a Higgs boson. We find that the predicted spin-independent cross section lies below the current LUX limit, although, for some choices of parameters, above the expected sensitivity of XENON1T or LZ.

1 Introduction

The radiative seesaw model [1], or scotogenic model as is also known, is a simple extension of the Standard Model (SM) that can simultaneously account for neutrino masses and dark matter. It contains an extra scalar doublet, H_2 , and at least two additional singlet fermions, N_i , $i = 1, 2, \dots$, all assumed to be odd under a Z_2 symmetry. In this model neutrino masses vanish at tree-level but are generated via quantum effects induced by the new fields. Furthermore, the lightest particle of the Z_2 odd sector, either the scalar doublet or the lightest fermion singlet, constitutes a dark matter candidate.

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The phenomenology of the scenario where the dark matter is the lightest fermion singlet has been extensively studied in recent years (see, *e.g.* [2–18]), however the potential signals in direct detection experiments have received much less attention. In [8] it was assumed that the two singlet fermions N_1 and N_2 are very degenerate, $\Delta M_N \sim \text{keV}$, such that inelastic scattering on nuclei can take place. In that case, the dominant contribution to dark matter direct detection comes from a one-loop induced magnetic dipole operator, being the predicted rates sizable in some instances. This conclusion holds, however, only in this restricted framework. In general, N_1 and N_2 have a much larger mass splitting and therefore the inelastic scattering on nuclei is kinematically forbidden.

The elastic scattering with nuclei is nonetheless possible, via the one-loop exchange of a photon, a Z boson and the Higgs boson. While the detection of the radiatively-induced dark matter-nucleon interactions is challenging, the impressive current sensitivity of direct detection experiments, as well as their steady increase in reach, might allow to set significant limits on the parameters of the model, or optimistically, allow the observation of signals in the future. More specifically, the current bound on the dark matter spin-independent interaction was set by the LUX experiment at the end of 2015, reaching a maximum value below 10^{-9} pb [19]. Future experiments are likely to improve the reach by almost three orders of magnitude [20]. In fact, the XENON1T experiment [21] recently started operation and it is expected to reach a sensitivity of order 10^{-11} pb. In addition, the LZ experiment [22, 23], the LUX successor, will start operating in 2018 and its expected sensitivity is of order 10^{-12} pb.

When N_1 is the lightest Z_2 odd particle, the observed dark matter density can be generated through the freeze-out, superWIMP or freeze-in mechanisms, with either warm or cold dark matter [2–5, 8–10, 15]. In the present work we will focus on the freeze-out mechanism, which requires sizable Yukawa couplings between the dark matter and the Standard Model particles. As is well known, the same Yukawa couplings that keep the dark matter particles in thermal equilibrium at high temperatures, and that eventually allow their freeze-out, also induce neutrino masses and rare charged lepton decays. The flavor mixing observed in neutrino oscillation experiments requires the dark matter particle to couple to more than one leptonic mass eigenstate. As a result, the model predicts sizable rates for the leptonic rare decays, which are generically in tension with the stringent experimental upper limits. Some works have been devoted to find solutions to this tension, by imposing concrete flavor structures in the leptonic sector [2, 4, 10, 24, 25].

In this paper, we perform a phenomenological analysis of the Yukawa sector of the model and we identify the regions of the parameter space compatible with the observed neutrino parameters, with the upper limits on rare leptonic decays, and with the generation of the observed dark matter abundance via thermal freeze-out. After identifying the viable parameter space of the model, we compute analytically the one-loop spin-dependent and spin-independent dark matter cross sections, as well as the anapole moment, and we confront the predictions of the model to the current experimental limits and to the expected sensitivity of future experiments. Notably, we not only find regions of the parameter space fulfilling all the experimental requirements without fine-tunings, but that for some choices of parameters the spin-independent cross section may indeed be large enough to produce signals at XENON1T or LZ.

The rest of the paper is organized as follows. In the next section, we review

the radiative seesaw model and introduce our notation. In Section 3 we analyze the viable parameter space of the model, in particular we identify those scenarios leading to a suppressed rate for $\mu \rightarrow e\gamma$. In section 4 we calculate the interaction terms of the dark matter with a nucleus via the exchange of a photon, a Z -boson or the Higgs boson for parameters leading to the observed dark matter abundance via thermal freeze-out, and we confront the predictions of the model to the upper limits on the scattering rate from direct detection experiments. Finally, in section 5 we present our conclusions.

2 The model

The radiative seesaw model, also known as the scotogenic model [1], is a simple extension of the Standard Model (SM) with a very rich phenomenology. The model contains one additional scalar doublet $H_2 = (H^+, H_2^0)^T$ and at least two Majorana singlet fermions N_i ($i = 1, 2, \dots$), all assumed to have masses in the range between a few GeV and a few TeV. Furthermore, the model postulates that the vacuum displays an exact Z_2 symmetry under which the new fields are odd while the SM fields are even. This symmetry prevents tree-level charged lepton flavor violation and renders stable the lightest odd particle in the spectrum, which becomes a dark matter candidate. In this model, the role of dark matter can be played by the neutral scalar or pseudo-scalar or by the lightest singlet fermion [2–5, 8, 11, 12, 26, 27]. In addition, this model can also account for neutrino masses [1, 9], explain the baryon asymmetry of the Universe [6, 13], generate new signals at colliders [3, 7], and induce observable rates for lepton flavor violating processes [14, 16].

The Lagrangian of the model is:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{N_i} + \mathcal{L}_{H_2} + \mathcal{L}_{\text{int}}, \quad (1)$$

where \mathcal{L}_{SM} is the Standard Model Lagrangian, which includes the Higgs potential $V(H_1) = -\mu_1^2 H_1^\dagger H_1 + \lambda_1 (H_1^\dagger H_1)^2$. Besides, \mathcal{L}_{N_i} and \mathcal{L}_{H_2} contain, respectively, the terms involving only the Z_2 -odd fermionic singlets N_i and the scalar doublet H_2 :

$$\mathcal{L}_{N_i} = \bar{N}_i i \not{\partial} P_R N_i - \frac{1}{2} M_i (\bar{N}_i^c P_R N_i + \text{h.c.}), \quad (2)$$

$$\mathcal{L}_{H_2} = (D_\mu H_2)^\dagger (D^\mu H_2) - \mu_2^2 H_2^\dagger H_2 - \lambda_2 (H_2^\dagger H_2)^2. \quad (3)$$

Here, and in the rest of the paper, we choose to work in the basis where the Z_2 -odd fermionic singlet mass matrix and the charged-lepton Yukawa matrix are diagonal. Finally, \mathcal{L}_{int} contains the interaction terms between the Z_2 -odd particles and the Standard Model particles:

$$\mathcal{L}_{\text{int}} = - \left(Y_{\alpha i} \bar{L}_\alpha \tilde{H}_2 P_R N_i + \text{h.c.} \right) - V_{\text{int}}(H_1, H_2), \quad (4)$$

with an interaction potential identical to the one in the inert doublet model [28–30]

$$V_{\text{int}} = \lambda_3 (H_1^\dagger H_1) (H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2) (H_2^\dagger H_1) + \frac{\lambda_5}{2} \left[(H_1^\dagger H_2)^2 + \text{h.c.} \right]. \quad (5)$$

We demand that the mass terms in the scalar potential satisfy $\mu_1^2 > 0$, $2\lambda_1\mu_2^2 > -\lambda_3\mu_1^2$, $2\lambda_1\mu_2^2 > -(\lambda_3 + \lambda_4 \pm |\lambda_5|)\mu_1^2$ and that the quartic couplings fulfill the vacuum

stability conditions $\lambda_1, \lambda_2 > 0$ and $\lambda_3, \lambda_3 + \lambda_4 - |\lambda_5| > -2\sqrt{\lambda_1\lambda_2}$. We also require that only the Z_2 -even scalar acquires a vacuum expectation value, $\langle H_1^0 \rangle = v/\sqrt{2}$, with $v = 246$ GeV, in order to render a vacuum also invariant under the Z_2 symmetry. Working in the unitary gauge, the scalar fields in the vacuum can be cast as:

$$H_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(H^0 + iA^0) \end{pmatrix}, \quad (6)$$

with h the SM Higgs boson. The masses of the new scalar particles are given by

$$\begin{aligned} m_{H^0}^2 &= \mu_2^2 + \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)v^2, \\ m_{A^0}^2 &= \mu_2^2 + \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5)v^2, \\ m_{H^\pm}^2 &= \mu_2^2 + \frac{1}{2}\lambda_3v^2, \end{aligned} \quad (7)$$

which are constrained by current experiments to satisfy [31, 32]: $m_{A^0} + m_{H^0} > M_Z$, $m_{H^\pm} \gtrsim 70$ GeV and $\max[m_{A^0}, m_{H^0}] \gtrsim 100$ GeV. Besides, we will set the Standard Model Higgs mass to 126 GeV [33, 34].

The complete Lagrangian expressed in terms of the mass eigenstates A^0, H^0, H^\pm, h is rather lengthy, therefore, here we will limit ourselves to write down only the interaction terms relevant for the dark matter phenomenology. These are the cubic interaction terms between two scalars and the Standard Model Higgs boson

$$V \supset \left[\frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)(H^0)^2 + \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5)(A^0)^2 + \lambda_3 H^+ H^- \right] v h, \quad (8)$$

the gauge interaction with the Z boson

$$\mathcal{L} \supset \frac{g}{2c_W} [i(1 - 2s_W^2)(H^+ \partial^\mu H^- - H^- \partial^\mu H^+) + (A^0 \partial^\mu H^0 - H^0 \partial^\mu A^0)] Z_\mu^0,$$

with c_W and s_W the cosine and sine of the weak mixing angle, respectively, and the Yukawa interaction of the scalars with the singlet fermions N_i

$$\mathcal{L} \supset -Y_{\alpha i} \left(\frac{1}{\sqrt{2}} \bar{\nu}_\alpha (H^0 - iA^0) - \bar{\ell}_\alpha H^- \right) P_R N_i + \text{h.c.}, \quad (9)$$

where $\alpha = e, \mu, \tau$ denotes a leptonic flavor index and $i = 1, 2, \dots$ runs over all fermionic singlets of the model.

One of the most notable features of the model is the generation at the one loop level of a neutrino mass term, induced the Yukawa couplings $Y_{\alpha i}$. The neutrino mass matrix reads:

$$[\mathcal{M}_\nu]_{\alpha\beta} = \frac{\lambda_5 v^2}{32\pi^2} \sum_k \frac{Y_{\alpha k} Y_{\beta k}}{M_k} \mathcal{I} \left(\frac{M_k^2}{m_0^2} \right), \quad (10)$$

with

$$\mathcal{I}(x) = \frac{x}{1-x} \left(1 + \frac{x}{1-x} \log x \right). \quad (11)$$

We are interested in this paper in scenarios where the Yukawa couplings are sizable, typically $\gtrsim \mathcal{O}(0.1)$, and m_0, M_k lie in the range between a few GeV and

a few TeV. Therefore, in order to generate neutrino masses smaller than ~ 1 eV, it is necessary a quartic coupling $|\lambda_5| \ll 1$. This requirement implies in particular $m_{H^0} \simeq m_{A^0}$, $m_{H^\pm}^2 - m_{H^0}^2 \simeq \lambda_4 v^2/2$. Furthermore, neutrino oscillation data restrict the flavor structure of the Yukawa couplings. To derive the most general form of the neutrino Yukawa matrix compatible with the neutrino oscillation data, we first cast the mass matrix as:

$$[\mathcal{M}_\nu]_{\alpha\beta} = \sum_k Y_{\alpha k} Y_{\beta k} \tilde{M}_k = \left[Y \tilde{M} Y^T \right]_{\alpha\beta}, \quad (12)$$

where $\tilde{M} = \text{diag}(\tilde{M}_1, \dots, \tilde{M}_n)$ and

$$\tilde{M}_k = \frac{\lambda_5 v^2}{32\pi^2 M_k}. \quad (13)$$

Finally, following [35], one obtains:

$$Y = U^* \sqrt{m_\nu} R \sqrt{\tilde{M}^{-1}}, \quad (14)$$

where U is the leptonic mixing matrix, $m_\nu = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$, m_{ν_i} being the light neutrino masses, and R is a complex orthogonal matrix, $R^T R = 1$, of dimension $3 \times n$, where n is the number of singlet fermions.

In the freeze-out framework, the dark matter abundance is determined by the cross-sections of the various self-annihilation and coannihilation processes. Assuming that the dark matter and the scalar mediator masses are sufficiently non-degenerate coannihilations can be neglected, thus the relic abundance simply depends on the total dark matter annihilation cross section; in this work we will take for concreteness $m_{H^+, H^0, A^0} \gtrsim 1.2M_1$. Expanding the cross section in powers of the relative dark matter velocity, $\sigma v = a + bv^2$, one finds

$$\Omega_{N_1} h^2 \simeq \frac{1.07 \times 10^9 \text{ GeV}^{-1} x_{\text{fo}}}{g_*^{1/2} M_{\text{Pl}}(a + 3b/x_{\text{fo}})}, \quad (15)$$

where $x_{\text{fo}} \equiv M_1/T_{\text{fo}}$, with T_{fo} the temperature at which the freeze-out takes place, and $g_*(x_{\text{fo}})$ is the number of relativistic degrees of freedom in that epoch; for typical values of the parameters, $T_{\text{f.o.}} \sim M_1/20$ and $g_*(x_{\text{f.o.}}) \sim 80$.

For the annihilation processes $N_1 N_1 \rightarrow \ell_\alpha^+ \ell_\beta^-$, $\nu_\alpha \bar{\nu}_\beta$, and neglecting the lepton masses, one obtains [2]

$$a = 0, \\ b = \frac{M_1^2 y_1^4}{48\pi} \left[\frac{M_1^4 + m_{H^+}^4}{(M_1^2 + m_{H^+}^2)^4} + \frac{M_1^4 + m_0^4}{(M_1^2 + m_0^2)^4} \right], \quad (16)$$

where $y_1^2 = \sum_{\alpha=1}^3 |Y_{\alpha 1}|^2$ is the modulus squared of the column vector $Y_{\alpha 1}$. Therefore, the dark matter relic abundance can be estimated to be

$$\Omega_{N_1} h^2 \simeq 0.12 \left(\frac{0.3}{y_1} \right)^4 \left(\frac{M_1}{100 \text{ GeV}} \right)^2 \frac{(1+x)^4}{x^2(1+x^2)}. \quad (17)$$

Here, $x \equiv M_1^2/m_S^2$, where m_S denotes a common mass for the scalar particles ($m_S = m_{H^+} = m_0$).

In this model, the same Yukawa interactions that generate neutrino masses and the freeze-out of the dark matter particles also induce at the one-loop level lepton flavor violating processes, such as $\ell_\beta \rightarrow \ell_\alpha \gamma$ and $\mu - e$ conversion in nuclei. The decay branching ratio for the process $\ell_\beta \rightarrow \ell_\alpha \gamma$ reads [2]

$$\text{Br}(\ell_\beta \rightarrow \ell_\alpha \gamma) = \frac{3\alpha_{\text{em}} \text{Br}(\ell_\beta \rightarrow \ell_\alpha \nu_\beta \bar{\nu}_\alpha)}{64\pi G_F^2 m_{H^\pm}^4} \left| \sum_k Y_{\alpha k} Y_{\beta k}^* F_2 \left(\frac{M_k^2}{m_{H^\pm}^2} \right) \right|^2, \quad (18)$$

where

$$F_2(z) = \frac{1 - 6z + 3z^2 + 2z^3 - 6z^2 \ln z}{6(1 - z)^4}, \quad (19)$$

which approximately reads $F_2(z) \simeq 1/(3z)$ when $z \gg 1$ and $F_2(z) \simeq 1/6$ when $z \ll 1$. On the other hand, the $\mu - e$ conversion in nuclei reads [14, 16]:

$$\text{CR}(\mu - e, \text{Nucleus}) \approx \frac{2m_\mu^5 \alpha_{\text{em}}^5 Z_{\text{eff}}^4 F_p^2 Z}{(4\pi)^4 \Gamma_{\text{capt}} m_{H^\pm}^4} \left| \sum_k Y_{ek} Y_{\mu k}^* H_2 \left(\frac{M_k^2}{m_{H^\pm}^2} \right) \right|^2, \quad (20)$$

where Z is the atomic number, Z_{eff} is the effective atomic charge, F_p is a nuclear matrix element and Γ_{capt} is the total muon capture rate; these are given, for different nuclei, in [16, 36]. Besides, $H_2(z) = \frac{1}{3}G_2(z) - F_2(z)$, with

$$G_2(z) = \frac{2 - 9z + 18z^2 - 11z^3 + 6z^3 \log z}{6(1 - z)^4}, \quad (21)$$

which has the asymptotic values $G_2(z) \simeq (-11/6 + \log z)/z$ for $z \gg 1$ and $G_2(z) \simeq 1/3$ for $z \ll 1$.

The current experimental limits $\text{Br}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [37], $\text{Br}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$ and $\text{Br}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$ [38], $\text{CR}(\mu - e, \text{Ti}) \leq 4.3 \times 10^{-12}$ [39], $\text{CR}(\mu - e, \text{Au}) \leq 7 \times 10^{-13}$ [40] set strong limits on the parameters of the model. In this paper we mainly focus on the rare decays $\ell_\beta \rightarrow \ell_\alpha \gamma$, which currently provide the most stringent limits on the model over most of the parameter space, however $\mu - e$ conversion in nuclei is likely to play also an important role in the future, due to the significant increase of sensitivity expected for this class of experiments [41–49]. Indeed, considering the generic case where $|Y_{e1}| \sim |Y_{\mu1}| \sim |Y_{\tau1}| \sim y_1/\sqrt{3}$, the expected branching ratio for $\mu \rightarrow e\gamma$ for the value of y_1 required by the freeze-out mechanism is approximately given by

$$\text{Br}(\mu \rightarrow e\gamma) \sim 4(2) \times 10^{-7} \left(\frac{M_1}{100 \text{ GeV}} \right)^{-2}, \quad (22)$$

for $m_{H^\pm}/M_1 = 1.5(10)$, which is orders of magnitude larger than the current upper limit, unless $M_1 \gtrsim 100 \text{ TeV}$, in tension with the requirement of partial wave unitarity for thermally produced dark matter [50]. However, as it will be shown in the next section, there exist choices of parameters where the rate can be naturally suppressed, and hence lead to viable dark matter scenarios of thermal freeze-out.

3 Scenarios with suppressed rates for $\mu \rightarrow e\gamma$

We consider a scenario with the minimal particle content necessary to reproduce the two oscillation frequencies measured in neutrino experiments and incorporating

a dark matter candidate, and which consists in adding to the Standard Model a Z_2 -odd scalar doublet, H_2 , and two singlet Z_2 -odd singlet fermions, N_1 and N_2 .¹ In this case, the orthogonal matrix R defined in Eq. (14) reads [52]:

$$R = \begin{pmatrix} 0 & 0 \\ \cos \theta & -\sin \theta \\ \zeta \sin \theta & \zeta \cos \theta \end{pmatrix}, \quad \text{for normal hierarchy,} \quad (23)$$

$$R = \begin{pmatrix} \cos \theta & -\sin \theta \\ \zeta \sin \theta & \zeta \cos \theta \\ 0 & 0 \end{pmatrix}, \quad \text{for inverted hierarchy.} \quad (24)$$

where θ is a complex parameter and $\zeta = \pm 1$ has been included to account for the possible reflections in the orthogonal matrix R .

We will focus in what follows in the case of normal hierarchy. Then, the Yukawa couplings explicitly read:

$$Y_{\alpha 1} = \sqrt{\tilde{M}_1^{-1}} (\sqrt{m_{\nu_2}} \cos \theta U_{\alpha 2}^* + \zeta \sqrt{m_{\nu_3}} \sin \theta U_{\alpha 3}^*), \quad (25)$$

$$Y_{\alpha 2} = \sqrt{\tilde{M}_2^{-1}} (-\sqrt{m_{\nu_2}} \sin \theta U_{\alpha 2}^* + \zeta \sqrt{m_{\nu_3}} \cos \theta U_{\alpha 3}^*). \quad (26)$$

These Yukawa couplings can be readily inserted in Eq. (18) to obtain the rates of the rare decays in terms of the low energy neutrino parameters, as well as the unknown parameters \tilde{M}_k , m_{H^\pm} and the complex angle θ .

To identify the scenarios with suppressed rate for $\mu \rightarrow e\gamma$ we first cast Eq. (18) as:

$$\text{Br}(\mu \rightarrow e\gamma) \propto \left| Y_{e1} Y_{\mu 1}^* F_2 \left(\frac{M_1^2}{m_{H^\pm}^2} \right) + Y_{e2} Y_{\mu 2}^* F_2 \left(\frac{M_2^2}{m_{H^\pm}^2} \right) \right|^2, \quad (27)$$

hence, this class of scenarios require, barring cancellations, especial choices of the neutrino parameters. More specifically, it is necessary that one of the terms in each addend is small, namely

$$\begin{aligned} Y_{\mu 1} \simeq 0 \quad \text{or} \quad Y_{e1} \simeq 0, \\ \text{and} \\ Y_{\mu 2} \simeq 0 \quad \text{or} \quad Y_{e2} \simeq 0 \quad \text{or} \quad F_2 \left(\frac{M_2^2}{m_{H^\pm}^2} \right) \simeq 0. \end{aligned}$$

Notice that $F_2(M_1^2/m_{H^\pm}^2) > 1/12$, since $M_1 < m_{H^\pm}$, and therefore cannot be small, however, since the mass ordering between M_2 and m_{H^\pm} is not fixed a priori, it is possible to find scenarios with $F_2(M_2^2/m_{H^\pm}^2) \simeq 0$ provided $M_2 \gg m_{H^\pm}$.

One can then identify scenarios with two texture zeros or one texture zero leading, without cancellations, to a suppressed rate for $\mu \rightarrow e\gamma$ and which will lead to predictions for other observables. Moreover, there will be scenarios without texture zeros, also with suppressed $\text{Br}(\mu \rightarrow e\gamma)$, although with the price of cancellations among terms. Let us discuss separately these three possibilities.

¹The minimal extension is not unique, since the same features also arise by adding to the Standard Model particle content one Z_2 -odd singlet fermion and two Z_2 -odd scalar doublets [51].

3.1 Two texture zeros

The simplest possibility to suppress the $\text{Br}(\mu \rightarrow e\gamma)$ consists on postulating two simultaneous zeros in the Yukawa matrices, namely: *i*) $Y_{e1} = 0, Y_{e2} = 0$, *ii*) $Y_{\mu1} = 0, Y_{\mu2} = 0$, *iii*) $Y_{e1} = 0, Y_{\mu2} = 0$, *iv*) $Y_{\mu1} = 0, Y_{e2} = 0$. Fixing two elements in the Yukawa matrix leads to a prediction on one of the low energy neutrino parameters [52–54]. Concretely, the choice *i*) leads to $|U_{13}| \simeq 0.23$, *ii*) to $|U_{13}| \simeq 0.25$, and *iii*) and *iv*) to $|U_{13}| \simeq 0.08$, all of them outside the 3σ range [0.126,0.178] obtained in [55] from the global fit to the solar, atmospheric, reactor, and accelerator neutrino data. This scenario is therefore disfavored by present data.

3.2 One texture zero

A second possibility consists in postulating one texture zero, $Y_{\mu k} = 0$ or $Y_{ek} = 0$ for $k = 1$ or $k = 2$, and $F_2(M_l^2/m_{H^\pm}^2) \simeq 0$ for $l \neq k$. Since we require N_1 to be the lightest Z_2 -odd particle in the spectrum, this possibility can only be realized if the spectrum is of the form $M_1 < m_{H^\pm} \ll M_2$ and either $Y_{\mu1} = 0$ or $Y_{e1} = 0$.

In the case $Y_{e1} = 0$, the angle θ in the matrix R reads:

$$\tan \theta = -\sqrt{\frac{m_{\nu_2}}{m_{\nu_3}}} \frac{U_{e2}^*}{\zeta U_{e3}^*}, \quad (28)$$

The flavor structure of the Yukawa couplings then becomes determined by the requirement of producing one texture zero and the low energy neutrino parameters m_2', m_3' and $U_{\alpha i}$. On the other hand, the overall size of the columns of the Yukawa matrices is determined by the free parameters \tilde{M}_k , which in turn depend on λ_5 , the singlet masses and the heavy Higgs mass scale m_0 and thus have a rather obscure physical interpretation. Therefore, we prefer to cast the Yukawa couplings in terms of the modulus of the column vectors $y_1^2 = \sum_{\alpha=1}^3 |Y_{\alpha 1}|^2$, $y_2^2 = \sum_{\alpha=1}^3 |Y_{\alpha 2}|^2$. More specifically, we obtain

$$Y_{\alpha 1} = \frac{y_1 e^{-i\omega/2}}{\sqrt{|U_{12}|^2 + |U_{13}|^2}} (U_{13}^* U_{\alpha 2}^* - U_{12}^* U_{\alpha 3}^*), \quad (29)$$

$$Y_{\alpha 2} = \frac{y_2 e^{-i\omega/2}}{\sqrt{m_{\nu_2}^2 |U_{12}|^2 + m_{\nu_3}^2 |U_{13}|^2}} (m_{\nu_2} U_{12}^* U_{\alpha 2}^* + m_{\nu_3} U_{13}^* U_{\alpha 3}^*), \quad (30)$$

with $\omega = \arg(m_{\nu_2} U_{12}^{*2} + m_{\nu_3} U_{13}^{*2})$.

These expressions in turn allow to express the branching ratios of the rare leptonic decays only in terms of low energy neutrino parameter, the masses of the particles of the Z_2 -odd sector and the overall size of the columns of the Yukawa coupling y_1, y_2 . For the case $Y_{e1} = 0$, the branching ratios for the electron-flavor violating processes read:

$$\text{Br}(\mu \rightarrow e\gamma) \simeq \frac{\alpha_{\text{em}} y_2^4}{192\pi G_F^2 M_2^4} |f_{11} f_{12}|^2, \quad (31)$$

$$\text{Br}(\tau \rightarrow e\gamma) \simeq \frac{\alpha_{\text{em}} y_2^4}{192\pi G_F^2 M_2^4} |f_{11} f_{13}|^2 \text{Br}(\tau \rightarrow e\nu_\tau \bar{\nu}_e), \quad (32)$$

$$\text{CR}(\mu - e, \text{Nucleus}) \simeq \frac{2m_\mu^5 \alpha_{\text{em}}^5 y_2^4 Z_{\text{eff}}^4 F_p^2 Z}{9(4\pi)^4 \Gamma_{\text{capt}} M_2^4} \left[\frac{17}{6} - \log\left(\frac{M_2^2}{m_{H^\pm}^2}\right) \right]^2 |f_{11} f_{12}|^2, \quad (33)$$

with

$$f_{\alpha\beta} \equiv \frac{m_{\nu_2} U_{\alpha 2}^* U_{\beta 2}^* + m_{\nu_3} U_{\alpha 3}^* U_{\beta 3}^*}{\sqrt{m_{\nu_2}^2 |U_{12}|^2 + m_{\nu_3}^2 |U_{13}|^2}}, \quad (34)$$

while the branching ratio for the electron-flavor conserving decay reads:

$$\text{Br}(\tau \rightarrow \mu \gamma) \simeq \frac{\alpha_{\text{em}} y_1^4}{768 \pi G_F^2 m_{H^\pm}^4} \frac{|U_{21}|^2 |U_{31}|^2}{(|U_{12}|^2 + |U_{13}|^2)^2} \text{Br}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu). \quad (35)$$

In particular, in this scenario there is a correlation between the rates of $\tau \rightarrow e \gamma$ and $\mu \rightarrow e \gamma$ given just in terms of low energy neutrino parameters:

$$\frac{\text{Br}(\tau \rightarrow e \gamma)}{\text{Br}(\mu \rightarrow e \gamma)} \simeq \left| \frac{m_{\nu_2} U_{12}^* U_{32}^* + m_{\nu_3} U_{13}^* U_{33}^*}{m_{\nu_2} U_{12}^* U_{22}^* + m_{\nu_3} U_{13}^* U_{23}^*} \right|^2 \text{Br}(\tau \rightarrow e \nu_\tau \bar{\nu}_e) \sim 0.02 - 4.5, \quad (36)$$

the concrete value depending on the value of the phases δ and ϕ' in the leptonic mixing matrix. Moreover, lower limits on the masses of the next-to-lightest singlet and the charged Higgs states follow, respectively, from the present bound on $\mu \rightarrow e \gamma$ and $\tau \rightarrow \mu \gamma$:

$$M_2 \gtrsim 2.4 \text{ TeV} \left(\frac{y_2}{0.3} \right), \quad (37)$$

$$m_{H^\pm} \gtrsim 120 \text{ GeV} \left(\frac{y_1}{0.3} \right). \quad (38)$$

The best present limit on the model parameters from $\mu - e$ conversion stems from experiments with Ti and Au, $\text{CR}(\mu - e, \text{Ti}) \leq 4.3 \times 10^{-12}$, $\text{CR}(\mu - e, \text{Au}) \leq 7 \times 10^{-13}$, and reads

$$M_2 \gtrsim 0.6 (1.0) \text{ TeV} \left(\frac{y_2}{0.3} \right) \quad \text{for Ti (Au)}, \quad (39)$$

where we have taken for concreteness $M_2/m_{H^\pm} = 10$. Given that the upper limit on M_2 scales as the fourth-power of the conversion rate, it would be necessary an increase in sensitivity by a factor ~ 200 in order to provide limits on the model competitive with those from $\mu \rightarrow e \gamma$; notably, this increase in sensitivity seems feasible in the future [49]. It should be borne in mind, though, that the rate for $\mu - e$ conversion is suppressed when $17 - 6 \log(M_2^2/m_{H^\pm}^2) \approx 0$, thus the lower limit on M_2 from the non-detection of the process $\mu \rightarrow e \gamma$ is more robust, since cancellations among amplitudes never occur.

The discussion above only relies on the assumptions $Y_{e1} \simeq 0$ and $M_1 < m_{H^\pm} \ll M_2$. Requiring that the dark matter is entirely produced via thermal freeze-out leads to a lower limit on the dark matter mass. Indeed, taking the value of y_1 required by thermal production from Eq. (17), and substituting in Eq. (35), we obtain

$$M_1 \gtrsim 140 \text{ GeV}. \quad (40)$$

An analogous calculation allows to obtain expressions for the Yukawa couplings in the case $Y_{\mu 1} = 0$. The angle θ must take the value

$$\tan \theta = -\sqrt{\frac{m_{\nu_2}}{m_{\nu_3}}} \frac{U_{\mu 2}^*}{\zeta U_{\mu 3}^*}, \quad (41)$$

therefore,

$$Y_{\alpha_1} = \frac{y_1 e^{-i\omega/2}}{\sqrt{|U_{22}|^2 + |U_{23}|^2}} (U_{23}^* U_{\alpha_2}^* - U_{22}^* U_{\alpha_3}^*), \quad (42)$$

$$Y_{\alpha_2} = \frac{y_2 e^{-i\omega/2}}{\sqrt{m_{\nu_2}^2 |U_{22}|^2 + m_{\nu_3}^2 |U_{23}|^2}} (m_{\nu_2} U_{22}^* U_{\alpha_2}^* + m_{\nu_3} U_{23}^* U_{\alpha_3}^*), \quad (43)$$

with $\omega = \arg(m_{\nu_2} U_{22}^{*2} + m_{\nu_3} U_{23}^{*2})$. The corresponding values for the branching ratios of the muon-flavor violating decays read:

$$\text{Br}(\mu \rightarrow e \gamma) \simeq \frac{\alpha_{\text{em}} y_2^4}{192 \pi G_F^2 M_2^4} |g_{21} g_{22}|^2, \quad (44)$$

$$\text{Br}(\tau \rightarrow \mu \gamma) \simeq \frac{\alpha_{\text{em}} y_2^4}{192 \pi G_F^2 M_2^4} |g_{21} g_{23}|^2 \text{Br}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_e), \quad (45)$$

$$\text{CR}(\mu - e, \text{Nucleus}) \simeq \frac{2 m_\mu^5 \alpha_{\text{em}}^5 y_2^4 Z_{\text{eff}}^4 F_p^2 Z}{9 (4\pi)^4 \Gamma_{\text{capt}} M_2^4} \left[\frac{17}{6} - \log \left(\frac{M_2^2}{m_{H^\pm}^2} \right) \right]^2 |g_{21} g_{22}|^2, \quad (46)$$

where $g_{\alpha\beta}$ is analogous to $f_{\alpha\beta}$, as defined in Eq. (34), with the substitution $U_{1i} \rightarrow U_{2i}$, while the branching ratio for the muon flavor conserving decay is:

$$\text{Br}(\tau \rightarrow e \gamma) \simeq \frac{\alpha_{\text{em}} y_1^4}{768 \pi G_F^2 m_{H^\pm}^4} \frac{|U_{11}|^2 |U_{31}|^2}{(|U_{22}|^2 + |U_{23}|^2)^2} \text{Br}(\tau \rightarrow e \nu_\tau \bar{\nu}_e). \quad (47)$$

This scenario leads to a correlation between the rates of $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e \gamma$:

$$\frac{\text{Br}(\tau \rightarrow \mu \gamma)}{\text{Br}(\mu \rightarrow e \gamma)} \simeq \left| \frac{m_{\nu_2} U_{22}^* U_{32}^* + m_{\nu_3} U_{23}^* U_{33}^*}{m_{\nu_2} U_{22}^* U_{12}^* + m_{\nu_3} U_{23}^* U_{13}^*} \right|^2 \text{Br}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu) \sim 1.4 - 28.8, \quad (48)$$

while the lower limits on the masses of the Z_2 -odd sector from rare leptonic decays are:

$$M_2 \gtrsim 2.1 \text{ TeV} \left(\frac{y_2}{0.3} \right), \quad (49)$$

$$m_{H^\pm} \gtrsim 120 \text{ GeV} \left(\frac{y_1}{0.3} \right). \quad (50)$$

On the other hand, the most stringent current limit from $\mu - e$ conversion in nuclei gives

$$M_2 \gtrsim 0.1 (0.2) \text{ TeV} \left(\frac{y_2}{0.3} \right) \quad \text{for Ti (Au)}, \quad (51)$$

again, for $M_2/m_{H^\pm} = 10$.

As for the case $Y_{e1} \simeq 0$, also for this case one can set a lower limit on the dark matter mass from requiring thermal production. Using Eqs. (17) and (47), we obtain

$$M_1 \gtrsim 170 \text{ GeV}. \quad (52)$$

We conclude this subsection remarking that the scenarios with $M_1 < m_{H^\pm} \ll M_2$ and $Y_{e1} = 0$, or $Y_{\mu 1} = 0$, yield the smallest possible rates for $\mu \rightarrow e \gamma$ in the absence of fine-tunings. For any other choices of parameters, and barring cancellations, the predicted rate for $\mu \rightarrow e \gamma$ will be larger and therefore the lower limits on the masses presented here can be regarded as conservative.

3.3 No texture zero

It is always possible to find a set of high energy parameters that leads to a suppressed rate for $\mu \rightarrow e \gamma$ by allowing cancellations among terms. This can be demonstrated noting first that $\text{Br}(\ell_\beta \rightarrow \ell_\alpha \gamma) \propto |P_{\alpha\beta}|^2$, with

$$P_{\alpha\beta} = \sum_k Y_{\alpha k} Y_{\beta k}^* F_2(x_k) \quad (53)$$

and $x_i = M_i^2/m_{H^\pm}^2$. Defining

$$Y'_{\alpha k} = Y_{\alpha k} \sqrt{F_2(x_k)}, \quad (54)$$

we have

$$P_{\alpha\beta} = \sum_k Y'_{\alpha k} Y'_{\beta k}^* = (Y' Y'^\dagger)_{\alpha\beta}. \quad (55)$$

In terms of the rescaled Yukawa matrix $Y'_{\alpha k}$, the neutrino mass matrix Eq. (12) reads:

$$[\mathcal{M}_\nu]_{\alpha\beta} = \sum_k Y'_{\alpha k} Y'_{\beta k} \tilde{M}'_k = \left[Y' \tilde{M}' Y'^T \right]_{\alpha\beta}, \quad (56)$$

with

$$\tilde{M}'_k = \tilde{M}_k / F_2(x_k). \quad (57)$$

Neutrino masses and the lepton flavor violating rates are then determined, respectively, by the symmetric matrix $\mathcal{M}_\nu = Y' \tilde{M}' Y'^T$ and by the Hermitian matrix $P = Y' Y'^\dagger$. As shown in [56, 57], for any P and \mathcal{M}_ν , it is possible to find matrices Y' and \tilde{M}' that solve Eqs. (55) and (56), and therefore, using Eqs. (54) and (57), matrices Y and \tilde{M} . In particular, there exists an infinite family of parameters leading to $\text{Br}(\mu \rightarrow e \gamma) = 0$, although most of these choices require a very large tuning among parameters. Indeed, the present limits on rare decays require

$$\begin{aligned} |P_{12}| &\lesssim 7 \times 10^{-5} \left(\frac{m_{H^\pm}}{300 \text{ GeV}} \right)^{-2}, \\ |P_{13}| &\lesssim 4 \times 10^{-2} \left(\frac{m_{H^\pm}}{300 \text{ GeV}} \right)^{-2}, \\ |P_{23}| &\lesssim 5 \times 10^{-2} \left(\frac{m_{H^\pm}}{300 \text{ GeV}} \right)^{-2}. \end{aligned} \quad (58)$$

Therefore, for Yukawa couplings of $\mathcal{O}(0.1)$, as required by thermal production, a fine cancellation among the different amplitudes contributing to the process $\mu \rightarrow e \gamma$ must take place in order to fulfill the stringent experimental upper limit in $|P_{12}|$, unless m_{H^\pm} lies in the multi-TeV scale.

In this scenario the rate for $\mu \rightarrow e \gamma$ is suppressed by cancellations, however these cancellations do not necessarily occur simultaneously for other processes with $\mu - e$ flavor violation, potentially leading to signals in future experiments searching for $\mu - e$ conversion in nuclei or $\mu \rightarrow 3e$. More specifically, in the scenario where $\text{Br}(\mu \rightarrow e \gamma)$ vanishes due to cancellations, the Yukawa couplings must be tuned to satisfy

$$Y_{e2} Y_{\mu 2}^* = -Y_{e1} Y_{\mu 1}^* F_2(x_1) / F_2(x_2). \quad (59)$$

Substituting in Eq. (20) and taking for concreteness $Y_{\alpha 1} \sim y_1/\sqrt{3}$, the $\mu - e$ conversion rate takes the form

$$\text{CR}(\mu - e, \text{Nucleus}) = \frac{m_\mu^5 \alpha_{\text{em}}^5 Z_{\text{eff}}^4 F_p^2 2Z}{\Gamma_{\text{capt}} (4\pi)^4 m_{H^\pm}^4} \frac{y_1^4}{9} |H_2(x_1) - H_2(x_2) F_2(x_1)/F_2(x_2)|^2. \quad (60)$$

For the mass spectrum $x_1 \ll x_2 \ll 1$ ($M_1^2 < M_2^2 \ll m_{H^\pm}^2$) we obtain

$$\text{CR}(\mu - e, \text{Nucleus}) \simeq \frac{m_\mu^5 \alpha_{\text{em}}^5 Z_{\text{eff}}^4 F_p^2 2Z}{\Gamma_{\text{capt}} (4\pi)^4 m_{H^\pm}^4} \frac{y_1^4 x_2^2}{9 \cdot 36} \quad (61)$$

$$\approx 1.9 (1.6) \times 10^{-17} \left(\frac{1 \text{ TeV}}{m_{H^\pm}} \right)^4 \left(\frac{y_1}{0.3} \right)^4, \quad \text{for Ti (Au)}, \quad (62)$$

where in the second line we have assumed $M_2/m_{H^\pm} = 1/10$, for illustration. On the other hand, for the mass spectrum $x_1 \ll 1$ and $x_2 \gg 1$ ($M_1^2 \ll m_{H^\pm}^2 \ll M_2^2$)

$$\text{CR}(\mu - e, \text{Nucleus}) \simeq \frac{m_\mu^5 \alpha_{\text{em}}^5 Z_{\text{eff}}^4 F_p^2 2Z}{\Gamma_{\text{capt}} (4\pi)^4 m_{H^\pm}^4} \frac{y_1^4}{9} \frac{(\frac{5}{2} - \log x_2)^2}{36} \quad (63)$$

$$\approx 8.5 (6.7) \times 10^{-13} \left(\frac{1 \text{ TeV}}{m_{H^\pm}} \right)^4 \left(\frac{y_1}{0.3} \right)^4, \quad \text{for Ti (Au)}, \quad (64)$$

where we have taken here instead $M_2/m_{H^\pm} = 10$. It is interesting that in the latter case the predicted rate for $\mu - e$ conversion is, for thermally produced dark matter, at the reach of projected experiments, provided $m_{H^\pm} \lesssim 1$ TeV; for the former case, however, the prospects for detection are poorer.

4 Dark matter direct detection

Since the Yukawa term in Eq. (9) is the only interaction between N_1 and the SM particles, quark-dark matter interactions do not occur at tree-level. On the other hand, at the one-loop level, effective couplings do appear between N_1 and other SM particles, including the photon, the Z boson and the Higgs boson (see Fig. 1).

Let us start considering the scenario where the cubic interactions between the Higgs and the Z_2 -odd scalars are very small, such that the dark matter coupling to the nucleon is dominated by the exchange of a gauge boson. The exchange of the Z -boson leads to an effective axial vector interaction term of the form $\xi_q \bar{N}_1 \gamma^\mu \gamma^5 N_1 \bar{q} \gamma_\mu \gamma^5 q$, where ξ_q reads:

$$\xi_q = \frac{y_1^2 a_q}{32\pi^2 M_Z^2} \left[(v_\ell + a_\ell) \mathcal{G}_2 \left(\frac{M_1^2}{m_{H^\pm}^2} \right) + (v_\nu + a_\nu) \mathcal{G}_2 \left(\frac{M_1^2}{m_0^2} \right) \right], \quad (65)$$

with $a_\ell = -\frac{g}{2c_W} \frac{1}{2}$, $v_\ell = -\frac{g}{2c_W} (\frac{1}{2} - 2s_W^2)$, $v_\nu = a_\nu = \frac{g}{2c_W} \frac{1}{2}$ and $a_q = \frac{1}{2} (-\frac{1}{2})$ for $q = u, c, t$ (d, s, b). The loop function $\mathcal{G}_2(x)$ is given by

$$\mathcal{G}_2(x) = -1 + \frac{2(x + (1-x) \ln(1-x))}{x^2}, \quad (66)$$

and takes values between 0 and 1 for $0 \leq x \leq 1$; for $x \lesssim 0.1$ it can be well approximated by $x/3$. The resulting spin dependent cross section per nucleon N is [58]

$$\sigma_{N,SD} = \frac{16}{\pi} \frac{M_1^2 m_N^2}{(M_1 + m_N)^2} J_N (J_N + 1) \xi_N^2, \quad (67)$$

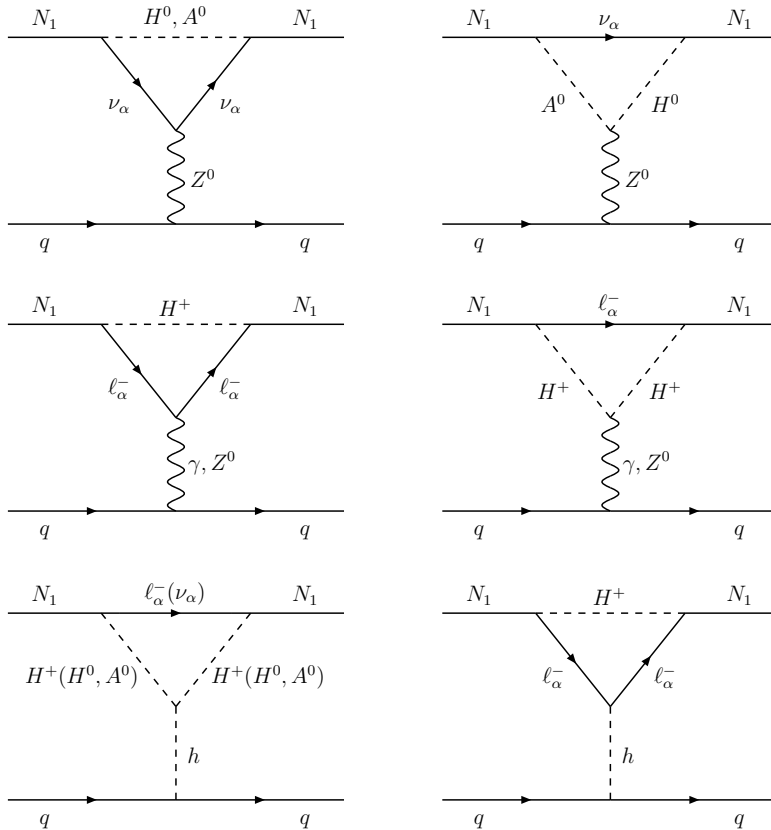


Figure 1: Diagrams contributing at one loop to the elastic scattering of dark matter particles off nuclei via the Z -boson exchange (first and second rows), photon exchange (second row) and Higgs exchange (third row).

with $\xi_N = \sum_{q=u,d,s} \Delta_q^N \xi_q$ and $\Delta_u^N = 0.842$, $\Delta_d^N = -0.427$, $\Delta_s^N = -0.085$ [59]. The value of the spin-dependent cross section can then be estimated to be

$$\begin{aligned} \sigma_{N,SD}^{\max} &\sim 10^{-4} \text{pb} \left(\frac{y_1}{3.0} \right)^4 \mathcal{G}_2 \left(\frac{M_1^2}{m_S^2} \right)^2 \\ &\sim 10^{-7} \text{pb} \left(\frac{M_1}{500 \text{ GeV}} \right)^2 \mathcal{H}_2 \left(\frac{M_1^2}{m_S^2} \right), \end{aligned} \quad (68)$$

where in the second line we have substituted the value of y_1 necessary to generate the observed dark matter abundance via thermal freeze-out, Eq. (17). Also, we have denoted m_S as the common mass of all the extra scalar particles and we have defined the function $\mathcal{H}_2(x) = (1+x)^4 \mathcal{G}_2(x)^2 / (x^2(1+x^2))$ which is monotonically increasing with x and takes values between 1/9 and 8 for $0 \leq x \leq 1$.

This estimate is confirmed by our numerical analysis, shown in Fig. 2, where we calculate the spin-dependent cross section induced by the Z -boson exchange scanning over the relevant free parameters of the model as follows:

$$\begin{aligned} 1 \text{ GeV} &\leq M_1 \leq 3.5 \text{ TeV}, \\ M_1 &\leq M_2 \leq 10 \text{ TeV}, \\ 1.2 M_1 &\leq m_{H^0}, m_{H^\pm} \leq 5 \text{ TeV}. \end{aligned} \quad (69)$$

All the points in the figure generate a the dark matter density via thermal freeze-out in agreement with the value measured by Planck [60], which we calculate using

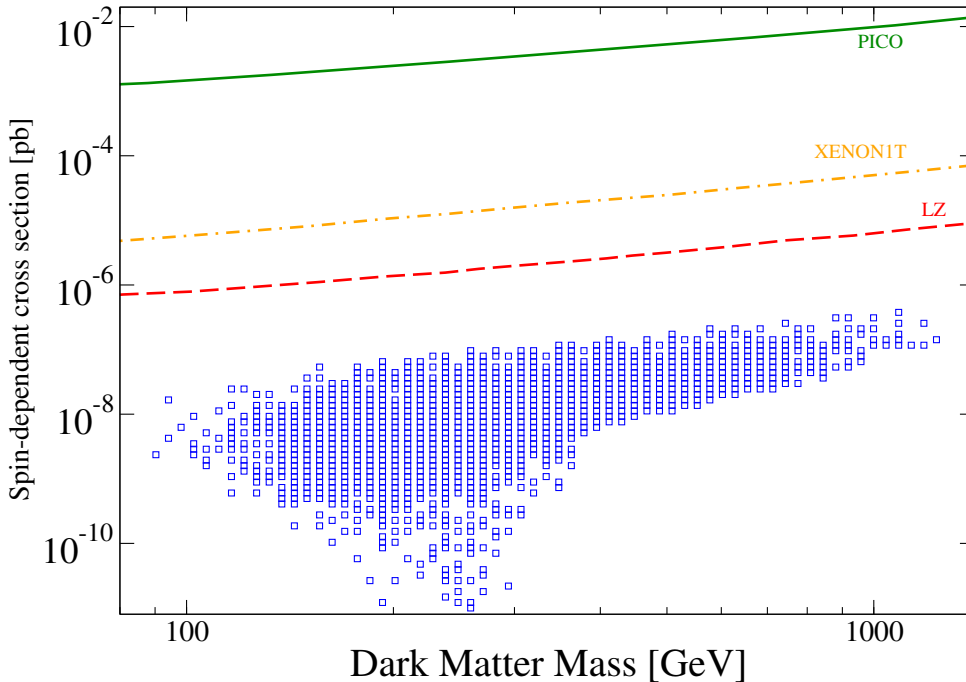


Figure 2: Spin-dependent cross section as a function of the dark matter mass for a sample of viable points of the model, compared to the current upper limit from PICO (green solid line) as well as to the projected sensitivities of XENON1T (yellow dot-dashed line) and LZ (red dashed line).

micrOMEGAs [61]. For comparison, we also show in the figure the current bound on the spin-dependent cross section from PICO (green solid line) [62] as well as the expected sensitivities of XENON1T (yellow dot-dashed line) and LZ (red dashed line) [20]. As apparent from the plot, the predicted scattering rate induced by the exchange of the Z-boson lies well below the sensitivity of present and projected experiments.

The dark matter Yukawa interactions also give rise to an effective electromagnetic coupling at the quantum level. Due to the invariance of the dark matter field under charge conjugation, the magnetic and electric dipole moment interactions identically vanish, and the leading contribution is the electromagnetic anapole moment [63–65]:

$$\mathcal{L}_A = \mathcal{A} \bar{N}_1 \gamma^\mu \gamma^5 N_1 \partial^\nu F_{\mu\nu}. \quad (70)$$

The anapole moment receives contributions from the exchange at one loop of each leptonic family, and reads [64]

$$\mathcal{A} = \mathcal{A}_e + \mathcal{A}_\mu + \mathcal{A}_\tau, \quad (71)$$

where

$$\mathcal{A}_\ell = -\frac{e|Y_{\ell 1}|^2}{96\pi^2 M_1^2} \left[\frac{3}{2} \ln\left(\frac{\eta}{\epsilon}\right) - \frac{1 + 3\eta - 3\epsilon}{\sqrt{(\eta - 1 - \epsilon)^2 - 4\epsilon}} \operatorname{arctanh}\left(\frac{\sqrt{(\eta - 1 - \epsilon)^2 - 4\epsilon}}{\eta - 1 + \epsilon}\right) \right], \quad (72)$$

with $\eta = m_{H^\pm}^2/M_1^2$, $\epsilon = m_\ell^2/M_1^2$ and $\ell = \mu, \tau$. The electron contribution depends on

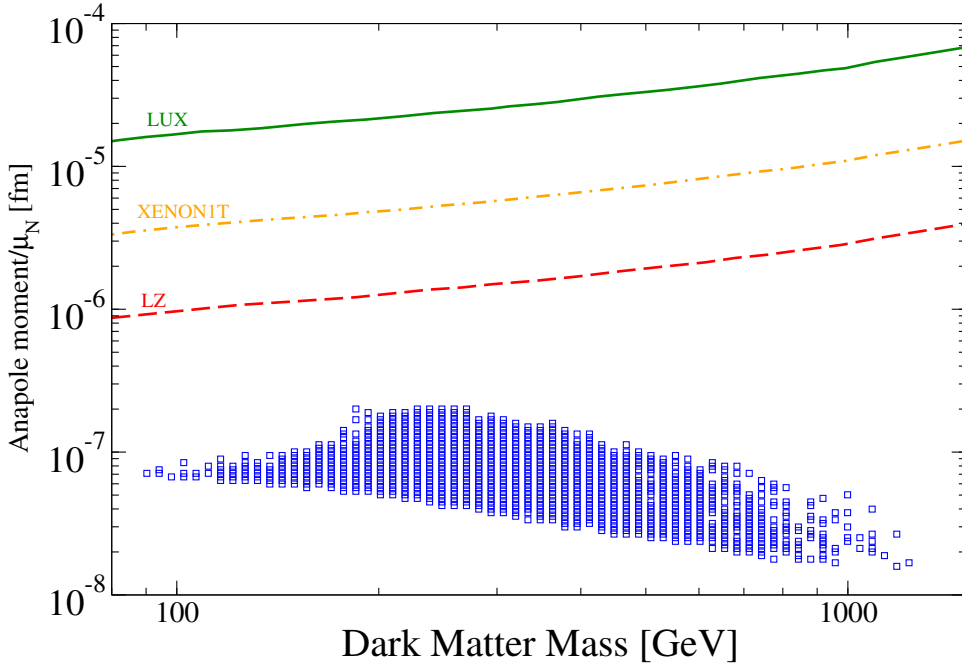


Figure 3: Anapole moment as a function of the dark matter mass for a sample of viable points of the model, compared to the current upper limit from LUX (green solid line) as well as to the projected sensitivities of XENON1T (yellow dot-dashed line) and LZ (red dashed line).

the momentum transfer q^2 and is given by

$$\mathcal{A}_e = -\frac{e|Y_{e1}|^2}{32\pi^2 M_1^2} \left[\frac{-10 + 12 \log \xi - (3 + 9\eta) \log(\eta - 1) - (3 - 9\eta) \log \eta}{9(\eta - 1)} \right], \quad (73)$$

with $\xi = |q^2|^{1/2}/M_1$ and $|q^2| \gg m_e^2$. We show in Fig. 3 the predicted anapole moment for a sample of points of the parameter space of the model, confronted to the current limit by the LUX experiment (green solid line) as well as to the projected sensitivities of XENON1T (yellow dot-dashed line) and LZ (red dashed line) experiments; the predicted anapole moment lies well below the projected reach of projected experiments. We then conclude that the observation of signals in direct detection experiments will be challenging, if the dark matter interaction with the nucleon is dominated by the gauge interactions.

The scattering rate of dark matter particles in a detector can be enhanced if the quartic couplings λ_3, λ_4 are sizable. If this is the case, the Higgs exchange diagrams shown in Fig. 1 induce an effective scalar interaction term between N_1 and the quark q of the form $\Lambda_q \bar{q}q \bar{N}_1 N_1$, with

$$\Lambda_q = -\frac{y_1^2}{16\pi^2 m_h^2 M_1} \left[\lambda_3 \mathcal{G}_1 \left(\frac{M_1^2}{m_{H^\pm}^2} \right) + \frac{(\lambda_3 + \lambda_4)}{2} \mathcal{G}_1 \left(\frac{M_1^2}{m_0^2} \right) \right] m_q, \quad (74)$$

where $y_1 = (\sum_\alpha |Y_{\alpha 1}|^2)^{1/2}$, and where we have neglected contributions proportional to the small charged lepton Yukawa couplings or to λ_5 . The loop function $\mathcal{G}_1(x)$ is defined as

$$\mathcal{G}_1(x) = \frac{x + (1-x) \ln(1-x)}{x}, \quad (75)$$

and takes values between 0 and 1 for $0 \leq x \leq 1$; for $x \lesssim 0.1$ it can be well approximated by $x/2$. This interaction leads to the spin-independent cross section σ_{SI} of N_1 off a proton, which reads

$$\sigma_{SI} = \frac{4}{\pi} \frac{M_1^2 m_p^2}{(M_1 + m_p)^2} m_p^2 \left(\frac{\Lambda_q}{m_q} \right)^2 f_p^2, \quad (76)$$

where m_p is the proton mass and $f_p \approx 0.3$ is the scalar form factor. The value of σ_{SI} is estimated to be

$$\sigma_{SI} \sim 5 \times 10^{-7} \text{pb} \left(\frac{\lambda_{3,4}}{3.0} \right)^2 \left(\frac{y_1}{3.0} \right)^4 \mathcal{G}_1 \left(\frac{M_1^2}{m_0^2} \right)^2 \left(\frac{100 \text{ GeV}}{M_1} \right)^2 \quad (77)$$

$$\sim 8 \times 10^{-11} \text{pb} \left(\frac{\lambda_{3,4}}{3.0} \right)^2 \mathcal{H}_1 \left(\frac{M_1^2}{m_0^2} \right) \quad (78)$$

where, again, y_1 was set by Eq. (17) and we have defined the function $\mathcal{H}_1(x) = (1+x)^4 \mathcal{G}_1(x)^2 / (x^2(1+x^2))$, which is monotonically increasing with x and takes values between 1/4 and 8 for $0 \leq x \leq 1$. Even for large quartic couplings, the predicted cross section lies about one order of magnitude below the current LUX limits, however future experiments might reach the necessary sensitivity to observe signals in this scenario. In Fig. 4 we show the expected spin-independent cross section for $\lambda_3 = 0.1$ (yellow circles), 1 (red crosses) and 3 (blue squares) from our scan of the parameter space, Eq. (69). For comparison, we also show in the figure the current bound from LUX [19] (black solid line), as well as the projected sensitivities of XENON1T (magenta dashed line) and LZ (green dashed line) [21, 22, 66]. As apparent from the plot, future experiments will be able to probe the singlet fermion dark matter scenario of the radiative seesaw model, for sufficiently large values of the quartic coupling λ_3 . On the other hand, points of the parameter space with small value of λ_3 lie below the neutrino coherent scattering limit, shown in the plot as a cyan line [20, 67].

5 Conclusions

We have investigated prospects for direct dark matter detection in the radiative seesaw model in a scenario where the dark matter candidate is the lightest singlet fermion. Pursuing a phenomenological approach, we have identified the regions of the parameter space which lead to the observed neutrino oscillation parameters and to the measured dark matter abundance via thermal freeze-out, while satisfying the stringent experimental limits on the rare charged lepton decays. Notably, we have found choices of parameters where the rate for the process $\mu \rightarrow e\gamma$ can be suppressed without invoking cancellations among the different amplitudes contributing to the process.

We have found that, for thermally produced dark matter particles, the direct detection rates mainly depend on the size of the quartic interaction terms between the Z_2 -odd scalars and the Standard Model Higgs boson and on the masses of the new particles of the model, but are totally uncorrelated to flavor observables, such as oscillation parameter or the rates for the rare charged lepton decays. When the cubic interactions are very small, the scattering process is dominated by the one-loop exchange of a photon, through an anapole interaction, and of a Z -boson, leading to

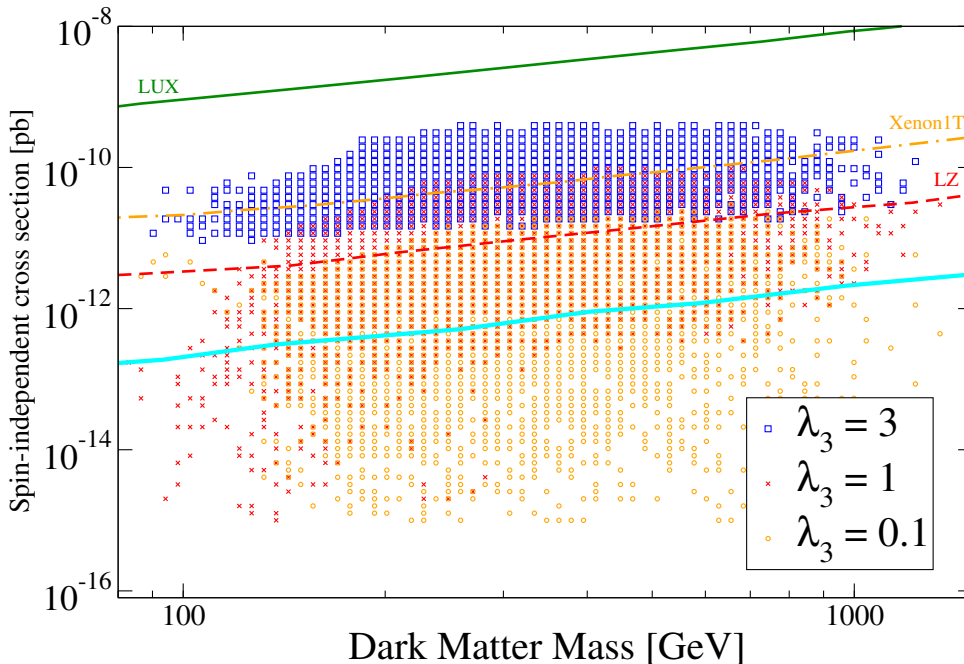


Figure 4: Spin-independent cross section as a function of the dark matter mass for a sample of viable points of the model, for different values of the coupling λ_3 , compared to the current upper limit from LUX (green solid line) as well as to the projected sensitivities of XENON1T (yellow dot-dashed line) and LZ (red dashed line). The cyan line shows the neutrino coherent scattering limit.

a spin-dependent scattering. Our analysis shows that the predicted anapole interaction and the spin-dependent scattering cross section unfortunately lie well below the sensitivity of present and foreseeable experiments. On the other hand, for sufficiently large quartic couplings, the scattering process is dominated by the exchange of the Higgs boson, leading to a spin-independent scattering. While present experiments are not yet probing this model, the upcoming XENON1T and LZ experiments will be able to probe points of the parameter space where the relevant quartic couplings are $\gtrsim \mathcal{O}(0.1)$.

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