



1 **Atmospheric CO₂ inversions at the mesoscale using data driven**
2 **prior uncertainties. Part1: Methodology and system evaluation**

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1 Abstract

2 Atmospheric inversions are widely used in the optimization of surface carbon fluxes at regional
3 scale using information from atmospheric CO₂ dry mole fractions. In many studies the prior flux
4 uncertainty applied to the inversion schemes does not reflect directly the true flux uncertainties
5 but it is used in such a way to regularize the inverse problem. Here, we aim to implement an
6 inversion scheme using the Jena inversion system and applying a prior flux error structure
7 derived from a model – data residual analysis using high spatial and temporal resolution over a
8 full year period in the European domain. We analyzed the performance of the inversion system
9 with a synthetic experiment, where the flux constraint is derived following the same residual
10 analysis but applied to the model-model mismatch. The synthetic study showed a quite good
11 agreement between posterior and “true” fluxes at European/Country and annual/monthly scales.
12 Posterior monthly and country aggregated fluxes improved their correlation coefficient with the
13 “known truth” by 7% compared to the prior estimates when compared to the reference, with a
14 mean correlation of 0.92. Respectively, the ratio of the standard deviation between
15 posterior/reference and prior/reference was also reduced by 33% with a mean value of 1.15. We
16 identified temporal and spatial scales where the inversion system maximizes the derived
17 information; monthly temporal scales at around 200 km spatial resolution seem to maximize the
18 information gain.

19



1 **1 Introduction**

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3 The continuous rise of the abundance of greenhouse gases in the atmosphere, especially due to
4 fossil fuel combustion, alerted the scientific community to systematically monitor these
5 emissions. The challenge is not limited only to revealing the spatial distribution of CO₂ sources
6 and sinks on continental scales, but also to accurately quantifying CO₂ emissions and their
7 uncertainties at country scales. In situ atmospheric measurements of the atmospheric CO₂
8 variability combined with inverse atmospheric models are used as an independent method to
9 provide “top down” flux estimates for comparison with estimates from “bottom up” methods.
10 The latter use local observations (e.g. eddy covariance), and combine these with ancillary data,
11 e.g. soil maps, satellite data, and terrestrial ecosystem models in order to spatially scale up local
12 flux estimates to larger regions (Jung et al., 2009). Both approaches act complementary, for
13 optimal comprehension of carbon sources and sinks in a “multiple constraint” (Schulze et al.,
14 2010) approach and emission inventories assessment. As these inventories are used to deduce
15 national emission estimates, in compliance with the Kyoto protocol requirements, accuracy is
16 essential.

17 An atmospheric inverse modeling system provides the link from atmospheric concentrations to
18 surface fluxes. However, the limited number of observations available for solving the system for
19 quite a number of unknowns (spatially and temporally resolved fluxes) makes the inverse
20 problem strongly under-determined. To solve the inverse problem the system incorporates
21 Bayes’ theorem and uses a-priori knowledge, provided by e.g. biosphere models and emission
22 inventories accompanied by corresponding uncertainty estimates. Then, the system optimizes the
23 a-priori fluxes by minimizing the difference between model predictions and observed
24 concentrations. For the current study only the biospheric fluxes were optimized, and emissions
25 from fossil fuel combustion are assumed to be known much better, as it is the case in almost all
26 published regional inversion studies. Inversion systems have been extensively used to derive
27 spatiotemporal flux patterns at global (e.g. Enting et al., 1995; Kaminski et al., 1999a; Gurney et
28 al., 2003; Mueller et al., 2008), and regional scale (e.g. Gerbig et al., 2003a; Peylin et al., 2005;
29 Lauvaux et al., 2012; Broquet et al., 2013).



1 The challenge in regional inversions is to reconstruct at high resolution the spatiotemporal flux
2 patterns, usually of the net ecosystem exchange (NEE). For that purpose currently deployed
3 global or regional inverse modeling schemes use different state spaces (i.e. the set of variables to
4 be optimized through the inversion process). Peters et al. (2007) split the domain of interest into
5 regions according to ecosystem type. Subsequently fluxes are optimized by using linear
6 multiplication factors to scale NEE for each week and each region. The pitfall of this system is
7 that a zero prior flux has no chance to be optimized and remains zero. Zupanski et al. (2007)
8 divided the NEE into two components, i.e. the gross photosynthetic production (GPP) and
9 ecosystem respiration (R). Then multiplicative factors for the gross fluxes were derived on the
10 grid scale, under the assumption of being constant in time. A step further made by Lokupitiya et
11 al. (2008) used the same approach but with an 8-week time window allowing for temporal
12 variations for the multiplicative factors. A different approach introducing the carbon cycle data
13 assimilation system (CCDAS) was implemented by Rayner et al. (2005) and Kaminski et al.
14 (2012) by constraining global parameters within a biosphere model able to control surface-
15 atmosphere exchange fluxes, against observed atmospheric CO₂ mole fractions, instead of the
16 fluxes themselves. Lauvaux et al. (2012) used a Bayesian approach based on matrix inversion,
17 separately optimizing day and night time fluxes at a weekly time scale for a limited simulation
18 period and domain. An attempt to assess which of these approaches better reproduces NEE was
19 made by Tolk et al. (2011). This study investigated the impact of different inversion approaches
20 via a synthetic experiment utilizing an ensemble Kalman filter technique and the same transport
21 model for all cases. They found that inversions which separately optimize gross fluxes within a
22 pixel inversion concept perform better on reconstructing the NEE, although they fail to obtain
23 the gross fluxes. Taking into consideration these findings we also choose the pixel based
24 inversions but optimizing the net biogenic fluxes as we are mainly interested in the total carbon
25 flux budget.

26 Introducing proper prior flux uncertainties is crucial for meaningful posterior estimates, as these
27 uncertainties weight the prior knowledge between different locations and times, as well as with
28 respect to the data constraint. The uncertainties have the form of a covariance matrix and can be
29 categorized in uncertainties of the prior fluxes, and uncertainties of the observational constraint,
30 which includes measurement and transport model uncertainties. While the observational
31 constraint may be more easily defined with the main diagonal of the covariance matrix



1 representing the uncertainty of the observations and the model at a specific time and location, our
2 knowledge for the prior uncertainty is limited. Early inversions assumed fully uncorrelated flux
3 uncertainties (Kaminski et al., 1999b), while spatial and temporal correlations were used later by
4 Rödenbeck et al. (2003), who investigated the autocorrelation of monthly CO₂ fluxes calculated
5 by a set of terrestrial and ocean models. In Rödenbeck (2005), spatial correlations for land fluxes
6 were assigned to a state space of 4° latitude x 5° longitude resolution. Slightly different
7 correlation length scales were considered for the meridional and zonal direction, assuming that
8 the climate zone of the later varies less than of the former. Flux correlations on land were
9 determined by assuming an exponential pulse response function with a length of 1275 km. This
10 leads to correlations with approximately twice the correlation length. Typically the spatial
11 correlations are considered more as a tool to regularize the inverse problem, rather than an
12 uncertainty feature. Schuh et al. (2010) obtained correlation lengths from Rödenbeck et al.
13 (2003) but with a much higher state space resolution of 200 km. Lauvaux et al. (2008) neglected
14 the spatial correlations to enlarge the impact of the data. Carouge et al. (2010a) inferred spatial
15 and temporal correlation lengths based on the agreement between posterior and “true” fluxes in
16 the framework of a synthetic experiment, where the “truth” is known. A different approach was
17 used in Peters et al. (2007) study where they interpret the length scale from a climatological and
18 ecological perspective, and use it to spread information within regions, which the network is
19 incapable to constrain. Ad-hoc solutions have also been used, assuming that daily fluxes have
20 smaller correlation lengths than monthly fluxes which are used by other studies (Peylin et al.
21 2005). More specifically Peylin et al. (2005) assumed 500 km for daily temporal resolution
22 compared to the much larger correlation lengths used by Rödenbeck for monthly flux resolution.
23 Michalak et al. (2004) implemented a geostatistical approach to describe the prior error structure.
24 Specifically the prior error covariance describes at which degree deviations of the surface fluxes
25 from their mean behavior at two different locations or times are expected to be correlated as a
26 function of the distance in space or in time. They simultaneously estimate posterior fluxes as
27 well as parameters controlling the model-data mismatch uncertainty and the prior flux
28 uncertainty, including spatial and temporal correlation lengths. Although this approach may be
29 considered as an objective way to infer spatial and temporal correlation lengths, it forces the
30 error covariance to be statistically consistent with the atmospheric data from the few regions
31 where station-to-station distances are small enough to be comparable to the correlation length



1 scales. Eddy Covariance stations (EC) can provide a more direct method to infer spatial and
2 temporal flux correlations. Chevallier et al. (2006) and Chevallier et al. (2012) introduced
3 autocorrelation analysis of the residual between fluxes simulated by biosphere models or
4 measured by EC to infer spatial and temporal error correlations. The derived error statistics were
5 implemented in a regional CO₂ inversion by Broquet et al. (2013).

6 Daily NEE flux residuals from model - data comparisons showed temporal correlations up to 30
7 days but very short spatial correlations up to 40 km (Kountouris et al. 2015). In such a case the a-
8 priori integrated uncertainty over time and space, e.g. annually and EU wide domain integrated,
9 according to the error propagation will be exceptionally small. For example a variance of 1.82
10 $\mu\text{mole.m}^{-2}.\text{s}^{-1}$ (from model – data differences) combined with the abovementioned correlation
11 scales yields an uncertainty of 0.12 GtC y⁻¹ for the total flux over Europe. This value is
12 significantly smaller than the assumed uncertainty which is typically used by the inversion
13 systems. For comparison we refer to studies from Rivier et al. (2010) and Peylin et al. (2005) (for
14 a slightly larger domain than ours) where an a priori uncertainty of approximately 1.4 GtC y⁻¹
15 and 1 GtC y⁻¹ respectively was used. Further, Peylin et al. (2013) found that the variance of the
16 posterior NEE fluxes for the European domain among 11 global inversions is also 3 to 4 times
17 larger (0.45 GtC y⁻¹). Although is not yet entirely clear what would be the “correct” value for the
18 prior uncertainty, it seems that in our study it should be increased not only to give enough
19 flexibility to the system to adjust but also to be at least comparable with other posterior
20 uncertainty estimates. A typical method is to inflate the spatiotemporal component by scaling
21 accordingly the prior error covariance. In a study by Lauvaux et al. (2012) two correlation
22 lengths were used at 300 and 50 km, and for the shorter scale the uncertainty was inflated by
23 increasing the RMS of the prior error covariance. The model - data analysis (Kountouris et al.
24 2015) does neither justify the use of large correlation scales nor largely inflated variances which
25 exceed the model-data flux mismatches, however it is consistent with an additional overall bias
26 error which can not be captured from the estimated spatiotemporal error structure. Hence an
27 appropriate approach would be to introduce two adjustable terms into the inversion system. One
28 term to reflect the data-derived error structure without error inflation (prior error covariance
29 matrix which describes the spatiotemporal component) and one term to represent a bias
30 component. To the best of our knowledge such an approach has not yet been used in inversion
31 systems.



1 This study primarily aims to use the information extracted from the model-EC data residuals
2 (spatiotemporal error structure) to define a data-driven error covariance rather than simply
3 assuming one, adopting a conservative one or an expert knowledge solution. For that, we
4 implement our previous methodology and findings regarding the prior uncertainty to atmospheric
5 inversions following Kountouris et al. (2015). As explained above, we implement two
6 uncertainty terms; the first one to reflect the true spatiotemporal error structure and the second
7 term referred to a bias term. We use the Jena inversion system (Rödenbeck, 2005; Rödenbeck et
8 al., 2009) for the regional scale consisting of a fully coupled system as described in Trusilova et
9 al. (2010), between the global three-dimensional atmospheric tracer transport model TM3
10 (Heimann and Körner, 2003) and the regional stochastic Lagrangian transport model STILT (Lin
11 et al., 2003). This scheme allows retrieving surface fluxes at much finer resolution (0.25°)
12 compared to global models. The first part of this study details the methodology of the prior error
13 implementation, and evaluates the system's performance through a synthetic data experiment.
14 The system evaluation is an extension of Trusilova et al. (2010) where the evaluation was limited
15 to the observation space only. We extend that to the flux space by comparing flux retrievals at
16 various spatial and temporal scales against synthetic "true" fluxes. Station locations and
17 observation times (including gaps) were created as in the real observation time series presented
18 in the second part of this study (Kountouris et al., 2016). That way we can use the synthetic
19 experiment to evaluate to what extent we can trust the results, if a real-data inversion is
20 performed. In the second part of this study (Kountouris et al., 2016) the regional inversion
21 system is applied to real observations of atmospheric CO_2 mole fractions from a network of 16
22 stations.

23 This paper is structured as follows. In Section 2 we present the inversion scheme and introduce
24 the settings of the atmospheric inversions. In Section 3 we present the results from a synthetic
25 inversion experiment aimed to assess the prior error setup, considering it as a step towards
26 atmospheric inversions using real atmospheric data with an objective, state of the art prior error
27 formulation. Discussion and conclusions are following in Section 4.

28



1 2 Methods

2

3 2.1 Inversion scheme

4

5 The Jena Inversion System (Rödenbeck 2005; Rödenbeck et al., 2009) was used for the current
6 study. The scheme is based on the Bayesian inference and uses two transport models, the TM3
7 model (Heimann and Körner, 2003) for global, and the STILT model (Lin et al., 2003) for
8 regional simulations. The advantage of the system is that it combines a global transport model
9 with a regional one without the need of a direct coupling along the boundaries. The global is
10 used to calculate fluxes from the far field (outside of the regional domain of interest), and
11 subsequently this information can be used to provide lateral boundary information for the
12 regional model. Primary input of the system is the observed mixing ratios c_{meas} . This vector
13 contains all measured mixing ratios at different times and locations. The modeled mixing ratios
14 c_{mod} given from a temporally and spatially varying discretized flux field f are computed from an
15 atmospheric transport model and can be formally expressed as

$$16 \quad c_{mod} = Af + c_{ini} \quad (1)$$

17 where c_{ini} is the initial concentration and A the transport matrix which maps the flux space to the
18 observation space. For the regional domain the transport matrix A has been pre-computed by the
19 STILT transport model. The system calculates the modeled concentrations when and where a
20 measurement exists in the c_{meas} vector.

21 In the following, we briefly describe the inverse modeling approach. For more details the reader
22 is referred to Rödenbeck (2005).

23 In grid-based atmospheric inversions the number of unknowns (spatially and temporally resolved
24 fluxes) is larger than the number of measurements (hourly dry mole fractions at different sites),
25 making the inverse problem ill-posed. In the Bayesian concept this can be remedied by adding a-
26 priori information. This information can be written as

$$27 \quad f = f_{fix} + F \cdot p \quad (2)$$



1 where f_{fix} is the a-priori expectation value of the flux, matrix F contains all the a-priori
2 information about flux uncertainties and correlations (implicitly defining the covariance matrix)
3 and p is a vector representing the adjustable parameters. The parameters p are uncorrelated with
4 zero mean and unit variance. This flux model represents just a different way to define the a-priori
5 probability distribution of the fluxes, than the traditional way where the a-priori error covariance
6 matrix is explicitly specified. The cost function describing the observational constrain is
7 expressed as

$$8 \quad J_c = \frac{1}{2} (c_{meas} - c_{mod})^T \cdot Q_c^{-1} \cdot (c_{meas} - c_{mod}) \quad (3)$$

9 where Q_c is the observation error covariance matrix. This diagonal matrix weights the mixing
10 ratio values considering measurement uncertainty, location-dependent model uncertainty and a
11 data density weighting. The latter ensures that the higher amount of data from continuous
12 measurements compared to the data from flask measurements would not lead to a considerably
13 stronger impact of these corresponding sites (Rödenbeck, 2005). This can also be formally
14 interpreted as a temporal correlation scale which ensures that the model-data-mismatch error is
15 not independent within a week, corresponding roughly to time scales of synoptic weather
16 patterns.

17 The inversion system seeks to minimize the following cost function that combines the
18 observational (Eq. 3) and the prior flux constrain

$$19 \quad J = J_c + \frac{1}{2} \cdot p^T \cdot p \quad (4)$$

20 The minimization of the cost function is done iteratively with respect to the parameters p by
21 using a Conjugate Gradient algorithm with re-orthogonalization (Rödenbeck 2005).

22

23

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1 2.2 Characteristics of the inversion set up

2

3 2.2.1 A-priori information and uncertainties

4

5 The a-priori CO₂ flux fields were derived from the Vegetation Photosynthesis and Respiration
6 Model, VPRM (Mahadevan et al., 2008). VPRM uses ECMWF operational meteorological data
7 for radiation (downward shortwave radiative flux) and temperatures (T2m), the SYNMAP
8 landcover classification (Jung et al., 2006), and EVI (enhanced vegetation index) and LSWI
9 (land surface water index) derived from MODIS (Moderate Resolution Imaging
10 Spectroradiometer). Model parameters were re-optimized for Europe using eddy covariance
11 measurements made during 2007 from 47 sites (a full site list is given in Kountouris et al.
12 (2015); we excluded some sites due to insufficient temporal data coverage or lack of
13 representativeness). To mediate the impact of data gaps, a data density weighting was introduced
14 that takes into account the coverage of different times of the day (using 3-hour bins) in the
15 different seasons. Optimized parameters are shown in Table 1. The net ecosystem exchange at
16 hourly scale and at 0.25° x 0.25° spatial resolution for 2007 was simulated with the optimized
17 parameters for the European domain shown in Fig. 1. The domain-wide aggregated biospheric
18 carbon budget for 2007 derived that way from VPRM was found to be -0.96 GtC y⁻¹ (i.e. uptake
19 by the biosphere). Note that without the density weighting an even stronger flux of -1.35 GtC y⁻¹
20 was derived, indicating the importance of proper treatment of data gaps by either gap-filling or
21 by the inclusion of weights.

22 Additionally, biogenic CO₂ fluxes were simulated with the BIOME-BGC model, specifically its
23 global implementation as GBIOME-BGCv1 (Trusilova and Churkina 2008) at the same 0.25° x
24 0.25° spatial and hourly temporal resolution. The purpose of the second flux field is to provide a
25 perfectly known flux distribution as “true” fluxes that can be used to generate synthetic
26 observations. The a-priori flux in a real-data inversion would have three components including
27 fossil fuel and ocean fluxes

$$28 \quad f_{pr} = f_{pr,nee} + f_{pr,ff} + f_{pr,oc} \quad (5)$$



1 We note that for the synthetic case the last two terms are set to zero. Similarly the deviation term
 2 (the data-derived correction to the a-priori fluxes) of the flux model consists of the terms
 3 referring to NEE, fossil fuel, and ocean fluxes but equivalently the last two terms are set to zero
 4 for the synthetic inversion.

$$5 \quad F \delta s = (F_{nee}, F_{oc}, F_{ff}) \begin{pmatrix} \delta s_{nee} \\ \delta s_{oc} \\ \delta s_{ff} \end{pmatrix} \quad (6)$$

6 Note that the a-priori error covariance matrix does not explicitly appear in the inversion, but is
 7 included though the second term in Eq. 8 (see section 2.2.2).

8 According to this formulation the columns of G_{Icor} and G_{xycor} contain the spatiotemporal extents
 9 of the individual NEE pulses (range of values between 0 and 1) and the diagonal matrix $f_{sh}(x,y,t)$
 10 contains the pixel-wise a priori uncertainties. These uncertainties were chosen to be flat
 11 (constant) in space and time. For more detailed information the reader is referred to Rödenbeck
 12 et al. (2005).

13 The total prior uncertainty was chosen according to the mismatch between VPRM and BIOME-
 14 BGCv1, calculated as the annual and domain wide integrated flux mismatch. Prior fluxes and the
 15 fluxes representing the synthetic truth are strongly different (-0.96 GtC y⁻¹ and -0.31 GtC y⁻¹ for
 16 VPRM and GBIOME-BGCv1, respectively). The error structure used for the synthetic study is
 17 estimated according to the method applied in Kountouris et al. (2015). Time-series of daily
 18 fluxes were extracted for both biosphere models at grid cell locations where an EC station exists.
 19 Then spatial and temporal autocorrelation analysis was performed on the daily model-model flux
 20 residuals, yielding a spatial correlation length scale of 566 km and a temporal correlation scale of
 21 30 days.

22 The eddy covariance station locations used for this analysis were exactly the same as in
 23 Kountouris et al. (2015) ensuring similarity in the derivation of the error structure for the
 24 synthetic data inversions. However of note is that for the synthetic data inversions, prior fluxes
 25 from VPRM model were not optimized against GBIOME-BGCv1 “true” fluxes.



1 The implicitly defined prior error covariance matrix contains diagonal elements of $(1.45 \mu\text{mol m}^{-2} \text{ s}^{-1})^2$, which reflect the variance from model-model flux mismatches at the 50 km spatial
2 resolution of the state space. Exponentially decaying spatial correlations were implemented with
3 a correlation scale of 766 km at the zonal and 411 km at the meridional direction, roughly
4 corresponding to the 566 km correlation scale yielded from the model-model residual
5 autocorrelation analysis and preserving the same zonal/meridional ratio as in the global
6 inversion. Temporal autocorrelation was set to 31 days, which is consistent with the Kountouris
7 et al. (2015) analysis. These scales result in an uncertainty for the spatiotemporal component
8 (E_{ST}) domain-wide and annually integrated of 0.44 GtC y^{-1} . We chose two different approaches to
9 increase the prior uncertainty at domain-wide and annually integrated scale such that it matches
10 the mismatch of 0.65 GtC y^{-1} between the two biosphere models. First we inflate the error by
11 scaling the error covariance matrix, this case is referred to as base case B1 hereafter. The second
12 approach, referred to as scenario S1, could be considered as a more formal way: we introduce an
13 additional degree of freedom to the inversion system by allowing for a bias term. This term is
14 spatially distributed according to the annually averaged VPRM respiration component, and is
15 kept constant in time. The error E_{BT} of the bias component was adjusted such that the total prior
16 error E_{tot} for annually and domain-wide integrated fluxes matches the targeted total uncertainty:
17

$$18 \quad E_{tot}^2 = E_{ST}^2 + E_{BT}^2 \quad (7)$$

19 This resulted in an overall uncertainty E_{tot} of 0.65 GtC y^{-1} , which is identical to the mismatch
20 between the two biosphere models.

21

22

23 **2.2.2 State space**

24

25 The inversion system optimizes additive corrections to three-hourly fluxes in a sense that the
26 posterior flux estimate can be given by the sum of a fixed a priori term (first term of the right
27 hand side in Eq. 8) and an adjustable term (second term in Eq. 8). The latter has a-priori a zero
28 mean and unit variance. The biogenic fluxes can be defined as follows:



$$1 \quad f(x, y, t) = f_{fix}(x, y, t) + f_{sh}(x, y, t) \cdot \sum_{m_x}^{N_x} \sum_{m_y}^{N_y} G_{tcor, m_x}(t) \cdot G_{xycor, m_x}(x, y) \cdot p_{inv, m_x, m_y} \quad (8)$$

2 where f_{sh} is a shape function which defines the adjustable term. The spatial and temporal
 3 correlation structures of the uncertainty are described by the pulse response functions G_{xycor} and
 4 G_{tcor} respectively. The term p_{inv} contains the adjustable parameters which they a-priori have, a
 5 Gaussian distribution with zero mean and unit variance.

6 For the S1 case the posterior flux estimates can be derived by adding the optimized bias flux
 7 field to Eq. 8

8

$$9 \quad f(x, y, t) = f_{fix}(x, y, t) + f_{sh}(x, y, t) \cdot \sum_{m_x}^{N_x} \sum_{m_y}^{N_y} G_{tcor, m_x}(t) \cdot G_{xycor, m_x}(x, y) \cdot p_{inv, m_x, m_y} + f_{sh}^{BT}(x, y) \cdot \sum_{m_x}^{N_x} G_{tcor, m_x}(t) \cdot p_{BT}$$

10 (9)

11 The bias term f_{sh}^{BT} follows a flux shape (here we used annually averaged respiration, with no
 12 temporal variation).

13

14 2.2.3 Observation vector and uncertainties

15

16 The observation vector c_{meas} contains mixing ratio observations at all site locations and sampling
 17 times. A common procedure to derive synthetic observations is to create a “true” flux field by
 18 adding some error realizations to the a-priori fluxes (Schuh et al., 2009; Broquet et al., 2011) or
 19 to perturb the resulting synthetic observations (Wu et al., 2011). For the current study instead we
 20 use a different biosphere model, the GBIOME-BGCv1 model, to derive biogenic CO₂ fluxes at
 21 hourly scale. Then a forward transport model run was performed to create synthetic mixing ratios
 22 at hourly resolution for each station location. This choice of using two different biosphere
 23 models for deriving the a-priori and the “true” fluxes is expected to increase the realism of the
 24 synthetic data study, given the fact that the real spatiotemporal flux distribution is highly
 25 unknown (though the model-to-model difference may not accurately reflect the model errors
 26 either). For the synthetic study, observations were created for the same station locations and



1 observation times as in the real observation time series which are used in the second part of this
2 study (Kountouris et al., (2016)). An overview of the atmospheric stations is given in table 2.
3 The data coverage per station is shown in Figure 2. Only daytime observations were considered
4 (11:00 – 16:00 local time) since the transport model is expected to perform worse during night
5 when a stable boundary layer forms. An exception is made for mountain stations that measure
6 the free troposphere, where only nighttime observations (23:00 – 04:00 local time) were
7 considered, as this time can be better represented by the transport model. In total 20273 hourly
8 observations from the year 2007 were used.

9 The model-data mismatch uncertainty associated with each measurement is expressed as a
10 diagonal covariance matrix, and contains measurement errors and errors from different
11 components describing the modeling framework (i.e. model errors due to imperfect transport,
12 aggregation errors, etc.) (Gerbig et al., 2003b). For the current study, all sites are classified
13 according to their characteristics (e.g. tall tower, mountain sites etc.), and uncertainties were
14 defined depending on the site class (Figure 2, legend on the right). The uncertainties are
15 considered as representative for current inverse modeling systems. Although the measurement
16 error covariance is a diagonal matrix, we do consider for temporal correlations via a data density
17 weighting (see Section 2.1).

18

19 **2.2.4 Atmospheric transport**

20

21 For the synthetic data study only the regional atmospheric model STILT was used to create the
22 observations with a forward run, and to perform the inversion. This was feasible since the
23 synthetic CO₂ observations are only influenced by fluxes occurring within the DoI, hence global
24 runs to retrieve boundary conditions at the edge of DoI are not necessary. The transport matrix
25 for the regional inversions was generated in form of pre-calculated footprints (sensitivities of
26 atmospheric observations to upstream fluxes) at 0.25 degrees spatial and hourly temporal
27 resolution for the full year 2007. STILT trajectory ensembles were driven by ECMWF
28 meteorological fields (Trusilova et al., 2010), and computed for 10 days backwards in time,
29 ensuring that nearly all trajectories have left the domain of interest.



1 2.3 Metrics for performance evaluation

2

3 Following Rödenbeck et al. (2003) we evaluate the goodness of fit for each station (station
4 specific χ^2). The modeled dry mole fractions should be with 68% probability within the $\pm 1\sigma$
5 range from the observed mole fractions. This is equivalent to the requirement that the dry mole
6 fraction part of the cost function defined as the sum of hourly squared differences, divided by the
7 uncertainty interval and the number of observations n (Eq. 10), should be close to unity.

$$8 \quad \chi_c^2 = \frac{\sum_i \frac{(\Delta c_i)^2}{\sigma_i^2}}{n} \quad (10)$$

9 Another important aspect is the reduced χ_r^2 metric that compares the a-priori model performance
10 with the specified error structure by dividing the squared residuals of optimized minus observed
11 dry mole fractions by the squared specified uncertainties. This is also equivalent to two times the
12 cost function at its minimum divided by the number of degrees of freedom (effective number of
13 observations) (Thompson et al., 2011):

$$14 \quad \chi_r^2 = 2 \frac{J_{\min}}{n} \quad (11)$$

15 Again, a correct balance should be close to unity. Smaller values suggest that the model
16 performance was better than specified in the covariance structure and hence the assumed
17 uncertainties (denominator) were conservative.

18 In flux space, we evaluate the inversion performance, by comparing the retrieved flux estimates
19 against the synthetic fluxes (“true”) at different temporal and spatial scales: annually and
20 monthly integrated fluxes, domain-wide and at country scale. In particular we are interested in
21 capturing the “true” fluxes down to country scale. For that we assess monthly posterior retrievals
22 which we compare to reference data (“true” fluxes), country aggregated, using a Taylor diagram.
23 This diagram provides a concise statistical summary of how well patterns match each other in
24 terms of their correlation and the ratio of their variances.

25



1 **3 Results**

2

3 The purpose of the synthetic study is to evaluate the system set-up with a realistic approach. To
4 evaluate the ability of the system to retrieve the synthetic true fluxes we visualize spatially
5 distributed fluxes and we study spatially integrated (domain and national scale) as well as
6 temporally (annual and monthly scale) integrated fluxes.

7

8 **3.1 CO₂ mole fractions**

9

10 A comparison of true and modeled CO₂ dry mole fractions from forward runs of the optimized
11 fluxes can reveal the goodness of fit, realized through the optimization process. Such a
12 comparison is presented in Figure 3 for the Schauinsland (SCH) continuous station. Both B1 and
13 S1 inversions significantly reduce the misfit between the synthetic (truth) and the a-priori mole
14 fractions. The RMSD between the prior/posterior from the “true” timeseries for all stations
15 (Table 3) shows an average reduction of around 74% and 76% for the S1 and B1 inversions
16 respectively. Prior correlations (prior vs. true dry mole fractions), have an averaged value of 0.46
17 which is increased to 0.93 for both inversions. Significant differences between the two inversions
18 were not found apart from a slightly larger decrease of the RMSD for the B1 case. Figure 4
19 summarizes the capability of the inversions to capture the true signal at each station location in
20 form of a Taylor diagram, indicating that the inversions showed a significant increase of the
21 correlation for all sites. Further the variance of the modeled time-series is significantly closer to
22 the variance of the true signal.

23 To estimate the goodness of fit we consider the station specific χ_c^2 values (Eq. 10), using here 7-
24 day aggregated residuals instead of hourly to match the temporal scale of one week of the
25 observation error. Values smaller than 1 are found for most of the stations with a mean value of
26 0.28 and 0.32 for the B1 and S1 cases respectively, suggesting a good fitting performance for all
27 stations and for both inversions. The results are comparable with those found in the Rödenbeck
28 et al. (2003) study. The reduced chi-squared (Eq. 11) was found to be 0.21 for both cases,
29 indicating that the error variance is overestimated making the error assumption rather
30 conservative.



1 3.2 Flux estimates and uncertainties

2

3 The spatial distributions of the annual biosphere-atmosphere exchange fluxes for the prior, the
4 known truth, and the posterior cases are presented in Figure 5. Note that annual fluxes between
5 the two biosphere models used for prior fluxes and true fluxes are substantially different. The
6 inversion significantly adjusts the spatial flux distribution mainly in central Europe, where a
7 denser atmospheric network exists. The absolute annual mean difference in fluxes ($|\text{mean}(\text{true} -$
8 $\text{prior})|$ and $|\text{mean}(\text{true} - \text{posterior})|$) is greatly reduced from $70.8 \text{ gCm}^{-2}\text{y}^{-1}$ to $14.7 \text{ gCm}^{-2}\text{y}^{-1}$ and
9 $24.6 \text{ gCm}^{-2}\text{y}^{-1}$ for the B1 and S1 inversions respectively. Detailed patterns, however, are not
10 well reproduced: the fraction of explained spatial variance in the true fluxes (measures as
11 squared Pearson correlation coefficient) decreases from the prior (0.17) to the posterior (0.07 and
12 0.06 for the cases B1 and S1, respectively). When evaluating this at monthly scales, the fraction
13 of explained spatial variance increases in the posterior estimates compared to the prior for winter
14 months from around 0-15% to about 15-50%, while during the growing season typically a
15 decrease from around 10-35% to about 0-34% is found. The accumulated footprint of the
16 atmospheric network is shown in Figure 6, clearly indicating the strongest constraint on fluxes in
17 central Europe. Interestingly both error structures from S1 and B1 inversions produce posterior
18 fluxes that have approximately the same spatial distribution. When separating the spatiotemporal
19 component from the bias component (in S1 case) we can identify differences between the two
20 inversions. Significant deviations of the spatial flux distribution between the spatiotemporal
21 components were found: The spatiotemporal component in the S1 case has a domain wide annual
22 flux correction of 0.39 GtC y^{-1} (prior – posterior) while the corresponding term in the B1 case
23 has a correction of 0.78 GtC y^{-1} . Nevertheless standard deviations of the corrections with respect
24 to the true spatial flux distribution (true – posterior) found to have no significant difference
25 ($6.88 \cdot 10^{-5}$ and $7.38 \cdot 10^{-5} \text{ GtC y}^{-1}\text{cell}^{-1}$ for S1 and B1 respectively). We do not observe any strong
26 correction in the south-eastern part of Europe as it cannot be “seen” from the atmospheric
27 network due to the distance to the observing sites and the prevailing westerly winds. This could
28 also be inferred from the flux innovation plots (see Figure 5) defined as the difference between
29 prior and posterior fluxes. Only very small or even no corrections occurred in this area.

30 We are specifically interested in the ability of the inversion system to capture integrated fluxes
31 over time and space. Figure 7 shows an overview of the domain-integrated fluxes at a monthly



1 and annual scale. Despite the remarkably larger a-priori (VPRM) sink compared to the synthetic
2 truth (GBIOME-BGCv1) during the growing season, both inversions, with and without the bias
3 term, produce posterior flux estimates that fully capture the "true" monthly and annually
4 integrated fluxes. While the monthly posterior estimates give no clear evidence on which
5 inversion performs better, retrievals at annual scale slightly favor the inversion without the bias
6 term (B1 case). A difference was observed in the prior uncertainties between the two inversions.
7 While both were scaled to have the same prior annual uncertainty, the B1 inversion has
8 systematically larger prior monthly uncertainties than the S1 as a result of the inflated
9 spatiotemporal component of the prior error covariance. Posterior uncertainties were found to be
10 similar, and include or are close to including (S1 case) the true flux estimates. The uncertainty
11 reduction for annually and domain-wide integrated fluxes, defined as the difference between
12 prior and posterior uncertainties normalized by the prior uncertainty, was found to be 73% and
13 69% for the S1 and B1 respectively.

14 In order to assess how well the posterior estimates agree with the true fluxes, root mean square
15 difference (RMSD) between true and posterior monthly integrated gridded fluxes were computed
16 (Table 4). Both inversions B1 and S1 show a similar reduction in the RMSD values compared to
17 the prior. The same picture emerges for the annually integrated fluxes.

18 Of particular interest is the performance of the system at regional scale, specifically at national
19 level. Figure 8 shows monthly fluxes for selected European countries, including the prior, true
20 and posterior estimates with the corresponding uncertainties. Both error structures show a similar
21 performance. Despite the large prior misfit, the system succeeded in retrieving monthly fluxes at
22 country level. Better constrained regions mainly located in central Europe show the ability to
23 broadly capture the temporal flux variation at monthly scale. Figure 9 summarizes in a Taylor
24 diagram the inversion performance for each EU-27 country, showing the improvement of
25 monthly and country aggregated fluxes (perfect match would be if the head of the arrow
26 coincides with the reference point marked as green bullet). It is worth mentioning that also for
27 regions that are less constrained by the network, such as Great Britain, Spain, Poland and
28 Romania, the inversions still improved the posterior estimates compared to the prior estimates
29 (see also Fig. 9).

30



1 **3.3 Evaluation with synthetic eddy covariance data**

2

3 In order to investigate the potential of using eddy covariance measurements for evaluating the
4 retrieved CO₂ fluxes, monthly fluxes from the prior (VPRM), the truth (GBIOME-BGCv1), and
5 the posterior for cases B1 and S1 were extracted at the grid cell locations where eddy covariance
6 stations exist, using the same 53 sites as in Kountouris et al. (2015). The corresponding fluxes
7 were then aggregated over all sites, using a weight that compensates for the asymmetry between
8 number of flux towers for specific vegetation types and the fraction of land area covered by the
9 specific vegetation type. Prior fluxes show a systematically larger uptake compared to the truth,
10 predominantly during the growing season with maximum differences of 0.8 gCm²day⁻¹ (Figure
11 10). Posterior estimates for both cases captured the magnitude of the true fluxes, with maximum
12 differences of around 0.3 gCm²day⁻¹ during June/July. A significantly larger correction is
13 apparent during spring and summer compared to winter and fall. The very close correspondence
14 of these results with those shown in Figure 7 for the domain-wide monthly flux budget clearly
15 shows that eddy covariance measurements can principally be used for validation of the inverse
16 estimates at monthly timescales.

17

18 **4 Discussion**

19

20 **4.1 Performance in flux space**

21

22 Results from the synthetic experiment showed the strengths but also the weaknesses of the
23 system to retrieve the “true” spatial flux distribution. Although the error structure applied to this
24 experiment was statistically coherent with the mismatch between prior and true fluxes, we note a
25 limited ability of the current atmospheric network to retrieve fluxes at local scales. For coarser
26 spatial scales (country level) the carbon budget estimates in the synthetic inversion showed a
27 quite good performance at monthly and annual temporal scales. Further we observed an average
28 reduction of the monthly uncertainties of 65% for the B1 case, and 64% for the S1 case. In



1 combination with the fact that the flux estimates reproduce the “truth” within the posterior
2 uncertainties, this gives us confidence in the accuracy of our estimates.

3 Prior error correlation in time and space limits the scale, at which information can be retrieved
4 from the inversion. The spatial correlation of several hundred kilometers implies that fluxes at
5 scales smaller than this cannot be significantly improved by the inversion, as the results clearly
6 showed. To assess this more quantitatively, the spatial correlation between a priori or retrieved
7 and true monthly fluxes is calculated for different spatial aggregation scales (starting at 0.25
8 degree, fluxes were aggregated to 0.5, and then in 1-degree steps up to 8 degree). Results shown
9 in Fig. 11 a) indicate a nearly continuous increase of the spatial correlation of prior and posterior
10 fluxes with increasing aggregation scale. The additional explained variance brought about by the
11 inversion, i.e. the difference between posterior (red/blue line) and prior (grey line) flux
12 correlation (r-square) with the truth, starts at low values around 0.1, and reaches values around
13 0.2 for scales larger or equal 2 degrees. Similarly, the spatial correlation between a priori and
14 true fluxes for a given spatial aggregation of 2 degrees, but for different temporal aggregation
15 scales ranging from 1 day to 128 days (Fig. 11 b) shows a continuous increase from about 0.23 to
16 0.42 (r-square), while the spatial correlation between retrieved and true fluxes only varies
17 slightly between 0.4 and 0.53 (Fig. 11 b), red and blue lines). Here, the additional spatial
18 variance explained by the retrieved fluxes is largest at around monthly time scales (differences
19 between prior and posterior r-square around 0.2), while at seasonal scales this additional
20 explained variance is only around 0.1. Overall, this analysis confirms that there are preferred
21 spatial and temporal scales at which the inversion retrieves the flux distribution best and where
22 thus most information is gained. This is not dependent on whether or not a bias term is included
23 in the state vector, as results for case B1 and S1 do not differ in this regard. It is important to
24 realize that all other scales, at which the inversion does not provide much information, need to be
25 properly represented by the a priori flux distribution. Thus the a priori fluxes need to be realistic
26 at short spatial scales below about 200 km, at seasonal temporal scales, and of course at hourly
27 time scales which are not retrieved by the inversion.

28 The annual spatial flux distribution of the B1 and S1 cases was found to be quite similar,
29 indicating that inflating the uncertainty by a factor of 1.5 (B1 case, see also 2.2.1 section) or
30 adding a bias component to compensate the inflation (S1 case) lead to a similar flux constraint.



1 This could be explained due to the long correlation length (566 km) which drastically reduces the
2 effective number of degrees of freedom, forcing the fluxes to be smoothly corrected, regardless
3 the use of the bias component.

4

5 **4.2 Performance in observation space**

6

7 The high RMSD reduction in combination with the high correlation values and the captured
8 variability between posterior and true dry mole fractions in the synthetic experiment suggest a
9 good performance of the inversion system to retrieve the “true” mixing ratios. Nevertheless this
10 is not surprising, as the atmospheric data are “fitted” by the inversion, and furthermore the
11 forward and the inverse runs used identical transport, without any impact from imperfections in
12 transport simulations.

13 The uncertainties in the flux space are statistically consistent with the model-model flux
14 mismatch. However the reduced χ_r^2 values obtained from the inversions were rather small
15 (around 0.21). This indicates that overall conservative uncertainties were assumed, and the small
16 χ_r^2 values are a result from the assumed uncertainties in the observation space. Indeed
17 uncertainties in the observation space include also transport uncertainties; however, given that
18 the same transport is used to create synthetic observations and to perform the inversion, there is
19 no actual model-data mismatch related to transport uncertainties, and so the assumed
20 uncertainties are overestimated.

21

22 **5 Conclusions**

23

24 This paper describes the setup and the implementation of prior uncertainties as derived from
25 model-eddy covariance data comparisons into an atmospheric CO₂ inversion. The inversion
26 system assimilates hourly dry air mole fractions from 16 ground stations to optimize 3-hourly
27 NEE fluxes for the study year 2007. Two different error structures were introduced to describe
28 the prior uncertainty by either inflating the error or by adding an additional degree of freedom



1 allowing for a long term bias. The need of this error inflation comes from the fact that the
2 spatiotemporal model - data error structure alone underestimates prior uncertainties typically
3 assumed for inversion systems at continental/annual scale. In this study we evaluate the Jena
4 inversion system by performing a synthetic experiment and expanding the evaluation also to the
5 retrieved fluxes, whilst only the observation space was evaluated in Trusilova et al. (2010).
6 Further we assess the impact when adding a bias term in the flux error structure. This study is a
7 preparatory step to retrieving European biogenic fluxes using a data driven error structure
8 consistent with model-flux data mismatches, which is described in the companion paper
9 (Kountouris et al. 2016).

10 Significant flux corrections and error reductions were found for larger aggregated regions (i.e.
11 domain-wide and countries), giving us confidence on the reliability of the results for a real data
12 inversion. We found a similar performance for both error structures. A more detailed analysis of
13 the spatial and temporal scales, at which the inversion provides a significant gain in information
14 on the distribution of fluxes, clearly confirms that a) fluxes at spatial scales much smaller than
15 the spatial correlation length used for the a priori uncertainty cannot be retrieved; b) the inversion
16 performs best at temporal scales around monthly, and c) especially the small spatial scales need
17 to be realistically represented in the a priori fluxes.

18

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25 data streams publication is an outcome of the International Space Science Institute (ISSI)
26 Working Group on "Carbon Cycle Data Assimilation: How to consistently assimilate multiple
27 data streams.

28

29



1 Appendix

2

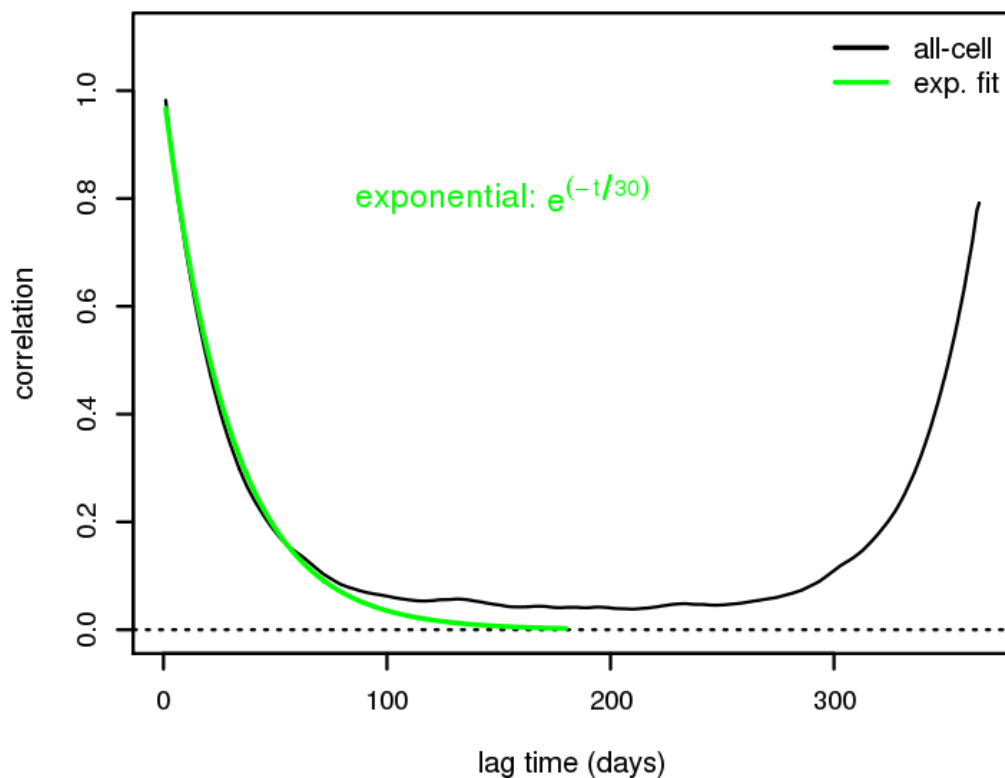
3 The exponentially decaying temporal autocorrelations is a feature newly implemented into the
4 Jena Inversion System. Temporal correlations are not directly defined as off-diagonal elements
5 in the a-priori error covariance, as the latter does not appear explicitly in the inversion. Rather,
6 the inversion system involves time series filtering in terms of weighted Fourier expansions. More
7 specifically the columns of matrix G_{cor} contain Fourier modes, weighted according to the
8 frequency spectrum that corresponds to the desired autocorrelation function. The reader is
9 referred to Rödenbeck (2005) for more information. Following Rödenbeck (2005) we define the
10 following spectral weight w :

$$11 \quad w = \frac{\nu_{\text{low}}}{\sqrt{\nu_{\text{low}}^2 + (2\pi\nu)^2}} \quad \text{A1}$$

12 where ν_{low} is the characteristic frequency. The characteristic frequency ν_{low} can be calculated
13 from the desired temporal autocorrelation time (30 days) of the exponential decay and is
14 expressed in years:

15 $\nu_{\text{low}} = 1/(1/12)$ where 1/12 is the autocorrelation time in years. Hence the characteristic frequency
16 corresponding to a monthly autocorrelation is 12.

17 To test numerically whether the implemented autocorrelation decay shape approximates an
18 exponential decay, an error realization of the characteristic frequency was added to the prior
19 fluxes, and the autocorrelation function as described in Kountouris et al. (2015) was calculated
20 numerically simultaneously for the flux time series of all grid cells. Then an exponentially
21 decaying function was fitted (Fig. A1) to derive the autocorrelation scale for the corresponding
22 frequency. The resulting autocorrelation shape indeed approximates very well an exponential
23 decay, with an e-folding time of precisely 30 days. The tight confidence bounds of the fitted
24 parameter (29.3 and 30.6 days within 95 % confidence interval), in combination with the small
25 residual sum-of-squares (0.14) suggests a very good approximation of the exponential decay.



1

2 Figure A1: Autocorrelation function for a characteristic frequency of the exponential filter. The
3 autocorrelation is calculated simultaneously for all the domain grid cells. The numerical
4 realization of the autocorrelation does not decay to zero because of the flux seasonality.

5

6

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1

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1 Table 1. Optimized VPRM parameters SW_0 , λ_{SW} , α , β for different vegetation classes^a

	SW_0	λ_{SW}	α	β
Evergreen forest	275	0.226	0.288	-1.10
Deciduous forest	254	0.215	0.181	0.84
Mixed forest	446	0.163	0.244	-0.49
Open shrub	70	0.293	0.055	-0.12
Crop	1132	0.086	0.092	0.29
Grass	528	0.119	0.125	0.017

2 ^aUnits are as follows: SW_0 : $W m^{-2}$; λ_{SW} : $\mu mole CO_2 m^{-2}s^{-1} / (W m^{-2})$; α : $\mu mole CO_2 m^{-2}s^{-1} / ^\circ C$;3 β : ($\mu mole CO_2 m^{-2}s^{-1}$).

4



- 1 Table 2. Information on the stations used for the regional inversions. Same network applied for
 2 the synthetic, and the real data inversions in Kountouris et al. (2016). In first column the term
 3 “type” stands for continuous (C) or flask (F) data.

Site Code / type	Name	Latitude (°)	Longitude (°)	Height (m.a.s.l.) (m)	Measurement height (above ground) (m)	Model height
BAL/F	Baltic Sea, Poland	55.50	16.67	8	57	28
BIK/C	Bialystok, Poland	53.23	23.03	183	90	90
CBW/C	Cabauw, Netherlands	51.58	4.55	-2	200	200
CMN/C	Monte Cimone, Italy	44.18	10.7	2165	12	670
HEI/C	Heidelberg, Germany	49.42	8.67	116	30	30
HPB/F	Hohenpeissenberg, Germany	47.80	11.01	934	50	10
HUN/C	Hegyhatsal, Hungary	46.95	16.65	248	115	96
JFJ/C	Jungfrauoch, Switzerland	46.55	7.98	3572	10	720
KAS/C	Kasprowy Wierch	49.23	19.93	1987	5	480
LMU/C	La Muela, Spain	41.36	-1.6	570	79	80
MHD/C	Mace Head, Ireland	53.33	-9.90	25	10	15
OXX/C	Ochsenkopf,	50.03	11.81	1022	163	163



	Germany						
PRS/C	Plateau Rosa,	45.93	7.71	3480	-	500	
	Italy						
PUY/C	Puy De Dome,	45.77	2.97	1465	10	400	
	France						
SCH/C	Schauinsland,	47.92	7.92	1205	-	230	
	Germany						
WES/C	Westerland,	54.93	8.32	12	-	15	
	Germany						



1 Table 3. RMSD (first column in ppm) and correlation coefficients (second column) between
 2 known truth and prior/posterior CO₂ dry mole fractions for daily “daytime” or “nighttime”
 3 averaged values and for each station. The third column shows χ^2 , the normalized dry mole
 4 fraction mismatch per degree of freedom for 7-day averaged residuals, as a measure of how well
 5 the data were fitted. The format for each station is as follows: RMSD | r² | χ^2 .

	Prior	B1	S1
BAL	4.78 0.07 18.44	0.89 0.97 0.48	1.02 0.96 0.37
BIK	5.28 0.43 15.50	1.20 0.97 0.18	1.29 0.97 0.25
CBW	8.60 0.04 74.29	0.99 0.99 1.31	1.06 0.99 1.34
CMN	2.68 0.33 6.31	0.74 0.93 0.08	0.78 0.92 0.10
HEI	11.39 0.37 12.97	1.83 0.98 0.36	1.84 0.98 0.37
HPB	7.73 0.35 26.58	1.01 0.99 0.21	1.19 0.99 0.31
HUN	6.50 0.63 31.89	1.36 0.98 0.21	1.46 0.98 0.25
JFJ	3.12 0.21 3.93	1.24 0.86 0.24	1.31 0.84 0.27
KAS	4.00 0.32 10.67	0.73 0.98 0.11	0.80 0.97 0.15
LMU	3.42 0.19 6.5	0.79 0.95 0.12	0.86 0.94 0.16
MHD	1.53 0.0002 0.83	0.65 0.09 0.16	0.68 0.06 0.17
OXK	6.10 0.21 38.50	3.35 0.76 0.76	3.40 0.75 0.80
PRS	2.32 0.15 2.46	0.70 0.92 0.30	0.74 0.91 0.33
PUY	4.27 0.15 12.06	0.68 0.97 0.06	0.73 0.15 0.09
SCH	4.76 0.26 21.17	0.90 0.97 0.07	0.95 0.97 0.09

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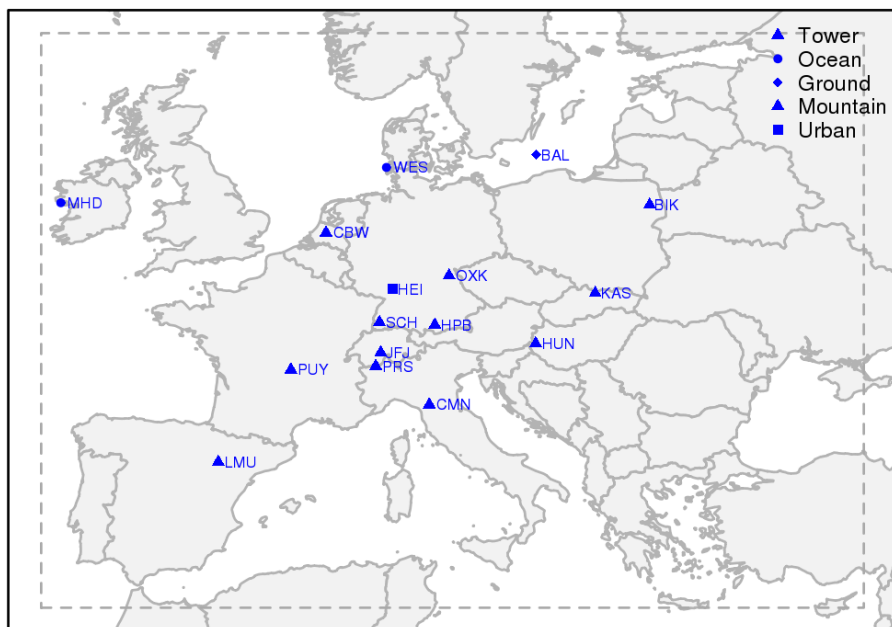
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- 1 Table 4. Performance of the two error structures expressed as the spatial RMSD of the optimized
- 2 monthly and annual NEE fluxes compared to the truth for the whole domain in $\mu\text{mole m}^{-2} \text{s}^{-1}$.

	Annual	JAN	FEB	MAR	APR	MAY	JUN	JUL	AUG	SEP	OCT	NOV	DEC
prior	0.38	0.61	0.53	0.55	1.06	1.26	1.56	1.17	0.94	0.65	0.57	0.63	0.63
B1	0.33	0.46	0.40	0.45	0.84	0.99	1.21	1.00	0.86	0.63	0.43	0.46	0.44
S1	0.34	0.48	0.41	0.45	0.86	1.01	1.24	1.03	0.86	0.63	0.45	0.47	0.45

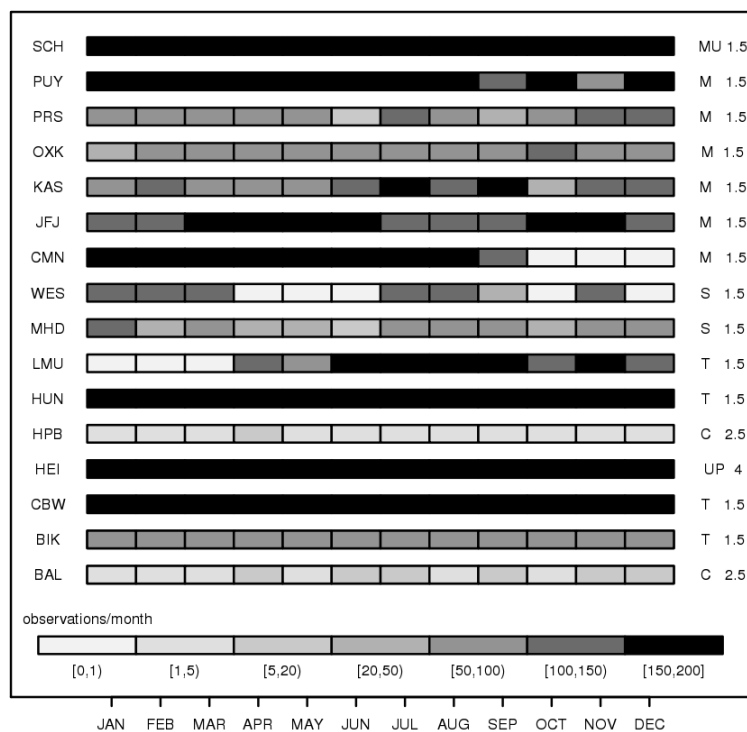
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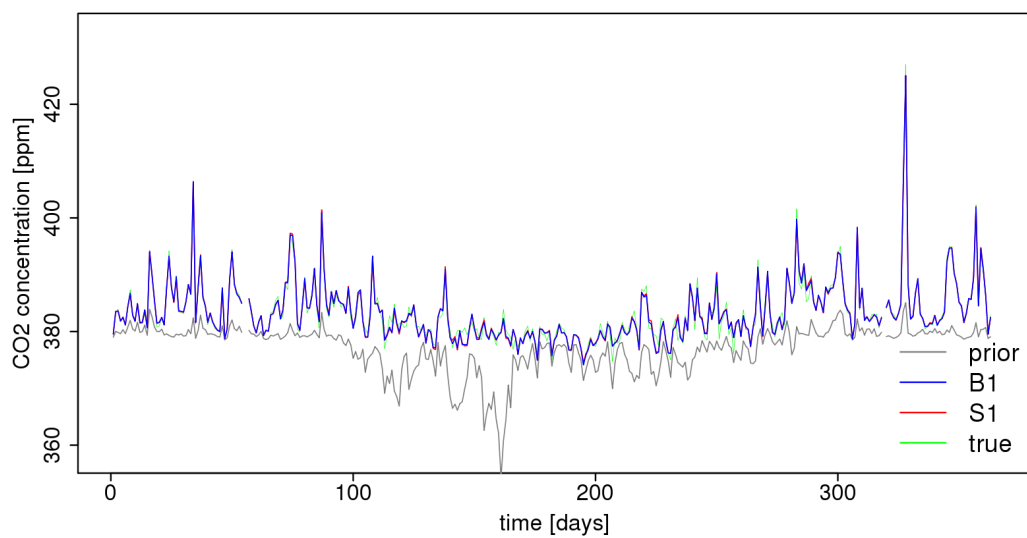
2 Figure 1. Domain of the inversions (dashed rectangle). Locations of the atmospheric
3 measurement stations are shown with blue marks. Red stars denote the eddy covariance locations
4 used for flux comparisons at grid scale.

5



1

2 Figure 2. Monthly data coverage plot for the atmospheric stations used in the regional inversions.
 3 Left column shows the code name and the right columns show the station class and the assigned
 4 uncertainty in units of ppm. “C” stands for continental sites near the surface, “T” for continental
 5 tall towers, “S” for stations near shore, “M” for mountain sites, “MU” for mountain sites with
 6 diurnal upslope winds and “UP” for urban pollutant.



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2 Figure 3. Daily nighttime (23:00-4:00 UTC) averages for prior, true, and posterior CO₂ dry mole
3 fraction time series for the mountain site Schauinsland. Time starts at 1st January 2007.

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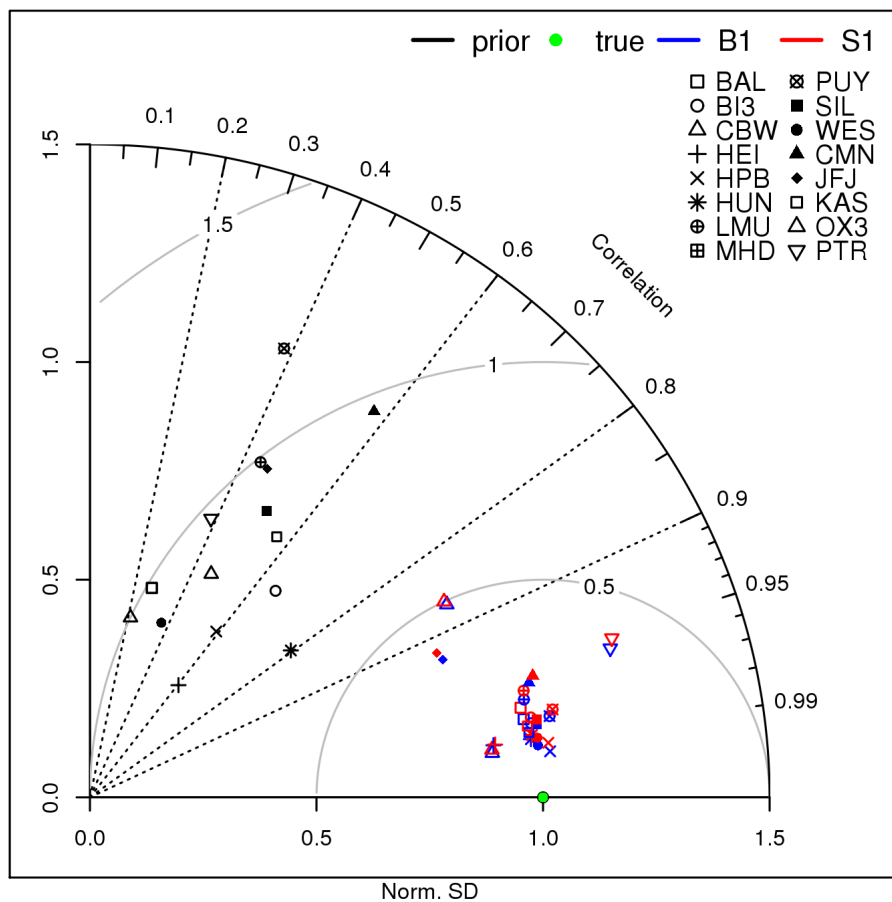
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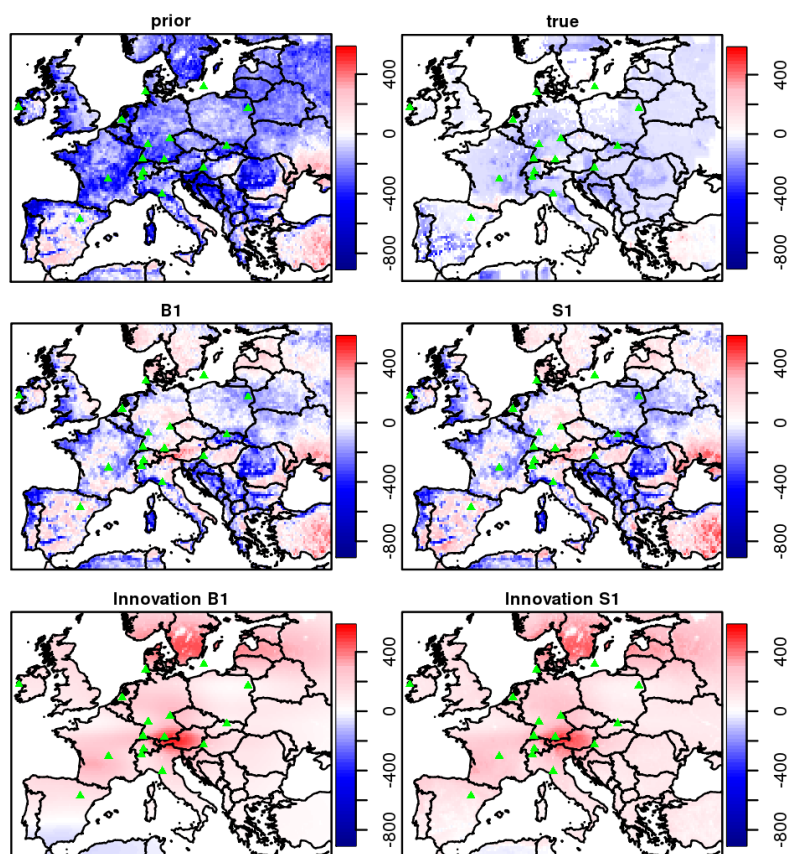
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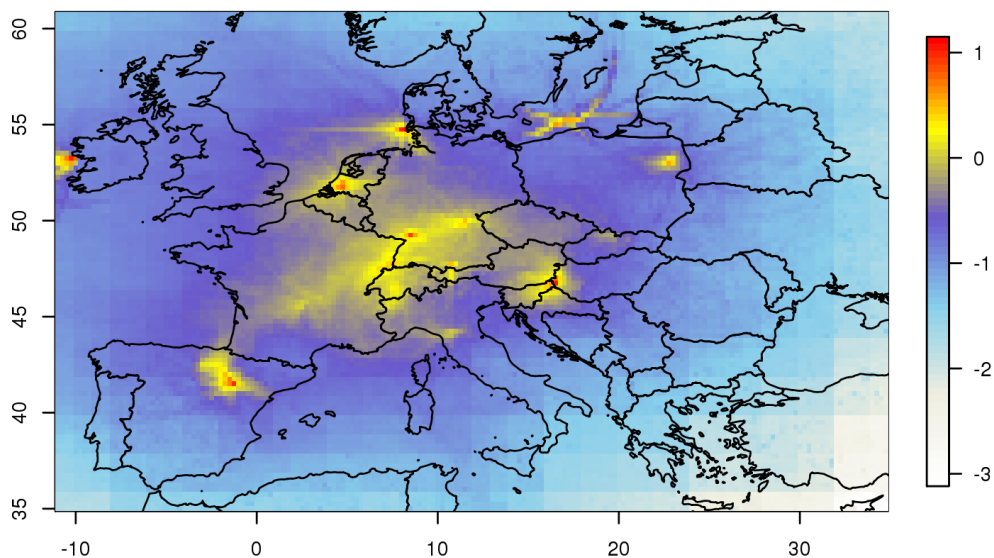
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2 Figure 4. Taylor diagram for modeled and measured time-series of CO₂ dry mole fractions. Prior
 3 (black), true (green, the perfect match of modeled and true time-series) and the different
 4 inversion cases (R0 blue; R1 red) are displayed. Different symbols denote different atmospheric
 5 stations. The normalized SD was calculated as the ration of the SD of the modeled time-series to
 6 the SD of observations.



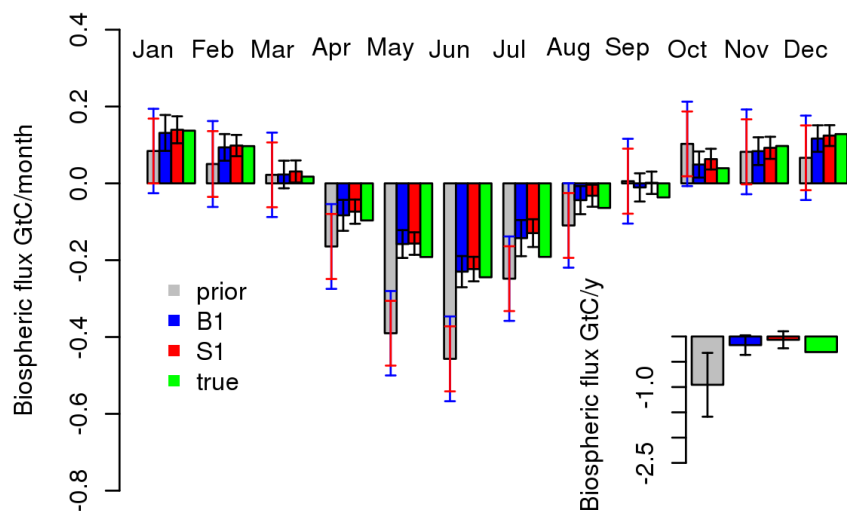
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2 Figure 5. Annual spatial distribution for the prior, true, and posterior biogenic flux estimates for
3 the two synthetic inversions S1 and B1 (top two rows), and flux innovation defined as the
4 difference posterior - prior (bottom row). Fluxes are given in units of $\text{gCy}^{-1}\text{m}^{-2}$.



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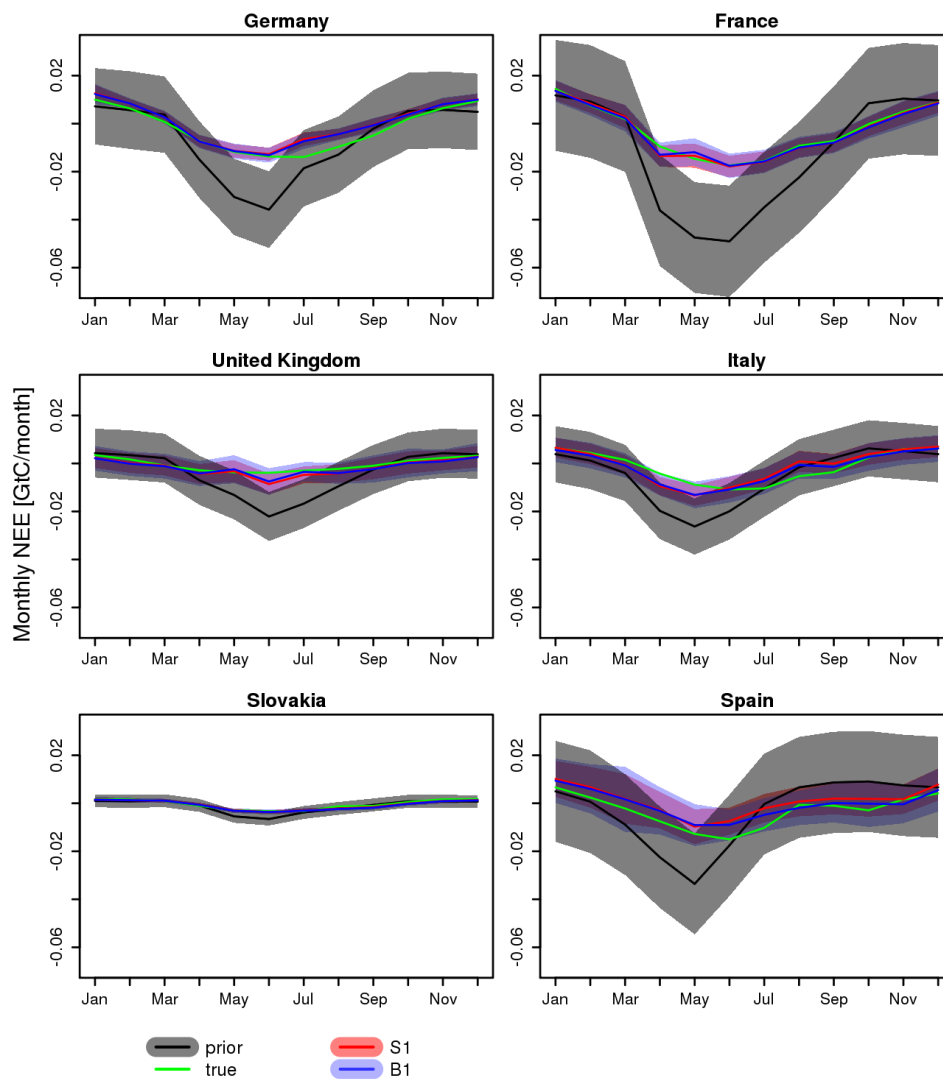
2 Figure 6. Annual integrated influence for 2007 of the current atmospheric network. Footprint
3 influence is presented in a logarithmic scale and units are in $\log_{10}[\text{ppm}/(\mu\text{mol}/\text{m}^2/\text{s})]$



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2 Figure 7. Monthly and annual carbon flux budget, integrated over the European domain. Note
3 that both inversions share the same annual prior uncertainty but monthly uncertainties differ.
4 Blue and red error bars denote the prior uncertainty for the B1 and S1 scenarios respectively.

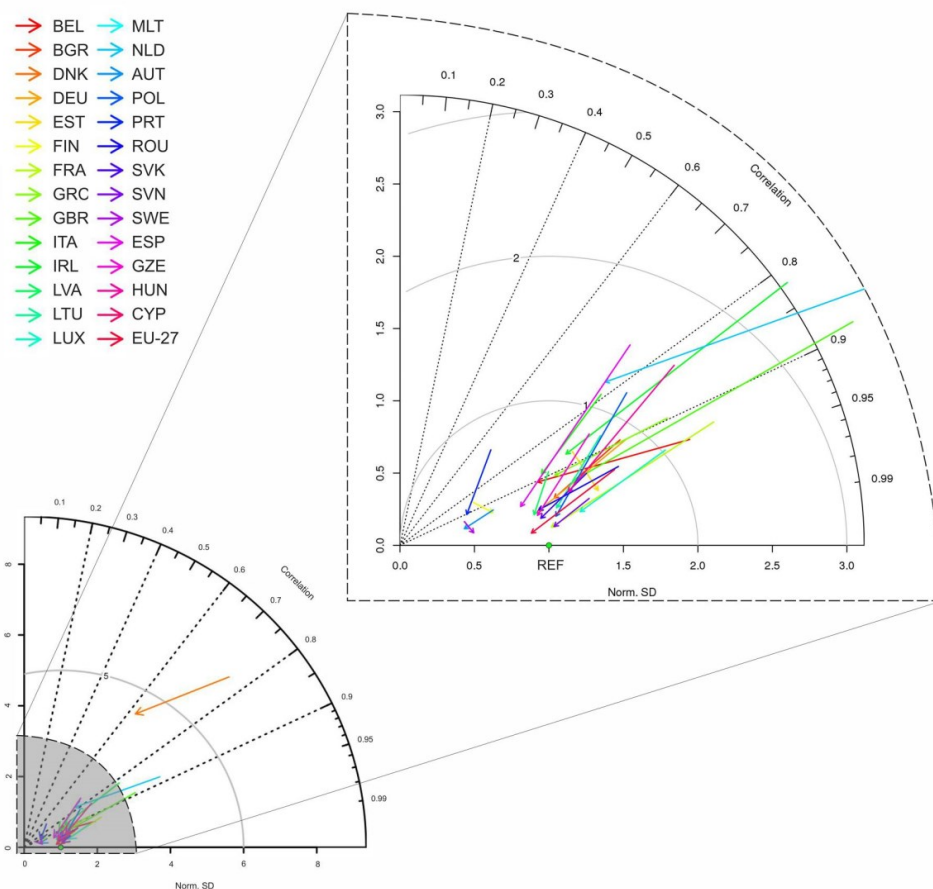
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2 Figure 8. Temporal evolution of monthly NEE for selected European countries for the synthetic
3 data inversion.

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2 Figure 9. Overview of the model performance summarized in a Taylor diagram. Posterior and prior
3 monthly and country scale aggregated biospheric fluxes are compared against the reference fluxes
4 (“true”). Each line corresponds to a different country. The starting point of each arrow shows
5 prior/reference comparison and the ending point the posterior/reference comparison. Ideally the ending
6 point should coincide with the green point which represents the reference model.

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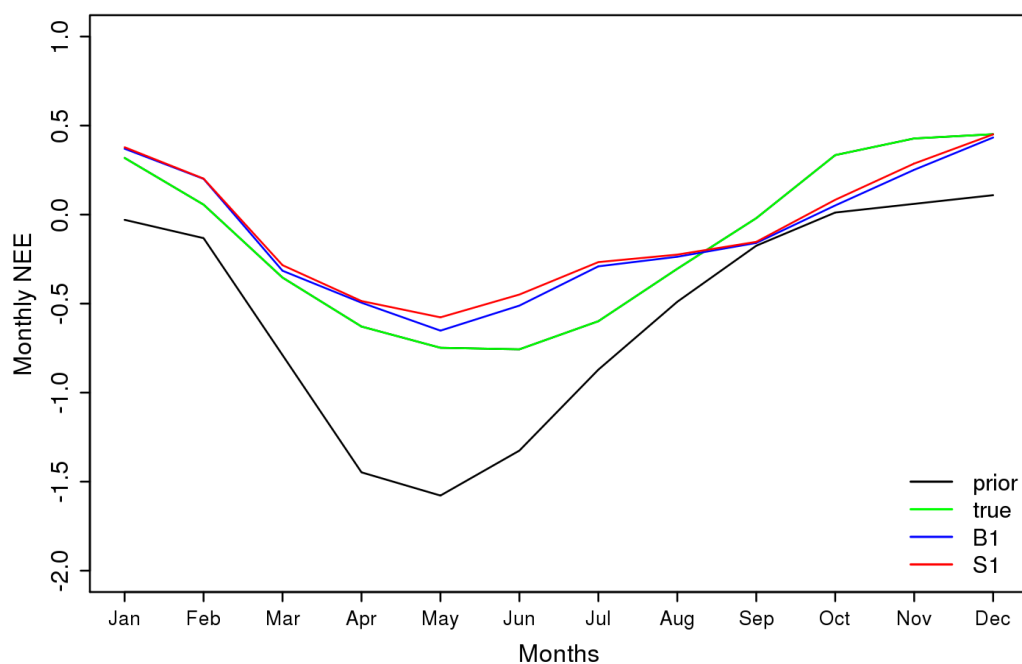
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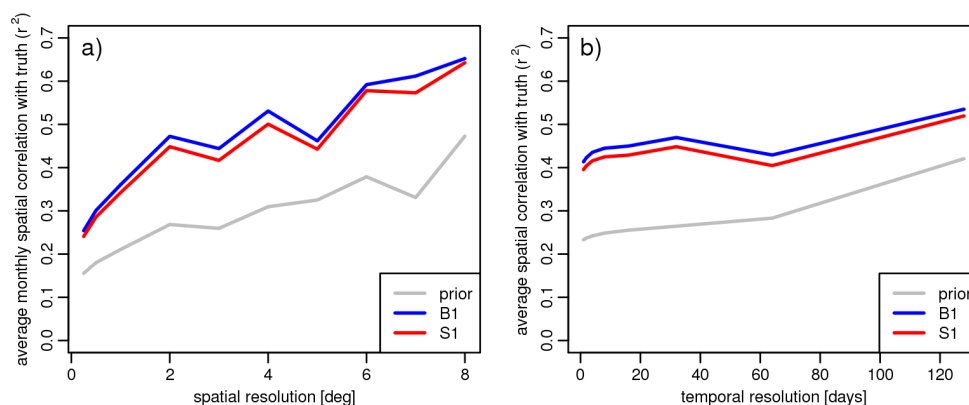


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Figure 10. Mean monthly NEE averaged over the 53 different eddy covariance site locations as reported in Kountouris et al. (2015). A priori (black), true (green), and posterior fluxes for scenarios B1 (blue) and S1 (red) are shown. Units are in $\text{gCm}^{-2}\text{day}^{-1}$.



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3 Figure 11. a): Mean spatial correlation of monthly fluxes with true fluxes as function of spatial
4 flux aggregation scale for prior fluxes (grey), and for posterior fluxes from scenarios B1 (blue)
5 and S1 (red). b): Mean spatial correlation of fluxes with true fluxes at 2 deg. spatial resolution as
6 function of temporal flux aggregation scale for prior fluxes (grey), and for posterior fluxes from
7 scenarios B1 (blue) and S1 (red).

8