

Max-Planck-Institut für Meteorologie

REPORT No. 78



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HAMBURG, JANUARY 1992

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January 1992

ABSTRACT

aspects of the Principal Oscillation Pattern (POP) analysis are used to Two study the joint normal modes of the coupled atmosphere-ocean system from a and dataset including both atmospheric (sea level pressure, 700-mb combined 200-mb zonal wind) and oceanic (sea surface temperature, Pacific sea level and the is that Pacific subsurface temperature) parameters. The first aspect modes of the be considered as normal Principal Oscillation Patterns can complexity the coupled system, a of of the analyzed system. Because straightforward method of studying these normal modes is to estimate them from the data. The second aspect of the POP analysis is that it can be considered The spectral types of the modes are spectral analysis. as a multivariate by-products of the POP analysis.

Six joint normal modes of the coupled atmosphere-ocean system are found in this study. For Mode 1, 2 and 3 whose spectra are white or nearly white, the atmosphere plays an important role. The associated oceanic anomalies seem to be generated by the anomalous atmospheric conditions. For the other modes which have most of their power on much longer time scales, the ocean is more actively involved. Modes 4 and 5 describe decadal time scale variations. Mode 4 is characterized by changes in SST in and all three tropical oceans, in organized convection over the West Pacific. The results allow us to speculate the extratropical further that these tropical features might excite changes in tropospheric and oceanic circulations. Mode 5 shows global scale SST anomalies and large anomalies in the Southern Hemispheric circulation. Mode 6 is the normal mode found in the coupled atmospheric-ocean system, it only oscillatory Niño/Southern Oscillation the El describes the quasi-cyclic behaviour of phenomenon.

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ISSN 0937-1060

1. INTRODUCTION

and subsurface available upper-air atmospheric length of At present. the offer a 30 years. These data sets records 20 to is about oceanic data the atmosphere-ocean possibility of constructing a more detailed data set for system. Two kinds of observational studies using (near) global data sets have been done so far. The first kind has been concerned with variability in one or a few of the parameters. The second kind has concentrated on one particular Oscillation (ENSO). Generally, Niño/Southern phenomenon, e.g. the El set is documented and some phenomena, data well variability within each well described. For variations are particular those with shorter time scales, on decadal time scales, although some time series are documented, the spatial distributions of such variations are less-known. There has been no study which systematically considers joint normal modes in a combined data set containing both global atmospheric and oceanic parameters.

The purpose of this paper is to detect and to understand joint modes on time decades) in the coupled months to years (probably to scales of used. combined data set is purpose atmosphere-ocean system. For that a temperature (SST), sea including ocean temperature, sea level, sea surface level pressure (SLP) and low and high level zonal winds. To identify signals Pattern (POP) the Principal Oscillation atmosphere-ocean system, within the analysis is used. The technique was introduced by Hasselmann (1988) and Storch temporal (1988). Its feasibility in capturing the spatial and al. et characteristics of one or two signals in a data set was shown by, among others, Xu and Storch (1990) and Xu (1991). In this paper, the POP analysis is described only briefly. In section 2, two aspects of the POP analysis are emphasized which are crucial for this paper, but were not explicitly used in the earlier studies. In Section 3, some ideas are described which can be used specify the physical processes involved in each signal. Data and data to processing are described in section 4. The joint modes that are found are presented and discussed in section 5. Conclusions are given in section 6.

2. IDENTIFYING THE SIGNALS: the POP analysis

a) POPS AS ESTIMATED NORMAL MODES

The following notations are used: vectors are given in **bold** and matrices in gothic. T denotes transpose, * represents the complex conjugate, and · indicates dot product.

The POP formalism assumes that an m-dimensional state vector $\mathbf{x}(t)$ is modeled by a linear equation:

$$\mathbf{x}(t+1) = \mathcal{B} \mathbf{x}(t) + \mathbf{n}(t)$$

(1)

where \mathfrak{B} is a constant matrix and $\mathbf{n}(t)$ represents the noise time series. The eigenvectors of \mathfrak{B} are called Principal Oscillation Patterns (POPs). Because, in the framework of the POP analysis, \mathfrak{B} is estimated from data (see e.g. Xu and Storch, 1991), the POPs can therefore be considered as estimated normal modes.

Generally for any dynamical model, the discrete form of linearized equations for disturbances can also be written in the form of the deterministic part of equation (1). Unlike in the POP analysis, in which the system matrix B is estimated from data and depends on the mean state derived from data over a linearized theoretical model is system matrix of a period, the certain a pre-specified mean state. determined from physical laws and depends on Therefore, there is an unambiguous correspondence between the estimated normal modes of the theoretically-determined normal а (POPs) and modes of data (1991) were able to show that the free Storch et al. physical system. atmospheric baroclinic waves can be described both by the POPs and by the most linearized quasi-geostrophic vorticity equation of a unstable normal modes with a zonally-symmetric basic state.

modes of the coupled interested in the normal are In this paper we atmosphere-ocean system. For this purpose, the straightforward approach is to estimate the system matrix and its normal modes from the data, rather than from theoretical equations.

Generally B is not symmetric so that the eigenvectors P and their eigenvalues λ are either real or appear in conjugate pairs. The state of x(t) may be described by the m POPs P:

$$\mathbf{x}(t) = \sum_{j}^{m} z_{j} \mathbf{P}_{j}$$
(2)

- Because eigenvector of a matrix is only defined to an arbitrary factor $ce^{i\theta}$ (for real eigenvector θ =0), we need to choose some standard normalization for the POPs. In this study, c is chosen so that the length of (real or imaginary part of) the eigenvector is equal to m. For a complex POP, θ needs also to be specified (see section 5.4).

According to (2), a signal in the form of $z_j P_j$ has the same unit as in x(t), i.e. if x(t) represents temperature anomalies in °C, $z_j P_j$ gives temperature anomalies in °C for the considered j-th signal. This notion is frequently used in section 5.

Because of the linear assumption made in (1), the evolution of coefficients is given by:

$$z_{j}(t+1) = \lambda_{j} z_{j}(t) + n_{j}(t)$$
 (3)

where $n_i(t)$ is related to n(t).

b) POP ANALYSIS AS MULTIVARIATE SPECTRAL ANALYSIS

Equation (3) can also be translated into the frequency domain. After some manipulations, the auto spectrum $\Gamma_{z_j}(\omega)$ of the POP coefficient time series $z_i(t)$ can be written:

$$\Gamma_{z_{j}}^{(\omega)} = \frac{\Gamma_{n_{j}}^{(\omega)}}{(e^{i\omega} - \lambda_{j}) (e^{-i\omega} - \lambda_{j}^{*})}$$
(4a)

where $\Gamma_{n_i}(\omega)$ is the auto spectrum of the noise $n_j(t)$. The auto spectrum $\Gamma_{z_i}(\omega)$ is a function of the noise auto spectrum $\Gamma_{n}(\omega)$ and the eigenvalue λ_{j} . If the POPs in equation (2) capture all signals in the data x(t), $\Gamma_n(\omega)$ should be at least smooth. In this study, the noise time series are also white Or they are white. Equation (4a) then calculated (not shown). As expected, presents different types of spectra depending on the magnitude of λ and whether λ is complex or real. In the following $|\lambda| < 1$ is assumed, which is usually true for stationary time series.

Peak Spectrum (λ is complex and $|\lambda| \rightarrow 1$)

This type of spectrum is obtained when an eigenvalue is complex, i.e. $\lambda_j = |\lambda_j| e^{i\Phi_j}$. For $|\lambda_j|=1$, a resonance peak occurs at frequency ϕ_j . For $|\lambda_j|<1$, spectrum (4a) exhibits a maximum centered at frequency ϕ_j with width determined by $|\lambda_j|$. The smaller $|\lambda_j|$ is, the broader the maximum is. The eigenvalue determines, therefore, not only the oscillation frequency but also the shape of the spectrum.

For a complex POP $\mathbf{P} = \mathbf{P}^{re}_{j} + i\mathbf{P}^{im}_{j}$, if $|\lambda_{j}|$ is near 1, the signal identified by the POP describes the oscillatory tendency¹:

with oscillation period $T_j = 2\pi/\phi_j$ and e-folding time - $\frac{1}{\ln |\lambda_j|}$.

Red Noise Spectrum (λ is real and $\lambda \rightarrow 1$) and White Noise Spectrum ($\lambda \rightarrow 0$)

In the case of a real eigenvalue, equation (4a) can be rewritten:

$$\Gamma_{z_{j}}^{z}(\omega) = \frac{\Gamma_{n_{j}}(\omega)}{(1-2\lambda_{j}\cos\omega+\lambda_{j}^{2})}$$
(4b)

which describes a red noise spectrum when $\lambda_{j} \rightarrow 1$, and a white noise spectrum when $\lambda_{j} \rightarrow 0$.

Equations (4a) and (4b) demonstrate that the POP analysis is able to quantify the spectral features of the corresponding pattern by a single number λ_i . analysis, which is used to the conventional univariate spectral Parallel to different frequency bands in a 1-dimensional time series, identify signals in considered as a 'multivariate spectral analysis', POP analysis the can be multivariate signals, across the whole available i.e. patterns, which isolates 1/(20 years)). In (in this study from 1/(2 month) to frequency interval optimal cases, the extensive second moment information in the high dimensional $\mathbf{x}(t)$ can be compressed into a manageable set of numbers (λ_i) and patterns (POPs).

¹ Equation (3) describes an anti-clockwise rotation in the 2-dimensional complex-plane. However, for a complex POP, the signal is represented by $z\mathbf{P}+z\mathbf{P}^{\mathsf{r}} = 2z^{\mathsf{re}}\mathbf{P}^{\mathsf{re}}-2z^{\mathsf{im}}\mathbf{P}^{\mathsf{im}}$, where \mathbf{P}^{re} , z^{re} (\mathbf{P}^{im} and z^{im}) are the real (imaginary) parts of the complex POP and POP coefficient. In practice, $2z^{\mathsf{re}}$ and $-2z^{\mathsf{im}}$ are used to describe the time evolution of signal \mathbf{P} and \mathbf{P}^{re} ($2z^{\mathsf{re}}$ and $-2z^{\mathsf{re}}$ are noted hereafter as the real and imaginary parts of the POP coefficient). Therefore, clockwise rotation as given in (5) is observed.

It is concluded that the POP analysis is not only useful for estimating normal modes of data, but also provides a simple diagnostic tool for expressing the spatial and spectral characteristics of these modes.

3. SPECIFYING PHYSICAL PROCESSES

Although the POP analysis provides an easy answer to the question of what the normal modes of the considered system look like, the results of a POP analysis do not suggest what physical mechanism is involved in each mode. For understanding these modes something else has to be done.

physical processes is to specify relationships specifying The basic idea for between well known processes and their corresponding anomaly distributions. The purpose of this section is to demonstrate these relationships in terms of the parameters used. Because joint modes of the coupled atmosphere-ocean study, I concentrate mainly system are considered in this on the air-sea processes. In the following discussion, SST is considered as only one possible subsurface temperature forcing for the atmosphere, and sea level and are treated as indicators of oceanic response to atmospheric forcing. The low and high level atmospheric parameters are used to describe the vertical structure of the atmospheric response to oceanic forcings.

a) EXTRATROPICAL SST AND THE OVERLYING ATMOSPHERE

In the extratropics, two kind of SST patterns associated with two different air-sea processes have been observed and documented in the literature.

First, if the atmosphere forces the ocean, it would be expected that in the presence of an anomalous anticyclone over the North Atlantic or North Pacific the SST pattern would show anomalous warming at the anticyclone's western and southern flank and cooling at its eastern and northern flank (see also Fig. 1b in Zorita et al., 1992). It is generally understood that the SST anomalies are produced by the warm marine and cold continental air advection brought about by the anomalous atmospheric circulation. This process was first proposed by Bjerknes (1962) and is supported by a GCM study for the North Pacific (Luksch and Storch, 1992). Because the warm marine and cold continental air advection is strongest during the winter time, the above mentioned air-sea process is strongest during the winter time.

In the second case, if the ocean forces the atmosphere, it would be expected that downstream of the positive SST anomalies the low level atmosphere would become warmer and wetter, and negative SLP anomalies would be observed east of the SST. anomalies (see also Fig. 1a in Zorita et al., 1992). This process, in which anomalous heating is balanced by horizontal advection of temperature, was proposed by Egger (1977) and Webster (1981).

b) TROPICAL SST AND THE OVERLYING ATMOSPHERE

In the tropics, anomalous heating is generally associated with an air-sea interaction process with positive feedback. The atmospheric response to a local heating involves large scale convection over the heating area as already indicated by a simple model (Gill, 1980). The atmospheric anomalies in turn favour the SST anomalies, so that more SST anomalies can be produced.

It is noted that, in the above mentioned pattern of tropical air-sea interaction processes, only local heating anomalies are considered. It is not clear for instance, how the atmosphere would react if the whole tropics were warmer.

c) SEA LEVEL AND THE OVERLYING ATMOSPHERE

If slow processes (changes in the shape of the ocean, or land uplift or sinking) are neglected, sea level variation μ' can be produced by three processes (Gill and Niiler, 1973):

$$\mu' = \mu'_{a} + \mu'_{a} + \mu'_{m} \tag{6}$$

The first term on the right hand side μ'_a is a direct local sea level response to the atmospheric pressure anomalies, known as the inverse barometric effect. An increase of atmospheric pressure P_a of 1 mbar produces a 1 cm depression of the sea level.

The second term μ'_s describes sea level changes caused by changes in the density of the column which imply an expansion or contraction of the column. Because of the strong relation between μ'_s and heat and fresh water fluxes which are not available for this study, the second term in equation (6) is not considered in this study.

The μ'_m term describes the sea level changes associated with motions in the

upper layers of the ocean. In this study, only wind driving motions are considered. In the oceanic interior, upper layer motions are generally induced by wind forcing via the Sverdrup relation, which fails in the western boundary the and equatorial regions. In this paper it is assumed that changes in western boundary current can be implicitly derived from interior flow changes, associated with is (northward) interior flow i.e. anomalous southward an anomalous northward (southward) return flow on the western boundary. On the Equator, other effects such as Ekman flux (pumping) or equatorial waves become dominant for sea level changes.

Except on the Equator, the sea level anomalies μ'_m are related to current anomalies via the geostrophic relation.

The barometric μ'_{a} is mainly forced *locally* by the atmospheric pressure. On the other hand, the response of sea level to motions is *not local* and, in the presence of large scale wind stress curl anomalies, it can be even basin wide.

d) OCEANIC RESPONSE IN THE UPPER 200 METERS

Different vertical structure of oceanic anomalies can be produced by changes in the structure of the mixed layer and the thermocline, and by reaction of barotropic and baroclinic modes. Although subsurface the ocean in term of are not sufficient for determining are used in this study, they temperatures Therefore, no further attempt is made to clarify processes. these physical causes of vertical structure of oceanic anomalies.

The summarized air-sea processes and their anomaly distributions are used in section 5 as a guide for understanding the joint modes of the atmosphere-ocean system.

4. DATA

The data used in this paper are monthly anomalies of:

i) The four degree latitude by ten degree longitude SST from the Comprehensive Ocean-Atmospheric Data Set (COADS, Woodruff et al., 1987) prepared by P. Wright (Wright et al., 1988).

ii) The five degree latitude by ten degree longitude temperature in the Pacific Ocean at 10, 50, 125, and 200 meter depth archived at Far Seas

Fisheries Research Laboratory in Japan and at the Scripps Institution of Oceanography in the U.S.A. This data are derived from $1^{0}x1^{0}$ XBT measurements taken at 12 levels and between the surface and about 250 meters. The original bi-monthly data are interpreted into monthly data via a simple time average procedure. In this paper, i) and ii) are used to form a data set for ocean temperature.

iii) Sea level station data in the Pacific collected by Wyrtki et al. (1988).

the Northern Hemisphere SLP iv) A combined data set of SLP including (20°N-50°N) stored at the National Center for Atmospheric Research (Boulder, generated the Bureau of Southern Hemisphere SLP $(10^{\circ}\text{S}-40^{\circ}\text{S})$ at USA), tropical (Melbourne, Australia) and the Research Center Meteorology (20°N-20°S) COADS SLP (Wright et al., 1988).

v) Zonal winds at 200 mb and 700 mb from the National Meteorological Center analysis (Wasington DC, USA), which are longitudinally smoothed resulting in a ten degree zonal resolution. The north-south resolution is unchanged with a meridional resolution of about 3.5° at 40° , and 5° in the equatorial region.

The spatial dimension of each data set considered in this paper is of the order of 10^2 to 10^3 . The order of the system matrix B in equation (1) for the 10^{3} then be 10^3 . To simplify the interpretation of combined data set would each data set is POPs and to concentrate on the large scale variations, compressed into the smaller space spanned by the first few EOFs. No effort is made to check the significance of the EOFs. Because the error in estimating the lower order EOFs is much larger than that of the higher order EOFs, only EOFs that explain more than 1% of the total variance are used in this study. The data information and results of the data compression are shown in Table 1.

The dimension of the combined system x(t) is then 95. In this paper the variances of the oceanic and atmospheric data are adjusted so that they are data are available in the Pacific because more It is noted that, equal. emphasized. The 95-dimensional that region might be variability region. in combined system is further compressed into the space spanned by the first 9 EOFs of this system. These EOFs, which are the input vector time series $\mathbf{x}(t)$ for the POP analysis, explain 56% of the variance of the combined data set and within the results obtained of the original data set. The about 45% 9-dimensional space are then translated back into the physical space.

TABLE 1:Informations of dimensions of the datasets, numbers of EOFs used for the combined dataset and variance explained by these EOFs for each data set.

data sets used	dimensions of the original data sets	no. of EOF used for the combined data set	variance explained by these EOFs
i & ii	1061	25	71%
iii	79	21	92%
iv	1331	23	81%
v	1656	26	76%
sum	4127	95	80% (averaged)

TABLE 2: Eigenvalue of each POP and standard deviation δ of each POP coefficient time series. For the complex Mode 6, standard deviations of the real and imaginary part of the coefficient are shown. The standard deviations δ are used in section 5 to estimate the averaged strength of each mode.

	λ	standard deviation δ_j
Mode 1 Mode 2 Mode 3 Mode 4 Mode 5 Mode 6	$\begin{array}{c} 0.15 \\ 0.40 \\ 0.66 \\ 0.86 \\ 0.92 \\ 0.93 \\ e^{i2\pi/51} \end{array}$	0.05 0.09 0.05 0.07 0.06 0.11 / 0.10

The EOF compression from a dimension of 4127 for the original data sets to 95 for the combined data set and to 9 for a subspace of the combined data set a two-step spatial filter: in the first step from а be interpreted as can dimension of 4127 to 95, small scale variations within each data set are compressed, and in the second step from a dimension of 95 to 9, small scale variations within the combined data set are compressed. Therefore, the POPs filtered data are likely large-scale joint modes of identified from spatially the coupled air-sea system.

Because data sets i) and v) begin in 1967 and 1968, and iii) in 1975, and most of the data sets end in 1986, the time period of the combined data set is chosen to be 1967 to 1986. In order to study the variability of the combined data set across the whole available frequency interval, *no time filter* is performed.

interpolation, the missing data are Rather than filling missing data by Thus each matrix element is estimated ignored in the EOF and POP calculation. EOF аге estimated The principal components $\alpha_{i}(t)$ for **e**, individually. according to a least squares fit by

$$\alpha_{i}(t) = \frac{\mathbf{e}_{i}^{\mathrm{T}} \cdot \mathbf{x}(t)}{\mathbf{e}_{i}^{\mathrm{T}} \cdot \mathbf{e}_{i}}$$
(7)

5. RESULTS

In the 9-dimensional subspace, two complex POPs together with their complex conjugates and 5 real POPs are found. One of the complex POPs has eigenvalue $\lambda=0.5$ e^{i2\pi/103}, but the coefficient time series has most of its power at a frequency much higher than 1/(103 months). Thus equation (5) is not a valid interpretation. We consider this POP to be "meaningless", and it is not considered in the following discussion. The eigenvalues of the other 6 POPs are listed in Table 2.

The eigenvalues indicate two white spectra with $|\lambda_{12}|=0.15, 0.4,$ and one spectrum with $\lambda_3=0.66$ which is not purely white or red, two red spectra with $|\lambda_{45}| = 0.86$, 0.92, and one peak spectrum with spectrum maximum around 51 months and an e-folding time of about 12 months. Fig.1 and Fig.2 show the POP and the spectra derived from the time series. As coefficient time series expected, both Fig.1 and Fig.2 confirm the spectrum types suggested by the eigenvalues. The oscillation period for the complex POP is about 40 months in Fig. 2f and is, therefore, overestimated by the complex eigenvalue.

To test the stability of the results, the POP analysis is also performed using different numbers of EOFs. It turns out that in all these cases only 6 POPs are interpretable, the others appear as "meaningless" POPs. In the following I will concentrate on the 6 signals P_j (j=1,...6) identified by the five real POP and one complex POP listed in Table 2.

In this section, two diagrams are usually shown for each POP, one for the atmospheric part of a POP (SLP, 700-mb and 200-mb zonal wind) and the second for the oceanic part of a POP (SST, Pacific subsurface temperature and sea level). For some of the signals, one or two parameters are not shown. In this case the variability in the missing variable is negligible or irrelevant for the considered mode, and therefore not presented.



Figure 1: POP coefficient time series of Mode 1 to Mode 6 as listed in Table 2.





5.1 JOINT NORMAL MODES: Mode 1, Mode 2 and Mode 3

As will be shown shortly, the three modes with smaller eigenvalues (Table 2 and Fig. 2a, 2b, 2c) have many features in common. For this reason they are considered together in this section.

a) CENTERS OF ACTION

The centers of action of each mode can be identified by the regions of large explained variance which are shaded in Fig.3, Fig.5 and Fig.7. All three modes are confined to the Northern Hemisphere: Mode 1 in the North Atlantic (Fig.3), Mode 2 in the North Pacific (Fig.5), and Mode 3 in the region from the central North Pacific to the North Atlantic (Fig. 7).

Although the wind field and the SLP field extend only to about 50°N, Fig.3, 5, and 7 bear strong resemblance respectively to the "Pacific/North America" (PNA), "East Atlantic" (EA) and "West Atlantic" (WA) teleconnection patterns noted by Wallace and Gutzler (1981). Similar to EA and WA, Mode 1 and Mode 3 describe north-south seesaws over the North Atlantic with the seesaw center in the Mode 1 being shifted southeastward relative to that in Mode 3.

For each mode, the POP patterns for 700-mb and 200-mb zonal wind are nearly identical (not shown). It indicates that these modes are barotropic.

b) SEASONAL DEPENDENCE

dependence. Fig.9 gives seasonal a All three of these modes show strong standard of the 3 POP coefficients larger than one frequency distribution positive and tums that strong each calendar month. It out deviation in negative amplitudes of these modes occur mostly during the winter season.

c) THE ROLE OF ANOMALOUS WARM AND COLD AIR ADVECTION

For Mode 2, positive SLP (Fig.5) and easterly anomalies (not shown) are found in the North Pacific, equivalent to an anomalous anticyclone over that region. The SST anomalies shown in Fig.6a are positive over the North Pacific near 40°N, i.e. at the western and southern flanks of the anticyclone which is indicated by the arrow, and negative in the east North Pacific and along the North American coast, i.e. at the anticyclone's eastern and northern flank. Considering the seasonal dependence of this mode, the spatial distributions of SST anomalies fit perfectly to the process associated with warm and cold air advection, rather than the process proposed by Egger and Webster.

For Mode 1 and 3, the role of anomalous warm and cold air advection, as indicated by the arrows in Fig. 4 and 8, can also be identified.

The results suggest that the anomalous heat fluxes associated with the anomalous warm and cold air advection control the large scale SST changes for all three modes. The maxima of variance explained by these modes are about 20% for the atmospheric parameters and about 5-10% for the oceanic parameters.

d) INVERSE BAROMETRIC EFFECT

In Mode 2, large sea level anomalies (Fig.6b) are found directly below the anomalous anticyclone in Fig.5. The maximal pressure anomaly given by z_2P_2 is about 9 mb (with z_2 = one standard deviation δ_2 =0.09, and P_2 =100mb), which is roughly balanced by the largest sea level anomaly of about -11cm (with $z_2 = \delta_2 = 0.09$, $P_2 = -1219$ mm). The inverse barometric effect seems to be the dominant effect for sea level anomalies shown in Fig.6b. For the Modes 1 and 3, no sea level data are available over the Atlantic.

e) ORIGIN OF THE SIGNALS

In a theoretical normal modes study, Simmons et al. (1983) suggested that the origin of the teleconnection patterns lies in the atmosphere. Consistent with their suggestion, our study shows further the way how the atmospheric and oceanic anomalies of these modes are related to each other. According to such relationship, we conclude that this is the internal dynamics of the atmosphere which generates the patterns shown in Fig.3, 5 and 7, and the ocean acts only passively.

on month to month time scales teleconnection patterns vary Because the atmospheric (Simmons et al., 1983) and the oceanic reaction time to the pressure anomalies and the anomalous warm and cold advection is short (shorter than one month), we suggest that for mode 3 which does not have a purely white noise spectrum, there must be some other processes which generate the low frequent part of the mode.



Figure 3: POP pattern of Mode 1 for the sea level pressure (in mb). Shaded area indicates explained variance larger than 20%.



Figure 4: POP pattern of Mode 1 for sea surface temperature (in $^{\circ}$ C). Shaded areas indicate explained variance larger than 3%.



Figure 5: POP pattern of Mode 2 for the sea level pressure (in mb). Shaded area indicates explained variance larger than 20%.



Figure 6: POP pattern of Mode 2 for a) sea surface temperature (in °C), and b) sea level (in mm). Shaded areas indicate explained variance larger than 5% for SST and 10% for sea level.



Figure 9: Frequency distribution of POP coefficients larger than one standard deviation for each calendar month.

5.2 THE JOINT NORMAL MODE ON DECADAL TIME SCALES: Mode 4

a) **TROPICAL FEATURES**

The most striking features of this mode are the large positive SST anomalies SST values in the western in all tropical oceans (Fig. 10a) with maximum Pacific on the Equator and in the subtropical Pacific and weak anomalies along the Equator in the eastern Pacific. The coefficient time series of this mode increase of the scale. The (Fig.2d) indicates variation on decadal time a amplitude of the POP coefficient time series since 1975 together with the positive sign of SST anomalies describes a pronounced increase of SST in the global tropical ocean up to several tenth C°.

of SSTs in excess in view of the evidence that atmosphere, the In support organized convection and the approximately 28°C are required to fact amplitude, the mode have rather small SST anomalies of this that the convection induced by this mode is expected to be found only over the Indonesian region and the East Pacific where, in the climatological mean, SSTs of about 28-29°C exist. Indeed, the most pronounced atmospheric feature in the (divergent) flow over the convergent anomalous the tropics (Fig.11) is Indonesian region and the West Pacific at 700-mb (200-mb) as indicated by the easterly Ocean and the the Indian anomalies over westerly (easterly) (Fig.11b). These patterns Pacific in Fig.11a the (westerly) anomalies over small suggestion that the tropical atmosphere does respond to lead to the amplitude variations of the tropical SST forcing (up to a few °C) and tenth the West displays organized convection centered over the Indonesian region and motion has increased this convective further that Pacific. Fig.2d indicates since the mid-seventies.

Fig.10b shows out-of-phase Pacific, tropical upper layer of the For the anomalies with positive values in the first 50 meters and negative values in West Pacific. This vertical structure is different lavers below in the the form that observed during ENSO (Fig.17b).

b) EXTRATROPICAL FEATURES

westerlies atmospheric the anomalous anomalies are largest extratropical The over the northern anomalous easterlies the central North Pacific and over that the is noted 200-mb (Fig.11). It North Pacific at both 700-mb and the North Pacific zonal wind is not located in the explained variance for



b) SUBSURFACE TEMPERATURE 10 m 20'N 111 0' 20°S -120 W 90°W 180 150°W 150°E 120°E 50 m 20 N 🗆 o 205-90'W 120 W 180 150°E 150°W 120'E 125 m 20'N -o 20°S -150°W 120 W 150°E 180 90'W 120°E 200 m 20'N o 20°S 150°W 90'W 180 120°W 150°E 120 E

Figure 10: POP pattern of Mode 4 for a) SST (in $^{\circ}$ C), b) the Pacific sub-surface temperature ($^{\circ}$ C), and c) Pacific sea level (in mm). Shaded areas indicate explained variance larger than 5% for temperature and 10% for sea level.



Figure 11: POP pattern of Mode 4 for a) 700-mb zonal wind (in m/s) and b) 200-mb zonal wind (in m/s). Shaded areas indicate explained variance larger than 5%.





coefficient time POP series Figure 12: a) global tropical SST averaged of Mode 4. b) 20°S, from 20°N to c) the over the area SST which is the difference Pacific North averaged SST in the northern between area North Pacific (60°N and the central -44°N) North Pacific (32°N 40°N), d) level sea anomalies averaged along coast of the east North Japan, level anomalies e) sea of South averaged along the east coast tropical convergent flow Japan, f) the indicated by the difference between zonal wind anomalies over the Indian Ocean and wind these over the Pacific. g) zonal central Nonh Pacific the anomalies over (20°N - 37°N). Units for temperature is °C, for sea level mm and for zonal wind m/s.

regions of anomaly maximum.

negative values zonally anomalies with large large SST the ocean, In orientated along 40°N and large sea level anomalies in the coastal regions are affected by the distribution is Certainly the sea level (Fig. 10a,c). found interesting oceanic interior. Nevertheless, there are in the scarcity of data patterns along the coast of Japan with negative anomalies in South and the positive anomalies in the North.

Is it possible that these atmospheric and oceanic changes are related to each other? The wind stress (τ) curl calculated from Fig.11a shows a zero line of curlt along 30°N which is located several degrees south of its climatological Sverdrup relation, anomalous the According to (not shown). position by zonal wind patterns such as that shown in Fig.11a circulation induced have anomalous southward (northward) Sverdrup transport south (north) should of 30°N, which in turn might generate northward (southward) return flow along boundary. The negative (positive) sea level anomalies along the the western consistent with such southern (northern) Japan (Fig. 10c) are East coast of Currents. Furthermore, the southward and Oyashio Kuroshio changes in the of the zero line of $curl \tau$ indicates a southward displacement of displacement The meridional with this current system. mass associated water the displacement of the water mass might be related to the zonally-orientated SST anomalies along 40°N. The time evolution (Fig.2d) suggests that the Kuroshio and the Oyashio Currents have become stronger since the mid-seventies. This decadal trend in the Kuroshio transport has also been noted by Qui and Joyce (1991).

The above discussion suggests that the extratropical oceanic anomalies which might be described by changes in the strength and the north- southward displacement of the subtropical and subpolar gyres in the North Pacific might be induced by wind changes over that area. However, to prove this idea, more data, especially more compact wind and sea level data, are needed.

In order to ensure that Mode 4 is not an artifact of the analysis technique, area averaged time series which characterize the features described above are calculated. By doing so, other signals in the form of $z_j \mathbf{P}_j$ (j=1,2,3,5,6) are subtracted from the original unfiltered anomaly fields.

Fig.12 shows (a) once again the POP coefficient time series, (b) global tropical SST averaged over the area from $20^{\circ}N$ to $20^{\circ}S$, (c) the North Pacific

SST which is the difference between area averaged SST in the northern North Pacific $(60^{\circ}N-44^{\circ}N)$ and in the central North Pacific $(32^{\circ}N-40^{\circ}N)$, (d) sea level averaged along the East coast of northern Japan, (e) sea level averaged along the East coast of southern Japan, (f) the convective flow indicated by the difference between zonal wind anomalies over the Indian Ocean and these over the Pacific, and (g) zonal wind anomalies over the central North Pacific $(20^{\circ}N-37^{\circ}N)$.

It is obvious from Fig.12 that the tropical and extratropical features described above indeed develop parallel to each other. The strength of the signal is of order of tenth °C for temperature, a few cm for sea level and a few m/s for zonal winds, as given by $z_A P_A$.

The relationship between the convective changes in the tropics and changes in the extratropical tropospheric circulation has been proposed by Flohn et al. (1990). However, the results shown in this section suggest a more detailed and complex picture of such relationship.

5.3 THE JOINT NORMAL MODE ON DECADAL TIME SCALES: Mode 5

The time series of Mode 5 shown in Fig.2e reveals a rather sharp jump during 1975/76. The pattern shown in Fig. 13a indicates that Mode 5 is connected with large-scale SST changes, namely negative anomalies in most parts of the Atlantic and the Indian Ocean, and out-of-phase structure in the Pacific which has negative values in the tropics and positive values in the subtropics. In contrast to Mode 4, where large explained variance is confined to the Pacific, Mode 5 shows large explained variance in SST in all three oceans (shaded areas in Fig. 13a).

The vertical structure of oceanic anomalies, indicated by the subsurface temperature in Fig.13b, resembles that of Mode 4. No signal (in terms of explained variance) is found in sea level.

For the atmospheric parameter, maxima of anomalies and explained variance are found mostly in the Southern Hemisphere at both 700 and 200 mb (Fig. 14a,b). In the tropics, a large-scale organized convection pattern is not observed. In the Southern Hemisphere, easterly anomalies are found over the southern oceans except for a small area in the western South Pacific near 40°S. The mean Southern Hemispheric winter circulation as described by van Loon (1972) is characterized by a strong westerly jet along 45° - 50° S with maximum values over



Figure 13: POP pattern of Mode 5 for a) sea surface temperature (in °C) and b) Pacific subsurface temperature. Shaded areas indicate explained variance larger than 10%.



Figure 14: POP pattern of Mode 5 for a) 700-mb zonal wind (in m/s) and b) a 200-mb zonal wind (in m/s). Shaded areas indicate explained variance larger than 10%.

the South Indian Ocean and South Atlantic, and a double jet structure in the western South Pacific with minimum values along 40° S. Fig.2e indicates that this mean circulation pattern changed very rapidly during 1975/76, with an anomalous weak jet over the southern Indian Ocean and the South Atlantic and an anomalous weak double jet structure over the western part of the South Pacific during the first half of the time period, and an anomalous strong jet and strong double jet structure during the second half of the period.

No air-sea process of the type summarized in section 3 can be identified for Mode 5. It is not clear at this stage, how and why the global-scale SST anomalies (Fig.13a) and the changes in the Southern Hemisphere circulation (Fig.14a, b) are related to each other.

5.4 THE JOINT OSCILLATORY NORMAL MODE: Mode 6

As mentioned in section 2, a complex POP is only defined to an arbitrary complex factor $e^{i\theta}$. I will show later that the complex Mode 6 describes the Southern Oscillation phenomenon. To simplify the interpretation, θ is chosen so that the imaginary part of the POP coefficient time series is maximally correlated (0.72) with the conventional Southern Oscillation Index (pressure

difference between Tahiti and Darwin). Therefore, the imaginary part of the POP, noted as P^{im} , describes the anomalies associated with the cold extreme of the ENSO phenomenon, and the real part, noted as P^{re} , corresponds to the intervening phase, i.e., conditions which appear about one year before a warm extreme.

a) ATMOSPHERIC AND OCEANIC FEATURES OF THE MODE 6

For SLP, the evolution from a cold extreme to a warm extreme is described by an eastward migration of the negative anomalies from the Indian Ocean and the West Pacific during a cold extreme (\mathbf{P}^{im} in Fig.15a), into the West and Central Pacific during the intervening phase (\mathbf{P}^{re} in Fig.16a), and finally into the Central and East Pacific during the warm extreme (-P^{im}). Associated with this wind anomalies is an eastward migration of low level westerly evolution Ocean in Indian westerlies the anomalous propagating from with observed Fig.15b into the West Pacific in Fig.16b and into the Central Pacific. At 200-mb the conditions during the extreme phase (Fig.15c) are well known with westerlies over the Central Pacific on the Equator and the strong anomalous the Pacific, whereas during subtropical easterlies the anomalous in found of the over most westerlies are (Fig.16c) strong intervening phase tropical oceans. It seems that the migration feature is more pronounced at the lower than at higher level.

The maximum of variance explained by this cyclic evolution is shown by the shaded areas in Fig.15 and Fig.16. For SLP, the signal in the Southern Hemisphere is stronger than that in the Northern Hemisphere. For the wind, the signal is strong in the West and Central Pacific at 700-mb, and over the Central Pacific and the subtropical South and North Pacific at 200-mb. The explained variance for both the low and high level parameters shows maximal values up to about 35% along the Equator and decreases rapidly poleward, especially for SLP and the 700-mb zonal winds.

In the ocean, there is little evidence of migration in the SST (Fig.17a, 18a). But in terms of the ocean temperature and sea level (Fig.17b,c and Fig. 18b,c), propagation of anomalies is clearly presented. The sea level anomalies (P^{im} with large positive during a cold event in Fig. 17c) are associated extension north of the over the West Pacific, which has a larger values On the Equator there is a minimum of Equator than south of the Equator. positive anomalies in the west part of the Pacific and a tongue of negative East Pacific. In the intervening stage (\mathbf{P}^{re}) in anomalies in the Central and





Figure 15: POP pattern of the imaginary part of Mode 6 for a) sea level pressure (in mb), b) 700-mb zonal wind (in m/s) and c) 200-mb zonal wind (in m/s). Shaded areas indicate explained variance larger than 15%.





Figure 16: POP pattern of the real part of Mode 6 for a) sea level pressure (in mb), b) 700-mb zonal wind (in m/s) and c) 200-mb zonal wind (in m/s). Shaded areas indicate explained variance larger than 15%.

Fig.18c), the positive sea level anomalies have now moved into the West and Central Pacific. The same evolution with even more detailed distribution is shown for the Pacific Ocean temperature in Fig.17b and Fig.18b. The largest temperature anomalies are reached during a cold extreme in the West Pacific at about 5°S at 200 meters deep, and at about 5°N-10°N at 125 meters deep. They then migrate equatorward and are located on the Equator in the west Central Pacific during the intervening stage.

Explained variances larger than 30% for sea level and larger than 30% for temperature are shown by shaded areas in Fig.17 and 18. As in the case of atmospheric parameters, maximal values are located in the equatorial regions.

b) AIR-SEA INTERACTIONS INVOLVED IN MODE 6

of the oscillatory normal mode appears as an The fact that ENSO atmosphere-ocean system is consistent with previous studies. The well defined mode in the Tropical Pacific, suggested as being a delayed oscillation mode (Suares and Schopf, 1988), and also found in an ocean GCM (Latif and Flügel, displays similar sea level evolution to that given by the oscillatory 1991) Mode 6: The positive sea level anomalies located off the Equator in the West equatorial anomalies in the tongue of negative sea level Pacific and the central and eastern Pacific in P^{im} (Fig.17c) resemble the sea level anomalies westward propagating Rossby waves and eastward propagating associated with Kelvin waves; and the positive anomalies in \mathbf{P}^{re} (Fig.18c) seem to have been reflected at the western boundary and appear as a Kelvin wave signal centered along the Equator. Also the atmospheric part of the evolution is consistent 1988). The new suggestion of this with that shown first by Barnett (1985, paper is that the oceanic mode is probably tied to the propagating features of the atmospheric anomalies.

oceanic propagating features the atmospheric and relation between the The appears as the following. The sea level anomalies in both the extreme phase and the intervening phase are likely to be produced by anomalous atmospheric pattern in Fig. 17c by easterly anomalies over the sea level conditions: the and the sea level pattern in Fig. 18c by westerly tropical Pacific (Fig.15b), It is speculated that the cyclic Pacific (Fig. 16b). the West anomalies over evolution of oceanic anomalies can be interpreted as the oceanic response to the eastward movement of the low level zonal wind anomalies.

Now what is the reason for the cyclic evolution of the wind anomalies? As



Figure 17: POP pattern of the imaginary part of Mode 6 for a) SST (in °C), b) the Pacific sub-surface temperature (in °C), and c) Pacific sea level (in mm). Shaded areas indicate explained variance larger than 30%.



Continue of Figure 17



Figure 18: POP pattern of the real part of Mode 6 for a) SST (in °C), b) the Pacific sub-surface temperature (in °C), and c) Pacific sea level (in mm). Shaded areas indicate explained variance larger than 30%.



Continue of Figure 18

discussed in section 3, SST is the only forcing for the overlying atmosphere in this context. During the extreme phase, a comparison between SST in Fig.17a and wind patterns in Fig.15 indicates that atmospheric anomalies appear as response to the heating anomalies with anomalous convection (an expression of low level convergence and upper level divergence) sitting over the warm water in the West during the cold phase and in the East during the warm phase. But during the intervening phase, no notable SST anomalies can be related to the anomalous westerlies over the West Pacific. This indicates that the movement of the wind anomalies is not forced by the SST.

6. CONCLUSIONS

a) ESTIMATED NORMAL MODES

A possibility of estimating normal modes of a complex system from data is presented in this paper. Although the analogy between the estimated normal modes (POPs) and the theoretical normal modes has been demonstrated by Storch et al. (1991) in an example of atmospheric baroclinic waves, our results show further evidences of this analogy for normal modes on longer time scales and complexity of the coupled Because of the complex system. more in a analysis seems to be the only techniques, at atmosphere-ocean system, the POP this stage, for studying the normal modes of this system.

the physical that modes from data is A disadvantage in estimating normal analysis by the involved in these modes cannot be determined processes procedure. The processes in the normal modes found are suggested objectively by using information summarized in section 3. More date and other theoretical studies are needed to prove the results.

b) MULTIVARIATE SPECTRAL ANALYSIS

The agreement between the spectrum given by an eigenvalue or derived from the corresponding POP coefficient time series demonstrates clearly the ability of the POP analysis to pick out the spatially coherent modes together with their spectral features summarized by the eigenvalues.

c) AIR-SEA PROCESSES ON DIFFERENT TIME SCALES

As mentioned in section 4, the modes found in this study are probably the *joint* normal modes of the coupled atmosphere-ocean system. The results

indicate that different air-sea processes are involved in these modes. Whereas the atmosphere is responsible for the modes which vary on month to month time scales, the role of the ocean becomes more important for the modes which vary on much longer time scales.

On month-to-month time scales, the large-scale oceanic anomalies could be understood as being forced by large-scale extratropical atmospheric anomalies. The SST anomalies were mainly caused by anomalous warm and cold air advection and the sea level anomalies appeared to be produced by the inverse barometric effect.

On decadal time scales, one air-sea process described in section 5.2 seemed to have its origin in the tropics. This mode shows large-scale SST anomalies in organized convection over the tropical West three tropical oceans and all speculate that of the patterns us to Pacific. A further investigation allows extratropical tropospheric the tropical variation could induce changes in this and subpolar subtropical changes in the circulation and these might cause gyres in the North Pacific.

oceanic anomalies seemed to the be tied to On ENSO time scales, cyclic results anomalies. However, the atmospheric eastward propagation of the during the is present only indicate that oceanic forcing in terms of SST extreme phase of ENSO, but not during the intervening phase.

ACKNOWLEDGEMENTS

I would like to express my gratitude to Klaus Hasselmann for his inspiration to this topic. I also like to thank Dennis Moore and Klaus Wyrtki for their suggestions about oceanic anomalies. Many thanks to Grant Branstator, Hans von Storch, Mojib Latif, Ute Luksch, Nanne Weber, Ernst Maier-Reimer, Jörg-Olaf Wolff, Eduardo Zorita and Gerd Bürger for many fruitful discussions. Thanks also to M. Grunert and D. Lewandowsky for preparing the diagrams, to P.B. Wright for editing the English, and to Jutta Bernlöhr and Heike Schriever for typing the manuscript.

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