

Supplementary Material

Performance of various density-functional approximations for cohesive properties of 64 bulk solids

Guo-Xu Zhang

*Fritz-Haber-Institut der Max-Planck-Gesellschaft, Faradayweg 4-6, 14195, Berlin, Germany and
School of Chemistry and Chemical Engineering, Harbin Institute of Technology, West Dazhi 92, 150001, Harbin, P. R. China*

Anthony M. Reilly

*Fritz-Haber-Institut der Max-Planck-Gesellschaft, Faradayweg 4-6, 14195, Berlin, Germany and
School of Chemical Sciences, Dublin City University, Glasnevin, Dublin 9, Ireland*

Alexandre Tkatchenko

*Fritz-Haber-Institut der Max-Planck-Gesellschaft, Faradayweg 4-6, 14195, Berlin, Germany and
Physics and Materials Science Research Unit, University of Luxembourg,
162a Avenue de la Faiencerie, L-1511, Luxembourg**

Matthias Scheffler

Fritz-Haber-Institut der Max-Planck-Gesellschaft, Faradayweg 4-6, 14195, Berlin, Germany

Comparison of FHI-aims and WIEN2k EOS calculations

Now we discuss the reliability of the numerical implementation of DFT approaches in the FHI-aims computational package for bulk crystals. The FHI-aims code offers accurate and efficient implementation of DFT with (semi-)local and hybrid functionals to obtain ground-state properties of periodic and cluster systems (up to systems with thousands of atoms).¹ For periodic solids, the performance of FHI-aims can be seen when comparing the present results with those reported using the WIEN2k code,² which is based upon the full-potential linearized augmented plane-wave and local orbitals method to solve the KS equations and is normally regarded as the reference for solid-state studies, as long as numerical accuracy is achieved. The WIEN2k code developers in Blaha’s group have carried out extensive tests on cohesive properties of solids using various density functionals. We compare our results with their work. For the same database of 55 solids, excellent agreement is found with the reported WIEN2k values using both the LDA and PBE functionals,^{3–5} with the mean absolute deviations of 0.003 Å for the lattice constant and 0.5 GPa for the bulk modulus. In their very recent work, Tran *et al.*⁶ have extended assessment to more newly developed functionals. We analyze the mean absolute deviations between the two codes for the cohesive properties of a test set of 40 cubic solids. As shown in table I, we have found that the LDA and PBE results agree closely, followed by PBEsol and SCAN with poorer agreement. For instance, the deviations between the two implementations of PBE are within 0.003 Å for the lattice constant, 33 meV for the cohesive energy, and 0.6 GPa for the bulk modulus. It should be noted that our SCAN calculations were carried out using the PBE orbitals and densities. This is because the functionality to perform SCAN calculations in self-consistent manner is not yet available within the FHI-aims code. Neither does the SCAN implementation in the WIEN2k. While the WIEN2k results are also non-self consistent, they pointed out that the error in the lattice constant induced by this non-self-consistent procedure can be of the order of ~ 0.02 Å and should be in most cases below 0.005 Å and that the effect on the cohesive energy should be below 50 meV/atom except in the eventual cases where self-consistency would yield a different atomic electronic configuration from the one obtained with PBE for the isolated atom.⁶ We have also compared our cohesive properties for SCAN with the reported self-consistent results using the VASP code,⁷ with the mean absolute deviations are within 0.007 Å for the lattice constant and 60 meV for the cohesive energy, in agreement with the discussion by Tran *et al.* Though there are other variables (such as basis sets and pseudopotentials) that may amplify differences due to non-self-consistency, both the WIEN2k and our results suggest the post-SCF procedure is an acceptable approximation. Such deviations will not affect the conclusions of the present work, especially as our focus is on the trends in errors and improved methods for describing a wider range of bulk solids and properties in a consistent and efficient way. Further comparison of FHI-aims with WIEN2k can be done based on fully self-consistent calculations of 71 elemental crystals. Lejaeghere and co-authors⁸ proposed a method for evaluating numerical errors between different DFT codes and a more close look at the deviations of our results from those of WIEN2k shows remarkably accurate implementation of FHI-aims. Based upon this criterion, a recent benchmarking study from a highly international collaboration demonstrates that a reproducible precision for DFT predictions can be achieved, and they show that FHI-aims is among the most reliable all-electron codes today.⁹

TABLE I. The mean absolute deviations of the lattice constants a_0 (Å), the cohesive energies E_0 (eV/atom), and the bulk moduli B_0 (GPa) between the present work and the reported WIEN2k calculations (taken from Ref. 6) using different DFAs for the dataset of 40 solids.

Functional	a_0	E_0	B_0
	(Å)	(eV/atom)	(GPa)
LDA	0.003	0.023	0.9
PBE	0.003	0.033	0.6
PBEsol	0.004	0.035	1.0
SCAN	0.005	0.048	2.4

FHI-aims DFT EOS results

TABLE II. Equilibrium lattice constants (\AA) of 24 metals. The zero-point energy (ZPE) was determined by calculating the phonon dispersion relation at a set of volumes, marked as ‘‘Corr.’’, and ‘‘Uncorr.’’ refers as to the non-ZPE-corrected values. Experimental values with ZPE are summarized in the last columns (at 0 K unless noted otherwise).

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.*
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
Li	3.366	3.387	3.436	3.462	3.434	3.461	3.409	3.437	3.474	3.503	3.466	3.490	3.477
Na	4.052	4.067	4.203	4.219	4.172	4.189	4.029	4.046	4.207	4.223	4.215	4.231	4.225
K	5.043	5.055	5.284	5.301	5.214	5.230	4.924	4.943	5.317	5.337	5.313	5.328	5.225
Rb	5.376	5.385	5.669	5.677	5.568	5.576	5.238	5.247	5.703	5.708	5.756	5.765	5.585
Ca	5.336	5.346	5.527	5.538	5.455	5.466	5.384	5.392	5.549	5.559	5.582	5.593	5.565
Sr	5.789	5.795	6.020	6.028	5.907	5.914	5.881	5.887	6.076	6.085	6.092	6.100	6.048
Ba	4.758	4.760	5.011	5.015	4.868	4.872	4.983	4.987	5.036	5.039	5.087	5.091	5.007
Al	3.985	3.998	4.041	4.054	4.015	4.028	3.948	3.957	4.014	4.028	4.020	4.033	4.032
Pb	4.879	4.884	5.036	5.041	4.929	4.933	5.068	5.072	4.970	4.974	5.009	5.014	4.905
Fe	2.747	2.750	2.831	2.834	2.786	2.790	2.856	2.860	2.818	2.822	2.897	2.903	2.861
V	2.924	2.929	2.996	3.001	2.957	2.962	2.997	3.001	2.971	2.975	2.970	2.974	3.028
Mo	3.111	3.114	3.161	3.164	3.130	3.132	3.163	3.166	3.143	3.146	3.145	3.147	3.144
W	3.134	3.136	3.183	3.185	3.153	3.155	3.184	3.186	3.150	3.152	3.173	3.175	3.162
Nb	3.247	3.250	3.310	3.313	3.271	3.274	3.322	3.325	3.294	3.297	3.305	3.308	3.296
Ta	3.250	3.253	3.318	3.320	3.278	3.280	3.328	3.330	3.274	3.276	3.328	3.330	3.301
Ni	3.423	3.429	3.518	3.524	3.462	3.468	3.492	3.499	3.458	3.465	3.512	3.519	3.513
Cu	3.521	3.527	3.631	3.638	3.564	3.571	3.597	3.604	3.558	3.565	3.633	3.640	3.603
Rh	3.754	3.758	3.830	3.834	3.779	3.783	3.822	3.826	3.785	3.789	3.797	3.801	3.798
Ir	3.813	3.815	3.870	3.872	3.829	3.831	3.856	3.859	3.814	3.816	3.840	3.843	3.835
Pd	3.842	3.846	3.942	3.947	3.873	3.878	3.939	3.944	3.890	3.895	3.929	3.934	3.881
Pt	3.895	3.897	3.970	3.973	3.917	3.920	3.959	3.962	3.910	3.913	3.949	3.952	3.916
Ag	4.004	4.009	4.149	4.155	4.052	4.058	4.159	4.165	4.083	4.088	4.153	4.159	4.069
Au	4.054	4.058	4.157	4.161	4.081	4.084	4.158	4.163	4.094	4.098	4.153	4.157	4.065
Th	4.885	4.887	5.033	5.036	4.926	4.929	5.119	5.121	4.933	4.936	5.110	5.112	5.074

* Li(20 K)¹⁰, Na(5 K)¹¹, K(5 K)¹¹, Rb(5 K)¹¹, Ca¹², Sr¹², Ba¹², Al¹³, Pb(5 K)^{14,15}, Fe^{4,5}, V^{4,5}, Mo^{4,5}, W^{4,5}, Nb^{4,5}, Ta^{4,5}, Ni(10 K)^{15,16}, Cu^{17,18}, Rh^{17,18}, Ir(5 K)¹⁴, Pd^{17,18}, Pt^{4,5}, Au(5 K)¹⁴, Ag^{17,18}, Th^{4,5}.

TABLE III. Equilibrium lattice constants (\AA) of 40 non-metallic solids.

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.*
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
LiF	3.913	3.944	4.066	4.103	4.005	4.042	3.971	4.008	3.971	4.003	4.003	4.040	4.010
LiCl	4.966	4.994	5.151	5.185	5.064	5.094	5.117	5.149	5.109	5.138	5.107	5.138	5.106
NaF	4.504	4.528	4.700	4.727	4.625	4.652	4.576	4.601	4.574	4.598	4.635	4.661	4.609
NaCl	5.469	5.491	5.698	5.721	5.600	5.624	5.575	5.598	5.585	5.607	5.645	5.667	5.595
MgO	4.164	4.180	4.254	4.272	4.214	4.231	4.200	4.216	4.194	4.210	4.208	4.224	4.207
MgS	5.139	5.153	5.231	5.245	5.182	5.197	5.179	5.193	5.195	5.208	5.207	5.221	5.202
TiC	4.261	4.271	4.333	4.345	4.293	4.304	4.311	4.322	4.319	4.329	4.307	4.318	4.330
ZrC	4.642	4.651	4.710	4.719	4.669	4.678	4.707	4.716	4.703	4.712	4.700	4.708	4.696
HfC	4.573	4.582	4.653	4.662	4.611	4.619	4.645	4.654	4.620	4.628	4.647	4.655	4.638
VC	4.088	4.099	4.156	4.167	4.117	4.128	4.119	4.131	4.134	4.145	4.112	4.123	4.160
NbC	4.427	4.434	4.486	4.495	4.450	4.458	4.462	4.470	4.473	4.481	4.461	4.469	4.470
TiN	4.172	4.182	4.247	4.258	4.204	4.214	4.247	4.258	4.225	4.235	4.213	4.223	4.239
ZrN	4.525	4.535	4.595	4.605	4.553	4.563	4.615	4.625	4.580	4.590	4.575	4.584	4.585
HfN	4.469	4.477	4.550	4.559	4.504	4.512	4.566	4.575	4.508	4.516	4.531	4.539	4.519
VN	4.042	4.051	4.117	4.130	4.073	4.083	4.111	4.124	4.091	4.102	4.073	4.083	4.135
NbN	4.356	4.362	4.421	4.429	4.380	4.386	4.424	4.431	4.403	4.409	4.392	4.398	4.379
C	3.532	3.545	3.572	3.586	3.555	3.568	3.551	3.564	3.551	3.564	3.549	3.561	3.567
Si	5.405	5.414	5.470	5.479	5.431	5.440	5.425	5.434	5.433	5.442	5.444	5.452	5.430
Ge	5.625	5.630	5.761	5.767	5.664	5.669	5.787	5.795	5.669	5.674	5.702	5.709	5.652
Sn	6.474	6.480	6.651	6.659	6.527	6.534	6.718	6.726	6.550	6.558	6.580	6.588	6.482
AlP	5.434	5.444	5.508	5.518	5.470	5.480	5.457	5.466	5.475	5.484	5.482	5.491	5.458
AlAs	5.630	5.637	5.730	5.735	5.675	5.680	5.711	5.716	5.675	5.680	5.694	5.698	5.652
AlSb	6.108	6.116	6.224	6.231	6.153	6.159	6.221	6.227	6.166	6.172	6.184	6.191	6.128
BN	3.582	3.595	3.626	3.640	3.607	3.621	3.603	3.616	3.605	3.618	3.601	3.614	3.607
BP	4.492	4.504	4.549	4.562	4.521	4.533	4.519	4.532	4.528	4.540	4.530	4.542	4.538
BAs	4.733	4.744	4.810	4.822	4.768	4.779	4.792	4.804	4.772	4.783	4.781	4.792	4.777
GaN	4.460	4.469	4.548	4.559	4.498	4.508	4.539	4.549	4.494	4.504	4.504	4.513	4.520
GaP	5.398	5.406	5.507	5.515	5.437	5.445	5.501	5.509	5.444	5.452	5.467	5.475	5.442
GaAs	5.607	5.612	5.747	5.753	5.659	5.665	5.772	5.778	5.656	5.662	5.692	5.697	5.641
GaSb	6.052	6.058	6.216	6.222	6.113	6.119	6.262	6.268	6.116	6.122	6.152	6.158	6.082
InP	5.828	5.835	5.960	5.969	5.876	5.884	5.961	5.969	5.894	5.903	5.907	5.914	5.861
InAs	6.027	6.033	6.186	6.192	6.082	6.088	6.232	6.238	6.093	6.099	6.125	6.131	6.036
InSb	6.451	6.454	6.633	6.641	6.510	6.515	6.700	6.708	6.524	6.530	6.561	6.568	6.469
SiC	4.330	4.341	4.381	4.392	4.358	4.368	4.328	4.340	4.353	4.363	4.353	4.363	4.358
ZnS	5.299	5.308	5.445	5.457	5.357	5.367	5.454	5.464	5.376	5.386	5.419	5.429	5.404
ZnSe	5.569	5.575	5.734	5.741	5.633	5.639	5.765	5.773	5.650	5.656	5.700	5.706	5.668
ZnTe	5.997	6.004	6.180	6.194	6.063	6.070	6.239	6.246	6.084	6.090	6.152	6.159	6.104
CdS	5.761	5.768	5.929	5.939	5.825	5.833	5.948	5.957	5.860	5.869	5.885	5.894	5.818
CdSe	6.011	6.017	6.197	6.203	6.080	6.085	6.247	6.253	6.114	6.119	6.147	6.152	6.050
CdTe	6.412	6.418	6.620	6.627	6.487	6.492	6.696	6.703	6.523	6.530	6.574	6.579	6.480

* LiF¹³, LiCl¹³, NaF¹³, NaCl¹³, MgO¹³, MgS^{19,20}, TiC^{21,22}, ZrC^{21,22}, HfC^{21,22}, VC²¹⁻²³, NbC^{21,22}, TiN^{21,22}, ZrN^{21,22}, HfN^{21,22}, VN^{24,25}, NbN^{22,26}, C²⁷, Si²⁸, Ge²⁸, Sn(20 K)^{29,30}, SiC^{14,17}, AlP³¹, AlAs³¹, AlSb³¹, BN²⁹, BP²⁹, BAs³², GaN³⁰, GaP³¹, GaAs³¹, GaSb³¹, InP³¹, InAs³¹, InSb³¹, ZnS(4.2 K)³³, ZnSe^{29,34}, ZnTe³⁵, CdS³⁶, CdSe³⁷, CdTe³⁷.

TABLE IV. Equilibrium bulk moduli (GPa) of 24 metals

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.*
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
Li	15.2	14.2	14.1	13.5	13.7	12.9	12.5	11.5	11.2	12.5	13.7	13.3	12.8
Na	9.1	8.9	7.7	7.5	7.7	7.6	8.4	7.9	8.0	7.9	7.8	7.6	7.5
K	4.5	4.7	3.6	3.57	3.8	3.4	5.3	5.6	3.4	3.7	3.4	3.4	3.7
Rb	3.6	3.6	2.8	2.79	3.0	2.9	5.0	5.0	2.9	3.2	2.5	2.5	3.1
Ca	18.8	18.5	17.4	17.1	17.9	17.6	22.0	21.6	18.3	18.2	17.2	17.3	18.4
Sr	14.3	14.3	11.5	11.4	12.7	12.6	17.0	16.8	10.7	10.6	11.3	11.2	12.4
Ba	10.3	10.2	8.8	8.8	8.8	8.0	11.8	11.8	8.8	8.8	8.4	8.4	9.3
Al	83.7	81.3	77.6	76.0	82.3	80.8	117.0	116.2	80.4	78.7	82.9	82.0	79.4
Pb	53.7	52.6	40.0	39.6	48.8	48.6	38.8	38.8	46.4	45.9	43.6	43.3	48.8
Fe	252.1	252.7	195.1	190.2	227.6	229.5	152.0	145.4	185.3	185.3	150.9	145.1	173.0
V	209.1	207.0	182.6	180.8	197.5	197.5	192.6	192.8	197.6	197.9	212.4	211.9	157.0
Mo	293.0	290.2	259.1	256.5	279.0	276.0	266.8	264.3	278.8	275.9	285.5	282.9	265.3
W	335.9	334.3	301.9	300.3	321.5	319.7	319.9	318.6	325.6	323.8	329.9	328.5	314.2
Nb	195.2	192.4	169.7	167.5	180.5	179.1	174.2	173.2	177.7	176.5	184.0	182.4	174.0
Ta	211.9	210.5	194.1	193.3	206.4	206.4	202.1	201.5	205.5	205.5	221.9	221.1	194.2
Ni	256.7	251.6	199.4	196.3	231.2	228.3	217.8	215.9	231.8	228.1	190.0	185.4	187.6
Cu	187.3	184.1	139.4	136.8	165.3	162.3	154.8	152.2	168.4	165.5	130.7	127.9	142.3
Rh	317.8	315.0	257.1	254.2	294.5	291.9	263.3	261.3	293.7	291.2	281.6	279.0	268.7
Ir	403.4	400.8	350.1	347.4	393.1	390.5	370.6	367.9	411.1	409.1	383.3	380.7	383.0
Pd	226.9	224.2	168.6	166.2	203.2	200.5	165.9	163.0	195.0	192.2	169.7	167.0	195.0
Pt	307.4	305.3	249.1	246.9	289.8	287.9	259.6	257.3	294.3	292.5	262.8	260.7	277.0
Ag	138.7	135.6	91.0	89.3	118.5	116.9	88.4	87.1	110.2	108.3	88.7	87.3	110.9
Au	194.6	192.8	139.7	137.7	176.5	174.2	135.1	133.5	168.3	166.1	141.6	140.2	180.9
Th	63.3	63.8	55.2	55.1	60.4	60.1	55.0	54.1	56.7	56.3	54.4	53.8	57.7

* Li³⁸, Na³⁹, K⁴⁰, Rb⁴¹, Ca¹², Sr¹², Ba¹², Al⁴², Pb⁴³, Fe^{44,45}, V⁴⁶, Mo⁴⁷, W⁴⁷, Nb⁴⁸⁻⁵⁰, Ta⁴⁷, Ni^{44,45}, Cu^{51,52}, Rh(4.2 K)⁵³, Ir⁵⁴, Pd⁵⁵, Pt^{56,57}, Au⁵², Ag⁵², Th^{57,58}.

TABLE V. Equilibrium bulk moduli (GPa) of 40 non-metallic solids

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.*
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
LiF	85.4	79.2	67.2	61.6	72.8	69.3	76.8	70.6	86.6	79.2	77.9	72.3	69.8
LiCl	40.8	39.7	31.7	29.8	35.0	32.6	35.0	32.2	36.3	35.3	35.1	32.8	35.4
NaF	61.7	58.8	45.3	42.6	49.1	46.9	53.7	51.2	56.4	53.9	49.2	48.3	51.4
NaCl	32.2	31.3	23.7	23.0	26.0	25.8	27.1	26.2	28.7	28.7	25.3	24.1	28.5
MgO	171.7	166.9	149.4	145.2	157.7	153.0	165.3	159.8	169.6	164.9	165.0	160.5	168.8
MgS	82.8	81.0	73.8	71.7	78.0	76.9	81.5	80.4	80.1	79.1	78.8	77.8	78.9
TiC	282.6	277.1	249.6	244.1	266.0	259.7	267.7	261.9	268.5	263.7	276.8	271.2	244.0
ZrC	246.6	242.5	222.0	218.1	235.1	231.7	230.0	226.2	231.4	228.1	237.0	234.0	226.0
HfC	260.2	255.2	236.5	233.6	250.2	247.4	249.2	246.6	254.0	250.6	248.2	245.3	275.0
VC	346.8	341.3	306.2	301.5	329.4	328.5	329.8	328.4	330.3	329.0	347.8	347.8	303.0
NbC	333.4	324.5	299.4	289.1	318.3	308.8	315.6	306.1	313.6	304.3	327.1	317.7	302.0
TiN	320.7	313.9	278.0	271.5	301.4	295.6	284.6	279.3	301.4	294.5	311.6	305.9	289.0
ZrN	283.7	277.8	250.3	245.0	276.6	270.9	244.8	240.4	265.8	260.9	269.8	265.0	215.0
HfN	301.7	296.1	260.8	254.5	277.5	272.8	257.7	251.5	284.6	280.8	283.8	280.5	306.0
VN	367.2	353.3	314.9	301.6	344.5	325.3	317.2	298.6	342.2	322.7	356.8	335.9	268.0
NbN	351.0	345.4	306.9	298.4	332.8	324.5	303.8	295.7	326.8	318.7	339.0	330.7	292.0
C	467.0	456.8	434.3	424.0	451.2	435.2	452.8	437.8	459.6	445.0	468.8	452.9	443.0
Si	96.2	94.6	88.6	87.5	95.3	94.8	97.7	97.5	99.1	99.0	97.6	97.4	99.2
Ge	72.4	70.2	59.4	57.3	66.9	66.0	58.3	56.5	72.2	71.3	70.2	67.9	75.8
Sn	44.9	43.8	35.9	35.4	41.4	39.4	35.0	34.8	41.8	40.7	43.2	42.8	53.0
AlP	89.4	87.4	82.4	81.4	86.6	84.6	91.1	89.1	89.5	87.4	94.5	91.6	86.0
AlAs	75.0	74.2	66.9	65.7	71.8	71.9	70.4	69.4	75.8	76.3	74.5	74.1	78.1
AlSb	56.0	55.8	49.2	49.0	54.3	55.0	51.6	51.7	56.3	56.7	55.2	54.5	59.3
BN	402.1	392.8	374.1	363.6	388.0	373.8	391.7	380.8	394.5	379.6	399.6	389.8	378.0
BP	175.2	171.5	162.0	158.5	169.5	165.9	170.1	166.5	171.1	168.9	173.0	169.7	173.0
AsB	146.6	143.8	131.7	128.7	140.8	138.4	134.2	131.6	145.6	143.1	143.3	140.4	148.0
GaN	201.6	197.7	172.0	168.0	188.9	184.9	179.6	176.0	193.7	189.5	197.4	193.3	200.0
GaP	89.1	87.4	76.6	75.5	85.1	83.7	81.1	79.5	88.0	86.7	87.9	86.4	88.7
GaAs	74.2	74.0	60.7	59.5	69.0	69.0	61.5	60.3	72.4	72.5	70.9	70.0	76.9
GaSb	55.5	55.1	44.5	44.0	52.0	51.8	44.0	43.7	53.6	53.4	53.0	52.7	56.3
InP	70.8	68.6	59.9	58.9	67.1	65.6	63.6	62.6	69.3	68.1	69.4	68.4	72.5
InAs	59.9	59.1	48.1	47.7	56.4	56.5	47.6	47.1	58.1	57.9	57.2	56.8	58.0
InSb	46.5	44.0	36.9	36.2	44.1	43.3	36.3	35.8	44.5	43.5	44.0	42.7	46.5
SiC	228.7	225.2	212.9	209.0	222.0	220.9	225.1	221.6	229.9	227.4	228.9	225.4	225.0
ZnS	86.4	84.6	69.7	68.8	79.0	76.5	74.6	74.1	79.9	77.6	77.0	75.9	77.2
ZnSe	71.5	71.4	56.7	55.5	65.3	64.5	58.2	57.2	66.1	65.1	63.3	61.9	64.7
ZnTe	55.4	54.9	43.3	43.0	50.5	50.6	42.1	42.8	50.6	49.8	48.9	48.6	52.8
CdS	68.0	64.3	53.5	52.8	61.5	59.8	57.7	56.7	61.5	60.1	60.8	59.3	64.3
CdSe	58.0	57.9	44.8	44.3	52.6	52.4	46.1	45.6	52.6	52.1	51.2	50.3	55.0
CdTe	46.2	48.2	35.2	33.5	41.6	40.1	35.2	34.8	41.3	39.3	40.1	39.4	44.5

* LiF⁵⁹, LiCl⁶⁰, NaF⁶⁰, NaCl⁶¹, MgO⁶², MgS¹⁹, TiC⁶³, ZrC⁶³, HfC (296 K)^{64,65}, VC⁶⁶, NbC^{67,68}, TiN⁶⁹, ZrN(300 K)²⁶, HfN(300 K)²⁶, VN(300 K)⁷⁰, NbN(300 K)²⁶, C^{17,18}, Si(77 K)⁷¹, Ge(4.2 K)⁷², Sn(90 K)^{73,74}, SiC⁷⁵, AlP^{13,76}, AlAs^{76,77}, AlSb^{76,77}, BN⁷⁸, BP⁷⁹, BAs³², GaN¹³, GaP^{76,77}, GaAs⁸⁰, GaSb^{76,77}, InP^{76,77}, InAs^{76,77}, InSb^{76,77}, ZnS⁸¹, ZnSe⁸¹, ZnTe⁸¹, CdS³⁷, CdSe³⁷, CdTe⁸¹.

TABLE VI. Equilibrium cohesive energies (eV/atom) of 24 metals. The experimental values are taken from Ref. 82 at 0 K.

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
Li	-1.80	-1.76	-1.68	-1.64	-1.75	-1.71	-1.88	-1.85	-1.60	-1.57	-1.62	-1.59	-1.63
Na	-1.25	-1.23	-1.10	-1.08	-1.17	-1.15	-1.45	-1.43	-1.08	-1.06	-1.06	-1.04	-1.11
K	-1.03	-1.02	-0.88	-0.88	-0.95	-0.94	-1.35	-1.34	-0.85	-0.84	-0.85	-0.84	-0.93
Rb	-0.94	-0.93	-0.79	-0.79	-0.83	-0.83	-1.31	-1.30	-0.75	-0.74	-0.73	-0.73	-0.85
Ca	-2.20	-2.18	-1.93	-1.91	-2.13	-2.10	-2.50	-2.48	-2.10	-2.08	-1.80	-1.78	-1.84
Sr	-1.89	-1.88	-1.64	-1.63	-1.85	-1.83	-2.24	-2.23	-1.83	-1.82	-1.57	-1.56	-1.72
Ba	-2.20	-2.19	-1.88	-1.87	-2.13	-2.11	-2.49	-2.48	-2.05	-2.04	-1.70	-1.69	-1.90
Al	-4.00	-3.96	-3.47	-3.44	-3.85	-3.81	-4.25	-4.20	-3.66	-3.62	-3.43	-3.39	-3.39
Pb	-3.78	-3.77	-3.02	-3.01	-3.40	-3.39	-3.59	-3.58	-3.01	-3.00	-2.93	-2.93	-2.03
Fe	-6.40	-6.35	-4.94	-4.90	-5.67	-5.63	-5.03	-4.99	-4.57	-4.53	-3.31	-3.27	-4.28
V	-6.74	-6.71	-5.42	-5.39	-6.02	-5.99	-6.21	-6.17	-4.58	-4.54	-3.61	-3.58	-5.31
Mo	-8.09	-8.05	-6.34	-6.30	-7.15	-7.11	-6.98	-6.95	-5.66	-5.63	-5.25	-5.22	-6.82
W	-10.23	-10.19	-8.46	-8.43	-9.26	-9.23	-9.95	-9.92	-8.73	-8.70	-7.81	-7.78	-8.90
Nb	-8.50	-8.47	-7.04	-7.01	-7.76	-7.73	-7.91	-7.88	-6.56	-6.53	-6.21	-6.18	-7.57
Ta	-9.59	-9.56	-8.19	-8.17	-9.01	-8.99	-8.76	-8.74	-8.46	-8.44	-7.77	-7.75	-8.09
Ni	-6.09	-6.05	-4.76	-4.72	-5.49	-5.45	-4.95	-4.91	-4.53	-4.49	-3.26	-3.22	-4.44
Cu	-4.54	-4.51	-3.52	-3.49	-4.03	-3.99	-4.28	-4.25	-3.94	-3.90	-3.10	-3.07	-3.49
Rh	-7.58	-7.55	-5.83	-5.80	-6.72	-6.68	-5.60	-5.57	-5.29	-5.26	-4.82	-4.79	-5.75
Ir	-9.32	-9.29	-7.45	-7.42	-8.48	-8.45	-7.16	-7.13	-7.55	-7.52	-6.41	-6.38	-6.94
Pd	-5.06	-5.02	-3.72	-3.70	-4.46	-4.43	-4.08	-4.05	-4.31	-4.28	-2.98	-2.96	-3.89
Pt	-7.15	-7.12	-5.59	-5.56	-6.50	-6.48	-5.81	-5.79	-5.86	-5.84	-5.47	-5.45	-5.84
Ag	-3.63	-3.60	-2.54	-2.52	-3.11	-3.09	-3.17	-3.15	-2.89	-2.87	-2.44	-2.42	-2.95
Au	-4.38	-4.36	-3.09	-3.07	-3.79	-3.77	-3.61	-3.59	-3.59	-3.58	-2.97	-2.96	-3.81
Th	-7.54	-7.53	-6.37	-6.35	-7.25	-7.23	-6.83	-6.82	-6.44	-6.43	-6.06	-6.05	-6.20

TABLE VII. Equilibrium cohesive energies (eV/atom) of 40 non-metallic solids

Solid	LDA		PBE		PBEsol		M06-L		SCAN		HSE06		Exp.*
	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	Uncorr.	Corr.	
LiF	-4.92	-4.86	-4.36	-4.30	-4.51	-4.45	-4.53	-4.47	-4.38	-4.32	-4.27	-4.21	-4.40
LiCl	-3.82	-3.78	-3.40	-3.37	-3.56	-3.52	-3.79	-3.75	-3.52	-3.49	-3.42	-3.38	-3.55
NaF	-4.36	-4.31	-3.83	-3.79	-3.97	-3.92	-4.08	-4.04	-3.88	-3.84	-3.74	-3.70	-3.93
NaCl	-3.48	-3.45	-3.11	-3.09	-3.24	-3.21	-3.59	-3.57	-3.28	-3.25	-3.13	-3.11	-3.33
MgO	-5.80	-5.72	-4.98	-4.91	-5.31	-5.24	-5.25	-5.18	-5.19	-5.11	-4.91	-4.84	-5.12
MgS	-4.31	-4.27	-3.71	-3.67	-4.03	-3.99	-4.10	-4.05	-3.97	-3.93	-3.76	-3.71	-4.00
TiC	-8.63	-8.55	-7.43	-7.35	-8.01	-7.92	-7.79	-7.71	-7.08	-7.00	-7.30	-7.21	-7.16
ZrC	-9.10	-9.03	-7.97	-7.91	-8.49	-8.43	-8.24	-8.17	-7.65	-7.58	-7.65	-7.58	-7.93
HfC	-9.26	-9.19	-8.10	-8.03	-8.73	-8.66	-8.31	-8.24	-8.13	-8.06	-7.90	-7.84	-8.11
VC	-8.34	-8.27	-7.07	-7.01	-7.68	-7.61	-7.31	-7.24	-6.62	-6.55	-6.12	-6.05	-6.94
NbC	-9.34	-9.27	-7.99	-7.92	-8.65	-8.58	-8.27	-8.20	-7.69	-7.62	-7.53	-7.46	-8.26
TiN	-8.29	-8.21	-7.02	-6.95	-7.58	-7.51	-7.25	-7.18	-6.60	-6.53	-6.76	-6.68	-6.69
ZrN	-8.76	-8.70	-7.56	-7.50	-8.07	-8.01	-7.72	-7.66	-7.14	-7.08	-7.13	-7.07	-7.52
HfN	-8.80	-8.74	-7.54	-7.49	-8.17	-8.11	-7.63	-7.58	-7.48	-7.42	-7.246	-7.191	-8.03
VN	-7.63	-7.57	-6.31	-6.26	-6.90	-6.84	-6.38	-6.33	-5.77	-5.72	-5.20	-5.14	-6.25
NbN	-8.52	-8.49	-7.11	-7.08	-7.76	-7.72	-7.25	-7.22	-6.71	-6.68	-6.51	-6.48	-7.50
C	-8.94	-8.76	-7.73	-7.55	-8.28	-8.10	-7.48	-7.30	-7.54	-7.36	-7.57	-7.39	-7.37
Si	-5.30	-5.23	-4.58	-4.51	-4.97	-4.91	-4.69	-4.63	-4.73	-4.67	-4.55	-4.49	-4.63
Ge	-4.59	-4.55	-3.76	-3.72	-4.23	-4.19	-3.83	-3.79	-3.97	-3.94	-3.75	-3.71	-3.87
Sn	-3.95	-3.93	-3.21	-3.19	-3.60	-3.58	-3.36	-3.34	-3.39	-3.37	-3.23	-3.21	-3.14
AlP	-4.81	-4.75	-4.11	-4.06	-4.46	-4.40	-4.23	-4.17	-4.26	-4.20	-4.11	-4.06	-4.26
AlAs	-4.46	-4.42	-3.71	-3.67	-4.08	-4.03	-3.83	-3.78	-3.87	-3.83	-3.74	-3.70	-3.78
AlSb	-3.97	-3.94	-3.27	-3.23	-3.62	-3.58	-3.42	-3.38	-3.41	-3.37	-3.30	-3.27	-3.30
BN	-8.05	-7.89	-7.01	-6.85	-7.41	-7.25	-6.76	-6.61	-6.83	-6.68	-6.79	-6.64	-6.60
BP	-6.23	-6.13	-5.36	-5.26	-5.74	-5.64	-5.20	-5.10	-5.31	-5.21	-5.23	-5.13	-5.04
AsB	-5.61	-5.53	-4.71	-4.63	-5.09	-5.01	-4.63	-4.55	-4.68	-4.60	-4.60	-4.52	-4.70
GaN	-5.38	-5.30	-4.41	-4.33	-4.85	-4.77	-4.35	-4.28	-4.44	-4.37	-4.29	-4.21	-4.48
GaP	-4.32	-4.27	-3.51	-3.46	-3.92	-3.87	-3.55	-3.51	-3.65	-3.61	-3.52	-3.47	-3.56
GaAs	-4.04	-4.00	-3.17	-3.14	-3.58	-3.55	-3.26	-3.23	-3.32	-3.29	-3.21	-3.17	-3.31
GaSb	-3.66	-3.64	-2.85	-2.82	-3.22	-3.20	-2.99	-2.97	-3.01	-2.98	-2.90	-2.87	-3.00
InP	-3.96	-3.92	-3.17	-3.14	-3.56	-3.52	-3.27	-3.23	-3.27	-3.23	-3.19	-3.15	-3.43
InAs	-3.74	-3.71	-2.92	-2.89	-3.30	-3.28	-3.04	-3.01	-3.02	-2.99	-2.94	-2.91	-3.05
InSb	-3.45	-3.43	-2.67	-2.65	-3.04	-3.02	-2.86	-2.84	-2.79	-2.77	-2.73	-2.71	-2.79
SiC	-7.40	-7.28	-6.41	-6.30	-6.88	-6.77	-6.45	-6.34	-6.47	-6.36	-6.35	-6.24	-6.36
ZnS	-3.71	-3.67	-2.91	-2.87	-3.30	-3.26	-3.06	-3.02	-3.15	-3.11	-2.96	-2.93	-3.17
ZnSe	-3.37	-3.34	-2.58	-2.55	-2.98	-2.95	-2.63	-2.60	-2.80	-2.77	-2.66	-2.63	-2.63
ZnTe	-2.95	-2.93	-2.11	-2.09	-2.26	-2.24	-2.19	-2.17	-2.31	-2.29	-1.99	-1.97	-2.41
CdS	-3.32	-3.28	-2.57	-2.53	-2.92	-2.89	-2.77	-2.74	-2.76	-2.72	-2.64	-2.61	-2.78
CdSe	-3.07	-3.04	-2.32	-2.30	-2.68	-2.66	-2.43	-2.41	-2.49	-2.47	-2.41	-2.39	-2.46
CdTe	-2.74	-2.72	-1.93	-1.91	-2.05	-2.03	-2.08	-2.06	-2.09	-2.07	-1.87	-1.85	-2.23

* LiF⁸³, LiCl⁸³, NaF⁸³, NaCl⁸³, MgO⁶², MgS^{84,85}, TiC^{83,86}, ZrC^{83,86,87}, HfC^{83,86}, VC^{83,86}, NbC^{83,86,87}, TiN⁸⁸, ZrN⁸⁷, HfN⁸⁹, VN⁸⁸, NbN⁸⁷, C⁸², Si⁸², Ge⁸², Sn⁸², SiC^{83,90}, AlP⁹¹, AlAs⁹¹, AlSb⁹², BN^{83,90}, BP⁹², BAs(300 K)⁹³, GaN^{83,90}, GaP^{83,90}, GaAs⁷⁷, GaSb⁹⁴, InP⁹⁴, InAs⁹⁴, InSb⁹⁴, ZnS^{92,95}, ZnSe^{92,95}, ZnTe^{92,95}, CdS⁹², CdSe⁹², CdTe⁹².

TABLE VIII. The mean absolute relative error (MARE, %) for the lattice constants a_0 , cohesive energies E_0 , and bulk moduli B_0 of the 23 semiconductor solids.

	LDA	PBE	PBEsol	M06-L	SCAN	HSE06
a_0	0.6	1.5	0.4	1.6	0.5	0.8
E_0	19.1	5.2	7.4	2.5	2.2	4.7
B_0	4.1	15.3	5.5	12.2	3.6	5.3
		PBE+vdW		M06-L+vdW		HSE06+vdW
a_0		0.7		1.0		0.3
E_0		3.6		5.2		4.1
B_0		7.8		9.4		4.3

TABLE IX. k -point meshes (kpts) settings for FHI-aims tier 2 calculations within LDA, GGAs, and MGGAs. For the hybrid HSE06 calculations, coarser densities are used due to the excessive computational cost.

Solid	kpts	Solid	kpts
Li	32×32×32	HfC	22×22×22
Na	28×28×28	VC	24×24×24
K	22×22×22	NbC	22×22×22
Rb	22×22×22	TiN	24×24×24
Ca	18×18×18	ZrN	22×22×22
Sr	18×18×18	HfN	22×22×22
Ba	24×24×24	VN	24×24×24
Al	24×24×24	NbN	22×22×22
Pb	20×20×20	C	46×46×46
Fe	38×38×38	Si	28×28×28
V	36×36×36	Ge	32×32×32
Mo	36×36×36	Sn	26×26×26
W	36×36×36	AlP	16×16×16
Nb	34×34×34	AlAs	16×16×16
Ta	34×34×34	AlSb	14×14×14
Ni	28×28×28	BN	24×24×24
Cu	28×28×28	BP	20×20×20
Rh	26×26×26	BAs	20×20×20
Ir	26×26×26	GaN	20×20×20
Pd	26×26×26	GaP	16×16×16
Pt	26×26×26	GaAs	16×16×16
Ag	24×24×24	GaSb	16×16×16
Au	24×24×24	InP	16×16×16
Th	20×20×20	InAs	16×16×16
LiF	24×24×24	InSb	14×14×14
LiCl	20×20×20	SiC	20×20×20
NaF	22×22×22	ZnS	16×16×16
NaCl	18×18×18	ZnSe	16×16×16
MgO	24×24×24	ZnTe	16×16×16
MgS	20×20×20	CdS	16×16×16
TiC	24×24×24	CdSe	16×16×16
ZrC	22×22×22	CdTe	14×14×14

- * alexandre.tkatchenko@uni.lu
- ¹ V. Blum, R. Gehrke, F. Hanke, P. Havu, V. Havu, X. Ren, K. Reuter, and M. Scheffler, *Comput. Phys. Commun.* **180**, 2175 (2009).
 - ² P. Blaha, K. Schwarz, G. K. H. Madsen, D. Kvasnicka, and J. Luitz, *WIEN2k, An Augmented Plane Wave Plus Local Orbitals Program for Calculating Crystal Properties* (Vienna University of Technology, Austria, 2001).
 - ³ F. Tran, R. Laskowski, P. Blaha, and K. Schwarz, *Phys. Rev. B* **75**, 115131 (2007).
 - ⁴ P. Haas, F. Tran, and P. Blaha, *Phys. Rev. B* **79**, 085104 (2009).
 - ⁵ P. Haas, F. Tran, and P. Blaha, *Phys. Rev. B* **79**, 209902(E) (2009).
 - ⁶ F. Tran, J. Stelzl, and P. Blaha, *J. Chem. Phys.* **144**, 204120 (2016).
 - ⁷ H. Peng, Z.-H. Yang, J. Sun, and J. P. Perdew, *Phys. Rev. X* **6**, 041005 (2016).
 - ⁸ K. Lejaeghere, V. V. Speybroeck, G. V. Oost, and S. Cottenier, *Crit. Rev. Solid State Mater.* **39**, 1 (2014).
 - ⁹ K. Lejaeghere, G. Bihlmayer, T. Bjrkman, P. Blaha, S. Blgel, V. Blum, D. Caliste, I. E. Castelli, S. J. Clark, A. D. Corso, S. d. Gironcoli, T. Deutsch, J. K. Dewhurst, I. D. Marco, C. Draxl, M. Duak, O. Eriksson, J. A. Flores-Livas, K. F. Garrity, L. Genovese, P. Giannozzi, M. Giantomassi, S. Goedecker, X. Gonze, O. Grns, E. K. U. Gross, A. Gulans, F. Gygi, D. R. Hamann, P. J. Hasnip, N. A. W. Holzwarth, D. Iuan, D. B. Jochym, F. Jollet, D. Jones, G. Kresse, K. Koepnik, E. Kkbenli, Y. O. Kvashnin, I. L. M. Locht, S. Lubeck, M. Marsman, N. Marzari, U. Nitzsche, L. Nordstrm, T. Ozaki, L. Paulatto, C. J. Pickard, W. Poelmans, M. I. J. Probert, K. Refson, M. Richter, G.-M. Rignanese, S. Saha, M. Scheffler, M. Schlipf, K. Schwarz, S. Sharma, F. Tavazza, P. Thunstrm, A. Tkatchenko, M. Torrent, D. Vanderbilt, M. J. v. Setten, V. V. Speybroeck, J. M. Wills, J. R. Yates, G.-X. Zhang, and S. Cottenier, *Science* **351**, aad3000 (2016).
 - ¹⁰ R. Berliner and S. A. Werner, *Phys. Rev. B* **34**, 3586 (1986).
 - ¹¹ C. S. Barrett, *Acta Cryst.* **9**, 671 (1956).
 - ¹² M. S. Anderson, C. A. Swenson, and D. T. Peterson, *Phys. Rev. B* **41**, 3329 (1990).
 - ¹³ K. H. Hellwege, ed., *Landolt-Börnstein, New Series, Group III* (Springer, Berlin, 1966).
 - ¹⁴ Y. S. Touloukian, R. K. Kirby, R. E. Taylor, and P. D. Desai, *Thermophysical Properties of Matter*, Vol. 12 (IFI/Plenum, New York, 1975).
 - ¹⁵ R. Gaudoin and W. M. C. Foulkes, *Phys. Rev. B* **66**, 052104 (2002).
 - ¹⁶ M. Kresch, O. Delaire, R. Stevens, J. Y. Y. Lin, and B. Fultz, *Phys. Rev. B* **75**, 104301 (2007).
 - ¹⁷ V. N. Staroverov, G. E. Scuseria, J. Tao, and J. P. Perdew, *Phys. Rev. B* **69**, 075102 (2004).
 - ¹⁸ V. N. Staroverov, G. E. Scuseria, J. Tao, and J. P. Perdew, *Phys. Rev. B* **78**, 239907(E) (2008).
 - ¹⁹ S. M. Peiris, A. J. Campbell, and D. L. Heinz, *J. Phys. Chem. Solids* **55**, 413 (1994).
 - ²⁰ Y. Takéuchi, S. Sasaki, K. A. Bente, and K. Tsukimura, *Acta Cryst.* **B49**, 780 (1993).
 - ²¹ W. B. Pearson, P. Villars, and L. D. Calvert, *Pearson's Handbook of Crystallographic Data for Intermetallic Phases* (American Society for Metals, Metals Park, Ohio, 1985).
 - ²² E. I. Isaev, R. Ahuja, S. I. Simak, A. I. Lichtenstein, Y. K. Vekilov, B. Johansson, and I. A. Abrikosov, *Phys. Rev. B* **72**, 064515 (2005).
 - ²³ W. K. Schubert, R. N. Shelton, and E. L. Wolf, *Phys. Rev. B* **23**, 5097 (1981).
 - ²⁴ N. A. Christensen and P. Roehammer, *J. Cryst. Growth* **38**, 281 (1977).
 - ²⁵ B. R. Zhao, L. Chen, H. L. Luo, M. D. Jack, and D. P. Mullin, *Phys. Rev. B* **29**, 6198 (1984).
 - ²⁶ X.-J. Chen, V. V. Struzhkin, Z. Wu, M. Somayazulu, J. Qian, S. Kung, A. N. Christensen, Y. Zhao, R. E. Cohen, H.-k. Mao, and R. J. Hemley, *Proc. Nat. Acad. Sci. U.S.A.* **102**, 3198 (2005).
 - ²⁷ S. Stoupin and Y. V. Shvyd'ko, *Phys. Rev. Lett.* **104**, 085901 (2010).
 - ²⁸ R. R. Reeber and K. Wang, *Mater. Chem. Phys.* **46**, 259 (1996).
 - ²⁹ O. Madelung, *Semiconductors: Data Handbook* (Springer, Berlin, 2004).
 - ³⁰ L. Schimka, J. Harl, and G. Kresse, *J. Chem. Phys.* **134**, 024116 (2011).
 - ³¹ I. Vurgaftman, J. R. Meyer, and L. R. Ram-Mohan, *J. Appl. Phys.* **89**, 5815 (2001).
 - ³² R. G. Greene, H. Luo, A. L. Ruoff, S. S. Trail, and F. J. DiSalvo, *Phys. Rev. Lett.* **73**, 2476 (1994).
 - ³³ R. R. Reeber, *Phys. Status Solidi A* **32**, 321 (1975).
 - ³⁴ G.-D. Lee, M. H. Lee, and J. Ihm, *Phys. Rev. B* **52**, 1459 (1995).
 - ³⁵ L. Ley, R. A. Pollak, F. R. McFeely, S. P. Kowalczyk, and D. A. Shirley, *Phys. Rev. B* **9**, 600 (1974).
 - ³⁶ S. J. Clark and J. Robertson, *Phys. Rev. B* **82**, 085208 (2010).
 - ³⁷ S. Sarkar, S. Pal, P. Sarkar, A. L. Rosa, and T. Frauenheim, *J. Chem. Theory Comput.* **7**, 2262 (2011).
 - ³⁸ R. A. Felice, J. Trivisonno, and D. E. Schuele, *Phys. Rev. B* **16**, 5173 (1977).
 - ³⁹ M. E. Diederich and J. Trivisonno, *J. Phys. Chem. Solids* **27**, 637 (1966).
 - ⁴⁰ W. R. Marquardt and J. Trivisgnno, *J. Phys. Chem. Solids* **26**, 273 (1965).
 - ⁴¹ E. J. Gutman and J. Trivisonno, *J. Phys. Chem. Solids* **28**, 805 (1967).
 - ⁴² G. N. Kamm and G. A. Alers, *J. Appl. Phys.* **35**, 327 (1964).
 - ⁴³ D. L. Waldorf and G. A. Alers, *J. Appl. Phys.* **33**, 3266 (1962).
 - ⁴⁴ O. L. Anderson, in *Physical Acoustics*, edited by W. P. Mason, Vol. III-B (Academic, New York, 1965).
 - ⁴⁵ V. L. Moruzzi and P. M. Marcus, *Phys. Rev. B* **48**, 7665 (1993).
 - ⁴⁶ G. A. Alers, *Phys. Rev.* **119**, 1532 (1960).
 - ⁴⁷ F. H. Featherston and J. R. Neighbours, *Phys. Rev.* **130**, 1324 (1963).

- ⁴⁸ G. A. Alers and D. L. Waldorf, Phys. Rev. Lett. **6**, 677 (1961).
- ⁴⁹ K. A. Jones, S. C. Moss, and R. M. Rose, Acta Met. **17**, 365 (1969).
- ⁵⁰ W. C. Hubbell and F. R. Brotzen, J. Appl. Phys. **43**, 3306 (1972).
- ⁵¹ W. C. Overton and J. Gaffney, Phys. Rev. **98**, 969 (1955).
- ⁵² W. B. Holzapfel, M. Hartwig, and W. Sievers, J. Phys. Chem. Ref. Data **30**, 515 (2001).
- ⁵³ E. Walker, J. Ashkenazi, and M. Dacorogna, Phys. Rev. B **24**, 2254 (1981).
- ⁵⁴ H. Cynn, J. E. Klepeis, C.-S. Yoo, and D. A. Young, Phys. Rev. Lett. **88**, 135701 (2002).
- ⁵⁵ D. K. Hsu and R. G. Leisure, Phys. Rev. B **20**, 1339 (1979).
- ⁵⁶ R. E. MacFarlane, J. A. Rayne, and C. K. Jones, Phys. Letts. **20**, 234 (1966).
- ⁵⁷ G. Simmons and H. Wang, *Single Crystal Elastic Constants and Calculated Aggregate Properties: A Handbook*, 2nd ed. (MIT Press, Cambridge, Massachusetts, 1971).
- ⁵⁸ G. Bellussi, U. Benedict, and W. B. Holzapfel, J. Less-Common Met. **78**, 147 (1981).
- ⁵⁹ C. V. Briscoe and C. F. Squire, Phys. Rev. **106**, 1175 (1957).
- ⁶⁰ J. T. Lewis, A. Lehoczy, and C. V. Briscoe, Phys. Rev. **161**, 877 (1967).
- ⁶¹ H. Spetzler, C. G. Sammis, and R. J. O'Connell, J. Phys. Chem. Solids **33**, 1727 (1972).
- ⁶² A. J. Cohen and R. G. Gordon, Phys. Rev. B **14**, 4593 (1976).
- ⁶³ R. Chang and L. J. Graham, J. Appl. Phys. **37**, 3778 (1966).
- ⁶⁴ W. Weber, Phys. Rev. B **8**, 5082 (1973).
- ⁶⁵ H. L. Brown, P. E. Armstrong, and C. P. Kempter, J. Chem. Phys. **45**, 547 (1966).
- ⁶⁶ V. A. Gubanov, A. L. Ivanovsky, and V. P. Zhukov, *Electronic Structure of Refractory Carbides and Nitrides* (Cambridge University Press, Cambridge, 1994).
- ⁶⁷ T. Amriou, B. Bouhafs, H. Aourag, B. Khelifa, S. Bresson, and C. Mathieu, Physica B **325**, 46 (2003).
- ⁶⁸ K. K. Korir, G. O. Amolo, N. W. Makau, and D. P. Joubert, Diam. Relat. Mater. **20**, 157 (2011).
- ⁶⁹ V. Zhukov, V. Gubanov, O. Jepsen, N. Christensen, and O. Andersen, J. Phys. Chem. Solids **49**, 841 (1988).
- ⁷⁰ J. O. Kim, J. D. Achenbach, P. B. Mirkarimi, M. Shinn, and S. A. Barnett, J. Appl. Phys. **72**, 1805 (1992).
- ⁷¹ J. J. Hall, Phys. Rev. **161**, 756 (1967).
- ⁷² L. J. Bruner and R. W. Keyes, Phys. Rev. Lett. **7**, 55 (1961).
- ⁷³ D. L. Price and J. M. Rowe, Solid State Commun. **7**, 1433 (1969).
- ⁷⁴ C. J. Buchenauer, M. Cardona, and F. H. Pollak, Phys. Rev. B **3**, 1243 (1971).
- ⁷⁵ R. D. Carnahan, J. Am. Ceram. Soc. **51**, 223 (1968).
- ⁷⁶ J. Tan, Y. Li, and G. Ji, Comput. Mater. Sci. **58**, 243 (2012).
- ⁷⁷ W. A. Harrison, *Electronic Structure and the Properties of Solids*, edited by Freeman (Freeman, New York, 1980).
- ⁷⁸ F. Aguado and V. G. Baonza, Phys. Rev. B **73**, 024111 (2006).
- ⁷⁹ W. Wuttling and J. Windscheif, Solid State Commun. **50**, 33 (1984).
- ⁸⁰ R. I. Cottam and G. A. Saunders, J. Phys. C: Solid State Phys. **6**, 2105 (1973).
- ⁸¹ J. G. Collins, G. K. White, J. A. Birch, and T. F. Smith, J. Phys. C: Solid State Phys. **13**, 1649 (1980).
- ⁸² C. Kittel, *Introduction to Solid State Physics*, 7th ed. (John Wiley & Sons., New York, 1996).
- ⁸³ M. W. Chase, Jr., ed., *NIST-JANAF Thermochemical Tables*, 4th ed. (AIP, New York, 1998).
- ⁸⁴ K. P. Thakur and J. D. Pandey, J. Inorg. Nucl. Chem. **37**, 645 (1975).
- ⁸⁵ R. Sanderson, *Inorganic Chemistry* (Reinhold, New York, 1967).
- ⁸⁶ F. Vines, C. Sousa, P. Liu, J. A. Rodriguez, and F. Illas, J. Chem. Phys. **122**, 174709 (2005).
- ⁸⁷ A. F. Guillermet, J. Häglund, and G. Grimvall, Phys. Rev. B **45**, 11557 (1992).
- ⁸⁸ J. Häglund, G. Grimvall, T. Jarlborg, and A. F. Guillermet, Phys. Rev. B **43**, 14400 (1991).
- ⁸⁹ A. F. Guillermet, J. Häglund, and G. Grimvall, Phys. Rev. B **48**, 11673 (1993).
- ⁹⁰ J. Paier, M. Marsman, and G. Kresse, J. Chem. Phys. **127**, 024103 (2007).
- ⁹¹ W. A. Harrison, *Electronic Structure and the Properties of Solids* (Dover, New York, 1989).
- ⁹² W. Martienssen, *Landolt-Börnstein, Numerical Data and Functional Relationships in Science and Technology-Crystal and Solid State Physics - New Series* (Springer, Berlin, 2005).
- ⁹³ H. Dumont and Y. Monteil, J. Cryst. Growth **290**, 410 (2006).
- ⁹⁴ T. Soma, J. Phys. C: Solid State Phys. **11**, 2669 (1978).
- ⁹⁵ S. Saha, S. Pal, P. Sarkar, R. A. L., and T. Frauenheim, J. Comput. Chem. **33**, 1165 (2012).