

Electron temperature estimation using the Pulse Height Analysis System at Wendelstein 7-X stellarator

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This paper presents measurements of the electron temperature in Wendelstein 7-X (W7-X) stellarator plasmas heated by electron-cyclotron-resonance (ECRH) during the first operational phase (OP1.1). The analysis of the slope of the observed X-ray continuum emission (in a semi-logarithmic plot) measured by the use of the Pulse Height Analysis (PHA) system, provides the information about the electron temperature (T_e) of the hydrogen plasma. The determination of this fundamental plasma parameter is based on the exponential dependence of the continuum radiation (Bremsstrahlung) on photon energy assuming Maxwellian distribution. In this paper, some experimental results of the estimated electron temperature are presented and compared to the results obtained from the simulations of X-ray spectrum and other diagnostic like the Thomson Scattering (TS) system.

Keywords: PHA diagnostic, electron temperature, stellarator, Wendelstein 7-X

1. Introduction

Wendelstein 7-X (W7-X) [1-2], a large optimized stellarator with superconducting coil system started its first operational phase (OP1.1) at the end of 2015. For OP1.1, the last closed flux surface (LFCS) was defined by five poloidal uncooled limiters made of graphite. The brief experimental campaign allowed the commissioning of installed diagnostic systems and W7-X components as well as the initial physics studies [3-5].

Electron temperature (T_e) as a one of the key plasma parameters, which indicate fusion performance, was routinely measured during the W7-X experiments. In the OP1.1 limiter configuration electron temperatures $T_e \leq 8$ keV have been achieved. The major tools for the T_e determination at W7-X are Thomson scattering (TS) [6] and Electron Cyclotron Emissions (ECE) [7] diagnostics. Both systems, which are capable to provide electron temperature profiles, have confirmed good agreement between their results throughout OP1.1 [8].

Measurements of T_e can be also performed by the Pulse Height Analysis (PHA) [9-12] system installed at W7-X, which primary purpose is impurity content estimation [13-14] and additionally characterization of nonthermal features of the plasma spectral emission [15]. The PHA spectra also provide information about line-integrated T_e , along the line-of-sight, as opposed to measurements from TS and ECE diagnostics. This additional use of PHA system may be helpful in confirming the results obtained by systems mainly intended to determination of this basic plasma parameter. For the investigation described in this paper, a set of data has been selected to demonstrate the system capability to measure T_e .

2. Experimental setup of the PHA system

The PHA system commissioned and tested during OP1.1 [16] was designed to provide spectra in the range from 0.7 keV up to 19 keV (for 1/e of detector response). It consists of 3 Silicon Drift Detectors (SDD) equipped with individual square pinholes and additional exchangeable Be filters of various thickness, to reduce the number of photon flux that reach the detectors. The first two detectors with a thickness of 450 μm and an active area of 10 mm^2 are equipped with an 8- μm Beryllium window, while the third one is characterized by a very thin polymer window. For the presented analysis, data in the range from 0.9 keV up to 10 keV (due to the MCA (multi-channel analyzer) settings) have been considered.

Despite the fact that similar systems are used for the measuring the soft-X ray radiations on many fusion devices, the PHA system working at W7-X stands out among the rest for several reasons. First of all, this diagnostic is characterised by satisfactory time resolution (100 ms), as well as the spatial resolution, for pinhole size 300×300 μm^2 , equal 2.5 cm. Also because of already mentioned additional filter exchanging system and energy resolution better than 200 eV, the PHA system provides an opportunity to observe light impurities (carbon (C) and oxygen (O)) what may be relevant in terms of monitoring some processes in plasma.

For $\langle T_e \rangle$ estimation described in this paper the 1st PHA channel (with additional 25 μm of Be filter) signals obtained for the trigger threshold of 1000 eV, the peaking time of 1 μs and the pinhole size of 300×300 μm^2 were

employed. This was because, during the OP1.1 only 1st PHA channel has been optimized to minimize pileup effect. In Fig.1 the line-of-sight (LOS) of detector 1 is shown. The LOS simulation, which is based on flux surface data (VIMEC) from magnetic configuration J (used during OP1.1)), shows that the mentioned detector should view almost (about 8,5 cm) through the plasma center.

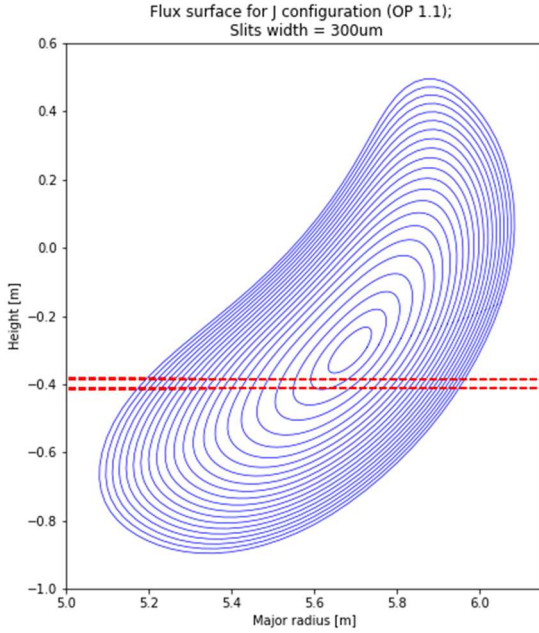


Fig. 1. Flux surfaces (blue) in the poloidal plane with the line-of-sight (red) observed by PHA Channel 1. Flux surfaces taken from VMEC calculation for W7-X program #20160309.025.

3. Determination of the electron temperature from the PHA spectra – theoretical description

The soft X-ray radiation from plasmas, is composed of free-free (Bremsstrahlung), free-bound (recombination radiation) and bound-bound (line radiation) emissions. The first two types of radiation form a continuum spectrum. The equation for hydrogenic bremsstrahlung plasma is as follows [17]:

$$\left(\frac{dP_{ff}}{dVdE}\right) ff = 3 \cdot 10^{-15} n_e \sum_i n_i Z_i^2 T_e^{-\frac{1}{2}} g_{ff} e^{\frac{-E}{k_B T_e}} \quad (1)$$

where dP_{ff} [W] is the power radiated by an impurity ion with the ion charge Z_i and ion density n_i per unit volume dV [m^3] as well as the energy interval dE [eV]. T_e [eV], n_e and E [eV] are the electron temperature, electron density and photon energy, respectively. g_{ff} is the Maxwell-averaged Gaunt factor, which is approximately equal 1 in most cases [Weller].

As in the free-bound case the radiation intensity is given by [15]:

$$\begin{aligned} \left(\frac{dP_{fb}}{dVdE}\right) fb &= 3 \cdot 10^{-15} n_e \sum_i n_i Z_i^2 T_e^{-\frac{1}{2}} g_{fb} e^{\frac{-E}{k_B T_e}} \beta \\ \beta &= \frac{\xi}{n_0^3} \frac{\chi_{Z-1}^{n_0}}{T_e} e^{\frac{-\chi_{Z-1}^{n_0}}{k_B T_e}} + \sum_{n>n_0} \frac{2}{n^3} \frac{\chi_{Z-1}^{n_0}}{T_e} e^{\frac{-Z^2 \chi_H}{n^2 k_B T_e}} \end{aligned} \quad (2)$$

Here, continuum radiation is due to the radiative recombination of ions with charge Z_i to Z_i-1 . χ_H is the ionization potential of hydrogen, χ_i is the ground state ionization potential and n is ground state principal quantum number.

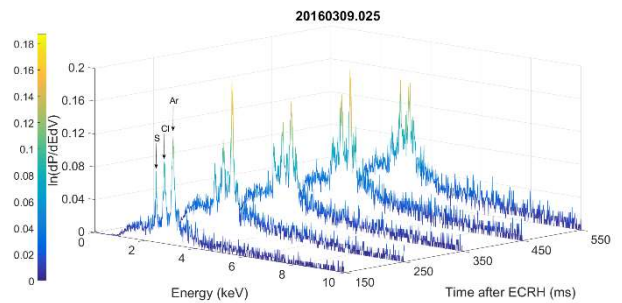
The principle of electron temperature determination from the continuum [11-12], is based on the exponential dependence describing bremsstrahlung radiation (eq.1). On the assumption that g_{ff} is independent of energy, T_e is directly calculated from the slope ($a = -\frac{1}{T_e}$) of a straight line fitted to the continuum radiation (in a semi-logarithmic plot of $dP_{ff}/dVdE$ vs Energy)

Additionally, the results obtained from experimental spectra are compared with the T_e from simulations to see if they agreed. In order to simulate the X-ray spectra (the continuum radiation in this particular case), a numerical code RayX was used. It is based on coronal equilibrium of impurities in hydrogen plasma. Moreover, in code, plasma inside cone of view of PHA diagnostic is divided into many subregions. In each subregions it is assumed that T_e and n_e are constant. In turn, the values of these specific parameters are taken from electron temperature $T_e(r)$ and density $n_e(r)$ profiles delivered by Thomson Scattering diagnostic. More detailed description of this code can be found in [18].

4. Experimental results

The results of the electron temperature estimation from PHA data presented in this section were obtained from the plasma discharge #20160309.025. This experiment featured a hydrogen plasma with argon tracer impurities for diagnostic purposes and ECRH heating at a stable level of 2 MW. The discharge duration was 700 ms.

(a)



(b)

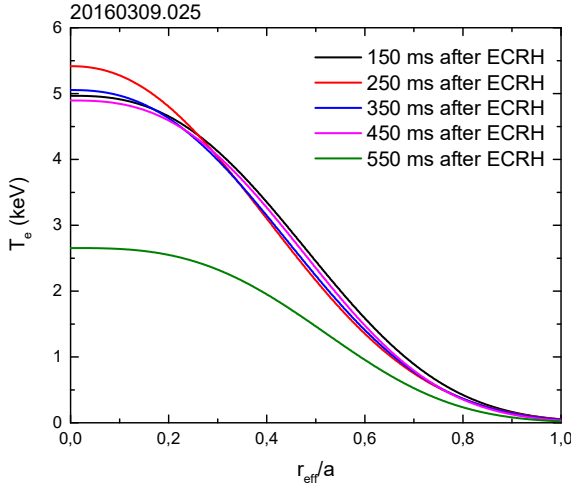


Fig.2. (a) Spectra at particular time frames for W7-X program #20160309.025 collected by PHA channel 1 and (b) corresponding $T_e(r)$ profiles provided by Thomson Scattering system

For this analysis, five time frames with PHA spectra have been used (cf. Fig 2). Each of them contains data from a 100 ms time interval. The first frame shows the data recorded 150 ms after ECRH start, while the last time frame is taken after 550 ms. In Figure 3, the spectra from the selected time frames are presented. In figure 2(b) the corresponding $T_e(r)$ profiles measured by Thomson scattering diagnostic (TS) are shown. The experimental points were fitted with the use of equation:

$$T_e(r) = T_{e0} \left[1 - \left(\frac{r}{a} \right)^m \right]^n \quad (3) \quad [12]$$

where T_{e0} is the central electron temperature, r is the effective radius, a is the minor radius, which was defined by the limiters in OP1.1 to ~ 0.49 m (in r_{eff}) and m, n are interpolation coefficients.

The choice of these particular time frames was dependent on two major factors. First, the quality of data provided by the PHA system needs to have feasible statistics (above $\sim 10\,000$ counts, negligible pile-up effects) which allows to observe clear continuum radiation. Second, the profiles of the electron temperature $T_{e(r)}$ and density $n_{e(r)}$ required for simulation should be satisfactory (physically acceptable). The procedure of estimation the electron temperature $\langle T_e \rangle$ is illustrated in Fig.3 on the example of the frame number 2 (250 ms after ECRH start).

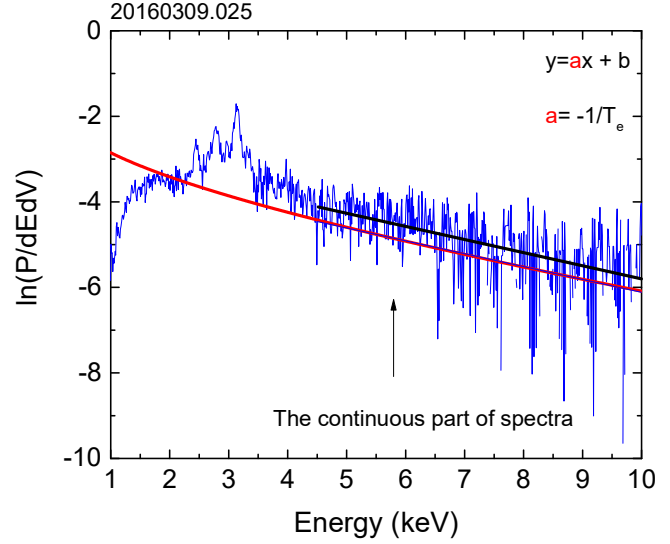


Fig. 3. Determination of the electron temperature from the slope of continuum radiation – on the basis of the PHA spectra (blue) and simulated one from RayX code (red).

In a semi-logarithmic plot of X-ray radiated power emission into energy interval and volume as a function of energy, the PHA spectrum (blue line) and simulated continuum radiation (red line) are presented. For both cases, experimental and simulated data, straight lines were fitted to the bremsstrahlung (using the method of least squares) in the energy range between 4.5 keV and 10 keV. This energy range was chosen because it is free of line radiation. For this specific frame 250 ms after ECRH start, $T_{e(r)}$ and $n_{e(r)}$ profiles (from a fit to the TS data, cf. Fig 2b) used in simulation have a central electron temperature $T_{e0} = 5.4$ keV and central electron density $n_{e0} = 1.92 \times 10^{19} \text{ 1/m}^3$ (both values are taken from Thomson measurements). As result, the average temperature estimated from the slope of the simulated continuum, is $\langle T_{e,\text{sim}} \rangle = (3.320 \pm 0.004)$ keV, while the result from the experimental PHA spectrum is $\langle T_{e,\text{exp}} \rangle = (3.22 \pm 0.22)$ keV. These values show good agreement between simulation based on TS data and PHA data analysis within the error bars. In the Tab.1, results for all five time frames of the pulse #20160309.025 are shown. The values of $\langle T_e \rangle$ estimated from both analyzes are very similar, especially for frames 2 and 3. The biggest differences between the obtained results appear, when the PHA spectra recorded a small number counts (below 10 000 counts/time frame) which leads to higher uncertainties in bremsstrahlung (frame 1). Also for frame 5, there is a discrepancy between experimental and simulation data. This is due to the fact that during OP1.1, the PHA time frames were not of equal length ($100 \text{ ms} \pm 50 \text{ ms}$, usually $\sim 105 \text{ ms}$), what led to time shifts. Both, in $\langle T_e \rangle$ from PHA spectra and simulations based on TS profiles, the errors were calculated as standard deviation of the line fitted to the Bremsstrahlung, due to the fact that the main source of errors in presented discharges is the statistics of the recorded counts.

Table 1. Comparison of the electron temperature estimated from the PHA spectra and simulations for discharge #20160309.025

Time after ECRH start (ms)	$\langle T_e \rangle$ from PHA spectra (keV)	$\langle T_e \rangle$ from simulations (keV) based on TS profiles
150 (frame1)	3.75 ± 0.72	3.180 ± 0.003
250 (frame2)	3.22 ± 0.22	3.320 ± 0.004
350 (frame3)	3.25 ± 0.24	3.230 ± 0.004
450 (frame4)	3.53 ± 0.25	3.210 ± 0.004
550 (frame5)	3.55 ± 0.22	2.050 ± 0.002

Although, the PHA system is set to observe across the plasma center, $\langle T_e \rangle$ values determined from experimental data are always lower than the central electron temperatures provided by the TS system (see $T_e(r_{\text{eff}}=0)$ in fig.2b). This could be explained by the fact that the that TS collects data directly through the plasma center, while the LOS of the 1st PHA channel system is located around 8.5 cm below the plasma center (according to VMEC equilibrium reconstructions of the flux surfaces).

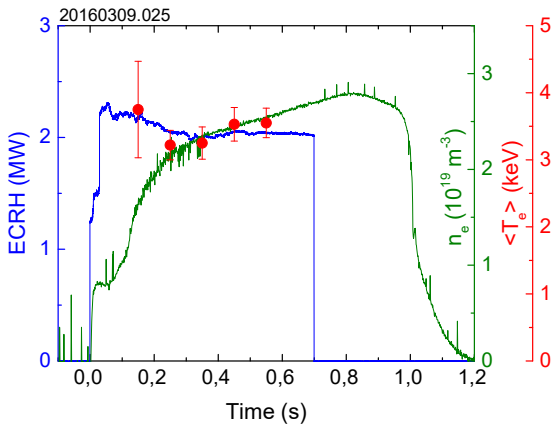


Fig. 4. The average electron temperature $\langle T_e \rangle$ estimated from the PHA spectra in comparison with ECRH heating and electron density

Moreover, on the basis of the presented pulse, $\langle T_e \rangle$ estimated from experimental spectra remains stable during the ECRH heating, which was set at an almost constant level of power (~ 2 MW during 700 ms). This typical trend is presented in Fig.4. Additionally, Fig.5 presents experimental results from PHA and TS systems including data from discharge #20160309.024 with different ECRH steps (from ~ 0.6 MW to 2 MW). In this particular case, the maximum difference between $\langle T_e \rangle$ (from PHA diagnostic) for the lowest and highest ECRH step is around 1 keV, although the heating power was increased by a factor of 4.

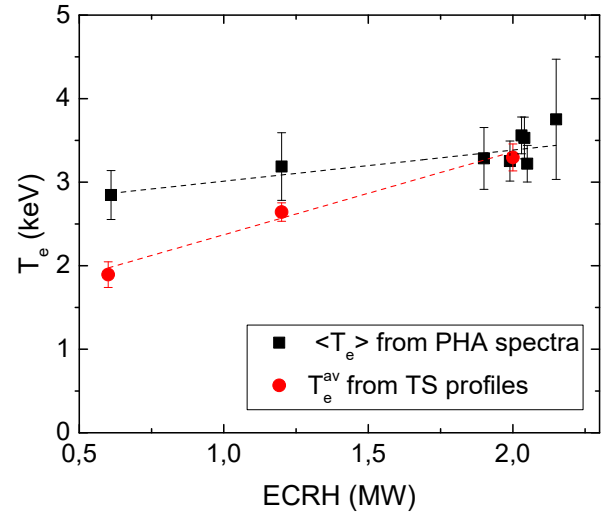


Fig. 5. The change of $\langle T_e \rangle$ with ECRH power for experimental data from discharges #20160309.024 and #20160309.035

A comparable trend was observed for the data obtained by the TS system. Here, the averaged T_e^{av} was calculated using the following formula:

$$T_a^{av} = \frac{\int_0^r T_e(r) n_e(r) dr}{\int_0^r n_e(r) dr} \quad (4).$$

The maximum difference between ECRH power extremes was $T_{e,max}^{av} = 1.4$ keV. The main discrepancy between results obtained by the PHA and TS systems, especially for the lowest value of ECRH heating, results from worst photon statistic collected by PHA system (for this particular case).

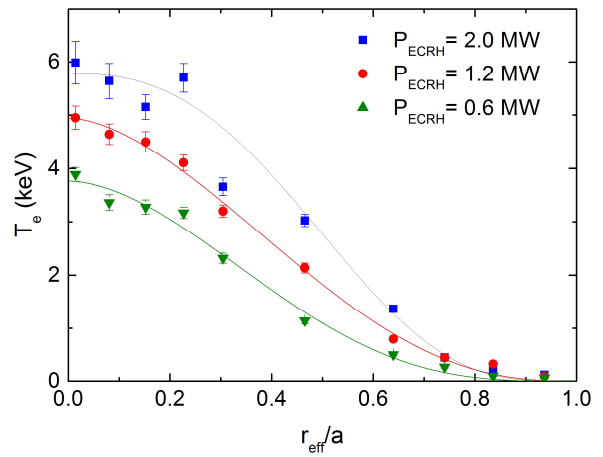


Fig. 6. $T_e(r)$ profiles based on measurements provided by Thomson Scattering system from discharge #20160309.024 with three different ECRH steps.

In Fig.6, The temperature profiles from Thomson scattering for the three ECRH steps are shown.

In order to understand the small responsiveness of the average temperature to the provided heating power, more detailed analysis of the temperature and density profiles are required, which is planned as a next step.

4. Conclusions

First experimental results obtained by the PHA system during the OP1.1, in combination with simulation one, shows that this soft X-ray diagnostic can be a helpful tool for plasma electron temperature determination as well. A correct estimation of T_e from the continuous part of the spectra was possible in the cases, where collected spectra had sufficient counting statistic. Results obtained by analysis of the experimental data were similar to those, which were derived from the simulated spectra based on Thomson Scattering profiles. Thanks to the PHA acquisition time, which is equal to 100 ms, in most cases it was possible to observe frequent changes of T_e during discharges. However, work on the quality of the data from a single time frame, for further T_e analysis is needed.

In the next experimental campaign of W7-X (OP1.2), a further optimization of the PHA system is planned. The aim is to measure spectra with higher number of counts and avoiding pile-up effects. As a result, it should be possible to determine T_e for all time frames during a typical W7-X pulse.

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