

# Constraining the $p$ -mode- $g$ -mode tidal instability with GW170817

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We analyze the impact of a proposed tidal instability coupling  $p$ -modes and  $g$ -modes within neutron stars on GW170817. This non-resonant instability transfers energy from the orbit of the



binary to internal modes of the stars, accelerating the gravitational-wave driven inspiral. We model the impact of this instability on the phasing of the gravitational wave signal using three parameters per star: an overall amplitude, a saturation frequency, and a spectral index. Incorporating these additional parameters, we compute the Bayes Factor ( $\ln B_{pg}^{pg}$ ) comparing our  $p$ - $g$  model to a standard one. We find that the observed signal is consistent with waveform models that neglect  $p$ - $g$  effects, with  $\ln B_{pg}^{pg} = 0.03^{+0.70}_{-0.58}$  (maximum a posteriori and 90% credible region). By injecting simulated signals that do not include  $p$ - $g$  effects and recovering them with the  $p$ - $g$  model, we show that there is a  $\simeq 50\%$  probability of obtaining similar  $\ln B_{pg}^{pg}$  even when  $p$ - $g$  effects are absent. We find that the  $p$ - $g$  amplitude for  $1.4 M_\odot$  neutron stars is constrained to  $\lesssim \text{few} \times 10^{-7}$ , with maxima a posteriori near  $\sim 10^{-7}$  and  $p$ - $g$  saturation frequency  $\sim 70$  Hz. This suggests that there are less than a few hundred excited modes, assuming they all saturate by wave breaking. For comparison, theoretical upper bounds suggest a  $p$ - $g$  amplitude  $\lesssim 10^{-6}$  and  $\lesssim 10^3$  modes saturating by wave breaking. Thus, the measured constraints only rule out extreme values of the  $p$ - $g$  parameters. They also imply that the instability dissipates  $\lesssim 10^{51}$  ergs over the entire inspiral, i.e., less than a few percent of the energy radiated as gravitational waves.

## I. INTRODUCTION

Detailed analysis of the gravitational-wave (GW) signal received from the first binary neutron star (NS) coalescence event (GW170817 [1]) constrains the tidal deformability of NSs and thus the equation of state (EOS) above nuclear saturation density [2–4]. Studies of NS tidal deformation typically focus on the linear, quasi-static tidal bulge induced in each NS by its companion. Such deformations modify the system’s binding energy and GW luminosity and thereby alter its orbital dynamics. The degree of deformation is often expressed in terms of the tidal deformability  $\Lambda_i \propto (R_i/m_i)^5$  of each component [5], or a particular mass-weighted average thereof ( $\bar{\Lambda}$ ) [2]. The strong dependence on compactness  $R/m$  means that a stiffer EOS, which has larger  $R$  for the same  $m$ , imprints a larger tidal signals than a softer EOS. Current analyses of GW data from the LIGO [6] and Virgo [7] detectors favor a soft EOS [3, 8]. Specifically, [2] finds  $\bar{\Lambda} \lesssim 730$  at the 90% credible level for all waveform models considered, allowing for the components to spin rapidly. The pressure at twice nuclear saturation density is also constrained to  $P = 3.5^{+2.7}_{-1.7} \times 10^{34}$  dyn/cm<sup>2</sup> (median and 90% credible region) [3] assuming small component spins. In addition to GW phasing, the EOS-dependence of  $\bar{\Lambda}$  should correlate with post-merger signals [9], possible tidal disruptions, and kilonova observations [10]. Observed light-curves for the kilonova suggest a lower bound of  $\bar{\Lambda} \gtrsim 200$  [11, 12].

Although some dynamical tidal effects are incorporated in these analyses (see, e.g., [2, 13]), the impact of several types of dynamical tidal effects are neglected because they are assumed to be small or have large theoretical uncertainties. These effects arise because tidal fields, in addition to raising a quasi-static bulge, excite stellar normal modes. Three such excitation mechanisms are (i) resonant linear excitation, (ii) resonant nonlinear excitation, and (iii) non-resonant nonlinear excitation (see,

e.g., [14]). The first occurs when the GW frequency (the oscillation frequency of the tidal field) sweeps through a mode’s natural frequency (see, e.g., [15–22]). However, since the GW frequency increases rapidly during the late inspiral, the time spent near resonance is too short to excite modes to large amplitudes. As a result, for modes with natural frequencies within the sensitive bands of ground-based GW detectors, the change in orbital phasing is expected to be small ( $\Delta\Psi \lesssim 10^{-2}$  rad) unless the stars are rapidly rotating [17–19]. The impact of resonant nonlinear mode excitation (i.e., the parametric subharmonic instability) is likewise limited by the swiftness of the inspiral [23].

The proposed  $p$ - $g$  tidal instability is a non-resonant, nonlinear instability in which the tidal bulge excites a low-frequency buoyancy-supported  $g$ -mode and a high-frequency pressure-supported  $p$ -mode [23–26]. It occurs in the inner core of the NS, where the stratification is weak and the shear due to the tidal bulge is especially susceptible to instability. Unlike resonantly excited modes, an unstable  $p$ - $g$  pair continuously drains energy from the orbit once excited, even after the orbital frequency changes significantly. There are many potentially unstable  $p$ - $g$  pairs, each becoming unstable at a different frequency and growing at a different rate. Although there is considerable uncertainty about the number of unstable pairs, their exact growth rates, and how they saturate, estimates suggest that the impact could be measurable with current detectors [27].

In this letter, we investigate the possible impact of the  $p$ - $g$  instability on GW170817 using the phenomenological model developed in [27]. The model describes the energy dissipated by the instability within each NS, indexed by  $i$ , in terms of three parameters: (i) an overall amplitude  $A_i$ , which is related to the number of modes participating in the instability, their growth rates, and their saturation energies, (ii) a frequency  $f_i$  corresponding to when the instability saturates, and (iii) a spectral index  $n_i$  describing how the saturation energy evolves with frequency. In Section II, we describe our models in detail. In Section III, we compare the statistical evidence for models that include the  $p$ - $g$  instability relative to those that do not. In Section IV, we investigate the

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constraints on the  $p$ - $g$  parameters from GW170817, and in Section V we conclude.

## II. PHENOMENOLOGICAL MODEL

Following [27], we extend a post-Newtonian (PN) waveform by including a parametrized model of the  $p$ - $g$  instability. For the initial PN model, we use the `TaylorF2` frequency-domain approximant (see, e.g., [28]) terminated at the inner-most stable circular orbit, which includes the effects of linear tides ( $\tilde{\Lambda}$ ) and spins aligned with the orbital angular momentum (the impact of misaligned spins on  $p$ - $g$  effects is not known). Waveform

$$\Delta\Psi(f) = -\frac{2C_1}{3B^2(3-n_1)(4-n_1)} \left[ \Theta_1 \left( \frac{f}{f_{\text{ref}}} \right)^{n_1-3} + (1-\Theta_1) \left( \frac{f_1}{f_{\text{ref}}} \right)^{n_1-3} \left( (4-n_1) - (3-n_1) \left( \frac{f}{f_1} \right) \right) \right] + (1 \leftrightarrow 2), \quad (1)$$

where  $f_i$  is the saturation frequency,  $f_{\text{ref}} \equiv 100$  Hz is a reference frequency with no intrinsic significance,  $C_i = [2m_i/(m_1 + m_2)]^{2/3} A_i$ ,  $B = (32/5)(GM\pi f_{\text{ref}}/c^3)^{5/3}$ ,  $\mathcal{M} = (m_1 m_2)^{3/5}/(m_1 + m_2)^{1/5}$ , and  $\Theta_i = \Theta(f - f_i)$  where  $\Theta$  is the Heaviside function. This approximant is slightly different than that of [27] because they incorrectly applied the saddle-point approximation to obtain the frequency-domain waveform from time-domain phasing [29]. This correction renders the  $p$ - $g$  instability slightly more difficult to measure than predicted in [27], although the observed behavior is qualitatively similar. Specifically, we find that in order to achieve the same  $|\Delta\Psi|$ ,  $A_i$  needs to be larger than [27] found by a factor of  $\sim (4-n_i)$ , although the precise factor also depends on the other  $p$ - $g$  parameters.

The  $\Delta\Psi$  expression contains three types of terms: a constant term, a linear term  $\propto (1-\Theta_i)f$ , and a power-law term  $\propto \Theta_i f^{n_i-3}$ . The constant term corresponds to an overall phase offset and is degenerate with the orbital phase at coalescence. The linear term corresponds to a change in the time of coalescence; because the  $p$ - $g$  instability transfers energy from the orbit to stellar normal modes, the binary inspirals faster than it would if the effect was absent. The power-law term accounts for the competition between the rate of  $p$ - $g$  energy dissipation and the rate of inspiral, both of which increase as  $f$  increases. As argued in [27], we expect  $n_i < 3$ , which implies that the phase shift accumulates primarily at frequencies just above the “turn-on” (saturation) frequency  $f \gtrsim f_i$ .

When  $n_i < 3$ ,  $p$ - $g$  effects are most important at lower frequencies whereas linear tides ( $\tilde{\Lambda}$ ) and spins ( $\chi_i = cS_i/Gm_i^2$ , where  $S_i$  is the spin-angular momentum of each component) have their largest impact at higher frequencies (see, e.g., [30]). The priors placed on the latter quantities can, however, affect our inference of  $p$ - $g$  pa-

rameters between different existing approximants may be important for small  $p$ - $g$  effects. However, by comparing the waveform mismatches between several other models (`TaylorF2`, `SEOBNRT`, `PhenomDNRT`, and `PhenomPNRT`, see [2]), we find these systematic become important for  $p$ - $g$  effects roughly an order of magnitude smaller than the upper limits set by our analysis (see Section IV). We expect `TaylorF2` to be reasonably accurate and defer a complete analysis of waveform systematics to future work.

Assuming the  $p$ - $g$  effects are a perturbation to `TaylorF2`, we find that they modify the phase in the frequency-domain by

rameters.

In order to account for a possible dependence on the component masses ( $m_i$ ), we parametrize our model using a Taylor expansion in the  $p$ - $g$  parameters around  $m_i = 1.4M_\odot$  and sample from the posterior using the first two coefficients. Our model computes  $A_i$  as

$$A_i(m_i) = A_0 + \left( \frac{dA}{dm} \Big|_{1.4M_\odot} \right) (m_i - 1.4M_\odot), \quad (2)$$

and uses  $A_0$  and  $dA/dm$  instead of  $A_1$  and  $A_2$ . The model uses similar representations for  $f_i$  and  $n_i$  in terms of the parameters  $f_0$ ,  $df/dm$ ,  $n_0$ , and  $dn/dm$ . We assume a uniform prior on  $\log_{10} A_0$  within  $10^{-10} \leq A_0 \leq 10^{-5.5}$ , a uniform prior in  $f_0$  within  $10 \text{ Hz} \leq f_0 \leq 100 \text{ Hz}$ , and a uniform prior in  $n_0$  within  $-1 \leq n_0 \leq 3$ . The priors on the first-order terms ( $dA/dm$ ,  $df/dm$ ,  $dn/dm$ ) are the same as those in [27]; when  $m_1 \sim m_2$ , they imply  $A_1 \sim A_2$ , etc.

We investigate GW170817 using data from several different frequency bands and with different spin priors, but unless otherwise noted we focus on results for data above 30 Hz with  $|\chi_i| \leq 0.89$ . Throughout this letter, results from GW170817 were obtained using the same data conditioning as [2], including the removal of a short-duration noise artifact from the Livingston data ([31] and discussion in [1]) along with other independently measured noise sources (see, e.g., [32–35]), calibration [36, 37], marginalization over calibration uncertainties, and whitening procedures [38, 39].

## III. MODEL SELECTION

Using GW data from GW170817, we perform Bayesian model selection. We compare a model that includes lin-



ear tides, spin components aligned with the orbital angular momentum, and PN phasing effects up to 3.5 PN phase terms ( $\mathcal{H}_{lpg}$ ) to an extension of this model that also includes  $p$ - $g$  effects ( $\mathcal{H}_{pg}$ ). Since we have nested models ( $\mathcal{H}_{lpg}$  is obtained from  $\mathcal{H}_{pg}$  as  $A_i \rightarrow 0$ )<sup>1</sup>, we use

$$\begin{aligned} \lim_{A_i \rightarrow 0} \left[ \frac{p(A_i|D, \mathcal{H}_{pg})}{p(A_i|\mathcal{H}_{pg})} \right] &= \lim_{A_i \rightarrow 0} \left[ \frac{1}{p(D|\mathcal{H}_{pg})} \int d\theta df_i dn_i p(D|\theta, A_i, f_i, n_i; \mathcal{H}_{pg}) p(\theta|\mathcal{H}_{pg}) p(f_i, n_i|A_i, \mathcal{H}_{pg}) \right] \\ &= \frac{1}{p(D|\mathcal{H}_{pg})} \int d\theta p(D|\theta; \mathcal{H}_{lpg}) p(\theta|\mathcal{H}_{lpg}) \left[ \frac{p(\theta|\mathcal{H}_{pg})}{p(\theta|\mathcal{H}_{lpg})} \right] \int df_i dn_i p(f_i, n_i|A_i, \mathcal{H}_{pg}) \\ &= \frac{p(D|\mathcal{H}_{lpg})}{p(D|\mathcal{H}_{pg})} \left\langle \frac{p(\theta|\mathcal{H}_{pg})}{p(\theta|\mathcal{H}_{lpg})} \right\rangle_{p(\theta|D, \mathcal{H}_{lpg})}, \end{aligned} \quad (3)$$

where  $\theta$  refers to all parameters besides the  $p$ - $g$  phenomenological parameters, we note that  $\int df_i dn_i p(f_i, n_i|A_i, \mathcal{H}_{pg}) = 1 \forall A_i$ , and  $\langle x \rangle_p$  denotes the average of  $x$  with respect to the measure defined by  $p$ . Assuming that  $p(\theta|\mathcal{H}_{pg}) = p(\theta|\mathcal{H}_{lpg})$ , we determine  $\ln B_{lpg}^{pg}$  from the ratio, as  $A_i \rightarrow 0$ , of the marginal distribution of  $A_i$  *a priori* to the distribution *a posteriori*

$$\ln B_{lpg}^{pg} = \lim_{A_i \rightarrow 0} [\ln p(A_i|\mathcal{H}_{pg}) - \ln p(A_i|D, \mathcal{H}_{pg})]. \quad (4)$$

We confirmed that this estimate agrees with estimates from both nested sampling [44] and thermodynamic integration [45].

Figure 1 shows  $\ln B_{lpg}^{pg}$  as a function of  $f_{low}$ , the minimum GW frequency considered. At a given  $f_{low}$ , we show the distribution of  $\ln B_{lpg}^{pg}$  due to the sampling uncertainty from the finite length of our MCMC chains. The solid and dashed curves correspond to the high-spin ( $|\chi_i| \leq 0.89$ ) and low-spin ( $|\chi_i| \leq 0.05$ ) priors discussed in [1–3].

For certain combinations of  $f_{low}$  and  $|\chi_i|$ , we find  $\ln B_{lpg}^{pg} > 0$ , suggesting  $\mathcal{H}_{pg}$  is more likely than  $\mathcal{H}_{lpg}$ . In order to assess how likely such values are, we calculate  $\ln B_{lpg}^{pg}$  for a large number of simulated, high-spin signals with  $A_i = 0$  and distinct realizations of detector noise from times near GW170817. We find that simulated signals without  $p$ - $g$  effects can readily produce  $\ln B_{lpg}^{pg}$  at least as large as the ones we measured from GW170817. In particular,  $\ln B_{lpg}^{pg}$  for the 30 Hz, high-spin data corresponds to a False Alarm Probability (FAP)  $\approx 50\%$ . We focus on the 30 Hz, high-spin data because it corresponds to the largest bandwidth investigated and the largest signal-to-noise ratio. The high-spin prior is the most inclusive prior considered, and therefore allows the most model freedom when fitting  $p$ - $g$  effects.

the Savage-Dickey Density Ratio (see, e.g., [40–42]) to estimate the Bayes Factor ( $B_{lpg}^{pg} = p(D|\mathcal{H}_{pg})/p(D|\mathcal{H}_{lpg})$ , where  $D$  refers to the observed data). Specifically, we sample from the model's posterior distribution [43] and calculate

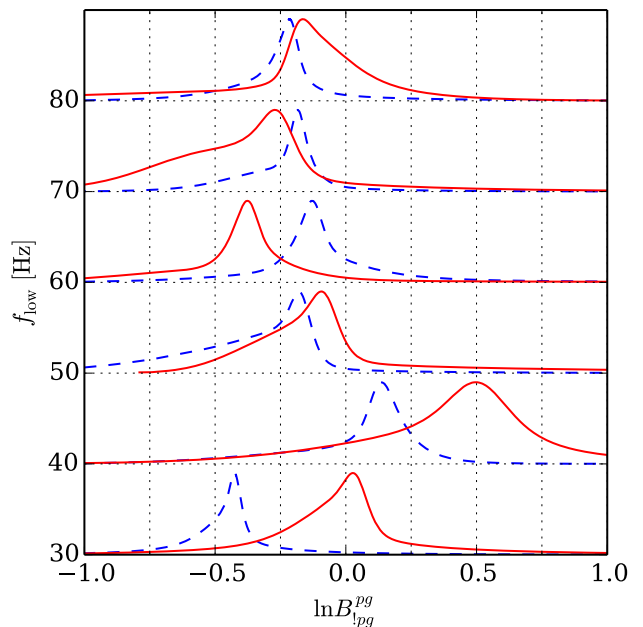


FIG. 1. Distributions of  $\ln B_{lpg}^{pg}$  due to sampling uncertainty for different values of  $f_{low}$ . The solid red curves assume high-spin priors ( $|\chi_i| \leq 0.89$ ) and the dashed blue curves assume low-spin priors ( $|\chi_i| \leq 0.05$ ).

In our model of the instability, the phase shift  $\Delta\Psi$  accumulates primarily at frequencies just above the saturation frequency  $f \gtrsim f_i$ . Therefore, if it is present, its impact should become more apparent as we decrease the minimum GW frequency considered from  $f_{low} \gg f_i$  to  $f_{low} \lesssim f_i$ . We do see some indication of this behavior in Fig. 1. However, we note that if our phenomenological model breaks down at  $f < f_i$  due to poor modeling of the pre-saturation behavior (e.g., if our step-function

<sup>1</sup> Since we use a uniform-in- $\log_{10} A_0$  prior,  $\mathcal{H}_{pg}$  does not formally include  $A_i = 0$ . Nonetheless, our lower limit on  $A_i$  is sufficiently small that  $\mathcal{H}_{lpg}$  is effectively nested in  $\mathcal{H}_{pg}$ .

turn-on at  $f_i$  is not a good approximation to the instability's induced phase shift), we might expect  $\ln B_{pg}^{pg}$  to decrease as we lower  $f_{\text{low}}$  below  $f_i$ .

#### IV. PARAMETER INFERENCE

We now investigate the constraints obtained from GW170817. Figure 2 shows the joint posterior distributions for both  $\mathcal{H}_{pg}$  and  $\mathcal{H}_{lpg}$ . We find that  $\mathcal{H}_{pg}$  and  $\mathcal{H}_{lpg}$  yield similar posterior distributions for all non- $p$ - $g$  parameters, including both extrinsic and intrinsic parameters. The constraints on the chirp mass ( $\mathcal{M}$ ), effective spin  $\chi_{\text{eff}} = (m_1\chi_1 + m_2\chi_2)/(m_1 + m_2)$ , and  $\tilde{\Lambda}$  are slightly weaker in  $\mathcal{H}_{pg}$  than  $\mathcal{H}_{lpg}$ . This is because  $\mathcal{H}_{pg}$  provides extra freedom to the signal's duration in the time-domain.

Regarding the  $p$ - $g$  parameters, we find a noticeable peak near  $A_0 \sim 10^{-7}$  with a flat tail to small  $A_0$ . We find  $A_0 \leq 3.3 \times 10^{-7}$  assuming a uniform-in- $\log_{10} A_0$  prior and  $A_0 \leq 6.8 \times 10^{-7}$  assuming a uniform-in- $A_0$  prior, both at 90% confidence.<sup>2</sup> We also find a peak at  $f_0 \sim 70$  Hz. The peaks persist when we analyze the data from each interferometer separately, with reasonably consistent locations and shapes (Fig. 2). However, we find that the simulated signals with  $A_i = 0$  can produce similar peaks, suggesting they may be due to noise alone. Similar to [27], we find that  $n_i$  is not strongly constrained and the gradient terms in the Taylor expansions are not measurable.

Theoretical arguments suggest an upper bound of  $A_0 \lesssim 10^{-6}$  [27]. Therefore, our  $A_0$  constraint only rules out the most extreme values of the  $p$ - $g$  parameters.

#### V. DISCUSSION

While GW170817 is consistent with models that neglect  $p$ - $g$  effects, it is also consistent with a broad range of  $p$ - $g$  parameters. The constraints from GW170817 imply that there are  $\lesssim 200$  excited modes at  $f = 100$  Hz, assuming all modes grow as rapidly as possible and saturate at their breaking amplitudes ( $\lambda = \beta = 1$  in Eq. (7) of [27]) and that the frequency at which modes become unstable is well approximated by  $f_0$ . For comparison, theoretical arguments suggest an upper bound of  $\sim 10^3$  modes saturating by wave breaking [27]. More modes may be excited if they grow more slowly or saturate below their wave breaking energy.

We can also use the measured constraints to place upper limits on the amount of energy dissipated by the  $p$ - $g$  instability. As Fig. 3 shows,  $p$ - $g$  effects dissipate

$\lesssim 2.7 \times 10^{51}$  ergs throughout the entire inspiral at 90% confidence. In comparison, GWs carry away  $\gtrsim 10^{53}$  ergs. This implies time-domain phase shifts  $|\Delta\phi| \lesssim 7.6$  rad (0.6 orbits) at 100 Hz and  $|\Delta\phi| \lesssim 32$  rad (2.6 orbits) at 1000 Hz after accounting for the joint uncertainty in component masses, spins, linear tides, and  $p$ - $g$  effects.

A  $g$ -mode with natural frequency  $f_g$  is predicted to become unstable at a frequency  $f_{\text{crit}} \simeq 45 \text{ Hz} (f_g/10^{-4} \lambda f_{\text{dyn}})^{1/2}$ , where  $f_{\text{dyn}}$  is the dynamical frequency of the NS and  $\lambda$  is a slowly varying function typically between 0.1 – 1 [25, 27]. Since the modes grow quickly, the frequency at which the instability saturates is likely close to the frequency at which the modes become unstable ( $f_0 \simeq f_{\text{crit}}$ ). If we assume that the observed peak near  $f_0 \sim 70$  Hz is not due to noise alone, then the maximum a posteriori estimate for  $f_0$  along with approximate values for the masses ( $1.4 M_{\odot}$ ) and radii (11 km) of the components [3] imply  $f_g \simeq 0.5$  Hz.

With several more signals comparable to GW170817, it should be possible to improve the amplitude constraint to  $A_0 \lesssim 10^{-7}$ . Obtaining even tighter constraints will likely require many more detections, especially since most events will have smaller SNR. Future measurements will also benefit from a better understanding of how the instability saturates. To date, there have only been detailed theoretical studies of the instability's threshold and growth rate [23–26], not its saturation. As a result, we cannot be certain of the fidelity of our phenomenological model.

While this letter was in final internal review, related work was posted [46] with, in particular, the conclusion that the  $\mathcal{H}_{lpg}$  model is strongly favored over the  $\mathcal{H}_{pg}$  model by a factor of at least  $10^4$ . We are investigating possible reasons for the differences between our conclusions.

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<sup>2</sup> The upper limit with a uniform-in- $A_0$  prior is larger only because we weight larger values of  $A_0$  more *a priori* than with a uniform-in- $\log_{10} A_0$  prior.

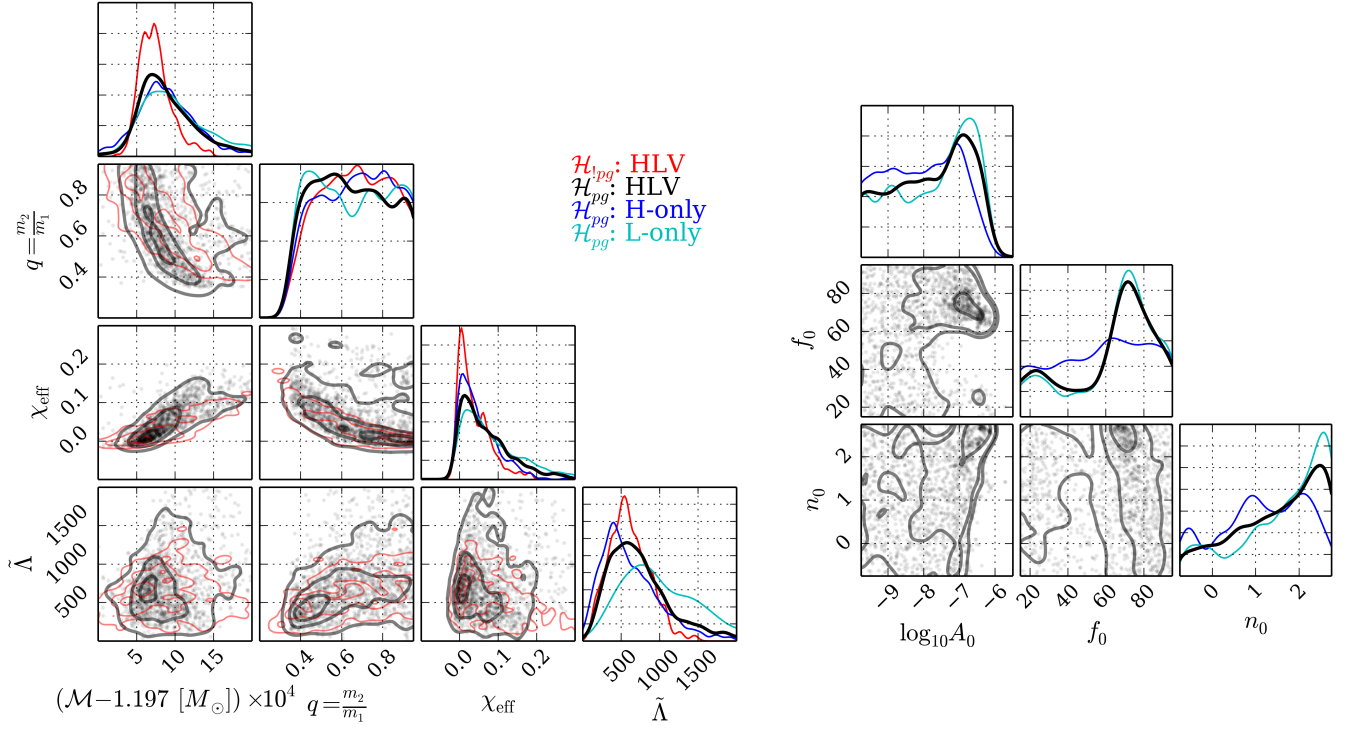


FIG. 2. Posterior distributions for  $\mathcal{H}_{lpg}$  (red) and  $\mathcal{H}_{pg}$  with Hanford, Livingston, and Virgo data (thick black, grey shading), Hanford data only (dark blue), and Livingston data only (light blue) using GW data above 30 Hz,  $|\chi_i| \leq 0.89$ , and a uniform-in- $\log_{10} A_0$  prior. *Left*: a subset of parameters shared by  $\mathcal{H}_{lpg}$  and  $\mathcal{H}_{pg}$ . *Right*: a subset of parameters belonging only to  $\mathcal{H}_{pg}$ . We only show one-dimensional posteriors for the single instrument data, although the multi-dimensional posteriors are similarly consistent with the full  $\mathcal{H}_{pg}$  data. Contours in the two-dimensional distributions represent 10%, 50%, and 90% confidence regions for the  $\mathcal{H}_{pg}$  and  $\mathcal{H}_{lpg}$  models, respectively.

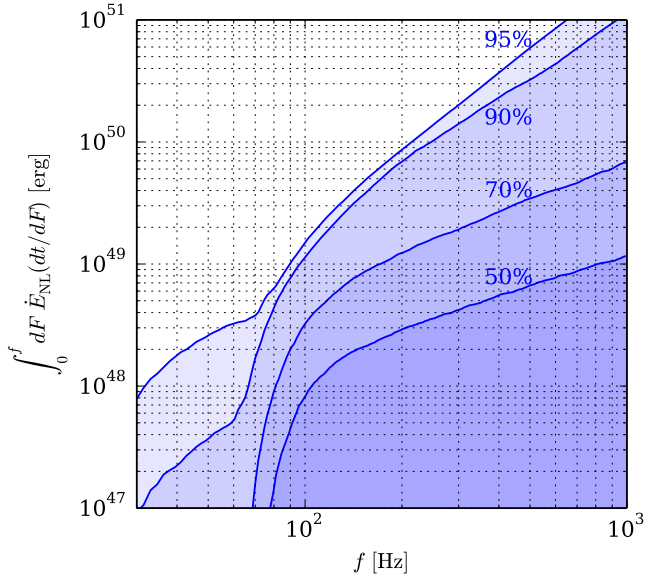


FIG. 3. Upper limits on the cumulative energy dissipated by the  $p$ - $g$  instability as a function of frequency. We note the relatively strong constraints at lower frequencies, where  $p$ - $g$  effects are more pronounced.

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