## **Phonon Decoherence of Quantum Dots in Photonic Structures:** Broadening of the Zero-Phonon Line and the Role of Dimensionality

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We develop a general microscopic theory describing the phonon decoherence of quantum dots and indistinguishability of the emitted photons in photonic structures. The coherence is found to depend fundamentally on the dimensionality of the structure resulting in vastly different performance for quantum dots embedded in a nanocavity (0D), waveguide (1D), slab (2D), or bulk medium (3D). In bulk, we find a striking temperature dependence of the dephasing rate scaling as  $T^{11}$  implying that phonons are effectively "frozen out" for  $T \lesssim 4$  K. The phonon density of states is strongly modified in 1D and 2D structures leading to a linear temperature scaling for the dephasing strength. The resulting impact on the photon indistinguishability can be important even at sub-Kelvin temperatures. Our findings provide a comprehensive understanding of the fundamental limits to photon indistinguishability in photonic structures.

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Disentangling a quantum system from its fluctuating environment is pivotal to the realization of coherent quantum bits. Controlling the sources of noise is particularly challenging in solid-state systems, which contain a myriad of mutually interacting quasiparticles. An example is semiconductor quantum dots (QDs), which have proven to be excellent quantum light sources [1]. Two important decoherence mechanisms of QDs are the fluctuating electrostatic [2,3] and spin [2,4,5] environments, but these can be neutralized under appropriate external control [6-9]. The electrostatic noise is particularly significant in engineered structures [10], but recent experiments have demonstrated how to efficiently suppress it [11,12]. The decoherence is then dominated by phonons, the acoustic vibrations of the crystal lattice [13–17]. Integrating the QDs into photonic devices is essential for obtaining deterministic and scalable light-matter interfaces [18-20]. Such photonic structures also contain a modified phononic environment due to the breakdown of translational symmetry. A unified description of how the modified phonon environment affects the coherence of ODs is lacking despite its vital importance for solid-state quantum optics [1]. Previous founding work concentrated on QDs in bulk media [14,15], generic models for 1D and 3D phonon baths [21], or the special case of linear phonon coupling in nanowires [22] and carbon nanotubes [23].

Here we present a general microscopic theory describing the influence of phonons on the coherence of QDs and the indistinguishability of the emitted photons in photonic (nano)structures. The model is applied to the four experimentally relevant systems of an In(Ga)As QD in a cavity, waveguide, slab, or bulk medium corresponding to different geometric dimensionality from 0D to 3D, see Fig. 1(d). The interaction with light is treated phenomenologically as a Markovian decay channel, which is the most abundant situation for applications such as coherent single-photon sources. The interplay between coherence and efficiency in the opposite limit of bulk phonons and non-Markovian light-matter interaction was recently explored in Ref. [24].

The impact of phonons on the photon emission from ODs can be seen clearly in the emission spectrum [13-17,22,25-35], which features broad sidebands superimposed on a narrow zero-phonon line (ZPL), cf. Fig. 1(a). The sidebands originate from rapid phonon emission or absorption on a picosecond time scale, see Fig. 1(c), while the ZPL arises from the long-time decay of coherence over nanosecond time scales. Because of the large spectral mismatch between the two processes, the incoherent sidebands can readily be filtered while maintaining a high efficiency of the photon source [7,24,36]. The fundamental limit to photon indistinguishability is therefore the interaction between the QD and phonons over long timescales, which is the main focus of the present Letter.

In a bulk medium, the broadening of the ZPL is described by an exciton-phonon coupling that is quadratic in phonon displacement [14], cf. Fig. 1(b). Here we obtain a simple expression for the dephasing rate,  $\Gamma_{3D}$ ,

$$\Gamma_{\rm 3D} = 3\pi \frac{v_s}{L} C_Q^2 \int_0^\infty d(qL) (qL)^{10} e^{-(qL)^2} N_q (N_q + 1), \qquad (1)$$

where  $C_0$  is a dimensionless constant defined later, L the radius of the QD wave function,  $v_s$  the speed of sound, and



FIG. 1. Phonon dephasing of spontaneous emission from QDs. (a) The emission spectrum consists of a ZPL and broad sidebands. (b) The quadratic coupling represents scattering of phonons through virtual excitations to a higher state and leads to ZPL broadening. (c) The linear coupling is associated with the emission or absorption of phonons by the QD. In bulk this leads to phonon sidebands in the emission. In nanostructures, an additional mechanism broadens the ZPL through long-wavelength deformations. (d) Error in two-photon interference versus temperature for QDs embedded in structures with different dimensionality. 0D corresponds to a QD in the center of a sphere with radius R = 80 nm, 1D to a cylindrical waveguide with radius  $\rho =$ 80 nm and the OD placed in the cross-sectional center (1D) or halfway off center (1D'), 2D to a QD in the center of a freestanding membrane with height 2h = 160 nm, and 3D to a bulk medium. Each structure is represented by two curves that correspond to a large (L = 4.5 nm) and small (L = 1.5 nm) wave function denoted with large and small triangles, respectively.

*q* and  $N_q$  the phonon wave number and occupation number, respectively. Remarkably, when the thermal wavelength is larger than the QD size,  $\lambda_{th} > L$ , corresponding to a temperature below a critical temperature  $T_c = \hbar v_s / k_B L$ , the phonons freeze leading to a rapid drop of the dephasing rate, cf. Fig. 1(d). This yields  $\Gamma_{3D}(T < T_c) \simeq 3\pi (v_s/L) \times$  $10! \times C_Q^2 (T/T_c)^{11}$  leading to highly coherent processes at  $T \lesssim 4$  K for realistic QD sizes. Nanostructures on the other hand are finite and can thus expand freely, resulting in longwavelength vibrations that broaden the ZPL already within the linear exciton-phonon coupling; see Fig. 1(c). The latter competes with the quadratic coupling to yield a nontrivial temperature dependence of the photon indistinguishability; cf. Fig. 1(d). We find that these processes severely limit the coherence in 1D and 2D nanostructures.

To derive the results we generalize the formalism developed in Ref. [14] and consider arbitrary structures with the electron-phonon Hamiltonian

$$H = \hbar \omega_{01} |1\rangle \langle 1| + \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} a_{\mathbf{q}}^{\dagger} a_{\mathbf{q}} + V |1\rangle \langle 1|, \qquad (2)$$

where  $|1\rangle$  is the QD excited state,  $a_{\mathbf{q}}^{\dagger}$  ( $a_{\mathbf{q}}$ ) the creation (annihilation) operator for the phonon mode with momentum  $\mathbf{q}$  and energy  $\hbar\omega_{\mathbf{q}}$ , and  $\hbar\omega_{01}$  is the QD transition energy, cf. Fig. 1(b). We assume low temperatures such that the QD excited states are not populated. The interaction term,  $V = V_L + V_Q$ , comprises a linear and a quadratic term in phonon displacement

$$V_L = \sum_{\mathbf{q}} L_{\mathbf{q}} A_{\mathbf{q}}, \qquad V_Q = \sum_{b,m} \left( \sum_{\mathbf{q}} Q_{\mathbf{q}b}^m A_{\mathbf{q}} \right)^2,$$
$$L_{\mathbf{q}} = M_{\mathbf{q}e}^{11} - M_{\mathbf{q}h}^{11}, \qquad Q_{\mathbf{q}b}^m = \frac{M_{\mathbf{q}b}^{1m}}{\sqrt{\Delta_m}}, \tag{3}$$

where  $A_{\mathbf{q}} = a_{\mathbf{q}} + a_{\mathbf{q}}^{\dagger}$ ,  $b = \{e, h\}$  denotes electron or hole,  $M_{\mathbf{q}b}^{mn}$  is the electron-phonon matrix element, and  $\Delta_m$  is the energy distance between the ground,  $|1\rangle$ , and *m*th state of the QD with  $m \ge 2$ . Time-reversal symmetry implies that all quantities can be chosen real. The interaction with phonons is dominated by the deformation-potential coupling [36,45]

$$M_{\mathbf{q}b}^{mn} = D_b \langle \boldsymbol{\psi}_b^m | \nabla \cdot \mathbf{u}_{\mathbf{q}} | \boldsymbol{\psi}_b^n \rangle, \tag{4}$$

where  $D_b$  is the deformation-potential constant,  $\psi_b^m$  the wave function of the *m*th state, and  $\mathbf{u}_{\mathbf{q}}$  the phonon displacement.

After excitation at t = 0, the QD coherence is described by the correlation function P(t) = $\langle \sigma^{-}(t)\sigma^{+}(0)\rangle = \langle T e^{-(i/\hbar)\int_{0}^{t} d\tau \tilde{V}(\tau)}\rangle$  [14,46], where T is the time-ordering operator, and  $\tilde{V}$  the potential in the interaction picture with respect to the free phonon Hamiltonian. P(t) can be evaluated numerically exact using the cumulant expansion [14,47], but we follow a simplified approach that captures the essential physics. We find that the QD-phonon interaction is weak, such that retaining the first two terms in the cumulant expansion is sufficient. The distribution, therefore, becomes Gaussian and is completely specified by the mean and standard deviation of the noise  $F(t) = -(i/\hbar) \int_0^t d\tau \tilde{V}(\tau)$ . The truncation is thus equivalent to treating the phonon bath as a Gaussian noise source, which yields  $P(t) \simeq$  $\exp(-i\mu_F)\exp\left[-\frac{1}{2}(\langle \mathcal{T}F^2(t)\rangle - \mu_F^2)\right]$ , where  $\mu_F = \langle F(t)\rangle$ . In Ref. [36] we show that this provides an excellent approximation to the exact numerical result. Inserting Eq. (3) into the above expression yields

$$P(t) = \exp\left[-i\mu_F + K_L(t) + K_Q(t)\right],$$

$$K_L(t) = -\frac{i}{2\hbar} \sum_{\mathbf{q}} |L_{\mathbf{q}}|^2 \iint_0^t dt dt' D_{\mathbf{q}}(t-t'),$$

$$K_Q(t) = \sum_{bmn} \iint_0^t dt dt' \left[\sum_{\mathbf{q}} Q_{\mathbf{q}b}^m Q_{\mathbf{q}b}^n D_{\mathbf{q}}(t-t')\right]^2, \quad (5)$$

where  $D_{\mathbf{q}}(t) = (-i/\hbar)[(N_{\mathbf{q}} + 1)e^{-i\omega_{\mathbf{q}}|t|} + N_{\mathbf{q}}e^{i\omega_{\mathbf{q}}|t|}]$  is the phonon Green function. The function  $K_L(t)$  stems from the linear electron-phonon interaction and is determined by a matrix element of the form  $M_{\mathbf{q}b}^{11} \propto \langle \psi_b^1 | \nabla \cdot \mathbf{u}_{\mathbf{q}} | \psi_b^1 \rangle$ , which shares the symmetry of the ground-state wave function, implying that  $K_L(t)$  couples to symmetric acoustic deformations, cf. Fig. 1(c). On the other hand,  $K_Q(t)$  is mediated by phonons that share the symmetry of the excited states.

In a bulk medium, the linear interaction  $K_L(t)$  does not contribute to the long-time decay of coherence; see Fig. 2(a). The quadratic coherence function  $P_O(t) =$  $\exp[K_O(t)]$  is evaluated for a spherical QD with Gaussian envelopes of radius L. Since  $K_O(t)$  is proportional to  $\Delta_m^{-2}$ , the inclusion of the first triply degenerate excited state, m = n = 2, gives the dominant contribution. Evaluating  $P_O(t)$  numerically yields a Markovian decay over long time scales, cf. Fig. 2(a), with  $\text{Re}[K_Q(t)] =$  $-\Gamma_{3D}t$ , and Im $[K_O(t)]$  contributes to a spectral shift. The dephasing rate can be calculated analytically by performing the time integration in Eq. (5) and using the long-time limit  $\omega_{\mathbf{q}}^{-2} \sin^2 \omega_{\mathbf{q}} t \simeq \pi t \delta(\omega_{\mathbf{q}})$ . This leads to Eq. (1) with  $C_O = (D_e^2/\Delta_e + D_h^2/\Delta_h)/3(2\pi)^2\rho_m v_s^2 L^3$ . This is plotted in Fig. 2(b) for GaAs parameters:  $v_s = 4780 \text{ ms}^{-1}$ , mass density  $\rho_m = 5.37 \text{ g cm}^{-3}$ ,  $D_e = -14.6 \text{ eV}$ , and  $D_h = -4.8 \,\mathrm{eV}$ . The energy distance to the excited states is taken to be  $\Delta_e = 2\Delta_h = 40 \text{ meV} \times L_0/L$  with



FIG. 2. Phonon dephasing in a bulk medium. (a) The linear (quadratic) exciton-phonon coupling affects the short-time (long-time) decay of coherence. Parameters: T = 10 K, L = 3 nm. (b) Phonon dephasing rate versus temperature for L = 1.5 nm (dashed line), L = 3 nm (solid line) and L = 4.5 nm (dotted line). The natural linewidth in a bulk medium is indicated by the dash-dotted line.

 $L_0 = 3$  nm, in accordance with theoretical estimates and experimental results [48–54]. This choice of parameters is justified in Ref. [36].

To relate the phonon decoherence to the quality of the photons emitted by the QD, we study a Hong-Ou-Mandel setup [55]. Here, the second-order correlation function determines the two-photon indistinguishability (TPI), which ranges from 0 (no indistinguishability) to 1 (perfect indistinguishability). If (i) the QD-light interaction is Markovian, (ii) the excitation happens instantaneously, (iii) the QD is a perfectly antibunched source of single photons, and (iv) the noise is stationary, the TPI is [56]

$$\text{TPI} = \Gamma_{\text{rad}} \int_0^\infty d\tau e^{-\Gamma_{\text{rad}}\tau} |P(\tau)|^2.$$
 (6)

In bulk,  $|P(t)| \simeq \exp(-\Gamma_{3D}t)$  leading to TPI =  $\Gamma_{rad}/(\Gamma_{rad} + 2\Gamma_{3D})$  after filtering out the sidebands, where  $\Gamma_{rad} \simeq 2\pi \times 160$  MHz is the radiative decay rate of the QD [57]. The resulting temperature dependence of the TPI is plotted in Fig. 1(d). Near-unity indistinguishabilities can be achieved at temperatures below a few Kelvin. Analytic solutions can also be found at high temperatures,  $\Gamma_{3D}(T > T_c) \simeq 3\pi^{3/2} \times (105/32)(v_s/L) \times C_Q^2(T/T_c)^2$ , with a quadratic temperature dependence.

In the following we study phonon decoherence in nanostructures [19,20,58,59]. The short-time dynamics results in phonon sidebands that are shaped by the density of states, but this modification is not significant for the sizes considered here [36]. The long-time dynamics can be split into two contributions,  $P_{ZPL}(t) = P_Q(t)P_{L0}(t)$ , where  $P_Q(t)$  stems from the quadratic coupling, and  $P_{L0}(t)$  is a nanostructure-specific low-frequency contribution to the linear coupling [21,22]. For simplicity we keep a fixed bulklike radiative decay rate throughout this work. In a realistic device this value may differ, in which case the results should be modified accordingly.

We start with a 0D nanosphere cavity, which resembles the geometry of colloidal QDs embedded in spherical shells [60]. The long-time coherence is plotted in Fig. 3(a) and stems solely from the quadratic coupling  $P_Q(t)$ . The decay is strongly non-Markovian because the phonons are reflected at the boundary and interact with the QD periodically; see the inset of Fig. 3(a). A simple expression for Re[ $K_Q(t)$ ] can be derived from Eq. (5) by using the long-time form  $\sin^2[(\omega_j - \omega_{j'})t]/(\omega_j - \omega_{j'})^2 \simeq t^2 \delta_{jj'}$ , where *j* is the index of the confined acoustic mode. This results in  $P_{\text{ZPL}}(t) = \exp(-S^2t^2)$  with

$$S^{2} = \frac{3}{2} \left( \frac{\pi}{2} \frac{v_{s}}{L} C_{Q} \right)^{2} \sum_{j} I_{j}^{4} \tilde{q}_{j}^{12} e^{-\tilde{q}_{j}^{2}} N_{\tilde{q}_{j}} (N_{\tilde{q}_{j}} + 1), \quad (7)$$

where  $\tilde{q}_j \equiv q_j L$ , and  $I_j$  is a dimensionless normalization factor of the (j, 1, 0) spheroidal mode [36,61]. The resulting



FIG. 3. Phonon dephasing in photonic structures and the role of dimensionality. (a) Decay of coherence for the same structures as in Fig. 1(d) except the 0D structure (R = 20 nm). Inset: initial decay of coherence (0–20 ps) for bulk (dotted line), sphere (solid line), and the  $t^2$  approximation for the sphere. (b) Corresponding emission spectrum. (c) Two-photon indistinguishability versus size of the structure. All plots are for T = 5 K, L = 3 nm.

emission spectrum without the radiative broadening,  $S(\omega) = \text{Re } \int_0^\infty dt P_{\text{ZPL}}(t) \exp(-i\omega t)$ , is Gaussian as depicted in Fig. 3(b). The TPI yields  $\text{TPI}_{0\text{D}} = \sqrt{\pi}r_s \exp(r_s^2) \operatorname{erfc}(r_s)$ , where  $r_s = \Gamma_{\text{rad}}/2\sqrt{2}S$ , and is plotted in Fig. 1(d). In general, the decoherence is stronger than in bulk. However, in the small temperature limit  $\lambda_{\text{th}} \gg R$ , the thermal energy is smaller than the lowest vibrational state of the sphere leading to negligible decoherence,  $1 - \text{TPI}_{0\text{D}} \propto \exp(-\hbar\omega/2k_BT)$ , as depicted in Fig. 1(d).

In the following, we discuss the dephasing of QDs embedded in 1D and 2D structures [20,62,63]. The quadratic interaction does not deviate significantly from bulk because  $K_O(t)$  is dominated by phonons with a wavelength comparable to the QD size while realistic photonic structures are much larger and do not affect those phonon modes. We therefore assume  $K_Q^{1D} \simeq K_Q^{2D} \simeq -\Gamma_{3D} t$ [36]. This is different for the linear interaction  $P_{1,0}$  [22,23]. For a freestanding 1D waveguide two families of acoustic modes contribute to dephasing with a finite  $\nabla \cdot \mathbf{u}$ : longitudinal expansions of the rod with a linear dispersion and thus a constant density of states at  $\omega \to 0$ , and flexural modes that bend the rod with a quadratic dispersion and a diverging density of states [36]. The former yield a Markovian decay that was found in Ref. [22] for a cylinder but here is generalized to an arbitrary cross-sectional shape and QD position with the rate

$$\Gamma_{\rm L0}^{\rm 1D} = \frac{(D_e - D_h)^2 (1 - 2\nu)^2 k_B T}{2A\rho_m v_{\rm 1D}^3 \hbar^2},\tag{8}$$

where *A* is the cross-sectional area,  $\nu = 0.299$  the GaAs Poisson ratio, and  $v_{1D} = v_s \sqrt{3 + 2\nu + 2/(\nu - 1)}$  the phonon speed along the waveguide axis. The total decay,  $\exp(-\Gamma_{1D}t)$ , with  $\Gamma_{1D} = \Gamma_{L0}^{1D} + \Gamma_{3D}$ , is plotted in Fig. 3(a). The coupling to flexural modes, on the other hand, depends on the QD position, and ranges from no coupling at points of high symmetry (e.g., the center of a cylinder) to large coupling away from such points. In Fig. 3(a) we plot the numerically evaluated coherence decay of a QD placed off center at a distance  $\rho/2$  from the center of a cylindrical waveguide of radius  $\rho$  (1D'). The decay is non-Markovian, scaling as  $P_{1D'} = e^{-\Gamma_{1D}t - \beta t^{3/2}}$  [36]. In both cases, the error in TPI scales as  $\propto T$  at low temperatures and is significant even for a waveguide with a diameter of hundreds of nanometers; see Figs. 1(d) and 3(c).

Next we consider a QD embedded in a freestanding 2D membrane with thickness 2h. To evaluate the coherence, we approximate the dispersion of the fundamental vibrational mode [64] as  $\omega = v_{2D}q_{\parallel}$  and discard the modes with  $q_{\parallel} > h^{-1}$  [36], where  $v_{2D} = v_s \sqrt{1 - 2\nu}/(1 - \nu)$ , and  $q_{\parallel}$  is the in-plane wave number. The linear scaling of the density of states with  $\omega$  yields

$$\operatorname{Re}[K_{2\mathrm{D}}] = -p\left[\gamma_E + \int_{\tilde{t}}^{\infty} d\tau \frac{\cos\tau}{\tau} + \ln\tilde{t}\right] - \Gamma_{3\mathrm{D}}t, \quad (9)$$

Here,  $p = (D_e - D_h)^2 (1 - 2\nu)^2 k_B T / 4\pi \rho_m h v_{2D}^4 (1 - \nu)^2 \hbar^2$ ,  $\tilde{t} = v_{2D} t / h$ , and  $\gamma_E$  is the Euler-Mascheroni constant. The coherence is plotted in Fig. 3(a) and results in a TPI that is dominated by the linear interaction at low temperatures as shown in Fig. 1(d). At long times  $(t \gg h / v_{2D})$ , Eq. (9) can be simplified to  $P_{2D} = (v_{2D} t / h)^{-p} \exp(-\Gamma_{3D} t)$ . QDs positioned away from the membrane center would also couple to flexural modes with quadratic dispersion resulting in a



FIG. 4. Suppressing phonon dephasing by clamping the photonic structures. The plot shows the photon infidelity versus thickness of SiO<sub>2</sub> (gray) surrounding a GaAs waveguide (dark gray) of radius 80 nm with a QD (small black triangle) in the center (solid line) and halfway off center (dashed line). Parameters: T = 5 K, L = 3 nm,  $v_{s,SiO2} = 5848$  ms<sup>-1</sup>,  $\rho_{m,SiO2} = 2.2$  g cm<sup>-3</sup>,  $\nu_{SiO2} = 0.17$ .

Markovian dephasing. Contrary to these examples, the 0D structure has a vanishing density of states at low frequencies. As used above, the dephasing is therefore only due to the quadratic coupling.

The theory developed above directly points towards methods of suppressing the malign impact of phonons. By mechanically clamping the structure, the coupling to the fundamental vibrational mode can be suppressed. This may be achieved by immersing the freestanding structure into another material (e.g., glass or semiconductor [65]) with a lower refractive index such that the light is still guided. We find that thicknesses as small as 1  $\mu$ m are sufficient to fully suppress the decoherence; see Fig. 4. This may provide a viable approach to obtain near-unity TPI.

In conclusion, we find that the degree of confinement of the nanostructure has a significant impact on the coherence. Bulk (3D) and maximally confined (0D) structures dephase the ZPL solely due to the quadratic exciton-phonon coupling, which becomes negligible at low temperatures, specifically for  $\lambda_{th} \gg L$  and  $\lambda_{th} \gg R$ , respectively. The decoherence in 1D and 2D structures is enhanced by long-wavelength vibrations mediated by the linear exciton-phonon coupling and can be important even at sub-Kelvin temperatures. The situation is more involved in the case of more complex structures such as photonic-crystal devices. We expect a photonic-crystal membrane to exhibit worse coherence than a 2D membrane of same thickness due to the holes that would slow down the long-wavelength phonons; see Eq. (9). A detailed calculation of the decoherence in photonic-crystal structures is an interesting question for further investigation.

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*Note added.*—Recently, a related preprint appeared (and was recently published [66]), which studies the phonon decoherence in bulk systems.

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