

## Supplementary Materials

### Local structure and Magnetic properties analysis of the $\text{La}_x\text{Eu}_{1-x}\text{PO}_4$ solid-solutions

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## Supplementary Figures

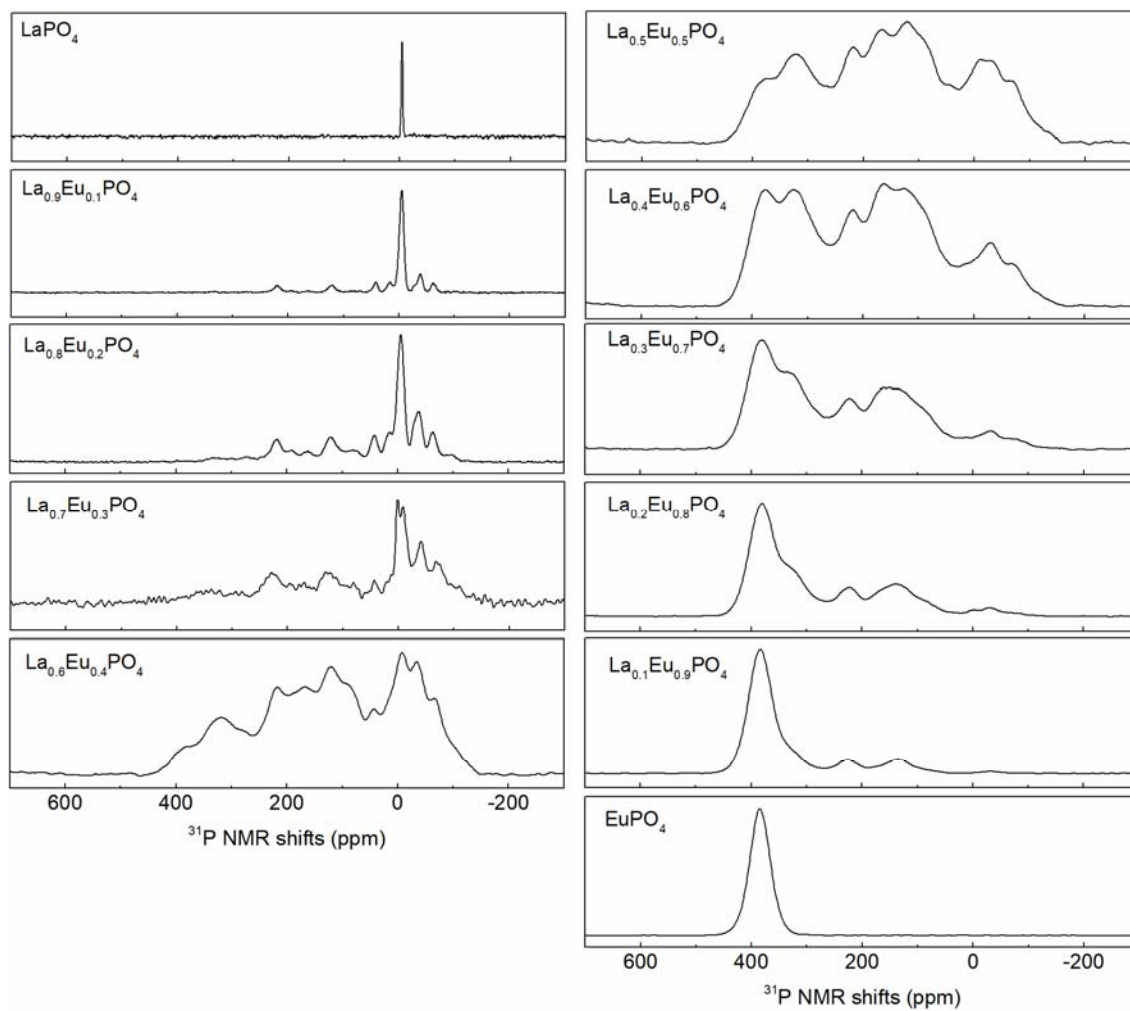


Figure S 1:  $^{31}\text{P}$  MAS NMR spectra of the  $\text{La}_x\text{Eu}_{1-x}\text{PO}_4$  series acquired at a spinning rate of 60 kHz on a 4.7 T Bruker NMR spectrometer.

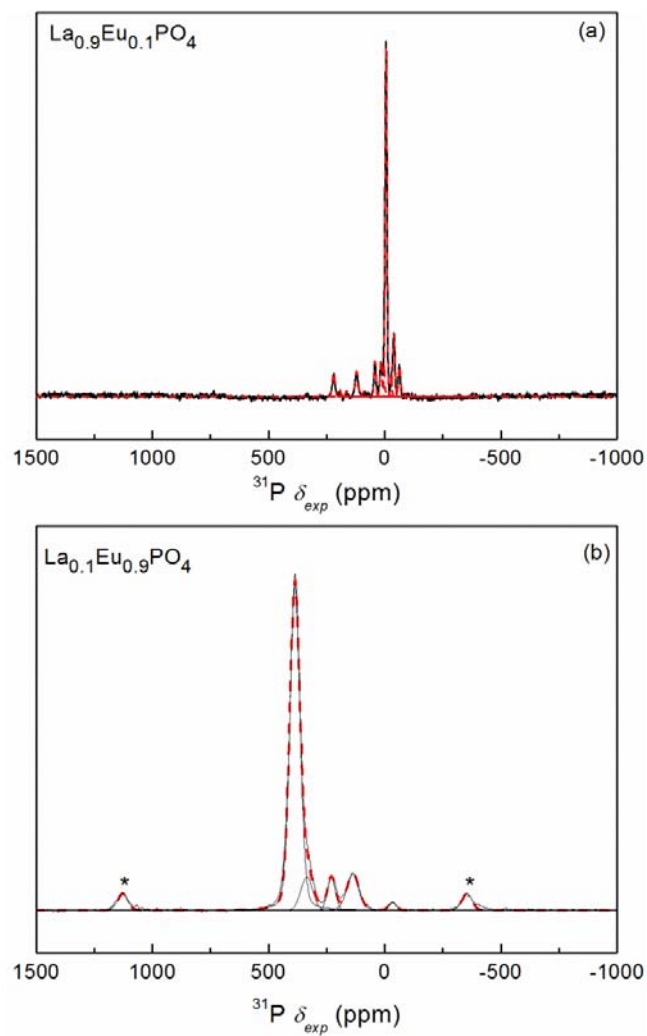


Figure S 2: Full  $^{31}\text{P}$  MAS NMR spectra of the  $\text{La}_x\text{Eu}_{1-x}\text{PO}_4$  samples ( $x=0.9$  and  $0.1$ ) acquired at a spinning rate of 60 kHz on a 4.7 T Bruker NMR spectrometer.

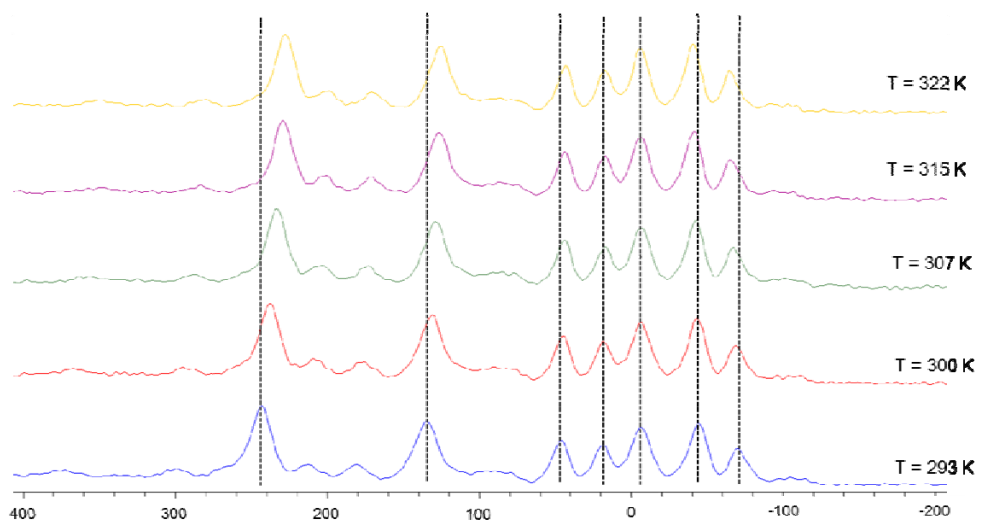


Figure S 3:  $^{31}\text{P}$  MAS-NMR spectra acquired at different temperatures for  $\text{La}_{0.9}\text{Eu}_{0.1}\text{PO}_4$ . The dashed lines are guides for the eye.

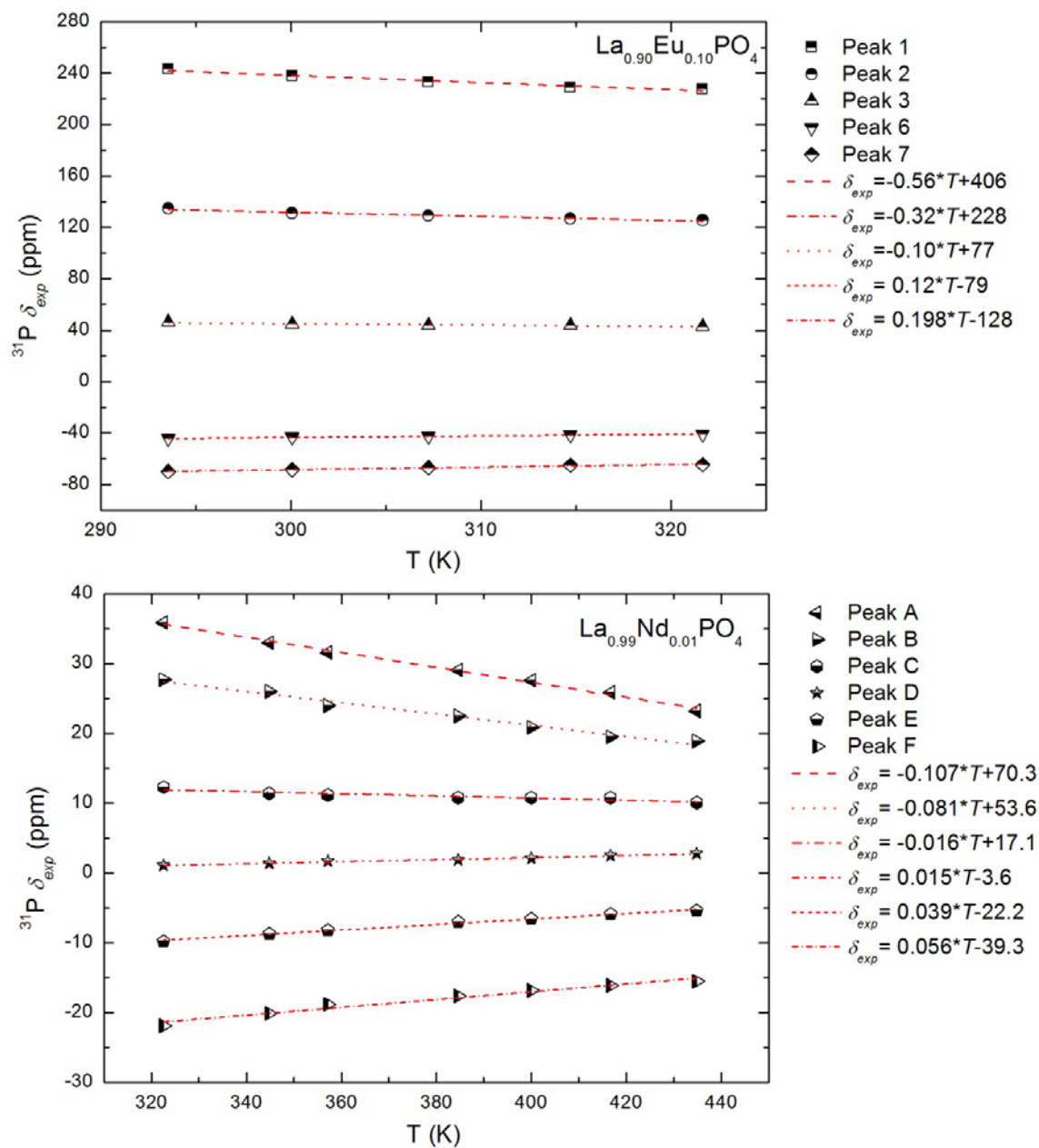


Figure S 4: Variation of the peaks position with temperature for the  $\text{La}_{0.9}\text{Eu}_{0.1}\text{PO}_4$  and  $\text{La}_{0.99}\text{Nd}_{0.01}\text{PO}_4$  solid solutions. In the present study, the experiments were recorded by at spinning frequencies of 45 kHz and varying the temperature between 293 and 322 K.

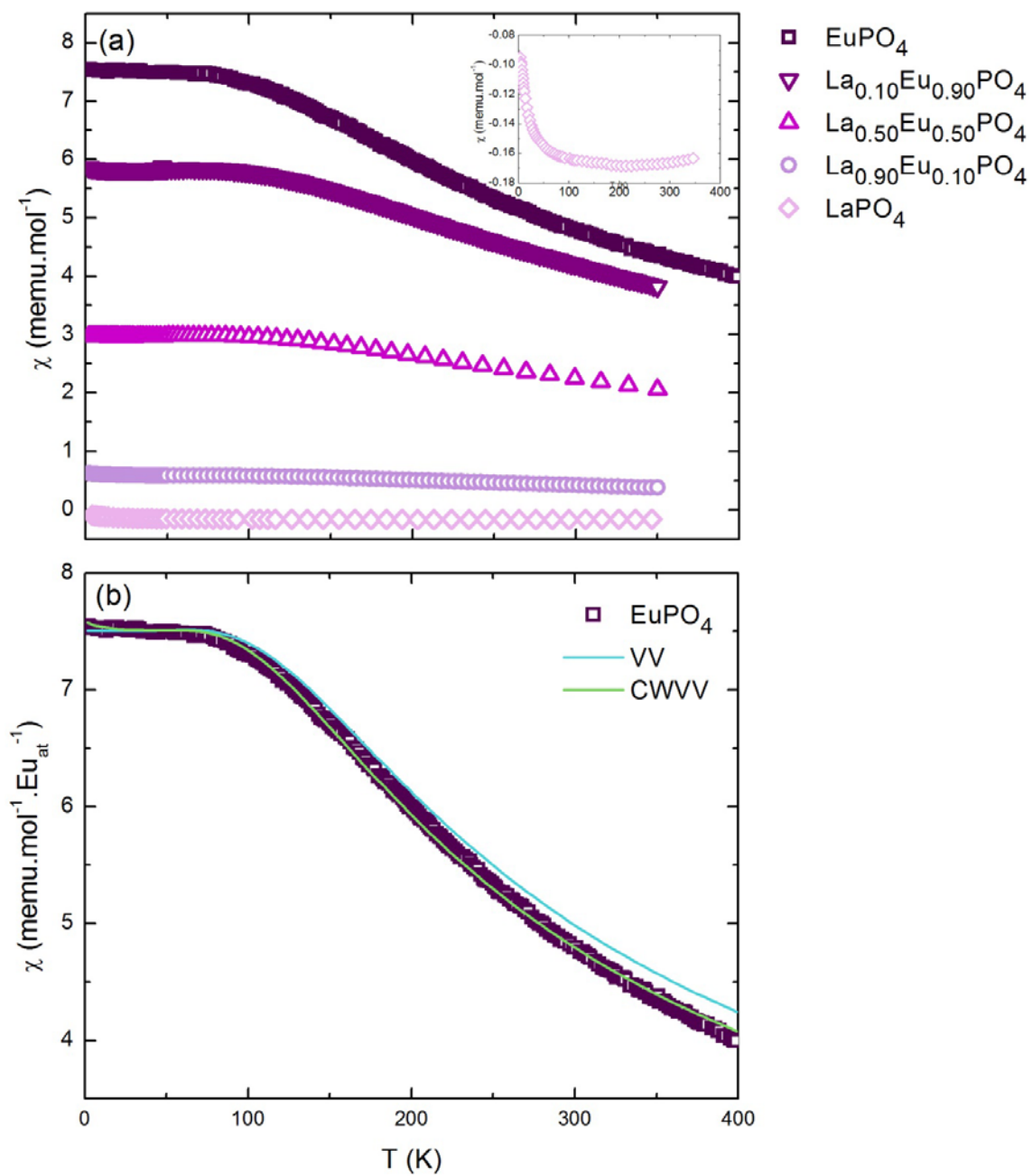


Figure S 5: Magnetic susceptibility curves and their corresponding fits. The inset shows a zoom on the  $\text{LaPO}_4$  magnetic susceptibility.

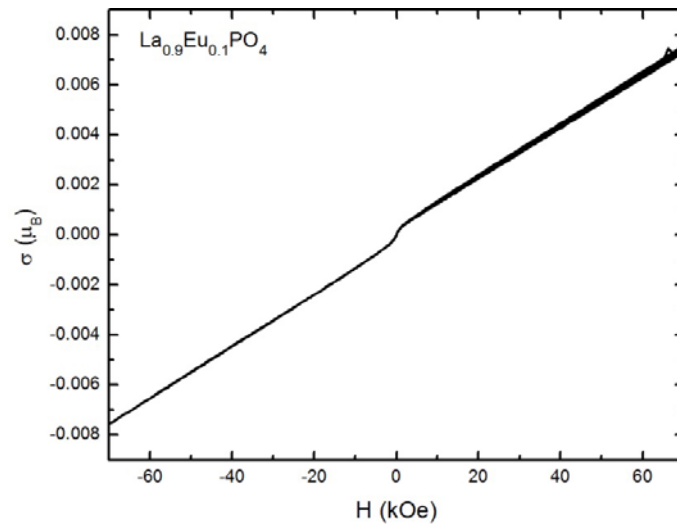


Figure S 6: Small hysteresis loop observed for  $\text{La}_{0.9}\text{Eu}_{0.1}\text{PO}_4$ .

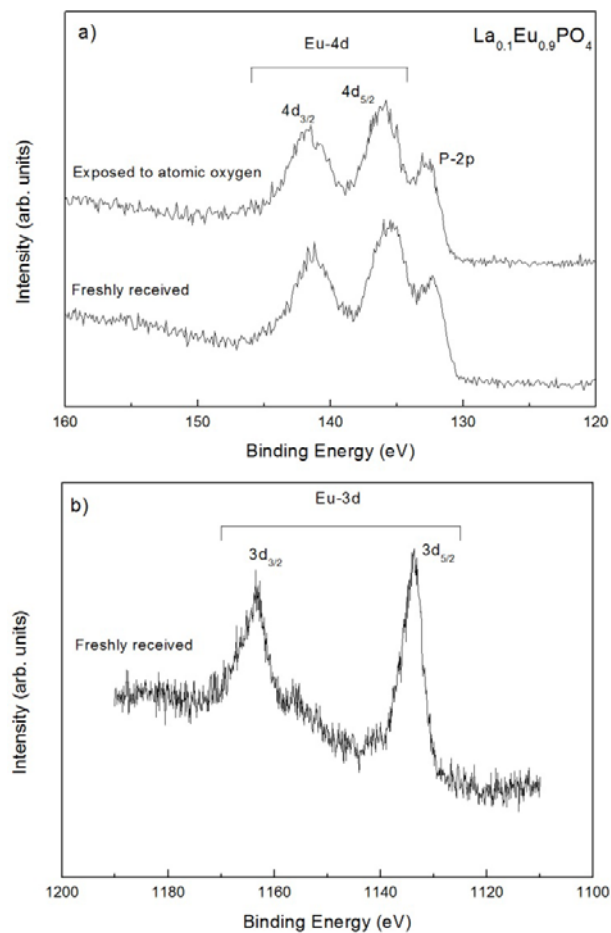


Figure S 7: XPS spectra of  $\text{La}_{0.1}\text{Eu}_{0.9}\text{PO}_4$  in the energy range of a) the Eu-4d and P-2p orbitals and b) the Eu-3d orbital.



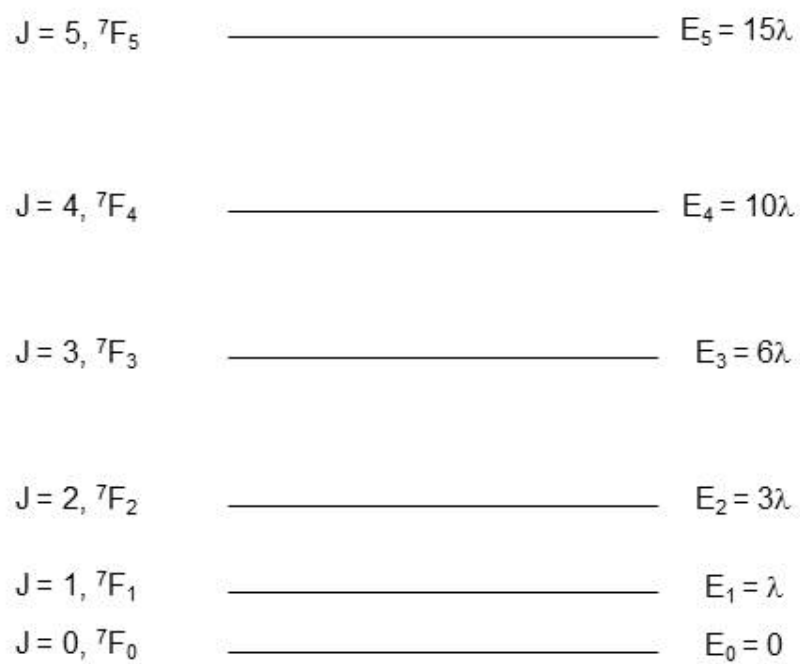


Figure S 8: Energy levels of the lowest multiplet  ${}^7F_J$  of  $\text{Eu}^{3+}$  at  $B_0 = 0$  T.

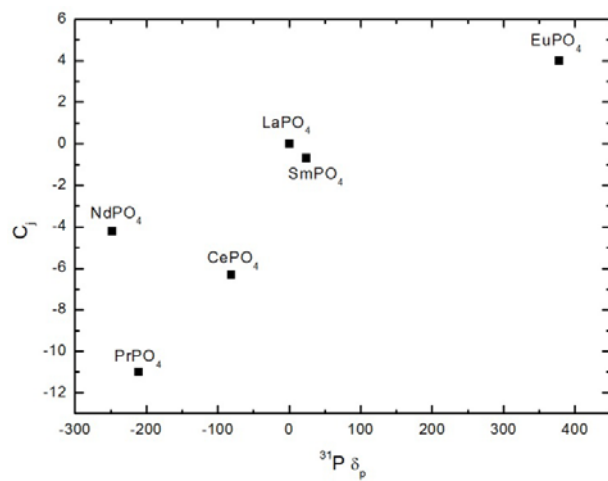


Figure S 9: Plot of the  $C_j$  constants<sup>2</sup> against the experimental shifts for the LnPO<sub>4</sub> series considering a constant  $A_{iso}$ .

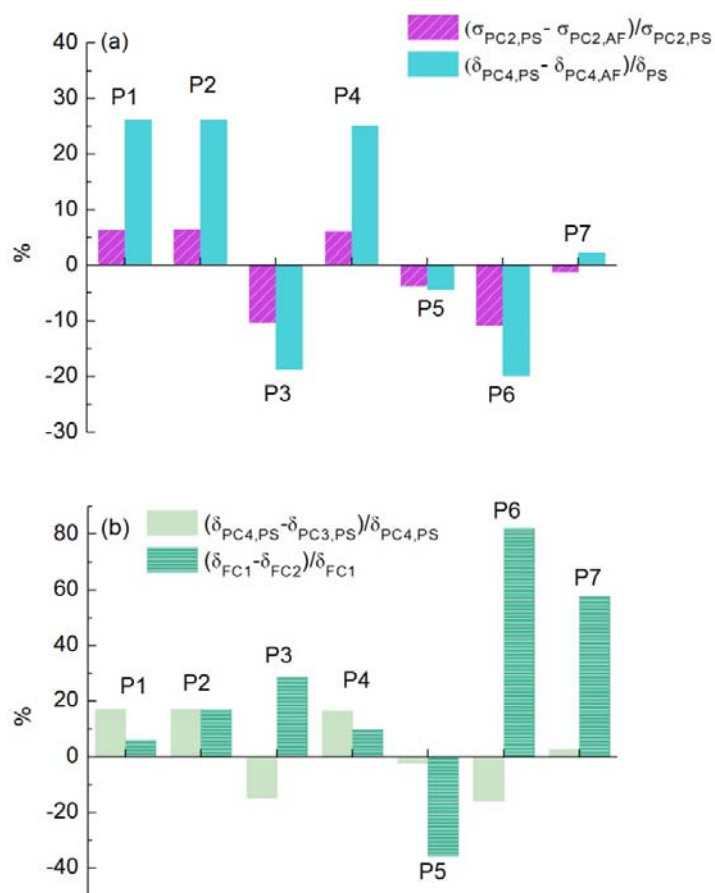


Figure S 10: Relative differences (in %) between (a) the shielding/shifts using the same approach but two sets of CFP and EL, and (b) the  $\delta_{PC}$  calculated using the two approaches or the two clusters using the CFP and EL determined during this study.

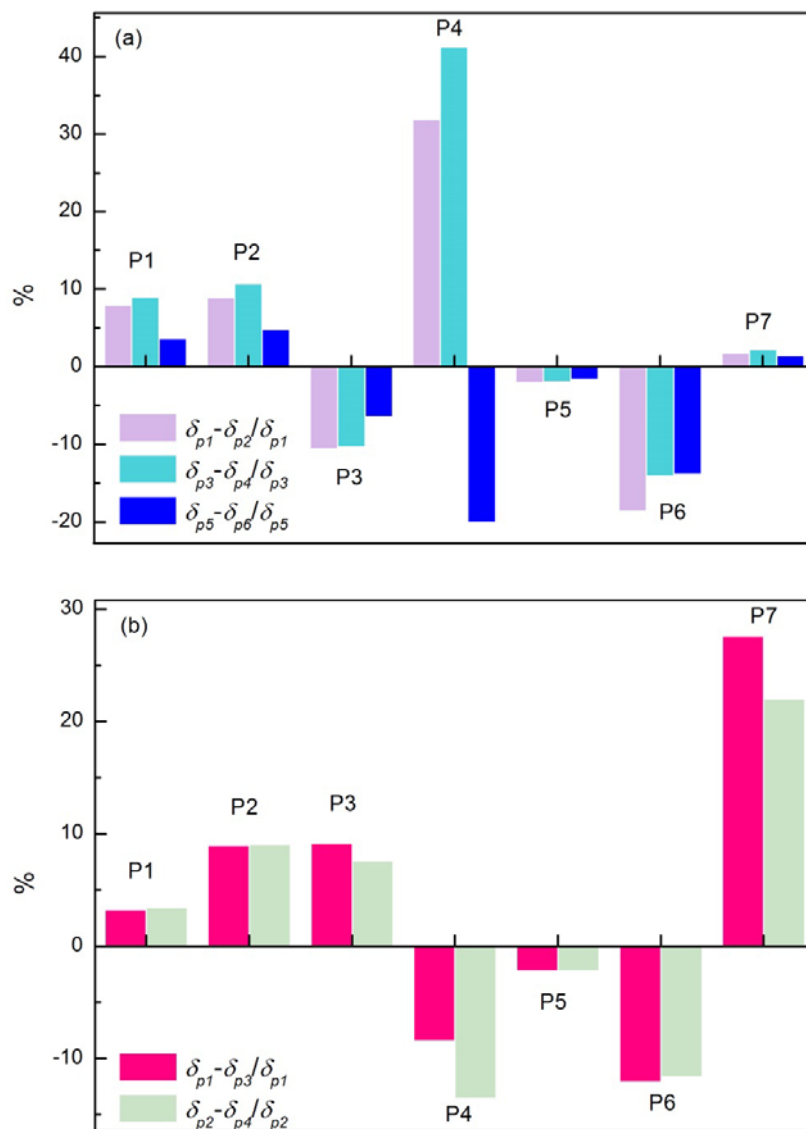


Figure S 11: Relative differences (in %) between the theoretical paramagnetic shifts.

## Supplementary Tables

Table S1: P-Ln distances ( $r$ ), P-O-Ln angle considering the crystalline structure ( $\theta_c$ ), polar angle ( $\theta_s$ ) and azimuthal angle ( $\varphi_s$ ) considering the Eu or La atom at the origin.

	LaPO <sub>4</sub>					EuPO <sub>4</sub>			
	$r(\text{\AA})$	$\theta_c(^{\circ})$	$\theta_s(^{\circ})$	$\varphi_s(^{\circ})$	$r_{\text{APO}}(\text{\AA})$	$r(\text{\AA})$	$\theta_c(^{\circ})$	$\theta_s(^{\circ})$	$\varphi_s(^{\circ})$
P1	3.217	174.5	86.5	88.96	3.216	3.114	174.8	102.9	88.4
P2	3.293	0	96.6	84.4	3.295	3.241	0	80.7	84.6
P3	3.503	78.8	87.1	-17.2	3.505	3.458	77.4	80.1	-16.6
P4	3.768	98.7	132.5	-23.9	3.766	3.681	99.1	140.6	-8.5
P5	3.769	110.2	21.4	-46.6	3.768	3.640	110.3	36.3	-60.1
P6	3.782	69.4	78.3	17.1	3.782	3.656	69.6	77.5	13.3
P7	3.816	109.1	138.1	32.89	3.822	3.711	108.6	142.2	13.0

Table S 2: Relaxation times  $T_1$  defined considering 3 main "regions" for the solid-solutions.

Sample name	Peak range	$\delta_{exp}$ ( $\pm 0.2$ ppm)	FWHM (ppm) ( $\pm 5$ %)	$T_1$ (s) ( $\pm 5$ %)
<b>La<sub>0.8</sub>Eu<sub>0.2</sub>PO<sub>4</sub></b>				
	1	218.2	24.5	0.38
	2	120.6	27.7	0.61
	3	42.7	15.7	1.6
	4	15.0	19.6	2.5
	5	-6.4	15.1	9.2
	6	-38.2	16.9	3.1
	7	-63.6	18.4	2.5
<b>La<sub>0.7</sub>Eu<sub>0.3</sub>PO<sub>4</sub></b>				
	R1			--
	R2	249.9 to 72.7		0.58
	R3	72.7 to -155.1		2.95
<b>La<sub>0.6</sub>Eu<sub>0.4</sub>PO<sub>4</sub></b>				
	R1	501 to 253.5		0.28
	R2	253.5 to 58.3		0.53
	R3	58.3 to -223.8		1.8s
<b>La<sub>0.5</sub>Eu<sub>0.5</sub>PO<sub>4</sub></b>				
	R1	501 to 253.5		0.29
	R2	253.5 to 23.9		0.5
	R3	23.9 to -205.7		1.4
<b>La<sub>0.4</sub>Eu<sub>0.6</sub>PO<sub>4</sub></b>				
	R1	504.8-264.4		0.2
	R2	264 to 35		0.41
	R3	34.7 to -194.9		2.3
<b>La<sub>0.3</sub>Eu<sub>0.7</sub>PO<sub>4</sub></b>				
	R1	501 to 263		0.25
	R2	263 to 37		0.43
	R3			--
<b>La<sub>0.2</sub>Eu<sub>0.8</sub>PO<sub>4</sub></b>				
	1	386.4		0.21
	2	335		0.25
	3	229.5		0.31
	4	136.7		0.43
	5	-33.6		--

Table S 3: Relative peak intensities (%) at various x values in the  $\text{La}_x\text{Eu}_{1-x}\text{PO}_4$  series for each  $(\text{P}(\text{La})_y(\text{Eu})_{7-x})$  unit (with  $0 \leq y \leq 7$ ) calculated using the randomly distributed network (RDN) model.

Units	x								
	0.9	0.8	0.7	0.6	0.5	0.4	0.3	0.2	0.1
$\text{P}(\text{La})_7(\text{Eu})_0$	48	21	8.2	2.8	0.8	0.2			
$\text{P}(\text{La})_6(\text{Eu})_1$	37	36.7	24.7	13.1	5.5	1.7	0.4		
$\text{P}(\text{La})_5(\text{Eu})_2$	13	27.5	31.8	26.1	16.4	7.7	2.5	0.4	
$\text{P}(\text{La})_4(\text{Eu})_3$	2	11.5	22.7	29	27.3	19.3	9.7	2.9	
$\text{P}(\text{La})_3(\text{Eu})_4$		2.9	9.7	19.3	27.3	29	22.7	11.5	2
$\text{P}(\text{La})_2(\text{Eu})_5$		0.4	2.5	7.7	16.4	26.1	31.8	27.5	13
$\text{P}(\text{La})_1(\text{Eu})_6$			0.4	1.7	5.5	13.1	24.7	36.7	37
$\text{P}(\text{La})_0(\text{Eu})_7$				0.2	0.8	2.8	8.2	21	48

Table S 4: Twenty seven calculated  $B_q^k$  ( $\text{cm}^{-1}$ ) parameters.

k	q	$B_q^k$
2	0	-623.214
2	1	-64.7431
2	-1	-42.1616
2	2	71.09481
2	-2	-13.2061
4	0	-321.383
4	1	470.4191
4	-1	190.8043
4	2	609.9013
4	-2	-49.677
4	3	511.5524
4	-3	-393.587
4	4	249.3432
4	-4	166.4712
6	0	606.2701
6	1	102.0181
6	-1	84.52455
6	2	-285.413
6	-2	41.23308
6	3	-369.142
6	-3	297.2502
6	4	36.26437
6	-4	53.23284
6	5	-274.948
6	-5	51.78076
6	6	-66.0227
6	-6	-196.456



Table S 5: Energy levels (cm<sup>-1</sup>) measured experimentally (Exp) and calculated theoretically (Theo).

	La <sub>0.9</sub> Eu <sub>0.1</sub> PO <sub>4</sub>	LaPO <sub>4</sub> -doped 1-5%Eu <sup>3+</sup>		EuPO <sub>4</sub>	Eu <sup>3+</sup> free ion	
	Theo	Luminescence		Theo	Theo	Theo <sup>3</sup>
		Exp	Theo			
<sup>7</sup> F <sub>0</sub>	0	0	0	0	0	0
<sup>7</sup> F <sub>1</sub>	273.5	261	262	327	379	374
	438	406	411	382		
	462	464	458	404		
<sup>7</sup> F <sub>2</sub>	931.3	943	954		1043	1036
	1023		978			
	1053	1021	1019			
	1143	1096	1091			
	1192	1178	1177			
<sup>7</sup> F <sub>3</sub>	1875	1853	1851		1896	1888
	1889	1881	1859			
	1948	1894	1895			
	1968	1917	1929			
	1992	1927	1936			
	2006	1944	1952			
	2012	1967	1962			
<sup>7</sup> F <sub>4</sub>	2744	2677	2675		2869	2866
	2806	2755	2751			
	2831	2792	2793			
	2880	2841	2852			
	2976	2863	2868			
	3015	2905	2906			
	3045	2933	2935			

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3067	2963	2955
3168		3006

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Cartesian coordinates of the cluster models

**Model 1** ( $P_1La_6Gd_1O_{25}H_{21}$ )

P	-0.057703	0.220772	-0.035765
O	0.427236	-0.098999	1.403164
O	-0.848535	-1.051057	-0.493262
O	1.092124	0.459872	-1.054013
O	-0.881530	1.525844	-0.094097
Gd	-0.690676	-2.294643	1.996706
La	0.428885	2.860224	-1.806844
La	2.206565	0.415701	3.037988
La	-3.377507	-1.307575	-0.941519
La	3.581051	0.203296	-1.064937
La	-2.961187	2.450582	0.859538
La	0.682847	-2.507956	-2.106707
O	-2.013245	-2.822103	-2.191171
O	1.142454	5.065903	-2.107609
O	5.855974	0.517125	-1.465584
O	3.307215	-1.022283	1.115073
O	-2.442380	2.166283	3.056582
O	-0.796759	2.082549	-3.581413
O	0.786452	-1.600236	3.721362
O	-5.397721	-2.386124	-0.974188
O	2.770212	2.186319	-2.319360
O	-4.955265	3.639091	0.820365
O	-1.577511	4.000626	-0.420962
O	0.721674	-3.351720	0.371844
O	3.442874	0.192275	5.036099
O	0.435505	-1.191589	-4.005133
O	3.290159	1.654468	1.046624
O	0.905241	2.178992	3.774844
O	0.853353	-4.732599	-2.771088
O	-1.598713	-4.132285	3.004019
O	3.085357	-1.987871	-2.064766
O	-3.730966	1.028964	-1.170909
O	-2.969500	-1.356922	1.433593
H	-0.681467	1.151517	-3.830932
H	0.950253	5.794046	-1.505927
H	-1.859144	4.890896	-0.661068
H	3.257427	2.614896	0.954500
H	3.364272	2.896653	-2.588195
H	6.487308	0.920156	-0.858991
H	-1.618599	1.880544	3.476974
H	-5.461433	3.762579	0.008520
H	-3.670260	-1.453398	2.089166
H	-2.277884	-3.430418	-2.890347
H	-5.754535	-3.257603	-0.778957
H	-3.270399	1.502233	-1.883428
H	0.374992	-5.402792	-2.267458
H	3.721419	-2.710079	-2.014467

H	0.998826	-0.446233	-4.244579
H	2.897744	-1.892197	1.003640
H	0.313087	2.798205	3.333996
H	3.111622	0.738947	5.760863
H	1.007532	-1.986567	4.574658
H	1.203565	-4.172022	0.524790
H	-2.047105	-4.945979	3.242783

**Model 2 (Gd<sub>1</sub>P<sub>7</sub>La<sub>11</sub>O<sub>40</sub>H<sub>11</sub>)**

Gd	0.22032000	0.19678300	-0.01391900
P	-2.95716200	-0.29062000	0.07266700
P	3.48175900	0.51484400	-0.36118600
P	-0.57664500	-1.93742300	2.98431300
P	-1.52196000	2.88531000	-2.09903200
P	1.84873700	-3.19960600	-0.35384100
P	0.73147300	3.43365700	1.22994600
P	-0.53179500	-1.55208800	-3.26548800
O	-2.13946200	0.92431100	0.56337100
O	-1.88103400	-1.25735300	-0.49726000
O	-3.82563000	-0.90526900	1.20132900
O	-3.96193600	0.04424700	-1.08130800
O	2.61306300	-0.10025000	0.76758600
O	2.47681800	0.84937200	-1.51485700
O	4.55757900	-0.45223800	-0.93111300
O	4.29930300	1.72919100	0.13041800
O	0.10931400	-0.64593700	2.42397300
O	0.59006500	-2.84342300	3.45860200
O	-1.54732000	-1.50756300	4.12036100
O	-1.49204600	-2.65328700	1.96711200
O	-0.35531400	1.97920100	-1.62465000
O	-2.49295100	3.31486600	-0.96302100
O	-0.83615500	4.17666300	-2.65936700
O	-2.43746400	2.16939300	-3.11628700
O	0.77285200	-2.23230900	0.21608100
O	2.71736900	-2.58394100	-1.48234700
O	2.85346700	-3.53393100	0.80000500
O	1.03112800	-4.41364500	-0.84534300
O	0.04544400	2.14255800	1.79038600
O	1.70176100	3.00420000	0.09388100
O	-0.43540500	4.33993900	0.75555900
O	1.64671100	4.14985800	2.24701000
O	0.38366900	-0.83640600	-2.24847700
O	-1.69839900	-0.64630100	-3.74000100
O	0.43897400	-1.98212000	-4.40164200
O	-1.21743100	-2.84380100	-2.70531800
La	-3.74593300	-2.46653700	3.11440600
La	-4.69126600	2.35605400	-1.96891100
La	2.69286200	-1.66127700	2.68080300
La	1.74760800	3.16107400	-2.40263200

La	-0.06574600	1.29961500	4.22783000
La	-1.32887700	-3.68651400	-0.26771400
La	5.11008700	-2.88136400	-0.70126800
La	-2.53808000	3.15789600	1.53358500
La	-3.80110200	-1.82821900	-2.96198800
La	3.90062900	3.96300200	1.09978600
La	2.63762600	-1.02327700	-3.39586000
O	5.58559500	4.84501300	2.22559700
H	6.35360800	5.22106200	2.66229200
O	3.50590200	4.59724300	-1.26563400
H	4.14192300	5.13550700	-1.75532300
O	4.93703600	-2.02848300	1.95812500
H	5.73882300	-1.55038100	2.20894000
O	2.14556500	0.41855000	4.38845200
H	2.92878100	0.76781800	4.83486200
O	-2.05168900	2.57450700	4.00904200
H	-2.80722000	2.58954400	4.61303900
O	-5.27289200	-1.90810900	4.68705000
H	-6.08346300	-2.01108700	5.19235700
O	-4.14347500	-4.27561900	1.87874500
H	-3.56789600	-4.96988200	1.48593300
O	-4.72528300	3.00044300	0.66180800
H	-5.55136300	2.75885100	1.10101500
O	-6.40571800	3.55864400	-2.69900900
H	-7.14878800	4.01037800	-3.10445300
O	2.34600700	1.49869500	-4.12636400
H	1.89913100	1.58219400	-4.98228800
O	4.74715800	-2.32197700	-3.18328400
H	5.48728600	-2.42855400	-3.79321700
O	7.09631400	-3.85034700	-0.84864600
H	7.90547300	-4.32072100	-1.06239000
O	-2.12953700	-5.67760900	0.52069000
H	-2.04556300	-6.63300300	0.57479600
O	-5.25349400	0.11806500	-3.37316700
H	-5.74027200	0.32073400	-4.18345600
O	-3.81810900	-3.44109700	-1.32845400
H	-4.34262800	-3.70761700	-0.55455300

## References

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