# PHOTOPRODUCTION OF $\rho^{\circ}$ ON HYDROGEN WITH TAGGED PHOTONS BETWEEN 4 AND 6 GeV 

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Abstract: We have measured the reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}$in the DESY 1 m Streamer Chamber.
The dominant $\rho^{\circ}$ production is analyzed in terms of various models.

## 1. INTRODUCTION

Previous studies [1-3] of $\rho^{\circ}$ production in the reaction

$$
\begin{equation*}
\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}, \tag{1}
\end{equation*}
$$

have shown that the $\pi^{+} \pi^{-}$mass distribution is skewed relative to a $p$-wave BreitWigner resonance shape and that the slope of the $t$-distribution ( $t$ is the four-momentum transfer squared from incident to outgoing proton) depends strongly on the effective di-pion mass. The skewing of the $\rho^{\circ}$ shape requires model-dependent background subtraction, thus introducing a significant uncertainty into the determination of the cross section for the channel

$$
\begin{equation*}
\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\mathrm{o}} \tag{2}
\end{equation*}
$$

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We have used three phenomenological models, namely a parametrization of the Breit-Wigner curve [3, 4], an interference model [5] and a simple pomeron exchange model [6]. The resulting cross sections are given in table 2.

## 2. EXPERIMENTAL SET-UP

A monochromatic $\mathrm{e}^{+}$beam (with energy settings of $6.5,4.3,3.5$ and 2.9 GeV ) crossing a 1.2 mm Al radiator produced a bremsstrahlung beam. For each photon in the selected energy region the recoil positron was bent onto a hodoscope of 12 overlapping scintillation counters. This defined 23 energy channels with widths between $\pm 60 \mathrm{MeV}$ and $\pm 30 \mathrm{MeV}$. These channels were calibrated by measuring the energy of $\mathrm{e}^{+} \mathrm{e}^{-}$pairs produced by the tagged photons in the streamer chamber.

The double-gap streamer chamber [7] was filled with a helium-neon gas mixture at 1 atm and was operated with a $500 \mathrm{kV}, 10 \mathrm{nsec}$ pulse. The pulse was supplied by a 14 stage Marx generator and formed by a 0.8 m co-axial Blumlein system. Built into the 22 kG magnet of the DESY bubble chamber, the chamber had a sensitive volume of $100 \times 60 \times(2 \times 16) \mathrm{cm}^{3}$.

A liquid hydrogen target ( 4 cm in length, 2.6 cm in diameter) was surrounded by a cylindric scintillation counter of 0.3 cm thickness and placed inside the chamber. Two counters in the plane perpendicular to the magnetic field recognized electron pair production. A shower counter was used as flux monitor.

## 3. ANALYSIS OF THE FILM

Approximately 800000 photographs were taken, showing a total of 40000 events on hydrogen and 100000 events on scintillation material. Part of the film was scanned twice, and the combined scanning efficiency was found to be greater than $99 \%$. In this paper, we are concerned only with the data in the energy region between 4.1 and 6.2 GeV . In this energy region we measured 1701 events of type (1). After three measurements about $5 \%$ of the events remained unmeasurable. For the geometric and kinematic reconstruction of the events, the CERN program chain (THRESH, GRIND) was used with minor changes. The vertex reconstruction allowed a complete separation of events produced in hydrogen and the scintillation material. The measurement resolution in space was $250 \mu \mathrm{~m}$.

## 4. CORRECTIONS

A detailed description of the corrections for our triggering biases will be published later. The following major corrections to the data were made: (a) The efficiency of the flux monitor was intensity dependent. Therefore our data were nor-
malized to the total $\gamma \mathrm{p}$ cross section [3] of $124.5 \mu \mathrm{~b}$ at 5 GeV ; (b) the cylindrical target counter was not fully efficient. The loss is topology dependent and amounts to ( $12 \pm 2$ ) \%; (c) hadronic events in which one particle hits one of the pair counters were vetoed. This loss has an average value of $(29 \pm 3) \%$.

## 5. RESULTS

The cross section for reaction (1) was found to be $20.9 \pm 1.7 \mu \mathrm{~b}$, in agreement with previous experiments $[1-3]$. The dominant feature of reaction (1) is the production of $\rho^{\circ}$. Fig. la shows the $\pi^{+} \pi^{-}$mass distribution and fig. 1 b the $t$-distribution for all events. The double differential cross section $\mathrm{d}^{2} \sigma / \mathrm{d} M_{\pi \pi} \mathrm{d} t$ for reaction (1) is given in table 1 . In order to obtain the cross section for $\rho^{\circ}$ production we used three models:
(a) Modification [3, 4] of the p-wave Breit-Wigner distribution by a factor $\left(M_{\rho} / M_{\pi \pi}\right)^{n(t)}$, where $n(t)$ is a free parameter.
(b) An interference model, where the $\rho^{0}$ production amplitude interferes with a Drell-type background [5].
(c) A pomeron-exchange model with $s$-channel $\gamma$ - $\rho$ helicity conservation [6].

In cases (a) and (b) maximum likelihood fits were made to the events of reaction (1) in $9 t$-intervals be tween $|t|_{\text {min }}$ and $|t|=0.54 \mathrm{GeV}^{2}$, taking into account also $\Delta(1236)$ production and a phase-space background. The results of the fits are given in table 2. The values of the slope and the forward cross sections were obtained assuming an $\exp (A t)$ dependence of the $\rho$ - production cross section.

In case (c) the two free parameters of the model, to be determined from experimental data, are the overall normalization $g$ and a mass-independent $t$-distribution slope $a$ (see ref. [6]). In fitting these parameters we used only the region 0.7 GeV $<M_{\pi \pi}<0.8 \mathrm{GeV}$ and $|t|<0.3 \mathrm{GeV}^{2}$. In this interval about $2 \%$ background were subtracted using the prism-plot method [8]. From $g$ and $a$ one can calculate within the pomeron exchange model all interesting quantities of reaction (2). They are given in table 2 c . The quoted errors are from the statistical uncertainties of the two fitted parameters $a$ and $g$ only. The extrapolation to the unphysical point $t=0$ was done by fitting the function $\exp \left(A t+B t^{2}\right)$ in the region $|t|<0.4 \mathrm{GeV}^{2}$ to the calculated differential $\rho^{o}$ cross sections $\mathrm{d} \sigma / \mathrm{d} t$. The $\Delta(1236)$ cross section was obtained by using the prism-plot method [8].

To study the helicity of the $\pi^{+} \pi^{-}$system in reaction (1) the angular distribution of one pion in the $\pi^{+} \pi^{-}$rest system was investigated, with the c.m.s. direction of flight of the $\pi^{+} \pi^{-}$system as polar axis. Fig. 2a shows the helicity density matrix elements for $M_{\pi \pi}<1.0 \mathrm{GeV}$, which were obtained from a maximum likelihood fit assuming $p$-wave dominance. They are consistent with $s$-channel helicity conservation ( $\rho_{00}=\rho_{1-1}=\operatorname{Re} \rho_{10}=0$ ) for $|t|$ values below $0.3 \mathrm{GeV}^{2}$. In addition fig. 2 b shows $\Sigma Y_{2}^{\mathrm{o}}\left(\Omega_{i}\right)$ and $\Sigma Y_{4}^{\mathrm{o}}\left(\Omega_{i}\right)$ as a function of $M_{\pi \pi}$. The sum is taken over all events, and $\Omega$ is the decay angle in the $s$-channel helicity system. The $Y_{2}^{0}$ moment shows the same (skewed) $\rho$-shape as the cross section, again consistent with a helicity

Table 1
Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}, 4.1<E_{\gamma}<6.2 \mathrm{GeV}$.

| $M(\mathrm{GeV})$ | ${ }^{\|t\|} \min ^{-0.03}$ | 0.03-0.06 | 0.06-0.09 | 0.09-0.12 | 0.12-0.15 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.32-0.36 | 0 | $65 \pm 65$ | 0 | 0 | $22 \pm 22$ |
| 0.36-0.40 | $77 \pm 77$ | $40 \pm 32$ | 0 | $18 \pm 18$ | $18 \pm 14$ |
| 0.40-0.44 | $150 \pm 94$ | $39 \pm 31$ | $16 \pm 16$ | $12 \pm 12$ | $35 \pm 22$ |
| 0.44-0.48 | $177 \pm 111$ | 0 | $91 \pm 49$ | $25 \pm 19$ | $6 \pm 6$ |
| 0.48-0.52 | $138 \pm 77$ | $79 \pm 35$ | $117 \pm 48$ | $10 \pm 10$ | $22 \pm 22$ |
| 0.52-0.56 | $200 \pm 99$ | $106 \pm 42$ | $111 \pm 39$ | $34 \pm 22$ | $32 \pm 20$ |
| 0.56-0.60 | $177 \pm 73$ | $91 \pm 35$ | $171 \pm 53$ | $80 \pm 35$ | $26 \pm 16$ |
| 0.60-0.64 | $177 \pm 69$ | $144 \pm 42$ | $204 \pm 57$ | $120 \pm 41$ | $59 \pm 25$ |
| 0.64-0.68 | $237 \pm 82$ | $300 \pm 67$ | $200 \pm 51$ | $201 \pm 50$ | $68 \pm 29$ |
| 0.68-0.72 | $418 \pm 128$ | $405 \pm 73$ | $368 \pm 73$ | $188 \pm 51$ | $125 \pm 38$ |
| 0.72-0.76 | $585 \pm 146$ | $499 \pm 81$ | $477 \pm 87$ | $348 \pm 70$ | $245 \pm 56$ |
| 0.76-0.80 | $490 \pm 145$ | $415 \pm 72$ | $326 \pm 62$ | $263 \pm 58$ | $202 \pm 48$ |
| 0.80-0.84 | $250 \pm 91$ | $242 \pm 48$ | $199 \pm 44$ | $150 \pm 43$ | $133 \pm 38$ |
| 0.84-0.88 | $30 \pm 19$ | $104 \pm 34$ | $63 \pm 24$ | $83 \pm 29$ | $51 \pm 23$ |
| 0.88--0.92 | $72 \pm 43$ | $81 \pm 28$ | $32 \pm 17$ | $79 \pm 30$ | $30 \pm 16$ |
| 0.92-0.96 | $7 \pm 7$ | $14 \pm 10$ | $8 \pm 8$ | $15 \pm 11$ | $32 \pm 17$ |
| 0.96-1.00 | 0 | $7 \pm 7$ | $8 \pm 8$ | $6 \pm 6$ | 0 |
| 1.00-1.04 | 0 | $8 \pm 6$ | $33 \pm 21$ | $31 \pm 16$ | $8 \pm 8$ |
| 1.04-1.08 | 0 | $9 \pm 9$ | $33 \pm 26$ | $9 \pm 9$ | $8 \pm 8$ |
| 1.08-1.12 | 0 | 0 | $9 \pm 9$ | $17 \pm 12$ | 0 |
| 1.12-1.16 | 0 | $16 \pm 11$ | 0 | $9 \pm 9$ | 0 |
| 1.16-1.20 | 0 | $7 \pm 7$ | 0 | 0 | 0 |
| 1.20-1.28 | 0 | $5 \pm 5$ | $7 \pm 5$ | $4 \pm 4$ | $5 \pm 5$ |
| 1.28-1.36 | 0 | $4 \pm 4$ | $4 \pm 4$ | 0 | $9 \pm 9$ |
| 1.36-1.44 | 0 | 0 | $8 \pm 6$ | $9 \pm 9$ | 0 |
| 1.44-1.52 | 0 | $4 \pm 4$ | $5 \pm 5$ | $12 \pm 10$ | 0 |
| 1.52-1.60 | 0 | 0 | 0 | $9 \pm 6$ | $10 \pm 7$ |
| 1.60-1.68 | 0 | 0 | 0 | 0 | 0 |
| 1.68-1.76 | 0 | 0 | 0 | 0 | 0 |
| 1.76-1.84 | 0 | 0 | 0 | 0 | 0 |
| 1.84-1.92 | 0 | 0 | 0 | 0 | 0 |
| 1.92-2.00 | 0 | 0 | 0 | 0 | 0 |
| $\mathrm{d} \sigma / \mathrm{d} t\left(\mu \mathrm{~b} / \mathrm{GeV}^{2}\right)$ | $127 \pm 23$ | $108 \pm 11$ | $100 \pm 11$ | $71 \pm 8$ | $47 \pm 6$ |

Double differential cross section $\mathrm{d} \sigma / \mathrm{d} M_{\pi \pi} \mathrm{d} t_{\mathrm{pp}}$ in $\mu \mathrm{b} / \mathrm{GeV}^{3}$.

Table 1 (continued).

| 0.15-0.18 | 0.18-0.24 | 0.24-0.30 | 0.30-0.39 | 0.39-0.54 | 0.54-0.80 | $\begin{gathered} \mathrm{d} \sigma / \mathrm{d} M \\ (\mu \mathrm{~b} / \mathrm{GeV}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | $7 \pm 4$ | 0 | 0 | $3 \pm 2$ |
| 0 | 0 | 0 | 0 | 0 | $1 \pm 1$ | $5 \pm 2$ |
| 0 | $9 \pm 7$ | $3 \pm 3$ | $4 \pm 4$ | 0 | $1 \pm 1$ | $9 \pm 3$ |
| $25 \pm 20$ | $10 \pm 8$ | 0 | $3 \pm 3$ | 0 | 0 | $11 \pm 4$ |
| $10 \pm 10$ | $10 \pm 8$ | $4 \pm 4$ | 0 | 0 | $1 \pm 1$ | $13 \pm 3$ |
| $11 \pm 11$ | $8 \pm 6$ | $4 \pm 4$ | $5 \pm 5$ | 0 | 0 | $16 \pm 4$ |
| $22 \pm 22$ | $13 \pm 8$ | $5 \pm 5$ | $5 \pm 4$ | 0 | $1 \pm 1$ | $20 \pm 4$ |
| $51 \pm 23$ | $25 \pm 12$ | $9 \pm 6$ | $5 \pm 3$ | $1 \pm 1$ | $1 \pm 1$ | $26 \pm 4$ |
| $92 \pm 39$ | $31 \pm 15$ | $8 \pm 6$ | $21 \pm 9$ | $3 \pm 3$ | $2 \pm 1$ | $39 \pm 6$ |
| $151 \pm 49$ | $96 \pm 25$ | $59 \pm 18$ | $28 \pm 10$ | $4 \pm 2$ | $2 \pm 1$ | $64 \pm 8$ |
| $230 \pm 54$ | $104 \pm 24$ | $76 \pm 23$ | $20 \pm 8$ | $13 \pm 6$ | $4 \pm 2$ | $88 \pm 9$ |
| $186 \pm 50$ | $91 \pm 23$ | $64 \pm 20$ | $33 \pm 12$ | $23 \pm 8$ | $5 \pm 3$ | $76 \pm 9$ |
| $27 \pm 14$ | $51 \pm 19$ | $23 \pm 11$ | $27 \pm 10$ | $5 \pm 3$ | $3 \pm 2$ | $40 \pm 5$ |
| $62 \pm 26$ | $48 \pm 16$ | $30 \pm 12$ | $14 \pm 8$ | $7 \pm 4$ | $4 \pm 2$ | $20 \pm 3$ |
| $9 \pm 9$ | $12 \pm 7$ | $12 \pm 7$ | $12 \pm 6$ | 0 | $1 \pm 1$ | $12 \pm 3$ |
| 0 | $14 \pm 8$ | $15 \pm 9$ | 0 | $7 \pm 4$ | $1 \pm 1$ | $6 \pm 1$ |
| $16 \pm 12$ | $8 \pm 6$ | $4 \pm 4$ | 0 | 0 | 0 | $2 \pm 1$ |
| $13 \pm 9$ | $9 \pm 6$ | $4 \pm 4$ | $2 \pm 2$ | $9 \pm 5$ | $4 \pm 2$ | $7 \pm 2$ |
| 0 | $13 \pm 8$ | 0 | 0 | $2 \pm 2$ | $1 \pm 1$ | $4 \pm 1$ |
| $4 \pm 4$ | $5 \pm 5$ | $4 \pm 4$ | $3 \pm 3$ | $3 \pm 2$ | 0 | $2 \pm 1$ |
| $30 \pm 24$ | $10 \pm 7$ | 0 | $16 \pm 8$ | $7 \pm 4$ | 0 | $5 \pm 2$ |
| 0 | $4 \pm 4$ | 0 | $10 \pm 6$ | $3 \pm 2$ | 0 | $2 \pm 1$ |
| $8 \pm 6$ | $8 \pm 4$ | $6 \pm 3$ | $1 \pm 1$ | $1 \pm 1$ | $1 \pm 1$ | $3 \pm 1$ |
| 0 | $2 \pm 2$ | $2 \pm 2$ | $2 \pm 2$ | $1 \pm 1$ | $2 \pm 1$ | $2 \pm 1$ |
| 0 | $6 \pm 4$ | $6 \pm 4$ | 0 | $4 \pm 2$ | 0 | $3 \pm 1$ |
| 0 | 0 | $6 \pm 4$ | $3 \pm 3$ | $1 \pm 1$ | 0 | $2 \pm 1$ |
| $2 \pm 2$ | $9 \pm 5$ | $4 \pm 3$ | $3 \pm 2$ | $2 \pm 1$ | 0 | $3 \pm 1$ |
| 0 | $6 \pm 6$ | $4 \pm 3$ | $5 \pm 3$ | $3 \pm 2$ | $1 \pm 1$ | $2 \pm 1$ |
| $4 \pm 4$ | $4 \pm 3$ | 0 | $1 \pm 1$ | $2 \pm 1$ | $1 \pm 1$ | $2 \pm 1$ |
| 0 | $3 \pm 2$ | $4 \pm 4$ | $1 \pm 1$ | $1 \pm 1$ | $2 \pm 1$ | $2 \pm 1$ |
| 0 | 0 | 0 | 0 | $3 \pm 2$ | $3 \pm 1$ | $1 \pm 1$ |
| 0 | 0 | 0 | 0 | $2 \pm 1$ | 0 | $1 \pm 1$ |
| $39 \pm 6$ | $26 \pm 3$ | $16 \pm 2$ | $10 \pm 2$ | $5 \pm 1$ | $2 \pm 1$ | $21 \pm 2$ |



Fig. 1. Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}, 4.1<E_{\gamma}<6.2 \mathrm{GeV}$. $\mathrm{a} . \mathrm{d} \sigma / \mathrm{d} M_{\pi \pi}$ in $\mu \mathrm{b} / \mathrm{GeV}$. The curve is a fit with model (a). b. $\mathrm{d} \sigma / \mathrm{d} t_{\mathrm{pp}}$ in $\mu \mathrm{b} / \mathrm{GeV}^{2}$.
conserving p-wave. The structure in the $Y_{4}^{0}$ moment at $M_{\pi \pi}<M_{\mathrm{p}}$ is suggestive of an interference between diffractive $\rho^{0}$ production and a Drell-type background amplitude [5]. It was checked that this structure is not a statistical effect induced by the strongly peaking $Y_{2}^{\mathrm{o}}$ moment.
Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}, 4.1<E_{\gamma}<6.2 \mathrm{GeV}$.

| Model | $\sigma\left(\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\mathrm{o}}\right)$ <br> $(\mu \mathrm{b})$ | $A$ <br> $\left(\mathrm{GeV}^{-2}\right)$ | $B$ <br> $\left(\mathrm{GeV}^{-4}\right)$ | $\mathrm{d} \sigma\left(\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\mathrm{o}}\right)$ <br> $\mathrm{d} t$ | $M_{\rho}$ <br> $\left(\mu \mathrm{b} / \mathrm{GeV}^{2}\right)$ | $\Gamma_{\rho}$ <br> $(\mathrm{GeV})$ | $\sigma\left(\gamma \mathrm{p} \rightarrow \Delta^{++} \pi^{-}\right)$ <br> $(\mu \mathrm{GeV})$ | $\sigma\left(\gamma \mathrm{p} \rightarrow \Delta^{\mathrm{o}} \pi^{+}\right)$ <br> $(\mu \mathrm{b})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | $18.1 \pm 1.5$ | $8.9 \pm 0.4$ |  | $156 \pm 15$ | 0.762 | 0.133 | $1.1 \pm 0.2$ | $0.4 \pm 0.1$ |
| (b) | $15.2 \pm 1.4$ | $8.0 \pm 0.5$ |  | $135 \pm 19$ | 0.762 | 0.133 | $0.9 \pm 0.3$ |  |
| (c) | $17.0 \pm 2.0$ | $9.7 \pm 0.8$ | $2.3 \pm 0.2$ | $159 \pm 20$ | 0.765 | 0.155 | $1.0 \pm 0.15$ | $0.5 \pm 0.1$ |

$\rho^{0}$ and $\Delta$ production cross section in terms of three models.
a)




$$
M_{\pi \pi}\left[\mathrm{G}_{\mathrm{e}} \mathrm{~V}\right]
$$

Fig. 2. 4.1 $<E_{\gamma}<6.2 \mathrm{GeV}$. a. Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\circ}$, density matrix elements of $\rho^{\circ}$ as a function of $t_{\mathrm{pp}}$. b. Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}$, moments $\Sigma Y_{2}^{\mathrm{o}}\left(\Omega_{i}\right)$ and $\Sigma Y_{4}^{\mathrm{o}}\left(\Omega_{i}\right)$ as a function of $M_{\pi \pi}$ for $t_{\mathrm{pp}}<0.5 \mathrm{GeV}^{2}$ (the sum is taken over all events).

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