Searching for BSM neutrino interactions in dark matter detectors

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Neutrino interactions beyond the Standard Model (BSM) are theoretically well motivated and have an important impact on the future precision measurement of neutrino oscillation. In this work, we study the sensitivity of a multi-ton-scale liquid Xenon dark matter detector equipped with an intense radioactive neutrino source to various BSM neutrino-electron interactions. We consider the conventional Non-Standard Interactions (NSIs), other more generalized four-fermion interactions including scalar and tensor forms, and light-boson mediated interactions. The work shows that with realistic experimental setups, one can achieve unprecedented sensitivity to these BSM neutrinoelectron interactions.

I. INTRODUCTION

The existence of small neutrino masses is calling for new physics. It is fairly reasonable to speculate that the interactions of neutrinos may also go beyond the Standard Model (BSM). Searching for BSM neutrino interactions is of increasing importance since they could make a considerable impact on future precision oscillation measurements. For example, it is known that the Non-Standard Interactions [1–4] of neutrinos may affect the measurement of δ_{CP} in long-baseline oscillation experiments [5–12]. Moreover, due to various well-known problems of the SM, theorists have for decades been looking for more satisfactory theories. As neutrino masses and mixing have become established, precision measurement of neutrino interactions are increasingly important in directing theoretical exploration.

Actually, if BSM neutrino interactions exist, charged leptons such as the electron are very likely to participate in these interactions as well, since neutrinos and charged leptons are embedded in $SU(2)_L$ doublets in the SM, and new interactions are generally expected to couple with the whole doublet. Many BSM theories such as Type II seesaw models [13–18], left-right symmetric models [19–21], and the various U(1) extensions [22–28], are some typical examples which introduce new interactions between neutrinos and charged leptons.

Therefore, searching for neutrino-electron BSM interactions is theoretically highly motivated and has been extensively studied in the literature [29–44]. So far the most precise measurement for $\nu_{\mu}(\bar{\nu}_{\mu})$ -e elastic scattering¹, comes from the CHARM II experiment [45, 46], which achieved a precision of 3%. For ν_e -e and $\bar{\nu}_e$ -e scattering, the best measurements come from LSND [47] and TEXONO [30] respectively, with only 20% precision. Recently there have been proposals [48–52] to using dark matter detectors with intense radioactive neutrino sources to measure neutrino scattering, that could lead to significant improvements. In particular, ton-scale liquid xenon (LXe) detectors [53–55] equipped with state-of-the-art ⁵¹Cr sources [56] (referred to as ⁵¹Cr-LXe throughout this paper), with their combination of a large mono-energetic ν_e flux, high electron density, and low backgrounds, offer a path to reaching unprecedented precision.

In this paper, we study the potential of ⁵¹Cr-LXe experiments for probing BSM neutrino interactions. Our previous study [52] showed that the combination of a 5 MCi ⁵¹Cr source and a 6 ton LXe detector could generate the tightest terrestrial constraint on neutrino magnetic moments, and competitive sensitivity to sterile neutrino oscillation. Therefore, we expect similar setups would have excellent sensitivity to a wide range of BSM neutrino interactions, including Non-Standard Interactions (NSIs), general four-fermion effective interactions (e.g., including tensor and scalar forms), and light and weakly coupled mediators (e.g. dark photons). The new physics scenarios considered in this work can also be tested in some other low-energy processes such as coherent elastic neutrino-nucleus scattering (CE ν NS) and atomic parity violation (APV)—for a recent study, see Ref. [57]. The main difference is that CE ν NS and APV test interactions between neutrinos and electrons. Although phenomenologically they are different, theoretically these interactions would be very closely correlated in some models. So combining both types of low-energy measurements could provide a complementary test of BSM theories.

The paper is organized as follows. In Sec. II, we introduce the basic experimental setup and evaluate the event rates of signals and backgrounds for several configurations. In Sec. III, we study the precision measurement of the SM parameters relevant to neutrino interactions. In Sec. IV, we include sensitivity studies for several types of BSM

¹ Quasi-elastic scattering processes such as $\nu_{\mu(\tau)} + e \rightarrow \mu(\tau) + \nu_e$ have little potential of finding new physics since the corresponding charged current interactions have been very precisely determined by μ and τ decays.

neutrino interactions which are widely discussed in the literature. Finally, we conclude and summarize the results in Sec. V.

II. EVENT RATES

Let us consider a general ⁵¹Cr-LXe experiment and evaluate the event numbers of ν -e scattering. In the ⁵¹Cr-LXe experiment, the number of ν -e scattering events appearing in the infinitesimal volume dV around position $\vec{r} \equiv (x, y, z)$ in the detector, during the time interval t to t + dt, with the recoil energy from T to T + dT can be evaluated as

$$dN = dV n_e dt dT \left[\int \phi \left(\vec{r}, t, E_\nu \right) \frac{d\sigma}{dT} \left(T, E_\nu \right) dE_\nu \right], \tag{1}$$

where n_e , ϕ , $\frac{d\sigma}{dT}$, and E_{ν} denote the electron number density, the neutrino flux, the differential cross section, and the neutrino energy respectively.

For a point-like radioactive source, ϕ has the following spatial and temporal dependence:

$$\phi\left(\vec{r}, t, E_{\nu}\right) = \phi_0 R_{\text{Cr51}}^0 \frac{1\,\text{m}^2}{r^2} e^{-t/\tau} f\left(E_{\nu}\right),\tag{2}$$

where

$$\phi_0 = 2.94 \times 10^{15} \text{ neutrinos/(MCi m}^2 \text{s}), \tag{3}$$

is the neutrino flux at 1 meter from a 1 MCi radioactive source; $\tau = 39.96$ days is the mean lifetime of ⁵¹Cr; R_{Cr51}^0 is the initial (t = 0) radioactivity; and $f(E_{\nu})$ describes the spectral shape, normalized by $\int f(E_{\nu})dE_{\nu} = 1$. The neutrino spectrum of ⁵¹Cr simply consists of mono-energetic neutrino emissions at 750 keV (90%) and 430 keV (10%):

$$f(E_{\nu}) = 0.9\,\delta(E_{\nu} - 750\,\mathrm{keV}) + 0.1\,\delta(E_{\nu} - 430\,\mathrm{keV}). \tag{4}$$

Since the source decays exponentially, it is useful to define a time-averaged activity,

$$\langle R_{\rm Cr51} \rangle \equiv \frac{R_{\rm Cr51}^0}{\Delta t} \int_0^{\Delta t} dt e^{-t/\tau} = \frac{\tau R_{\rm Cr51}^0}{\Delta t} \left[1 - e^{-\Delta t/\tau} \right],\tag{5}$$

relative to the initial activity, R_{Cr51}^0 , and the exposure time, Δt . Likewise, an average distance between the detector and the source, r_{avg} , can be defined as:

$$\frac{1}{r_{\rm avg}^2} \equiv \langle \frac{1}{r^2} \rangle = \frac{1}{V} \int \frac{dV}{r^2}.$$
(6)

With these averaged values, it is equivalent use the following replacement in our analyses:

$$\phi(\vec{r}, t, E_{\nu}) \to \phi_0 \frac{1\,\mathrm{m}^2}{r_{\mathrm{avg}}^2} \langle R_{\mathrm{Cr51}} \rangle f(E_{\nu}) \equiv \phi_{\mathrm{avg}}(E_{\nu}), \qquad (7)$$

while collapsing the time and space integrals to the Δt and the detector fiducial volume, V. Hence the number of events in the recoil energy bin $[T_i, T_i + \Delta T]$ can be written as

$$N_i = V n_e \,\Delta t \,\int_{T_i}^{T_i + \Delta T} \Phi(T) dT,\tag{8}$$

with

$$\Phi(T) \equiv \int \phi_{\text{avg}} \left(E_{\nu} \right) \frac{d\sigma}{dT} \left(T, \ E_{\nu} \right) dE_{\nu}, \tag{9}$$

where $\phi_{\text{avg}}(E_{\nu})$ has been defined in Eq. (7).

For a detector with a cylindrical fiducial region, r_{avg} can be computed analytically (see Appendix A). We take the same geometrical profile as Ref. [52], i.e., the height (h) and diameter (d) of the cylinder are h = d = 1.38 m, and

the source is L = 1 m below the bottom. Using Eq. (A5), this profile has $r_{\text{avg}} = 1.63$ m and contains 6 tons of LXe, which corresponds to $Vn_e = 1.5 \times 10^{30}$ electrons.

Plugging in the definition of ϕ_{avg} , the integral in Eq. (9) works out as

$$\Phi(T) = \frac{1\,\mathrm{m}^2}{r_{\mathrm{avg}}^2} \langle R_{\mathrm{Cr51}} \rangle \phi_0 \left[0.9 \, \frac{d\sigma}{dT} (T, \ E_\nu = 750 \,\mathrm{keV}) + 0.1 \, \frac{d\sigma}{dT} (T, \ E_\nu = 430 \,\mathrm{keV}) \right]. \tag{10}$$

In practical calculations, we also need the maximal recoil energy, $T_{\rm max}$, which is defined as the maximal recoil of electron that can be generated by a certain E_{ν} :

$$T_{\rm max} = \frac{2E_{\nu}^2}{2E_{\nu}^2 + m_e} \approx \begin{cases} 559 \text{ keV} & (E_{\nu} = 750 \text{ keV}) \\ 270 \text{ keV} & (E_{\nu} = 430 \text{ keV}) \end{cases}.$$
 (11)

For $T > T_{\text{max}}$ the corresponding $\frac{d\sigma}{dT}$ in Eq. (10) is set to zero. In Tab. I, we summarize useful quantities for the configurations considered in this work. The event numbers with the SM ν -e elastic scatting cross section [58] are evaluated using Eq. (8) and presented in Fig. 1. Regarding backgrounds, we assume a "normal" level [59], which includes the solar neutrino background and decays of embedded radioactive isotopes (¹³⁶Xe, ⁸⁵Kr, ²²²Rn, etc.), for configuration A; and a "¹³⁶Xe depleted" level, which consists of the normal solar background with only 10% of the normal level from radioactive decays, for configurations B and C. In configurations B and C, the background rate is further decreased by halving the exposure time, Δt . Finally, in configuration C, the signal-to-noise ratio is further increased by the use of a more intense source.

III. MEASUREMENT OF THE SM PARAMETERS

The study of neutrino-electron scattering has played an important role in the precision electroweak tests of the SM—see Chapter 10 of PDG [60]. For instance, the CHARM II experiment, which has performed the most precise measurement of ν_{μ} -e and $\overline{\nu}_{\mu}$ -e scattering thus far, has determined the electroweak mixing angle, $\sin^2 \theta_W$, to be:

$$\sin^2 \theta_W = 0.2324 \pm 0.0083, \text{ (CHARM II, 1994)},$$
 (12)

with about 3% precision [46]. In comparison $\stackrel{(-)}{\nu_e}$ scattering experiments have not yet achieved such precision. The best measurements of ν_e -e and $\overline{\nu}_e$ -e scattering come from LSND [47] and TEXONO [30] respectively:

$$\sin^2 \theta_W = \begin{cases} 0.248 \pm 0.051 & (\nu_e \cdot e \text{ LSND}) \\ 0.251 \pm 0.031 \pm 0.024 & (\overline{\nu}_e \cdot e \text{ TEXONO}) \end{cases}.$$
(13)

We will show that a ⁵¹Cr-LXe experiment could provide a superior precision measurement of $\sin^2 \theta_W$, which not only exceeds that of these aforementioned experiments, but also reverses the current situation in which $\nu_{e}^{(-)}$ scattering is less precise than $\overset{(-)}{\nu_{\mu}}$ scattering.

In the SM, the low energy interactions of neutrinos and electrons can be described by the effective Lagrangian

$$\mathcal{L}_{\rm NC+CC} \supset \frac{G_F}{\sqrt{2}} \overline{\nu}_e \gamma^\mu (1 - \gamma^5) \nu_e \overline{\psi_e} \gamma^\mu \left[g_V - g_A \gamma^5 \right] \psi_e, \tag{14}$$

where, for ν_e -e scattering, g_V^e and g_A^e are given at the tree level by

$$g_V^e = 2\sin^2\theta_W + \frac{1}{2} \text{ and } g_A^e = \frac{1}{2},$$
 (15)

	$R^0_{ m Cr51}$	Δt	$\langle R_{\rm Cr51} \rangle$	background	$r_{\rm avg}$	Vn_e
Configuration A	5 MCi $^{51}\mathrm{Cr}$	100 days	1.83 MCi	normal	$1.63 \mathrm{~m}$	1.5×10^{30}
Configuration B	5 MCi $^{51}\mathrm{Cr}$	50 days	$2.85 \mathrm{MCi}$	¹³⁶ Xe depleted	$1.63 \mathrm{~m}$	1.5×10^{30}
Configuration C	$10~{\rm MCi}~^{51}{\rm Cr}$	$50 \mathrm{~days}$	$5.71 \mathrm{MCi}$	136 Xe depleted	$1.63 \mathrm{~m}$	1.5×10^{30}

Table I. Configurations of the ⁵¹Cr-LXe experiment considered in this work.

which includes both the neutral current (NC) and the charged current (CC) contributions. At the tree level, the differential cross section for ν -e scattering is given by [58]:

$$\frac{d\sigma}{dT} = \frac{m_e G_F^2}{2\pi} \left[g_1^2 + g_2^2 \left(1 - \frac{T}{E_\nu} \right)^2 - g_1 g_2 \frac{m_e T}{E_\nu^2} \right],\tag{16}$$

where T is the electron's recoil energy and

$$g_1 \equiv g_V + g_A \quad \text{and} \quad g_2 \equiv g_V - g_A. \tag{17}$$

The experimental value of $\sin^2 \theta_W$ is well determined at the Z-pole and found to be 0.23122 (defined in the Modified Minimal Subtraction ($\overline{\text{MS}}$) scheme [60]). At low energies ($\leq 0.1 \text{ GeV}$), its value can be extrapolated theoretically using renormalization group equation (RGE) running [61]:

$$\sin^2 \theta_W \approx 0.23865$$
 (low energy limit). (18)

Including the radiative corrections, the expressions of g_V and g_A should also be modified [62]:

$$g_V^e \approx 2.00128 \sin^2 \theta_W + 0.4828$$
 and $g_A^e \approx 0.4936$. (19)

Taking $\sin^2 \theta_W$ as a varying parameter, one can measure it in the ⁵¹Cr-LXe experiment, as a low-energy precision test of the SM. The simulated data is generated assuming the numerical values in Eqs. (18) and (19), and including the backgrounds shown in Fig. 1. Then we perform a χ^2 -fit on the data to obtain the 1 σ confidence level (CL) of $\sin^2 \theta_W$. The results are presented in Fig. 2 and Tab. II. Comparing these results with the current state-of-the-art from CHARM II, LSND, and TEXONO, we see that the ⁵¹Cr-LXe experiment is able to reach unprecedented precision on $\sin^2 \theta_W$ as measured by ν -e scattering, even in the least sensitive configuration that we have considered.

In Fig. 2, we show the role of 51 Cr-LXe measurements in probing the RGE running of $\sin^2 \theta_W$. So far, the most precise measurements of $\sin^2 \theta_W$ are from colliders, including LEP, LHC, SLC, and Tevatron. All the colliders essentially measure the value of $\sin^2 \theta_W$ only at the Z-pole scale. Other measurements, including the weak charge of protons (Q_{weak}), Atomic Parity Violation (APV), and electron deep-inelastic scattering (eDIS), are located at various lower energy scales. This plot shows that a precision probe of the RGE running of $\sin^2 \theta_W$, is still needed at the lowest energies, which a 51 Cr-LXe measurement (marked in red as LXe-A, B and C) would provide.

The ⁵¹Cr-LXe experiment would also provide a high precision measurement of the weak coupling parameters g_V^e and g_A^e . We performed a simultaneous χ^2 -fit of g_V^e and g_A^e based on Eqs. (16) and (17). Fig. 3 shows the fit result in



Figure 1. Signal compared to background in the 51 Cr-LXe experiment. Three configurations (A, B, C) are considered, with the details described in Tab. I. Configurations B and C have much larger signal/background ratios than A.



Figure 2. Measurement of $\sin^2 \theta_W$ at different energy scales (μ). The red error bars represent the precision of LXe-A, LXe-B, and LXe-C expected from this work. The other measurements are from Fig. 10.2 of the PDG [60]. Measurements from earlier neutrino elastic scattering experiments do not have sufficient precision to be included in this plot.

the (g_V^e, g_A^e) plane, and compares it with the measurements from TEXONO, LSND, and CHARM II, where for $\nu_{\mu}^{(-)} - e$ scattering measurements of CHARM II, the weak coupling constants are converted using $g_V^e = g_V^{\mu} + 1$ and $g_A^e = g_A^{\mu} + 1$. Due to low statistics, TEXONO and LSND appear as long bands, which are mainly determined by the total event numbers with little impact from spectral information. In other words, TEXONO and LSND effectively measured only the total cross section since their low-statistics measurements were not sensitive to spectral distortions from variations of g_V and g_A . The CHARM II measurement, which has much higher statistics, gives $g_V^{\mu} = -0.035 \pm 0.017$ and $g_A^{\mu} = -0.503 \pm 0.017$ (see the overlap of two orange bands). However, since the neutrino energy is much higher than the electron mass in CHARM II, it also has some discrete parameter degeneracy—the cross section is approximately invariant when $(g_V^{\mu}, g_A^{\mu}) \rightarrow (g_A^{\mu}, g_V^{\mu})$ and exactly invariant under $(g_V^{\mu}, g_A^{\mu}) \rightarrow (-g_V^{\mu}, -g_A^{\mu})$. For the ⁵¹Cr-LXe experiment, depending on the signal/background ratio, similar situation may appear as well. This can be understood by reformatting the cross section in powers of T/E_{ν} :

$$\frac{d\sigma}{dT} = \frac{m_e G_F^2}{2\pi} \left[\left(g_1^2 + g_2^2 \right) - \left(2g_2^2 + g_1 g_2 \frac{m_e}{E_\nu} \right) \frac{T}{E_\nu} + g_2^2 \left(\frac{T}{E_\nu} \right)^2 \right],\tag{20}$$

which implies that for low recoil energies $(T/E_{\nu} \ll 1)$ we essentially measure only $g_1^2 + g_2^2$, while higher energy recoils are also sensitive to $2g_2^2 + g_1g_2\frac{m_e}{E_{\nu}}$. With these two factors determined, (g_1, g_2) would be approximately known up to some discrete ambiguities. This explains why configurations A and B have two separate low- $\Delta\chi^2$ regions, while for configuration C, this degeneracy is broken by the higher signal/background measurement, which is also sensitive to the quadratic term in T/E_{ν} .

	Configuration A	Configuration B	Configuration C
precision of $\sin^2 \theta_W$	0.23865 ± 0.0055	$0.23865^{+0.0041}_{-0.0037}$	$0.23865^{+0.0023}_{-0.0031}$
relative precision	$\pm 2.3\%$	$^{+1.7\%}_{-1.6\%}$	$^{+1.0\%}_{-1.3\%}$

Table II. Precision of the $\sin^2 \theta_W$ measurement in the three ⁵¹Cr-LXe configurations considered.

IV. BSM NEUTRINO INTERACTIONS

In many BSM theories, neutrinos have new interactions, which can be categorized into two types, (i) interactions mediated by heavy particles, and (ii) interactions mediated by light particles.

For heavy mediators, one can integrate them out and study the effective four-fermion interactions. As a modelindependent approach, one can write down all possible effective four-fermion interactions of neutrinos with electrons (as we are considering elastic neutrino-electron scattering). The most extensively studied effective interactions are the Non-Standard Interactions (NSIs, reviewed in [1–4]) which lead to interesting phenomenology in neutrino oscillations. In addition, one can consider the most general four-fermion operators with all possible Lorentz invariant forms considered, including Scalar, Pseudoscalar, Vector, Axialvector, and Tensor (SPVAT) interactions [29, 33, 35, 63–72]. We will study the sensitivity of a 51 Cr-LXe experiment to both frameworks.

For light mediators, the interactions can be much more multifarious. As a demonstration of light mediator sensitivity, we will study a light Z' with a very weak gauge coupling. Such a scenario is particular important for dark matter studies [73–84] since additional U(1) symmetries have been widely used to stabilize the dark mater candidates.

A. Non-Standard Interactions

NSIs in ν -e scatting are usually formulated by the following Lagrangian:

$$\mathcal{L}_{\rm NSI} \supset 2\sqrt{2}G_F \overline{\nu}_{\alpha} \gamma^{\mu} P_L \nu_{\beta} \overline{\psi_e} \gamma^{\mu} \left[\epsilon^L_{\alpha\beta} P_L + \epsilon^R_{\alpha\beta} P_R \right] \psi_e, \tag{21}$$

where ψ_e is the Dirac spinor of the electron, $\epsilon^L_{\alpha\beta}$ and $\epsilon^R_{\alpha\beta}$ are flavor-dependent constants, and $P_{L/R} \equiv (1 \mp \gamma^5)/2$. This Lagrangian originates in some models with heavy vector bosons that interact with neutrinos and electrons (see, e.g., [85]). In addition, purely scalar interactions can also generate NSIs at the loop level, and these loop-induced NSI could potentially be very large in the presence of some secret neutrino-scalar interactions [86].

Including NSIs, the cross section of ν_e -e scattering can be derived by summing the cross sections of the three processes $\nu_e + e \rightarrow \nu_\alpha + e$, where $\alpha = e, \mu$ or τ , which is

$$\frac{d\sigma}{dT} = \frac{m_e G_F^2}{2\pi} \left[\tilde{g}_1^2 + \tilde{g}_2^2 \left(1 - \frac{T}{E_\nu} \right)^2 - x_{12} \frac{m_e T}{E_\nu^2} \right],\tag{22}$$



Figure 3. Sensitivity of ⁵¹Cr-LXe experiment to weak couplings parameters, g_V^e and g_A^e , compared to existing constraints. The solid blobs represent the expected constraints, centered on the SM values, for the LXe-A, LXe-B, and LXe-B configurations in this work. Prior constraints from TEXONO (blue) and LSND (red) are taken from Fig. 10.1 of PDG [60], and the CHARM II constraint comes from Ref. [46].



Figure 4. Sensitivity at 90% CL of a ⁵¹Cr-LXe experiment on the NSI parameters, compared to the existing bounds from the LSND and TEXONO experiments [87].

Table III. Current NSI bounds from Ref. [3] compared with future ⁵¹Cr-LXe bounds (Configs. A, B, and C).

	ϵ^P_{ee}	$\epsilon^P_{e\mu}$	$\epsilon^P_{e au}$
known bounds $(P = L)$	$[-0.021, \ 0.052]$	$[-0.13, \ 0.13]$	$[-0.33, \ 0.33]$
known bounds $(P = R)$	$[-0.07, \ 0.08]$	$[-0.13, \ 0.13]$	$[-0.19, \ 0.19]$
Config. A $(P = L)$	$[-0.017, \ 0.015]$	$[-0.14, \ 0.14]$	$[-0.14, \ 0.14]$
Config. A $(P = R)$	$[-0.10, \ 0.08]$	$[-0.17, \ 0.17]$	$[-0.17, \ 0.17]$
Config. B $(P = L)$	$[-0.009, \ 0.009]$	$[-0.12, \ 0.12]$	[-0.12, 0.12]
Config. B $(P = R)$	$[-0.06, \ 0.05]$	$[-0.16, \ 0.16]$	$[-0.16, \ 0.16]$
Config. C $(P = L)$	$[-0.006, \ 0.006]$	$[-0.09, \ 0.09]$	$[-0.09, \ 0.09]$
Config. C $(P = R)$	$[-0.040, \ 0.036]$	$[-0.13, \ 0.13]$	$[-0.13, \ 0.13]$

with $\tilde{g}_{1}^{2}, \, \tilde{g}_{1}^{2}$ and x_{12} defined as

$$\tilde{g}_1^2 \equiv \left(g_V + g_A + 2\epsilon_{ee}^L\right)^2 + \sum_{\beta \equiv u\,\tau} \left(2\epsilon_{e\beta}^L\right)^2,\tag{23}$$

$$\tilde{g}_2^2 \equiv \left(g_V - g_A + 2\epsilon_{ee}^R\right)^2 + \sum_{\beta = \mu, \tau} \left(2\epsilon_{e\beta}^R\right)^2,\tag{24}$$

$$x_{12} \equiv \left(g_V + g_A + 2\epsilon_{ee}^L\right) \left(g_V - g_A + 2\epsilon_{ee}^R\right) + \sum_{\beta = \mu, \tau} \left(2\epsilon_{e\beta}^L\right) \left(2\epsilon_{e\beta}^R\right).$$
(25)

Note that there is no interference between the three processes because they have different flavor neutrinos in the final state. But for $\alpha = e$, there is interference between the NSI and the SM interactions, which significantly enhances the sensitivity to ϵ_{ee}^{L} and ϵ_{ee}^{R} .

sensitivity to ϵ_{ee}^{2} and ϵ_{ee}^{2} . In Fig. 4, we present the result of a χ^{2} -fit analysis on the NSI sensitivity. The χ^{2} -fit is performed each time for a pair of $(\epsilon_{e\alpha}^{L}, \epsilon_{e\alpha}^{R})$ with the other ε 's set to zero. Because the cross section is completely symmetric under the μ - τ exchange, ν_{e} -e scattering should have exactly the same sensitivities to $(\epsilon_{e\mu}^{L}, \epsilon_{e\mu}^{R})$ and to $(\epsilon_{e\tau}^{L}, \epsilon_{e\tau}^{R})$. So they are shown in the same plot in the right panel. As we can see, $(\epsilon_{ee}^{L}, \epsilon_{ee}^{R})$ would be stringently constrained by the ⁵¹Cr-LXe experiment while $(\epsilon_{e\mu}^{L}, \epsilon_{e\mu}^{R})$ and to $(\epsilon_{e\tau}^{L}, \epsilon_{e\tau}^{R})$ would be less constrained due to the lack of interference.

The ⁵¹Cr-LXe bounds are compared to the current known bounds on NSIs. In general, direct measurements of neutrino-electron scattering and measurements of neutrino oscillation are sensitive to the NSIs considered here. In

particular, there have been bounds from LSND and TEXONO that can be readily superposed on our results, as shown in Fig. 4. As for other bounds, we refer to Ref. [3] for the recently updated summary, which have been included in Tab. III. We conclude that for most NSIs parameters, the ⁵¹Cr-LXe sensitivity to NSIs would generally exceed the current known bounds.

B. SPVAT interactions

More generally one can adopt an effective field theory (EFT) approach to study BSM neutrino interactions and write down all the possible Lorentz invariant operators as follows:

$$\mathcal{L} \supset \frac{G_F}{\sqrt{2}} \sum_{a=S,P,V,A,T} \overline{\nu} \Gamma^a \nu \left[\overline{\psi_e} \Gamma^a (C_a + D_a i_a \gamma^5) \psi_e \right], \tag{26}$$

with

$$\left(\Gamma^{S}, \ \Gamma^{P}, \ \Gamma^{V}, \ \Gamma^{A}, \ \Gamma^{T}\right) \equiv \left(\mathbf{1}, \ i\gamma^{5}, \ \gamma^{\mu}, \ \gamma^{\mu}\gamma^{5}, \ \sigma^{\mu\nu} \equiv \frac{i}{2}[\gamma^{\mu}, \gamma^{\nu}]\right).$$
(27)

Here C_a and D_a are real constants if $i_a = i$ for a = S, P and T; and $i_a = 1$ for a = V and A. It should be noted that this reduces to the SM Lagrangian when $(C_V, D_V, C_A, D_A) = (g_V, -g_A, g_A, -g_V)$ and all other C_a and D_a are zero.

Regarding theoretical motivations, the first four types (a = S, P, V and A) could originate from integrating out some heavy scalar or vector mediators. The tensor interactions could be generated by integrating out heavy charged scalar mediators following necessary the Fierz transformations [88]. For Dirac neutrinos, all the SPVAT interactions could exist with 10 free parameters (C_a, D_a) in Eq. (26). For Majorana neutrinos, there are further constraints on the SPVAT interactions such that the allowed parameter space is actually smaller, containing only 6 free parameters [33]. Such a difference could be used to distinguish between Dirac and Majorana neutrinos [89]. In this work, we will ignore the additional constraints of Majorana neutrinos and simply take the full parameter spaces containing 10 parameters into consideration.

In this model space, the cross section of ν_e -e scattering is given as follows [33]:

$$\frac{d\sigma}{dT} = \frac{m_e G_F^2}{2\pi} \left[x_1 + 2x_2 (1 - \frac{T}{E_\nu}) + x_3 (1 - \frac{T}{E_\nu})^2 + x_4 \frac{MT}{4E_\nu^2} \right],\tag{28}$$

where

$$x_{1} \equiv \frac{1}{4} \left(C_{A} - D_{A} + C_{V} - D_{V} \right)^{2} + \frac{1}{2} C_{P} C_{T} + \frac{1}{8} \left(C_{P}^{2} + C_{S}^{2} + D_{P}^{2} + D_{S}^{2} \right) - \frac{1}{2} C_{S} C_{T} + C_{T}^{2} + \frac{1}{2} D_{P} D_{T} - \frac{1}{2} D_{S} D_{T} + D_{T}^{2},$$
(29)

$$x_2 \equiv -\frac{1}{8} \left(C_P^2 + C_S^2 + D_P^2 + D_S^2 \right) + C_T^2 + D_T^2, \tag{30}$$

$$x_3 \equiv \frac{1}{4} \left(C_A + D_A - C_V - D_V \right)^2 - \frac{1}{2} C_P C_T + \frac{1}{8} \left(C_P^2 + C_S^2 + D_P^2 + D_S^2 \right)$$

$$+\frac{1}{2}C_T C_S + C_T^2 - \frac{1}{2}D_P D_T + \frac{1}{2}D_S D_T + D_T^2,$$
(31)

$$x_4 \equiv -(C_V - D_A)^2 + (C_A - D_V)^2 + C_S^2 - 4C_T^2 + D_P^2 - 4D_T^2.$$
(32)

In our analysis we are interested in extracting the non-SM part, so in our χ^2 -fit we define

$$(\delta C_a, \ \delta D_a) \equiv (C_a, \ D_a) - (C_a, \ D_a)^{\text{SM}},\tag{33}$$

and make a 2-parameter fit for each pair of $(\delta C_a, \delta D_a)$. The result is presented in Fig. 5. For a = S or P, the ⁵¹Cr-LXe experiment would reach sensitivity around $0.5 \sim 2$. For the other cases, the measurement could be even more precise. Note that for a = V or A, there is parameter degeneracy which would be removed in configuration C. The situation is similar to Fig. 3, with the reason explained at the end of Sec. III.



Figure 5. Constraints on the SPVAT parameters. The color coding is the same as Fig. 4.



Figure 6. Constraints on the gauge coupling of light Z'. The constraints of TEXONO, CHARM II, and GEMMA are taken from Ref. [34], other constraints are taken from Refs. [49, 90]. The green dashed curve is for ⁵¹Cr-LXe with configuration A, and dot-dashed for configuration C. Configuration B is not shown here for simplicity, which should be between the dashed and dot-dashed curves.



Figure 7. Constraints on the mass mixing α and kinetic mixing ϵ of light Z'. The constraints of TEXONO, CHARM II, and GEMMA are taken from Ref. [34]. The green dashed curve is for ⁵¹Cr-LXe with configuration A, and dot-dashed for configuration C. Configuration B is not shown here for simplicity, which should be between the dashed and dot-dashed curves.

C. light Z'

Recently a generic light neutral vector boson (commonly referred to as light Z') has received extensive research interest due to its connection with dark matter [73–84]. Elastic neutrino scattering is intrinsically sensitive to light mediators which usually show effect only in soft (low-momentum transfer) scattering processes, where, for most other particles, the electromagnetic force would be an overwhelming background. Due to their very weak SM interaction, neutrino scattering makes a very clean environment for probing new forces mediated by other light mediators [34, 44, 68, 71, 90–94]. The Lagrangian of light Z' that concerns ν -e scattering is generally formulated as follows

$$\mathcal{L} \supset -\frac{g_{Z'}}{2} Z'_{\mu} \left[\overline{\nu} \gamma^{\mu} \nu + \overline{\ell} \gamma^{\mu} \ell \right] - \frac{1}{2} m_{Z'}^2 Z'_{\mu} Z'^{\mu}, \tag{34}$$

where $g_{Z'}$ is the gauge coupling and ℓ is a charged lepton. Depending on the models, there could be different charge assignments. Here we simply assume the charge assignments are the same as the $U(1)_{B-L}$ model (i.e., all leptons have the same charge). In generic Z' models, the Z' boson has both kinetic mixing and mass mixing with the SM Z^0 boson. As it has been studied in Ref. [64], in the presence of both mixing, the Z' and Z^0 interactions can be formulated as

$$\mathcal{L} \supset J_Z^{\mu} Z_{\mu} + J_{Z'}^{\mu} Z_{\mu}', \tag{35}$$

where J_Z^{μ} and $J_{Z'}^{\mu}$ are mixtures of the SM neutral current $J_{\rm NC}$ and a new current J_X :

$$J_{Z'}^{\mu} = c_{\alpha} J_{\rm NC}^{\mu} - s_{\alpha} J_{X}^{\mu}, \tag{36}$$
$$J_{Z'}^{\mu} = s_{\alpha} J_{\rm NC}^{\mu} + c_{\alpha} J_{Y}^{\mu}. \tag{37}$$

$$J_{Z'}^{r} = s_{\alpha} J_{\rm NC}^{r} + c_{\alpha} J_{X}^{r}. \tag{37}$$

Here α is the mass mixing angle with $(c_{\alpha}, s_{\alpha}) \equiv (\cos \alpha, \sin \alpha)$. The leptonic part of the SM neutral current $J_{\rm NC}^{\mu}$ is

$$J_{\rm NC}^{\mu} = \frac{g}{c_W} \left[\overline{\nu}_L \gamma^{\mu} \frac{1}{2} \overline{\nu}_L + \overline{e}_L \gamma^{\mu} \frac{2s_W^2 - 1}{2} \overline{e}_L + \overline{e}_R \gamma^{\mu} s_W^2 \overline{e}_R + \cdots \right],\tag{38}$$

while the explicit form of J_X^{μ} is given by [64]:

$$J_X^{\mu} = \frac{1}{2c_W\sqrt{1-\epsilon^2}} \left[\overline{\nu}\gamma^{\mu} \left(-c_W g_{Z'} \right) \overline{\nu} + \overline{\nu}_L \gamma^{\mu} \left(g\epsilon s_W \right) \overline{\nu}_L + \overline{e}\gamma^{\mu} \left(-c_W g_{Z'} + g\epsilon s_W \right) \overline{e} + \overline{e}_R \gamma^{\mu} \left(g\epsilon s_W \right) \overline{e}_R + \cdots \right].$$
(39)

The kinetic mixing ϵ is defined as $L \supset -\frac{1}{2}\epsilon F^{\mu\nu}F'_{\mu\nu}$ where $F^{\mu\nu}$ and $F'_{\mu\nu}$ are the gauge field tensors of the SM $U(1)_Y$ and the new U(1) respectively.

The contribution of Z' to the ν_e -e cross section can be included by adding an energy-dependent term to (g_1, g_2) in Eq. (16):

$$(g_1, g_2) \to (g_1, g_2) + \frac{(\delta_1, \delta_2)}{4\sqrt{2}G_F \left(2m_e T + m_{Z'}^2\right)},$$
(40)

where (δ_1, δ_2) depends on $g_{Z'}$, ϵ and α . When studying the effect of one of these three parameters, we assume the other two are negligibly small. Under this assumption, the expressions of (δ_1, δ_2) are given as follows:

$$(\delta_1, \ \delta_2) = (g_{Z'}^2, \ g_{Z'}^2), \text{ for } g_{Z'} \neq 0, \ \epsilon = \alpha = 0,$$
(41)

$$(\delta_1, \ \delta_2) = \left(\frac{g^2 s_W^2 \epsilon^2}{c_W^2 (1 - \epsilon^2)}, \ \frac{2g^2 s_W^2 \epsilon^2}{c_W^2 (1 - \epsilon^2)}\right), \text{ for } \epsilon \neq 0, \ g_{Z'} = \alpha = 0,$$
(42)

$$(\delta_1, \ \delta_2) = \left(\frac{g^2 s_\alpha^2 \left(2s_W^2 - 1\right)}{c_W^2}, \ \frac{2g^2 s_\alpha^2 s_W^2}{c_W^2}\right), \text{ for } \alpha \neq 0, \ g_{Z'} = \epsilon = 0.$$
(43)

Using Eqs. (40) to (43), we study the sensitivity of the Cr-LXe experiment to the three parameters $g_{Z'}$, ϵ , α and present the results in Figs. 6 and 7, in comparison with other known bounds taken from Refs. [34, 49, 90]. For the gauge coupling $g_{Z'}$ shown in Fig. 6, in general, neutrino-electron scattering experiments (CHARM II, TEXONO, and GEMMA) provide the leading constraints prior to some constraints obtained from atomic physics and measurements of muon and electron anomalous magnetic moments, $(g-2)_e$ and $(g-2)_{\mu}$. They are also complementary to some other constraints from fixed target experiments, astrophysical observations (energy loss in the sun and globular clusters), and the B-Factories. Due to its low threshold and high statistics, the ⁵¹Cr-LXe experiment would significantly improve upon existing constraints from neutrino-electron scattering. In the low mass limit, the ⁵¹Cr-LXe experiment has sensitivity to small $g_{Z'}$ down to 10^{-7} . For heavy Z', it would exceed the CHARM II experiment which is based on high-energy neutrino beams. The bounds on the kinetic mixing ϵ and the mass mixing α in Fig. 7 are similar to the $g_{Z'}$ bounds. Even with configuration A, the ⁵¹Cr-LXe experiment could provide the most stringent constraints on all these Z' parameters, showing its the great potential in constraining or probing the new physics of light Z'.

V. CONCLUSION

In this work, we have studied the potential for ν_e -e scattering in a LXe dark matter detector using ⁵¹Cr as a radioactive neutrino source (⁵¹Cr-LXe). Assuming a 5 MCi ⁵¹Cr source located 1 m below a 6-ton LXe detector with the current state-of-the-art background and running for 100 days (configuration A), one can already achieve a high statistics (1.2×10^4 signal events) measurement of ν_e -e scattering. However, only the low energy part ($T \leq 100$ keV) of the recoil spectrum can be efficiently measured while the higher energy signal would be submerged by the background, as shown in Fig. 1. To enhance the signal/background ratio at high T so that the full recoil spectrum ($0 < T \leq 559$ keV) can be measured, the background must be reduced by, for example, using ¹³⁶Xe-depleted LXe and a shorter exposure time. For this purpose, we also considered configurations B and C (see Tab. I) for which the signal is greater than the background over the whole spectrum (see Fig. 1).

Based on these three configurations, we study low energy precision measurement of the SM parameters $\sin^2 \theta_W$, g_V and g_A . For $\sin^2 \theta_W$, we find that $1 \sim 2\%$ precision can be attained, as presented in Fig. 2, and Tab. II. As for g_V and g_A), such an experiment would provide the most precise measurement among $\nu_e^{(-)}$ scattering experiments (see Fig. 3), and be comparable to the CHARM II measurements based on $\nu_\mu^{(-)}$ scattering. Due to this high precision, we expect that the ⁵¹Cr-LXe experiment would be excellent at constraining BSM neutrino interactions. Indeed, according to our analyses, it would generate leading or complementary constraints on NSIs, SPVAT interactions, and light Z', as presented in Figs. 4, 5, and 6 respectively. For example, take NSIs, the most extensively studied scenario: the ⁵¹Cr-LXe experiment is sensitive to six of the NSI parameters, namely ϵ_{ee}^L , ϵ_{ee}^R , $\epsilon_{e\mu}^L$, $\epsilon_{e\tau}^R$, and $\epsilon_{e\tau}^R$. In Tab. III and Fig. 4 we show that $\epsilon_{e\mu}^L$, $\epsilon_{e\tau}^R$, and $\epsilon_{e\tau}^R$ would be constrained to the limit around 0.1 ~ 0.2, and ϵ_{ee}^L and ϵ_{ee}^R can be more stringently constrained due to the interference with the SM signal, sometimes even down to 6×10^{-3} . These constraints would generally exceed the existing bounds, which would be important for future long baseline experiments such as DUNE and T2HK. In addition, probing SPVAT interactions and light Z' in ν_e -e scattering would shed light on the fundamental theories of both neutrinos and dark matter.

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Appendix A: Geometrical calculation of r_{avg}

According to the definition of r_{avg} in Eq. (6), we have

$$\frac{1}{r_{\rm avg}^2} = \frac{1}{V} \int dV \frac{1}{r^2} = \frac{1}{V} \int \frac{1}{r^2} dx dy dz,$$
 (A1)

where the volume is

$$V = \pi (d/2)^2 h. \tag{A2}$$

Here the Cartesian coordinate x-y-z is set in such a way that z is the cylindrical axis the x-y is the horizontal plane. By defining

$$R^2 \equiv x^2 + y^2,\tag{A3}$$

we can compute the integral in the cylindrical coordinate system:

$$\int \frac{1}{r^2} dx dy dz = \int \frac{R}{(R\cos\theta)^2 + (R\sin\theta)^2 + z^2} dz dR d\theta$$

= $\int_0^{d/2} dR \int_L^{L+h} \frac{2\pi R}{R^2 + z^2} dz$
= $\pi d \tan^{-1} \left(\frac{2(h+L)}{d}\right) - \pi d \tan^{-1} \left(\frac{2L}{d}\right)$
+ $\pi L \log \frac{L^2 \left(d^2 + 4(h+L)^2\right)}{(d^2 + 4L^2) (h+L)^2} + \pi h \log \frac{d^2 + 4(h+L)^2}{4(h+L)^2}.$ (A4)

Therefore, the result is

$$r_{\rm avg} = \left[\frac{4L}{d^2h}\log\frac{L^2\left(d^2+4(h+L)^2\right)}{(d^2+4L^2)\left(h+L\right)^2} + \frac{4}{d^2}\log\frac{d^2+4(h+L)^2}{4(h+L)^2} - \frac{4}{dh}\tan^{-1}\left(\frac{2L}{d}\right) + \frac{4}{dh}\tan^{-1}\left(\frac{2(h+L)}{d}\right)\right]^{-\frac{1}{2}}.$$
(A5)

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