1	Supporting Information for						
2	Quantification of the Arctic Sea Ice-Driven Atmospheric Circulation						
3	Variability in Coordinated Large Ensemble Simulations						
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52 Section S1.

Fig. S1 shows the spatial maps of SLP SIC-driven variability of individual AGCM using only ten members in order to compare with results shown in Fig. 2. We also randomly chose 10 members out of 130 members across seven AGCMs (Fig. S2n) to show the strength of SIC-driven is largely model-independent.

57 Fig. S2 shows the quantification of the relationship between ensemble size and the 58 portion of total variance explained by the Arctic-averaged (65°N-90°N) SIC-driven 59 variability and the other components. For SLP, the contribution of internal atmospheric 60 noise increases to more than 90% as the ensemble size becomes 15 (Fig. S2a). 61 Correspondingly, the SST/GHG-driven variability exponentially decreases to ~10% 62 (Fig. S2b) with 15 members, while the SIC-driven variability decreases to ~15% (Fig. 63 S2c). At the same time, the covariance (multiplied by -1 for comparison to others) 64 decreases to ~15%, while the residual variances remain very small (dashed lines near 65 zero in Fig. S2d). Using 130 member, the SIC-driven variability is only ~1.5%. The 66 total variance estimate remains nearly constant and has very little dependence on the 67 ensemble size (not shown). Therefore, the variance is misleadingly attributed to the 68 SST/GHG or SIC forcing instead of the internal variability when using small ensemble 69 size. The same analysis for SAT is shown in Figs. S2e-h.

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Table S1. Summary of the AGCMs used in this study

	Model Name	CESM2- WACCM6	LMDZOR6	NorESM2- CAM6	EC-Earth3	CMCC-CM2-HR4	ECHAM6.3	HadGEM3	Multi-model ensemble
	Institution	WHOI-NCAR	LOCEAN-IPSL	NERSC	DMI	CMCC	MPI-M	UoS	
	Horizontal resolution (lat x lon)	0.95° x 1.25° (~100 km)	1.26° x 2.5° (~150 km)	0.94° x 1.25° (~100 km)	T255 (~80 km)	0.9° x 1.25° (~100 km)	T127 (~100km)	0.83° x 0.55° (~60 km)	Interpolated to 0.95° x 1.25° (~100 km)
	# of vertical levels (top level)	70 (0.001 hPa)	79 (0.01 hPa)	32 (3.4 hPa)	91 (0.01 hPa)	30 (2 hPa)	95 (0.01hPa)	85 (85 km)	
	# of ensemble members	30	30	20	20	10	10	10	130
	Adjustment of SST/SIC	Yes	Yes	Yes	Yes	No	Yes	No	
	CMIP6 External Forcing used	CMIP6	HighResMIP	CMIP6	CMIP6	HighResMIP	CMIP6	HighResMIP	
127	Reference	Gettelman et al. (2019)	Hourdin et al. (2019)	Bentsen et al. (2013)	EC-Earth (2019) Thomas et al. (2019)	Cherchi et al. (2018)	et.al.(2013) Mueller et. al. (2018)	Walters et al. (2017)	
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Figure S1. Arctic SIC-driven variance of DJF SLP using first ten members for (a) CESM2-WACCM6, (b) LMDZOR6, (c) NorESM2-CAM6, (d) EC-Earth3, (e) CMCC-CM2-HR4, (f) ECHAM6.3, and (g) HadGEM3-GC3.1. (h)-(k) The same as (a)-(d) but using second ten members. (1)-(m) The same as (a)-(b) but using third ten members. (n) The same as others but using 10 members randomly selected out of 130 members across seven AGCMs. The number in the parenthesis denotes ensemble size used. The cyan contour lines denote values larger than 6 hPa² with interval 2 hPa². The black circle corresponds to 65°N to denote the Arctic Circle.



163 Figure S2. Ensemble size dependency for the ratio of estimated variances for each 164 component to the total variance in percentage. The top row is for the Arctic Circle-165 averaged (65°N-90°N) DJF SLP decomposed into (a) internal atmospheric variability, 166 (b) SST/GHG-driven variability, (c) SIC-driven variability, and (d) covariability 167 between the SIC-driven and SST/GHG-driven components. For each given ensemble size, the ensemble members are randomly sampled without replacement 10,000 times. 168 169 The color shadings indicate the 95-percentile range from 10,000 random selection and 170 the average is plotted with the solid curves. (e)-(h) The same as (a)-(d) but for the nearsurface air temperature in the same domain. The dashed lines in (d) and (h) are ratios 171 172 for the residual components, which the 95-percentile ranges are also labeled but too 173 small to be shown with the scale used here.