

Neutron production from thermonuclear reactions in laser-generated plasmas

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The production of intense neutron beams via thermonuclear reactions in laser-generated plasmas is investigated theoretically. So far, state-of-the-art neutron beams are produced via laser-induced particle acceleration leading to high-energy particle beams that subsequently interact with a secondary target. Here we show that neutron beams of two orders of magnitude narrower bandwidth can be obtained from thermonuclear reactions in plasmas generated by Petawatt-class lasers. The intensity of such neutron beams is about one or two orders of magnitude lower than the one of the state-of-the-art laser-driven neutron beams. We study to this end the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by Petawatt-class lasers interacting with D_2 gas jet targets and CD_2 solid-state targets. The results also shows the possibility of direct measurements of reaction rates at low temperatures of astrophysical interests. In addition, the use of CD_2 solid-state targets can also lead to great enhancements on the plasma screening compared to the case of D_2 gas jet targets, opening new possibilities to study this so far unsolved issue in the field of astrophysics.

I. INTRODUCTION

Thermonuclear reactions occur in plasma environments in which the thermal energy of the ions can overcome the electrostatic repulsion in a collision between nuclei, leading to nuclear reactions¹. The development of laser technology in the past decades provides a powerful tool for the study of nuclear reactions in laser-generated plasmas. Lasers provide the opportunity to access plasma parameter regimes which cannot be accessed in accelerator-based experiments, such as direct measurements of nuclear reactions in nucleosynthesis-relevant energies and plasma effects on nuclear reactions²⁻⁵, and might thus significantly advance our understanding in astrophysics. On the other hand, industrial applications of such studies, such as laser-induced ignition which may provide a future source of alternative energy⁵⁻⁷, have also attracted a great deal of attention.

Neutron production is one of the key areas of the field of nuclear reactions in laser-generated plasmas⁸⁻¹³. Normally the experimental access to high neutron flux is mainly at large-scale reactor and accelerator-based facilities. However, the development of Petawatt-class lasers provides the opportunity of having intense neutron beams generated by comparatively smaller-scale laser facilities¹¹⁻¹³. The common solution for neutron production in Petawatt-class laser facilities is via high-energy particle beams interacting with a target (beam-target interaction), in which lasers are used for the acceleration of particles. In this manner, intense neutron beams with the order of 10^9 - 10^{10} per pulse can be obtained¹¹⁻¹³.

In this article, we study intense neutron beams produced from thermonuclear reactions in laser-generated plasmas. We analyze the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by Petawatt-class lasers interacting with D_2 gas jet targets and CD_2 solid-state targets. In-

tense neutron beams with narrow bandwidth can be obtained from thermonuclear reactions in plasmas generated by Petawatt-class lasers, which are about two orders of magnitude narrower in the neutron-energy bandwidth compared to today's state-of-the-art laser-driven neutron beams¹². The intensity of such neutron beams is about one or two orders of magnitude lower than the one of the state-of-the-art laser-driven neutron beams¹². Such intense neutron beams with narrow bandwidth have numerous applications in both industry and fundamental research, such as the interrogation of material and life science^{14,15}, nuclear fission and fusion research¹⁶, and neutron capture experiments for fundamental nuclear physics and nuclear astrophysics¹⁷. On the other hand for the low temperature regime, the results show the possibility of direct measurements of reaction rates at low temperatures of astrophysical interests^{2,18}. The use of CD_2 solid-state targets can also lead to great enhancements on the plasma screening compared to the case of D_2 gas jet targets, offering the possibility to access to this so far unsolved issue in astrophysics^{2,5,18}.

We note that in order to obtain nuclear reaction rates in astrophysical plasmas such as the core of stars or nucleosynthesis-relevant environments, extrapolations from accelerator-based experimental data to low energies are required^{2,5,18}. Direct measurements of reaction rates in laser-generated plasmas provide the chance for an alternative solution². On the other hand, in plasmas, long-range electric fields are screened down by the dynamic flow of particles moving in response to electric fields. Owing to this charge screening effect, nuclear reactions could be drastically affected inside plasmas. The plasma screening effect for nuclear reactions has been intensively studied theoretically¹⁹⁻³⁰, but remains an unsolved issue as experimental tests have not been performed so far.

We note that neutron production by irradiating deuterated polystyrene or D_2 targets at ultrahigh intensity has been achieved experimentally and investigated theoretically³¹⁻³⁸. Laser pulses with ultrahigh intensity ($\sim 10^{19}$ W/cm² or even higher) have been used, lead-

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ing to the neutron production mechanism of the ion beam-target interaction, in which the ion beam is generated by the laser-target interaction then produces neutrons through the ion beam-target interaction. In contrast, here we focus on a different regime of relatively low laser intensity ($\leq 10^{18}$ W/cm²) to avoid contributions of the beam-target interaction from energetic ions. Moreover, with Petawatt-class lasers and low intensity, we can create plasmas lasting for a timescale longer than the electron-ion equilibration time. Under this condition, the plasma can achieve thermal equilibrium, leading to thermonuclear reactions.

We first study the neutron events as functions of the plasma temperature assuming a general spherical plasma model, and calculate the neutron spectra in Sec. II. Then we model the plasma formation by the particle in cell (PIC) method for CD₂ solid-state targets in Sec. III. Plasma screening effect for thermonuclear reactions is discussed in Sec. IV to show the astrophysical interests of the study. Then we conclude the paper with a brief summary in Sec. V. We use the centimetre-gram-second system of units with $k_b = 1$, unless for some quantities the units are explicitly given.

II. NEUTRON PRODUCTION IN SPHERICAL PLASMAS

Reactions of interests can be expressed as $n_1 + n_2 \rightarrow n_3 + n_4$, where n_k stands for the number of the nuclear species k . The reaction rate per unit volume is³⁹

$$P_{12} = \rho N_A \Lambda_{12 \rightarrow 34}, \quad (1)$$

where ρ is the matter density, N_A is Avogadro number, and $\Lambda_{12 \rightarrow 34} = N_A \langle \sigma v \rangle_{12} Y_1 Y_2 \rho / (n_1!)$, with $Y_k = X_k / A_k$ (X_k is the mass fraction and A_k is the mass number), σ the nuclear reaction cross section, and v the relative velocity of the reactants. Then the total event number N_t is

$$N_t = \int dV dt P_{12}. \quad (2)$$

Assuming a uniform plasma with a spherical shape, the total event number is $N_t = P_{12} V \tau_p$ with the plasma volume V and the plasma lifetime τ_p . The plasma lifetime can be provided by the hydrodynamic expansion^{40,41},

$$\tau_p = R_p \sqrt{m_{\text{ion}} / (T_e Z_{\text{ion}})}, \quad (3)$$

where R_p is the plasma radius, m_{ion} is the ion mass, T_e is the plasma temperature [in Eq. (3), T_e is in units of erg], and Z_{ion} is the ion charge state.

We first consider the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by D₂ gas jet targets. The highest density of gas jets so far is around 10^{21} cm⁻³^{42,43}. In this case, the plasma volume can be estimated by $V = E_{\text{laser}} f_{\text{abs}} / [T(n_{\text{ion}} + n_e)]$, where E_{laser} is the laser pulse energy and f_{abs} is the laser absorption fraction. The

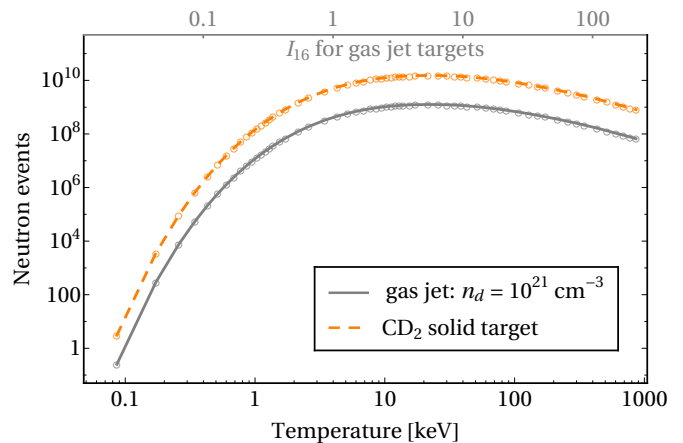


FIG. 1. Neutron events as functions of the temperature in plasmas generated by D₂ gas jet targets and CD₂ solid-state targets. A laser pulse with energy $E_{\text{laser}} = 500$ J is assumed, and carbon and deuterium ions are assumed to be fully ionized. For gas jet targets, a laser absorption fraction $f_{\text{abs}} = 0.1$ is assumed. For CD₂ solid-state targets, a laser absorption fraction $f_{\text{abs}} = 0.2$ is assumed and the carbon number density of the target is 4×10^{22} cm⁻³. The top frame shows the laser intensity to generate the plasma according to the scaling law Eq. (4), and it is valid for the gas jet case. I_{16} is the laser intensity in units of 10^{16} W/cm². We note that, realistically, for the case of CD₂ solid-state targets the heating of the target is mainly conducted by hot electrons generated in the laser-target interaction, which overcomes the limit of direct heating by lasers above the critical density. PIC simulations are needed to model the plasma generation, which will be discussed in Sec. III. Here In order to understand the accessible range of neutron events as a function of the plasma temperature in the case of CD₂ solid-state targets, we assume at first the simple spherical plasma model.

number of neutron events per laser shot as a function of the plasma temperature is shown in Fig. 1, for the case of the deuterium number density $n_d = 10^{21}$ cm⁻³. A laser pulse with energy $E_{\text{laser}} = 500$ J and the laser absorption fraction $f_{\text{abs}} = 0.1$ are assumed. Reaction rates of ${}^2\text{H}(d, n){}^3\text{He}$ are taken from the NACRE II database³⁹. As shown in Fig. 1, the neutron events reach a maximal value of approximately 10^9 per pulse at a temperature of approximately 10 keV.

For low density cases, i.e., plasmas generated by D₂ gas jet targets, following Refs.^{44,45}, we connect the laser parameter to the electron temperature by the scaling law

$$T_e \sim 3.6 I_{16} \lambda_\mu^2 \text{ keV}, \quad (4)$$

where I_{16} is the laser intensity in units of 10^{16} W/cm² and λ_μ is the wavelength in microns⁴⁶⁻⁴⁸. The electron-ion equilibration time^{49,50} is ~ 100 ps for the temperature of a few keV. With the high power laser and relatively low intensity, the plasma lifetime is more than 500 ps. Therefore, the plasmas under consideration last long enough to reach thermal equilibrium, which is rare in laser driven platforms. We thus assume thermal equilibrium to model

the outcome of the thermonuclear reaction. The result of neutron events from the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by D_2 gas jet targets is shown in Fig. 1 (see the top frame). A laser wavelength $1.053 \mu\text{m}$ is assumed. It is shown that the laser intensity at approximately 10^{16} W/cm^2 is favourable for neutron productions. We note that the scaling described by Eq. (4) is limited to the non-relativistic regime, hence the prediction for high laser intensities ($\sim 10^{18} \text{ W/cm}^2$) is not precise. However, we focus on the temperature of a few keV (corresponding to the laser intensity in the order of 10^{16} W/cm^2); the result for high laser intensities is shown for the sake of comparison. We note also that in order to heat spherical plasmas directly by lasers, the density of the plasma cannot exceed the laser's critical density, i.e., $\approx 10^{21} \text{ cm}^{-3}$ for lasers with $1.053 \mu\text{m}$ wavelength.

We consider also CD_2 solid-state targets. The high-density case is of particular interests also in astrophysics, since many interesting aspects of astrophysics involve very high densities ($\sim 10^{26} \text{ cm}^{-3}$), e.g., the core of a star where nuclear reactions play important roles for the evolution of the star as well as the nucleosynthesis. We note that in the high density regime, plasmas cannot be heated directly by lasers as discussed above. In this regime the heating of the target is mainly conducted by hot electrons generated in the laser-target interaction which overcomes the limit of direct heating by lasers above the critical density, and experiments and simulations have shown that it is possible to heat targets at the solid-state density to temperatures of a few hundreds eV or even a few keV^{44,51-53}. PIC simulations are needed to model the plasma generation, which will be discussed in Sec. III. Here, in order to understand the accessible range of the neutron events as a function of the plasma temperature in the case of CD_2 solid-state targets, we assume at first the simple spherical plasma model to obtain the neutron events, which are shown also in Fig. 1. The result shows that the neutron events reach a maximal value of approximately 10^{10} per pulse at a temperature of approximately 10 keV.

We note that the angular distribution of neutrons produced from thermonuclear reactions is isotropic. If one uses this neutron source as a neutron beam with a certain direction, then only part of the neutrons can be used. However, neutron beams produced via laser-induced particle acceleration leading to high-energy particle beams that subsequently interact with a secondary target have also a quite large angle divergence or even are isotropic¹¹⁻¹³. The state-of-the-art laser-driven neutron beams reach a maximum intensity of 10^{10} n/sr in the direction of the ion beam, with intensities in other directions less than half of the maximum value¹². Thus, the intensity of the neutron beams reached here is about one order of magnitude lower than the one of the state-of-the-art laser-driven neutron beams. As also shown in Fig. 1, a significant number of events can be achieved at temperatures of few hundreds eV for both cases of D_2 gas jet targets and CD_2 solid-state targets, and a measurable

number of events can be achieved even at temperatures of $\sim 100 \text{ eV}$ for the case of CD_2 solid-state targets. This may allow us to make direct measurements of reaction rates at low temperatures of astrophysical interests^{2,18,39}.

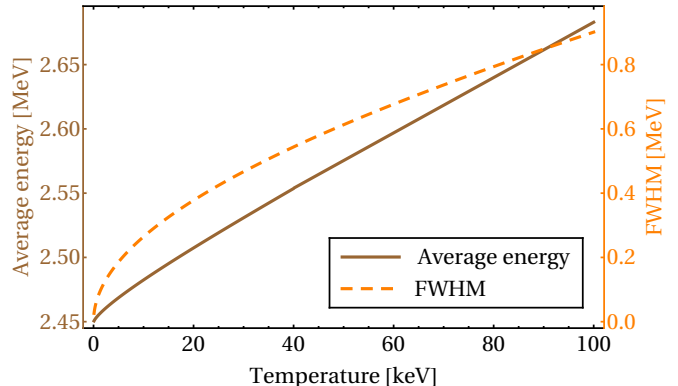


FIG. 2. Average energy (brown solid curve; y-axis: left frame) and FWHM (orange dashed curve; y-axis: right frame) of neutrons produced from the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas as functions of the plasma temperature.

In order to calculate the neutron spectra, we follow the relativistic calculation of fusion product spectra for thermonuclear reactions introduced in Refs.^{54,55}. The average neutron energy and FWHM of the neutron spectrum for the reaction ${}^2\text{H}(d, n){}^3\text{He}$ as functions of the plasma temperature are shown in Fig. 2. It is shown that for a plasma with a temperature of a few keV, the FWHM of the neutron spectrum is in the order of 100 keV. This is about two orders of magnitude narrower than the one of the state-of-the-art laser-driven neutron beams¹², which is in the order of 10 MeV or even higher¹².

III. NEUTRON PRODUCTION IN HIGH-DENSITY PLASMAS GENERATED BY LASERS

We now turn to the generation of plasmas in laser experiments in the high density case. Experiments and simulations have shown that it is possible to heat targets at the solid-state density to temperatures of a few hundreds eV or even a few keV^{44,51-53}. Since in this regime the heating of the target is mainly conducted by secondary particles, i.e., hot electrons generated in the laser-target interaction, a more sophisticated model is necessary compared to the low-density case. We have performed a 2-dimensional (2-D) PIC simulation using the EPOCH code⁵⁶. A CD_2 target is assumed, with a carbon number density of $4 \times 10^{22} \text{ cm}^{-3}$, a thickness of $1 \mu\text{m}$ (x -axis) and a length of $5 \mu\text{m}$ (y -axis). The laser propagates along the x -axis, with a Gaussian profile in time with a FWHM of 100 fs and a Gaussian profile in the y -axis centring at the center of the target with a FWHM of $2 \mu\text{m}$. The peak intensity and wavelength of the laser are 10^{18} W/cm^2 and $1.053 \mu\text{m}$, respectively. The size

of the simulation box is $4 \mu\text{m} \times 6 \mu\text{m}$, and the target is located at the center of the simulation box. A rigid mesh with 800×1200 cells is used. The time step is 1.12×10^{-17} s. A linear preplasma with thickness $0.5 \mu\text{m}$ is considered in front of the target (the preplasma depends on the interaction of the prepulse of the laser with the target, and as a representative order, the preplasma assumed here is based on a similar ratio of the preplasma length to the target thickness in Ref.⁵³). Carbon and deuterium ions are assumed to be fully ionized, and the numbers of pseudoparticles per cell are 50, 100, and 400 for carbon ions, deuterium ions, and electrons, respectively.

The simulation and analysis have been performed until 2.5 ps, and the electron temperature starts getting stable from 2.0 ps. The electron temperature in the solid-target region at 2.5 ps is shown in Fig. 3(a). It is shown that the target can be heated to a few keV at the solid-state density in the laser focal spot. With such density and temperature, we obtain the neutron production rate per unit volume of the reaction ${}^2\text{H}(d, n){}^3\text{He}$, shown in Fig. 3(b). We assume again thermal equilibrium, based on the following analysis. For the considered solid-state density, the electron-ion equilibration time^{49,50} is approximately 10 ps for the temperature of a few keV. We note that the density of the plasma decreases after 2.5 ps as the plasma expands. Following the hydrodynamic model in Ref.⁴¹, the plasma expansion leads to a neutron production timescale of approximately of 20 ps, and the effect of the plasma expansion on collision rates in the timescale of approximately 20 ps of interaction time leads to a deviation of approximately 20%. Due to radiative processes, the plasma is also cooling. Estimates by the collisional-radiative code FLYCHK⁵⁷ show that the timescale of the radiative cooling of the plasma at a temperature of around 1 keV with the solid-state density is approximately 30 ps. Thus, the plasma lasts long enough to reach thermal equilibrium. Therefore, the use of the energy density at 2.5 ps for neutron production as an approximation is justified.

The normalised neutron distribution dN_r/dE_n (normalised by the total neutron number per pulse) from the whole solid-target region is shown in Fig. 3(c) as a function of the neutron energy E_n . It is shown that the energy bandwidth of the neutron beam is approximately 100 keV, which is about two orders of magnitude narrower than the one of the state-of-the-art laser-driven neutron beams¹².

The 2-D PIC simulation predicts a conversion efficiency from laser energy to neutron yield of $10^6 n/J$. We note that, in order to exactly model the physical system, 3-D PIC simulations with the exact size of the target and laser focal spot are required, which are however impossible for Petawatt-class lasers with an intensity of 10^{18} W/cm² because of a lack of computing power. In order to model the plasma, a 2-D PIC simulation has been performed here. Obviously, the 2-D simulation cannot exactly describe the physical system since it misses information on one of the dimensions. In order to check

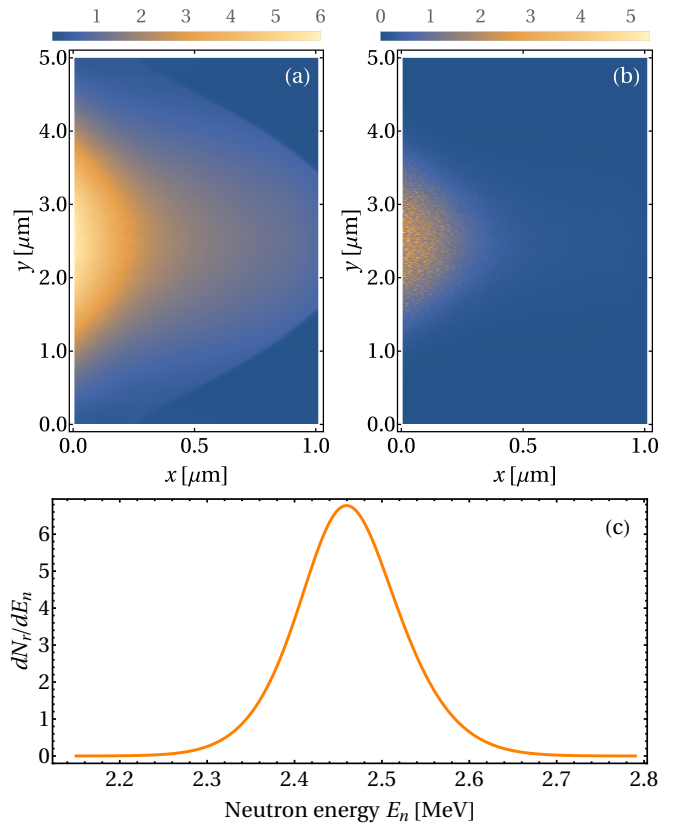


FIG. 3. Results in the solid-target region of the 2-D PIC simulation at 2.5 ps. (a): Temperature in units of keV. (b): Neutron production rate per unit volume of the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in units of $10^{25} \text{cm}^{-3} \text{s}^{-1}$. (c): Normalised neutron distribution (dN_r/dE_n). A CD_2 target with a carbon number density of $4 \times 10^{22} \text{cm}^{-3}$ is assumed, and carbon and deuterium ions are assumed to be fully ionized. The laser has a Gaussian profile in time with a FWHM of 100 fs and a Gaussian profile in the y -axis with a FWHM of $2 \mu\text{m}$. The peak laser intensity is 10^{18}W/cm^2 and the laser wavelength is $1.053 \mu\text{m}$.

the possible influence of laser intensity variation in the laser focal spot, we have also performed a 1-D PIC simulation, which in principle could be applied for any size of the laser focal spot by completely neglecting the information on the latter. The 1-D PIC simulation predicts similar results as the 2-D PIC simulation in the region of the laser focal spot. This indicates that edge effects, losses, and gradients, which all very much depend on the actual geometry in a real scenario, will not lead to a dramatic change for the neutron production case. Therefore the insight gained on a simplified scale in our 2-D PIC simulation may imply a similar conversion efficiency from laser energy to neutron yield for a certain amount of driver energy on the scale of 500 J for the current state-of-the-art laser systems. This would lead to the generation of a neutron beam with approximately 10^9 neutrons per pulse with a laser pulse energy of 500 J. The intensity of

such neutron beam is about 2 orders of magnitude lower than the one of the state-of-the-art laser-driven neutron beams (maximum intensity 10^{10} n/sr)¹².

As discussed in many experiments of neutron productions by irradiating deuterated polystyrene or D₂ targets at ultrahigh intensity, the ion beam-target interaction is responsible for neutron productions. As shown in Ref.³⁶, the contribution from the ion beam-target interaction is suppressed for the relatively low laser intensity under consideration ($\leq 10^{18}$ W/cm²). Re-scaling the laser energy to our case, neutron events from the beam-target interaction [${}^2\text{H}(d, n){}^3\text{He}$] are more than 3 orders of magnitude less than our results. Other possible neutron sources from the reactions ${}^2\text{H}(d, pn){}^2\text{H}$, ${}^2\text{H}(e, en)p$, ${}^2\text{H}(\gamma, n)p$, and ${}^{12}\text{C}(d, n){}^{13}\text{N}$ are negligible³⁶ in our case. We note that neutron beams produced by thermonuclear reactions start delayed due to the required electron-ion equilibration time when compared to neutrons driven by laser ion acceleration concepts.

IV. PLASMA SCREENING EFFECTS

As a further advantage, we analyze the plasma screening effect for thermonuclear reactions^{2,5,18,58}. Due to the plasma screening effect, the reaction rate can be enhanced by a factor¹, $\langle\sigma v\rangle_{\text{scr}} = g_{\text{scr}}\langle\sigma v\rangle$. In weakly coupled plasmas, the screening enhancement factor is^{19,20,58}

$$g_{\text{scr}} = \exp[Z_1 Z_2 \alpha / (T \lambda_D)], \quad (5)$$

with the Debye length λ_D , the fine-structure constant α , and nuclear charges of the reactants Z_1 and Z_2 . The plasma screening enhancement factor for the reaction ${}^2\text{H}(d, n){}^3\text{He}$ is shown in Fig. 4. It is shown that the plasma screening effect for the reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by D₂ gas jets is negligible. However, the plasma screening effect is greatly enhanced in the case of CD₂ solid-state targets. As neutron events are measurable for low temperatures shown in Fig. 1, it may lead to the possibility of direct measurements of the plasma screening effect for thermonuclear reactions.

Furthermore, low temperature plasmas generated by CD₂ targets may reach the condition for strong screening¹⁹, $Z_1 < \rho^{1/3}$ and $0.23 Z_1^{2/3} z (\xi \rho)^{1/3} T_6^{-1} > 1$ (for $T \sim 100$ eV, $0.23 Z_1^{2/3} z (\xi \rho)^{1/3} T_6^{-1} \sim 1$). Here T_6 is the plasma temperature in units of 10^6 K and $\xi = \sum_i (X_i Z_i) / A_i$. In this case, the plasma screening enhancement factor is

$$g_{\text{scr}} = \exp\left\{0.205 \left[(Z_1 + Z_2)^{5/3} - Z_1^{5/3} - Z_2^{5/3} \right] (\xi \rho)^{1/3} T_6^{-1} \right\}. \quad (6)$$

The strong screening enhancement factor for the case of CD₂ solid targets is shown in Fig. 4. For temperatures of ~ 100 eV, the strong screening enhancement factor is significantly different from the weak screening one, which could lead to the experimental determination of the strong screening effect for fusion reactions in plasmas.

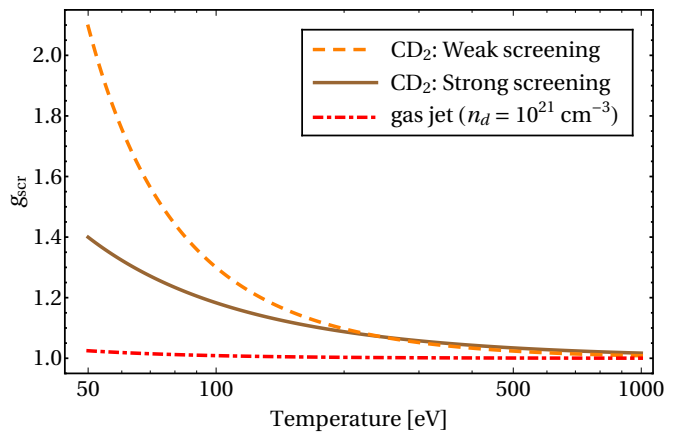


FIG. 4. Plasma screening enhancement factor for the reaction ${}^2\text{H}(d, n){}^3\text{He}$ as functions of the plasma temperature, in plasmas generated by D₂ gas jets with $n_d = 10^{21}$ cm⁻³ (weak-screening: red dot-dashed curve), and in plasmas generated by CD₂ solid-state targets (weak-screening: orange dashed curve; strong-screening: brown solid curve). Carbon and deuterium ions are assumed to be fully ionized. The carbon number density of CD₂ solid-state targets is 4×10^{22} cm⁻³.

V. SUMMARY

In conclusion, we have studied the production of intense neutron beams via thermonuclear reactions in laser-generated plasmas. The reaction ${}^2\text{H}(d, n){}^3\text{He}$ in plasmas generated by Petawatt-class lasers interacting with D₂ gas jet targets and CD₂ solid-state targets has been analyzed. Intense neutron beams of about two orders of magnitude narrower bandwidth can be obtained from thermonuclear reactions, as compared to the state-of-the-art laser-driven neutron beams^{12,13}. The intensity of such neutron beams is about one or two orders of magnitude lower than the one of the state-of-the-art laser-driven neutron beams, which indicates that the spectral brightness is similarly high or even higher than the one of the state-of-the-art laser-driven neutron beams. Such neutron beams with narrow bandwidth have numerous advantages in the applications in industry and fundamental research, such as in the interrogation of material and life science^{14,15} using a neutron beam, and neutron capture experiments for fundamental nuclear physics and nuclear astrophysics¹⁷. Compared to the state-of-the-art laser-driven neutron beams with a broad bandwidth, narrow bandwidth of the beam could lead to more clear and better understandable signal, as it avoids a large divergence and uncertainty in the probe energy (for the interrogation) or the reactant energy (for the neutron capture). Furthermore, for applications involved resonance processes, the spectral brightness is important for the number of the events that can be obtained.

We have also pointed out the possible astrophysical implications of our work, i.e., direct measurements of reaction rates at low temperatures of nucleosynthesis-

relevant energies, and the great enhancement on the plasma screening effect which may open new possibilities to study this so far open issue in astrophysics.

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