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Organizing principles for vegetation dynamics

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Supplementary Table 1. Examples of optimality-based plant models

Process/Trait	Optimality hypothesis	References	Test	Traditional approach in DGVMs
<i>Leaf scale optimality</i>				
Photosynthetic capacity	<i>Fitness proxy:</i> Leaf net carbon assimilation <i>Optimized variables:</i> leaf N allocation to the light and Rubisco limited photosynthetic capacities <i>Benefits:</i> Photosynthesis <i>Costs:</i> Respiration <i>Constraints and drivers:</i> Structural leaf N, light, Temperature (T), [CO ₂]	Coordination hypothesis (Maire et al. 2012)	Gas exchange data	PFT-dependent photosynthetic capacity
	<i>Fitness proxy:</i> Leaf net carbon assimilation <i>Optimized variables:</i> leaf N allocation to the light and Rubisco limited photosynthetic capacities and storage <i>Benefits:</i> Photosynthesis <i>Costs:</i> Respiration <i>Constraints and drivers:</i> light, T, [CO ₂]	(Xu et al. 2012, Ali et al. 2016, Quebbeman and Ramirez 2016)	Gas exchange data	
Leaf stomatal conductance and photosynthesis	<i>Fitness proxy:</i> Minimized C cost per C assimilation <i>Optimized variables:</i> Photosynthetic capacity and water conducting capacity per C assimilation <i>Benefits:</i> Photosynthesis <i>Costs:</i> Construction and maintenance C costs of capacities <i>Constraints and drivers:</i> VPD, T, altitude	Least cost hypothesis (Prentice et al. 2014), (Wang et al. 2017) (Stocker et al. 2019)	Leaf ¹³ C and flux tower measurement across a range of different environments	PFT-dependent photosynthetic capacity and generic light- and temperature responses
Stomatal conductance	<i>Fitness proxy:</i> Daily C gain <i>Optimized variable:</i> stomatal conductance (g_s) over time <i>Benefits:</i> Daily photosynthesis <i>Constraint and driver:</i> transpiration rate	(Cowan and Farquhar 1977, Manzoni et al. 2013)	Gas exchange data	Empirical model with 2 or 3 PFT specific parameters
	<i>Fitness proxy:</i> Net carbon gain <i>Optimized variable:</i> g_s <i>Benefits:</i> Photosynthesis <i>Costs:</i> C costs of hydraulic damages <i>Constraints and drivers:</i> T, humidity, light, wind speed, [CO ₂], soil water potential	(Sperry et al. 2017) (Wolf et al. 2016, Anderegg et al. 2018)	Leaf trait data	
Leaf life span	<i>Fitness proxy:</i> C gain per unit time <i>Optimized variable:</i> Leaf lifespan <i>Benefits:</i> Photosynthesis (declines with leaf age) <i>Costs:</i> Respiration	(Kikuzawa 1991, Xu et al. 2017)	Plant trait data	PFT dependent Leaf longevity

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Leaf thermo-regulation	<p><i>Fitness proxy:</i> Leaf C gain per leaf C invested</p> <p><i>Optimized variable:</i> Leaf T</p> <p><i>Benefits:</i> Photosynthesis</p> <p><i>Costs:</i> Leaf C investment</p> <p><i>Constraints and drivers:</i> LMA, T_{90}, g_s, LDMC, leaf temperature acclimation rate (τ)</p>	(Michaletz et al. 2016)	Gas exchange data. Trait data: LMA, T_{90} , g_s , LDMC, τ	Not considered
Leaf angle	<p><i>Fitness proxy:</i> Canopy photosynthesis</p> <p><i>Optimized variables:</i> Leaf angle</p> <p><i>Benefits:</i> Photosynthesis</p> <p><i>Costs:</i> Respiration</p> <p><i>Constraint and driver:</i> LAI</p>	(Hikosaka and Hirose 1997)	Herbaceous plant canopy data	Not explicitly considered
Leaf size	<p><i>Fitness proxy:</i> Leaf water use efficiency of photosynthesis</p> <p><i>Optimized variables:</i> Leaf size</p> <p><i>Benefits:</i> Photosynthesis</p> <p><i>Costs:</i> Water use</p> <p><i>Constraints and drivers:</i> Light, T, humidity</p>	(Parkhurst and Loucks 1972)	Observed leaf sizes in tropical trees, herbs, and lianas	Not considered
SLA, and leaf N per area	<p><i>Fitness proxy:</i> Canopy net C gain</p> <p><i>Optimized variables:</i> LAI, N per leaf area</p> <p><i>Benefits:</i> Photosynthesis</p> <p><i>Costs:</i> Respiration</p> <p><i>Constraints and drivers:</i> Canopy N and water use</p>	(McMurtrie and Dewar 2011)	Plant trait data	PFT-dependent
<i>Whole plant scale optimality</i>				
Rooting depth	<p><i>Fitness proxy:</i> Net C gain</p> <p><i>Optimized variable:</i> Rooting depth</p> <p><i>Benefits:</i> C gain = WUE \times water use</p> <p><i>Costs:</i> Root respiration</p> <p><i>Constraint:</i> Precipitation that predicts evapotranspiration (E)</p>	(Guswa 2010, Yang et al. 2016)	Water balance-based observations of E	PFT-dependent
Root and shoot C allocation	<p><i>Fitness proxy:</i> Balanced growth (target plant C:N ratio)</p> <p><i>Optimized variable:</i> Fraction of productivity allocated to roots or shoots</p> <p><i>Benefits:</i> None explicit</p> <p><i>Costs:</i> None explicit</p>	(Reynolds and Chen 1996)	Theoretical model (not statistically tested against data)	Fixed fractions of NPP, PFT dependent
	<p><i>Fitness proxy:</i> Net growth</p> <p><i>Optimized variable:</i> ESS for root biomass</p> <p><i>Benefits:</i> C gain</p> <p><i>Costs:</i> Leaf and root turnover, respiration</p> <p><i>Constraints and drivers:</i> Soil water and N, light</p>	(Farrior et al. 2013)	Field trials in grassland	
	<p><i>Fitness proxy:</i> Net C gain</p> <p><i>Optimized variables:</i> Root:shoot ratio, leaf N concentration</p> <p><i>Benefits:</i> C gain</p> <p><i>Costs:</i> respiration</p>	(Ågren and Franklin 2003)	Experiments with birch seedlings and tomato plants	

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Leaf phenology	<p><i>Fitness proxy:</i> Net C gain <i>Optimized variable:</i> LAI <i>Benefits:</i> C gain <i>Costs:</i> Respiration, leaf growth <i>Constraints and drivers:</i> Light, T, soil moisture *Not strictly optimization, but dynamic adjustment of LAI to increase productivity</p>	(Caldararu et al. 2014)	Satellite-based LAI from the MODIS	Empirical function of climate variables, PFT-dependent
	<p><i>Fitness proxy:</i> Long-term mean net C gain <i>Optimized variable:</i> LAI during the dry season <i>Benefits:</i> C gain <i>Costs:</i> Respiration, leaf growth <i>Constraints and drivers:</i> Soil moisture under stochastic rainfall, N availability</p>	(Vico et al. 2017)	Satellite-based fraction of drought-deciduous vegetation	
	<p><i>Fitness proxy:</i> Growth per leaf biomass <i>Optimized variable:</i> Leaf habit – evergreen or deciduous <i>Benefits:</i> Growth <i>Costs:</i> C costs of respiration and transpiration <i>Constraints and drivers:</i> Length of growing season, seasonality, soil fertility</p>	(Givnish 2002)	Qualitative patterns of leaf habit and climate	
Leaf mass per area and leaf life span	<p><i>Fitness proxy:</i> Net C gain <i>Optimized variable:</i> ESS for leaf mass per area <i>Benefits:</i> C gain <i>Costs:</i> C for leaf construction and respiration <i>Constraints and drivers:</i> Soil N mineralization</p>	(Weng et al. 2017)	Plant trait data	Fixed PFT dependent
C allocation in trees	<p><i>Fitness proxy:</i> Life-time reproductive production <i>Optimized variable:</i> ESS for leaf, stem and root biomass <i>Benefits:</i> Reproductive production <i>Costs:</i> biomass turnover, respiration, mortality <i>Constraints and drivers:</i> Light and water availability</p>	(Farrior et al. 2015)	Theoretical model	Fixed fractions of NPP, PFT dependent
	<p><i>Fitness proxy:</i> Life-time reproductive production <i>Optimized variable:</i> ESS for leaf, stem and root biomass <i>Benefits:</i> Reproductive production <i>Costs:</i> biomass turnover, respiration, mortality <i>Constraints and drivers:</i> Light and nutrient availability</p>	(Dybzinski et al. 2011)	Fluxnet data on NPP	

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C and N allocation in trees	<p><i>Fitness proxy:</i> Net C gain</p> <p><i>Optimized variables:</i> Fine roots, canopy N, Vertical distribution of leaf N, LAI</p> <p><i>Benefits:</i> C gain</p> <p><i>Costs:</i> Turnover of leaves and roots, respiration</p> <p><i>Constraints and drivers:</i> Soil N availability, [CO₂]</p>	(Franklin et al. 2009)	FACE experiments	Fixed fractions of NPP, PFT dependent
Dynamic C allocation	<p><i>Fitness proxy:</i> Life-time reproductive production</p> <p><i>Optimized variables:</i> Roots, Shoot, Storage, Reproduction over time</p> <p><i>Constraints and drivers:</i> Soil moisture, light</p>	(Iwasa 2000)	Theoretical model	Fixed fractions of NPP, PFT dependent
Foliage cover and photosynthetic capacity, canopy conductance, rooting depth and fine root distribution	<p><i>Fitness proxy:</i> Net C gain</p> <p><i>Optimized variables:</i> projected cover, photosynthetic capacity, canopy conductance, fine root distribution (dynamic); rooting depth, tree cover (static)</p> <p><i>Benefits:</i> Access to water and light for photosynthesis</p> <p><i>Costs:</i> Respiration, leaf and root turnover</p> <p><i>Constraints and drivers:</i> light, [CO₂] and water availability</p>	(Schymanski et al. 2009, 2015)	Eddy covariance, FACE experiments	PFT-dependent, static or prescribed
LAI of crop plants	<p><i>Fitness proxy:</i> Net C gain</p> <p><i>Optimized variable:</i> LAI (dynamic)</p> <p><i>Benefits:</i> Photosynthesis per LAI increase including N resorption from senescing leaves</p> <p><i>Costs:</i> Respiration, senescing leaves</p> <p><i>Constraints and drivers:</i> Canopy N, Fraction N resorbed at leaf senescence</p>	(Franklin and Ågren 2002)	Crop experiments	Empirical function of degree-days
Tree height	<p><i>Fitness proxy:</i> ESS for net C gain</p> <p><i>Optimized variable:</i> height</p> <p><i>Benefits:</i> C gain</p> <p><i>Costs:</i> C for construction and respiration</p>	(King 1990, Valentine and Mäkelä 2012)		Allometric function of stem diameter
Mycorrhizal C allocation	<p><i>Fitness proxies:</i> ESS for net growth of trees and ESS for N uptake strategy of mycorrhizal fungi</p> <p><i>Optimized variable:</i> C export to mycorrhiza, leaves and stem, fungal allocation to N uptake</p> <p><i>Benefits:</i> C gain</p> <p><i>Costs:</i> C use for N uptake and tissue turnover</p> <p><i>Constraints and drivers:</i> Soil N availability, [CO₂], connectivity among trees and fungi</p>	(Franklin et al. 2014)	Experimental forest plots	Not considered

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	<i>Fitness proxies:</i> Tree biomass <i>Optimized variable:</i> C export to mycorrhiza <i>Benefits:</i> C and N gain <i>Costs:</i> C allocation to mycorrhiza <i>Constraints and drivers:</i> Soil N availability and soil organic matter decomposability	(Baskaran et al. 2017)	Experimental forest plots	Not considered
Hydraulic traits and stomatal conductance	<i>Fitness proxies:</i> long-term mean transpiration rate (assumed proportional to GPP) <i>Optimized variable:</i> responses of xylem hydraulic conductivity and g_s to dry conditions <i>Benefits:</i> C gain (assumed proportional to GPP) <i>Costs:</i> reduced C gain due to inefficient water use <i>Constraints and drivers:</i> Soil moisture under stochastic rainfall	(Manzoni et al. 2014)	Global hydraulic trait datasets	Trait values are PFT dependent
	<i>Fitness proxies:</i> C gain over a year <i>Optimized variable:</i> Variable g_s over time <i>Benefits:</i> C gain over time <i>Costs:</i> Loss in C gain due to reduced plant water potential <i>Constraints and drivers:</i> Drought length and frequency, $[CO_2]$	(Bartlett et al. 2019)	Inter-trait relationships in tropical evergreen forest	
Defense	<i>Fitness proxies:</i> Net growth <i>Optimized variable:</i> C allocation to defense <i>Benefits:</i> Net growth <i>Costs:</i> C cost of defense <i>Constraints and drivers:</i> Grazing intensity	(Fagerstrom et al. 1987)	Theoretical model	Not considered
Xylem/phloem transport	<i>Fitness proxy:</i> energy export from loading phloem (proportional to square of net C gain) <i>Optimized variable:</i> canopy water potential <i>Benefits:</i> sucrose export to plant tissues <i>Costs:</i> maintenance of phloem flow <i>Constraints and drivers:</i> Limited transpiration rate	(Huang et al. 2018)	Theoretical model	Not considered

Abbreviations: $[CO_2]$ = atmospheric CO_2 concentration, E = evapotranspiration, ESS = evolutionary stable strategy, GPP = gross primary productivity, g_s = Stomatal conductance, LAI = leaf area index, LDMC = leaf dry matter content, LMA = leaf mass per area, N = nitrogen, NPP = net primary productivity, PFT = plant functional type, T = temperature, T90 = temperature range with photosynthesis >90% of photosynthesis at optimal T, τ = leaf temperature acclimation rate, VPD = vapor pressure deficit, WUE = water use efficiency

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