



In-situ interferometric monitoring of optical coatings

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Abstract: We present a new method for the *in situ* measurement of the amplitude and phase of the reflection coefficient of a plane substrate installed in a mechanical holder rotating at high speed (120 turns per minute) during the deposition of optical thin films. Our method is based on digital holography and uses a self-referenced scheme to cancel the effects of the severe constraints generated by the vibrational and thermal environment of the deposition machine.

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1. Introduction

The realization of complex optical filtering functions requires perfect control of the deposition process as well as accurately monitoring the optical thicknesses of the deposited layers in real time. This is today achieved through the simultaneous use of energetic deposition techniques, that provide dense layers with stable refractive index properties, and *in situ* optical monitoring systems [1,2].

These optical systems record continuously an optical characteristic of the growing stack, such as its transmittance T at a specific wavelength λ_0 (monochromatic monitoring) or the spectral dependence $T(\lambda)$ of this transmittance over a wide wavelength range (broadband monitoring). In the first case, the material change is triggered either when the time derivative of the transmittance is canceled (turning point monitoring, well suited for the deposition of quarterwave layers) or when this transmittance is equal to a specified value (trigger point monitoring, more versatile). For the broadband monitoring, the material change is triggered by the minimization of a cost function that quantifies the difference between the recorded spectrum and a target spectrum defined by modeling. Most of the time, these monitoring methods are really effective, but they can be inaccurate in some specific situations, such as the deposition of very thin layers or that of matching layers between two stacked Fabry-Perot cavities; the deposition of the corresponding layers can be here stopped by using a time criterion defined from the layer thickness specified by the design and the value of the deposition rate determined during the previous steps of the stack manufacturing.

To avoid these open-loop steps, it could be interesting to implement a complementary monitoring approach, whose measurement principle is different from those used so far, for instance by replacing intensity measurements with phase determination. Ellipsometry could provide an appropriate answer to such a general objective [3–5], but its practical use on moving substrates is challenging and its implementation constraints are fully different of those of the monitoring systems already used by the Optical Thin Films Group of the Institut Fresnel on its deposition machines, and that are mainly based on monochromatic and/or broadband monitoring systems working in transmission or reflection [6,7]. Moreover, the physical data provided by ellipsometry ($\tan \Psi$, $\cos \Delta$) are not in direct connection with the final optical properties specified

for thin-film filters. This is why we chosen to investigate if an interferometric measurement of the coefficient of reflection r of a stack is possible in the harsh conditions of a deposition machine.

Previous studies have shown that such interferometric measurements can be practically managed within operational deposition chambers [8–10]. In particular, the set-up proposed by Lee and coworkers [8,9] seemed to fulfill most of our objectives. It uses a polarimetric Michelson interferometer equipped with a micro-polarizer pixelated camera to achieve an instantaneous acquisition of four different phase states of the field reflected or transmitted by the sample [11,12]. Moreover, a tunable retarder is used together with a low coherence source to record only the result of the interference between the fields reflected by the coated front face and by the uncoated rear face, used here as a reference surface [8]. But this means that the measurement is also sensitive to any phase variations between these two surfaces, such as that induced by a temperature change in the witness glass.

To overcome this problem and relax the alignment constraints between the sample and the reference mirror of the Michelson interferometer, we have chosen to develop an alternative approach using a self-referenced interferometric configuration, in which the phase information is obtained by digital holography processing [13].

In section 2, we first present the main characteristics of the deposition machine, the self-referenced scheme we implemented for the substrate as well as the structure of the interferometric measurement set-up. section 3 is devoted to the presentation of a theoretical model that predicts the temporal change in the data provided by the interferometric set-up throughout the deposition of single layers (high index and low index), but also provides a detailed description of the data processing used to extract the modulus and phase of the reflection coefficient. In section 4, we present the main experimental results obtained with this interferometric configuration and we analyze the agreement between the recorded phase information and the predictions of our theoretical model. Finally, we conclude and define the possible applications of our method (section 5).

2. Materials and methods

2.1. Deposition machine

The deposition machine uses a dual ion beam sputtering technique (DIBS) to obtain dense layers of high purity oxides. Figure 1 illustrates the inside of the vacuum chamber showing three planar targets of silicon, tantalum, and hafnium mounted on a rotating mechanism. Each material is deposited by sputtering the surface of the corresponding target with a highly energetic argon ion beam (not visible in the picture) in a reactive oxygen atmosphere. During the growth of the layers, a second lower-energy ion beam, mixing argon and oxygen, is directed towards the sample to adjust the stoichiometry of each oxide layer (SiO_2 , Ta_2O_5 , HfO_2) and improve their packing density.

The sample to be coated is a plane silica window 25 mm in diameter, 1 or 2 mm thick, installed in a rotating substrate holder, as shown on the left of Fig. 1 (distance between the substrate center and the rotation axis about 53 mm). The rotary movement of the substrate (rotation speed 120 turns per minute) is used to improve the uniformity of the layers deposited at the bottom surface of this sample. This sample can be illuminated with a collimated probe beam from the top of the machine through the entrance window, and this beam is shifted sideways by a periscope. This probe beam is thus fixed relative to the machine, which means that it is necessary to synchronize any transmission or reflection measurement with the rotation of the substrate holder [7].

2.2. Measurement system

The design of the interferometric measurement system must take into account three main constraints, namely:

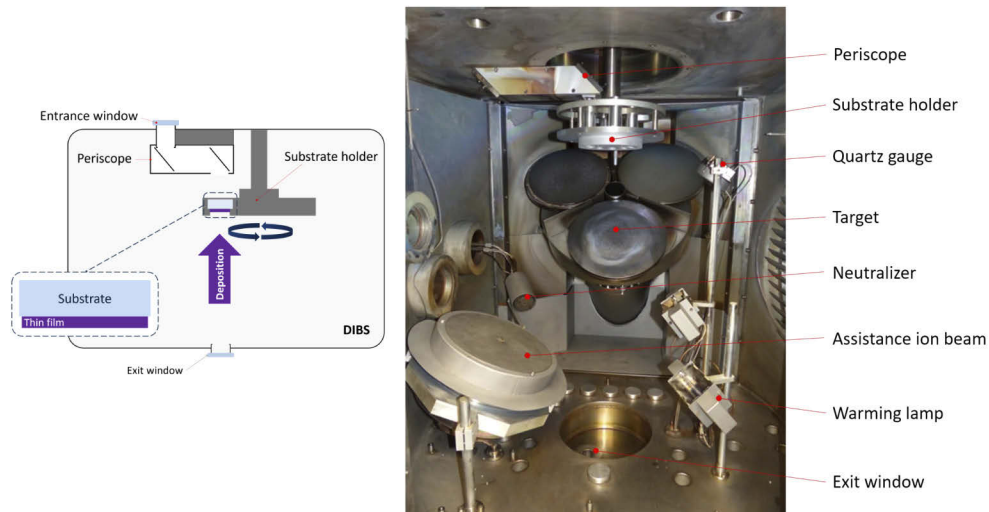


Fig. 1. The DIBS deposition machine (on the left, schematic view of the substrate configuration; on the right, picture of the inside of the machine).

1. a continuous displacement of the sample with respect to the machine frame, which can be caused by thermal expansion of the chamber and wobbling of the substrate holder,
2. the vibration of the machine caused by the vacuum pump,
3. the presence of a parasitic signal due to the reflection of the probe light beam from the top face of the substrate.

To overcome the first constraint, we insert a very thin plane steel ring between the bottom face of the substrate and the substrate holder, as shown in Fig. 2. This annular stop prevents the deposition of any material onto the outer zone of the substrate, and this uncoated circular crown can be used as a local reference for the interferometric measurement of the layer thickness deposited over the central zone. Consequently, the result of a measurement is the difference $\Delta\phi$ between the phase values recorded at the center (ϕ_C) and in the outer annular zone (ϕ_A) respectively of the substrate.

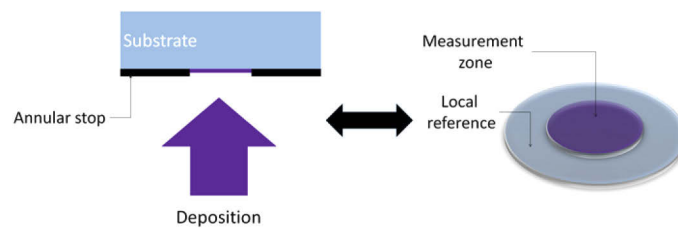


Fig. 2. Principle of the substrate self-referencement.

To solve the vibrations problem, we used a powerful light source working in triggered mode, synchronized to the substrate holder rotation (2 Hz) and emitting a very short pulse (10 μ s), allowing an instantaneous interference state when the witness sample is centered on the probe beam to be recorded. Spurious interference signals are suppressed in the same way as that implemented by Lee et al. [8], namely the use of a low coherence source.

We installed on the top of the deposition machine a high stiffness optical bench holding a Michelson type interferometer with one arm formed by the periscope-substrate assembly, as shown in Fig. 3. A low coherence source (superluminescent diode, central wavelength $\lambda_0 = 830$ nm, spectral bandwidth $\Delta\lambda = 17$ nm) is coupled into a single mode fiber whose output end is placed in the focal plane of an aspherical lens with a focal length of 150 mm. The collimated beam provided by this assembly is divided into two perpendicular arms by a cube beam splitter. The light beam transmitted by the splitter (reference beam) is reflected by a plane mirror mounted on a motorized translation stage, while the beam reflected downwards by the same beam splitter (probe beam) illuminates the whole surface of the witness substrate after passing through the periscope. Both reflected beams are recombined by the splitter cube and detected by a low-noise 14-bit CCD camera with 1600×1200 pixels of $7.4 \mu\text{m}$ square. Finally, a low-distortion photographic lens is used to image the bottom surface of the witness sample on this CCD matrix.

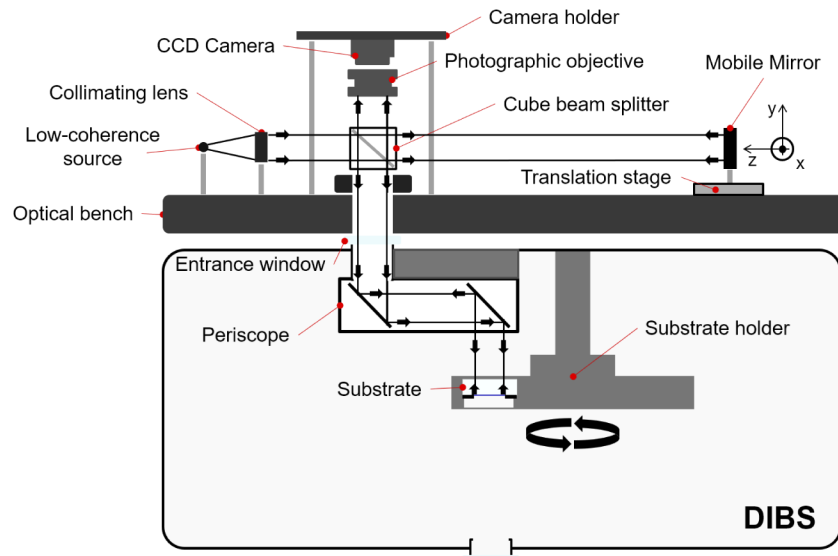


Fig. 3. Schematic representation of the interferometric set-up installed on the top of the DIBS vacuum chamber.

A small tilt is introduced between the two end-mirrors of the Michelson interferometer, in order to produce a quasi-parallel fringes pattern at the surface of the CCD, as shown in Fig. 4.

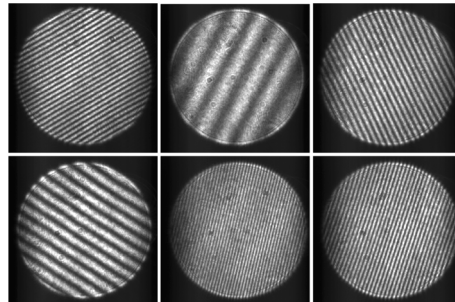


Fig. 4. Examples of interferograms recorded by the CCD camera on a mirror sample.

To ensure a good quality recording of this fringe pattern by the CCD matrix, it is first necessary for the pixel size p to be not greater than one sixth of the fringe period P , i.e.

$$p \leq \frac{P}{6} = \frac{\lambda_0}{12\theta} \quad (1)$$

where θ is the instantaneous value of the tilt angle between the two end-mirrors. This leads a maximum tilt angle of approximately 10 milliradians (0.6 degree) to be specified between the two end-mirrors of the Michelson interferometer. However, this fringe pattern must also be recorded with good contrast, which requires that the changes of the relative axial position between these two end-mirrors be less than half the coherence length l_c of the source, i.e.

$$\delta z \leq \frac{l_c}{2} = \frac{\lambda_0^2}{2\Delta\lambda} \sim 20 \mu\text{m}. \quad (2)$$

To relax this axial stability constraint up to 100 μm , while maintaining the benefits of the low coherence interferometric scheme, an additional bandpass filter (central wavelength 830 nm, spectral bandwidth 3.2 nm) is placed in front of the CCD camera; furthermore, this filter reduces the amount of parasitic light seen by the CCD matrix.

3. Theoretical model

3.1. Reflection coefficient

As emphasized in section 2.2, the result of a measurement is the difference between the phase values recorded in the central zone C and the annular zone A, i.e. to a first approximation,

$$\Delta\phi = \phi_C - \phi_A = \rho_C - \rho_A \quad (3)$$

where ρ is the phase of the reflection coefficient r , defined as

$$r = \sqrt{R} e^{i\rho}. \quad (4)$$

Figure 5 gives a schematic view of the measurement method. For the reference zone A, the reflection coefficient is given by:

$$r_A = \frac{\tilde{n}_s - \tilde{n}_v}{\tilde{n}_s + \tilde{n}_v} \quad (5)$$

where \tilde{n}_s (respectively \tilde{n}_v) is the effective index of the substrate (respectively vacuum). Consequently, in normal incidence:

$$r_A = \frac{n_s - 1}{n_s + 1} \Rightarrow \rho_A = 0. \quad (6)$$

Similarly, for the central zone C, the reflection coefficient is given by [14,15]:

$$r_C = \frac{\tilde{n}_s - Y_0}{\tilde{n}_s + Y_0} \quad (7)$$

where Y_0 is the complex admittance of the bottom interface of the substrate (i.e. the top interface of the stack). For example, in the case of a single layer, we have, again in normal incidence

$$r_C = \frac{n_1(n_s - n_v) \cos \delta_1 - i(n_s n_v - n_1^2) \sin \delta_1}{n_1(n_s + n_v) \cos \delta_1 - i(n_s n_v + n_1^2) \sin \delta_1} \quad (8)$$

where δ_1 is the phase term associated to this layer. That leads to the following expression for the phase ρ_C :

$$\rho_C = \arctan \left[\frac{2n_s n_1 (n_1^2 - n_v^2) \sin 2\delta_1}{(n_1^2 + n_v^2)(n_s^2 - n_1^2) + (n_1^2 - n_v^2)(n_s^2 + n_1^2) \cos 2\delta_1} \right]. \quad (9)$$

Figure 6 shows the variation of the phase difference $\Delta\phi = \rho_C - \rho_A$ versus the thickness of the deposited layer, on the left for SiO_2 and on the right, for Ta_2O_5 . Note that the non-linearity of

this relation increases with the mismatch between the refractive index of the layer and that of the substrate. Note also that the deposition of a silica layer onto a silica substrate can be monitored using this interferometric approach even if their refractive indices are identical; this would be impossible in the case of intensity monitoring.

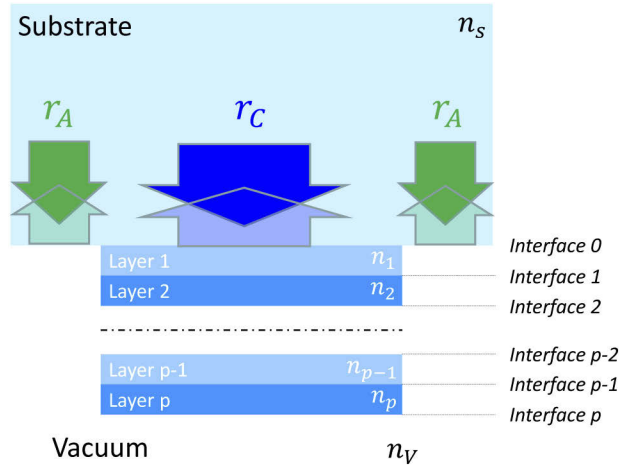


Fig. 5. Schematic view of the measurement method.

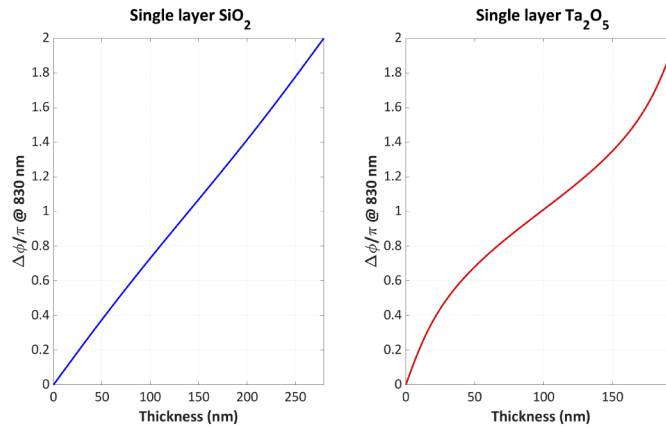


Fig. 6. Theoretical variation of the phase difference $\Delta\phi$ versus the thickness of the deposited layer (on the left, silica; on the right, tantala).

3.2. Data processing

Quite generally, the signal recorded by the CCD matrix is described by the following relation:

$$S(x, y) = S_0(x, y) + S_1(x, y) \cos \left[\frac{4\pi}{\lambda} (\alpha x + \beta y) + \Phi(x, y) \right] \quad (10)$$

where α and β are the components of the tilt angle along x and y axes.

Figure 7(a) shows a false color representation of this fringe pattern when the central zone of a substrate is coated with a 90 nm thick Ta₂O₅ layer (numerical modelling). The surface

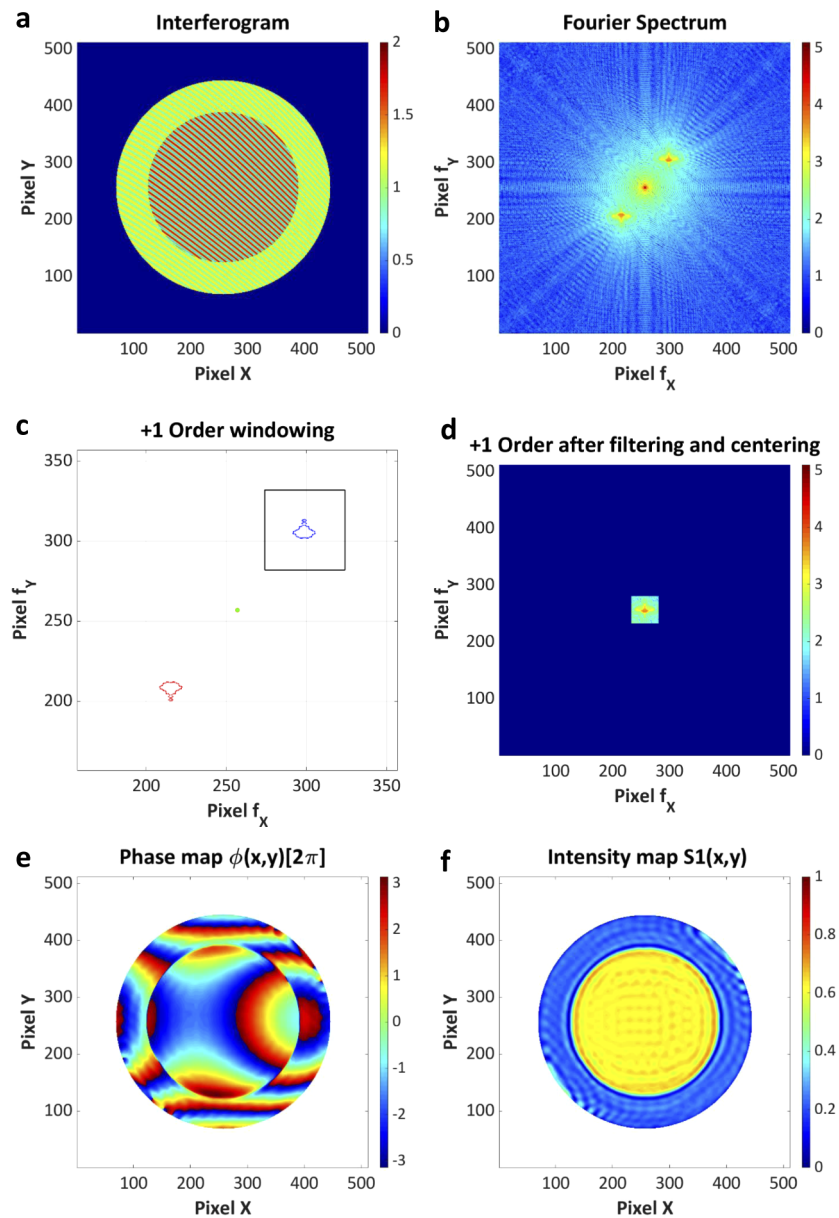


Fig. 7. Numerical modelling of the different steps used for the data processing [Graph a, intensity $S(x,y)$ recorded by the CCD for $S_0 = 1$ - Graph b, modulus of Fourier spectrum in log units - Graph c, square 'brick wall' windowing applied to the +1 order - Graph d, +1 order of the Fourier spectrum after filtering and centering (log units) - Graph e, map of the phase divided by 2π - Graph f, map of the intensity S_1].

flatness error of this substrate is roughly λ , causing a slight deformation of the fringes, almost imperceptible on the illustration.

A 2D fast Fourier transform is applied to this digitized signal, resulting in three separate orders (see Fig. 7(b) for a false color representation of this Fourier spectrum in log scale), in accordance

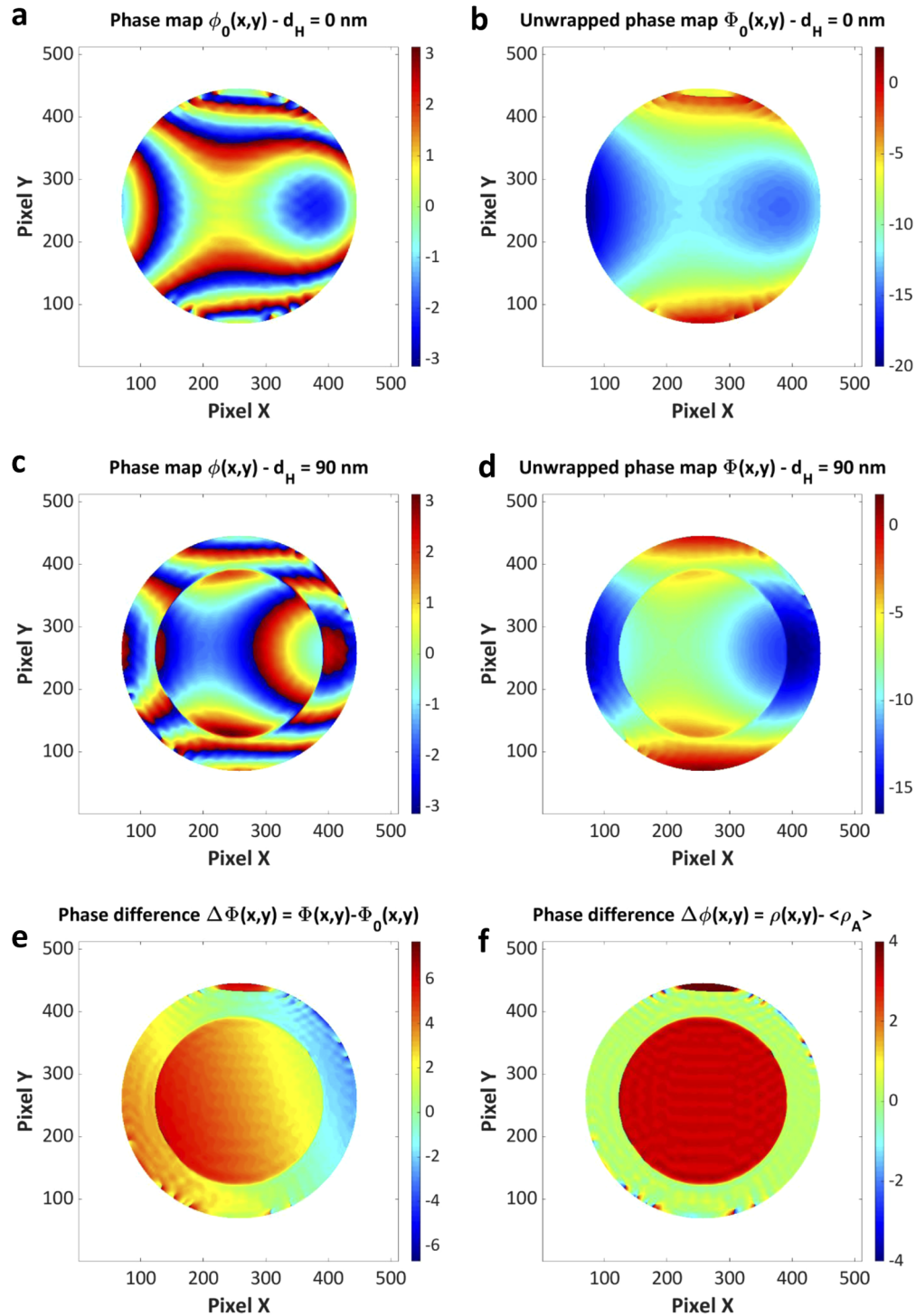


Fig. 8. False color representation of the phase maps used to extract the phase difference between the central zone and the reference annular zone (modeled data, all graphs in radians, see text for more details).

with the following expression:

$$\widetilde{S}(f_x, f_y) = \widetilde{S}_0(f_x, f_y) + \widetilde{S}_+(f_x - 2\alpha/\lambda, f_y - 2\beta/\lambda) + \widetilde{S}_-(f_x + 2\alpha/\lambda, f_y + 2\beta/\lambda) \quad (11)$$

where \widetilde{S} is the Fourier transform of S and where $S_{\pm}(x, y)$ is defined by:

$$S_{\pm}(x, y) = \frac{1}{2} S_1(x, y) e^{\pm i\Phi(x, y)}. \quad (12)$$

Windowing is then applied to this spectrum around the first order (square 'brick wall' filter, see Fig. 7(c)) and the filtered data are re-centered on the spatial frequency origin (see Fig. 7(d)). Note that the quality of this windowing requires that the ± 1 orders are sufficiently far from the central zero order. Experimentally, this is achieved by using a tilt angle θ greater than 5 milliradians, by applying a Hamming window [16] on the recorded interferograms to smooth the transition between the image of the sample and the background, and by using a 'brick wall' filter with self-adaptive elliptical shape in the frequency space.

An inverse 2D fast Fourier transform is applied to this re-centered signal to recover the function $S_+(x, y)$. A modulo 2π determination of the phase $\Phi(x, y)$ is given by

$$\phi(x, y) = \arctan \left\{ \frac{\Im[S_+(x, y)]}{\Re[S_+(x, y)]} \right\} \equiv \Phi(x, y) \pmod{2\pi} \quad (13)$$

while the modulus of $S_+(x, y)$ is simply equal to $2S_1(x, y)$ (see Figs. 7(e) and 7(f) respectively). Note in Fig. 7(f) the deformation of the phase map levels caused by the initial surface flatness error of the substrate.

Finally this phase, modulo 2π , is transformed into an absolute value, via a phase unwrapping procedure based on the algorithm developed by Herraiez et al. [17]. Some examples of phase maps recorded before and after unwrapping are shown in Fig. 8: at the top (graphs a and b) before coating, and in the middle (graphs c and d) after deposition of a half-wave layer of Ta_2O_5 (modeled data).

By subtracting the unwrapped phase map recorded without coating from that recorded during deposition, the influence of the flatness error of the substrate is canceled (see Fig. 8(e)). However, to simulate the effects of vibration, the tilt of the substrate is modified in our modeling program before each new acquisition: this explains the graded color changes observed in the central and annular zones. By subtracting the tilt value determined over the reference annular zone, this effect is canceled and the phase difference $\rho_C - \rho_A$ (see Fig. 8(f)) is finally obtained, as expected.

4. Experimental results

The left of Fig. 9 shows an overall view of the deposition machine with, on the top, the interferometric measurement system, and to the right of the same figure, a closer view of the upper part of this experimental set-up. Note that the reference arm of the Michelson interferometer is folded using two plane mirrors at 45 degrees to satisfy dimensional constraints.

4.1. Preliminary characterizations

Before applying this interferometric set-up to monitoring the deposition of a single layer, some preliminary tests were carried out to quantify its intrinsic performance.

The first test consists in using the motorized translation stage to scan the axial position of the reference mirror over a distance that allows the intensity of the echoes respectively associated with the reflection from the front face and from the rear face of a 2 mm thick bare silica substrate located in the substrate holder to be recorded. The result of this measurement is shown in Fig. 10. Each maximum of visibility corresponds to a position of the reference mirror for which interference with an optical path difference of zero occurs. Consider the blue dots in the graph of

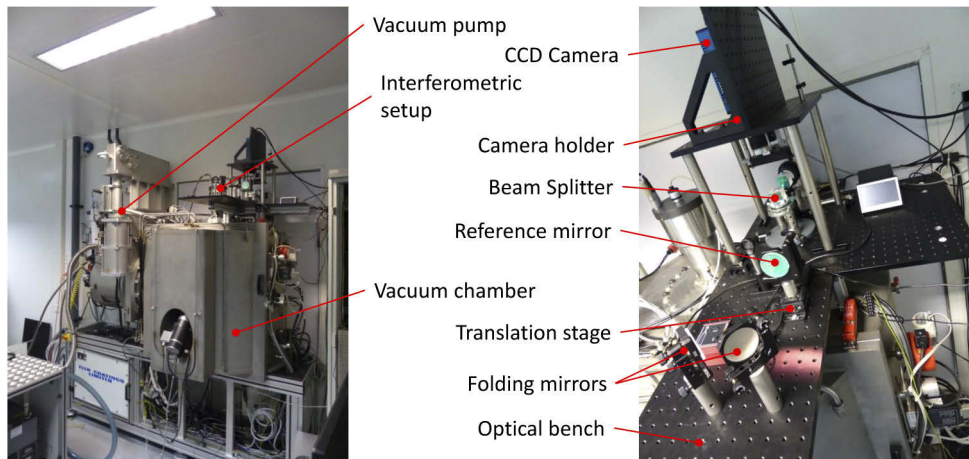


Fig. 9. Photographs of the experimental set-up (on the left, overall view of the deposition machine; on the right, a closer view of the upper part of the interferometric set-up).

Fig. 10, recorded when the deposition chamber is filled with air: the left maximum ($z = 7.632$ mm) corresponds to the reflection from the top face of the substrate, while the right maximum ($z = 10.716$ mm) is associated with the reflection from its bottom face. The distance between these two maxima, i.e. 3.084 mm, is in good agreement with the optical thickness of the substrate (2 mm). When the same recording is made under vacuum (red dots graph of Fig. 10), the positions of both maxima are slightly shifted toward the low z values, in accordance with the refractive index decrease (approximately 3×10^{-4}) caused by an air-to-vacuum transition: indeed, this change causes a slight decrease in the optical path length of the Michelson arm whose substrate is the end-mirror. However, the distance between these two echoes is not changed ($10.413 - 7.329 = 3.084$ mm), since the optical thickness of the substrate is not affected by this air-to-vacuum transition. Finally, note that the full width at half maximum of each of these echoes is sufficiently narrow to guarantee that there is no overlap.

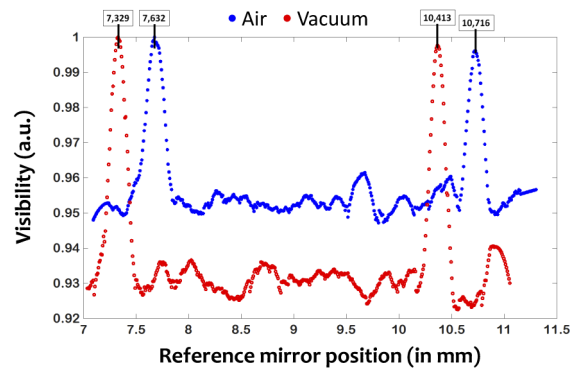


Fig. 10. Recording of the axial position of the echoes associated with the reflection from both faces of the substrate (blue dots, in air; red dots, in vacuum).

The second test consists in recording the time fluctuations of the phase difference $\Delta\phi$ measured over approximately 5 minutes on the same bare silica substrate in both static and dynamic configurations, i.e. with and without rotation of the substrate holder. The results are summarized in Tab.1, where Δ is the optical path difference associated with $\Delta\phi$ [$\Delta = \Delta\phi \times (\lambda/2\pi)$].

Table 1. Intrinsic performance of the set-up in static and dynamic configurations (mean values and standard deviations)

Configuration	$\langle \Delta\phi \rangle$ (radians)	$\sigma_{\Delta\phi}$ (radians)	$\langle \Delta \rangle$ (nm)	σ_{Δ} (nm)
static	0.005	0.015	0.7	2.0
dynamic	0.014	0.065	1.8	8.6

To estimate the accuracy in term of deposited thickness, we have to divide these data by 2 (reflective configuration) and take into account the refractive index of the layer: this leads for instance to a measurement noise σ_d of about 2 nm in the case of a Ta₂O₅ layer.

4.2. Monitoring the deposition of a single layer

Figure 11 shows two examples of results obtained during the deposition of a Ta₂O₅ layer.

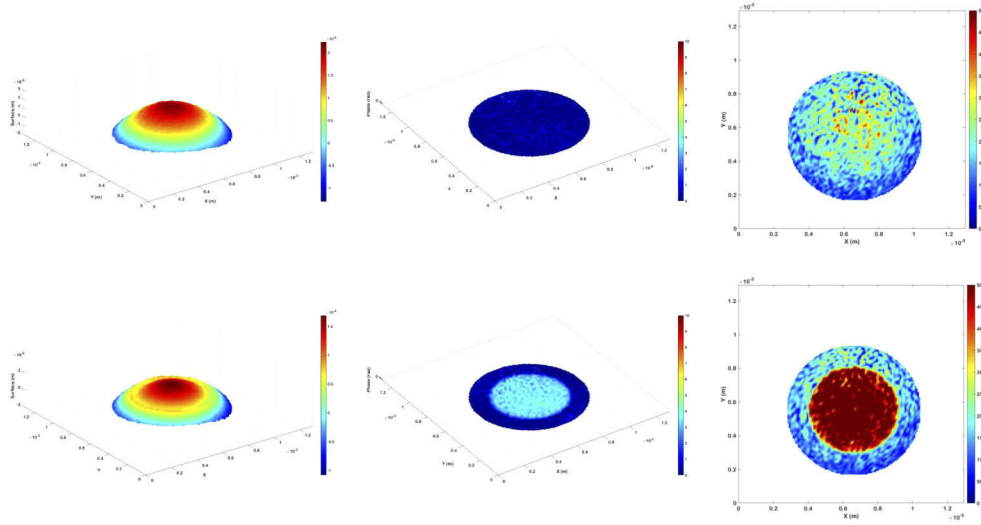


Fig. 11. Examples of shape, phase and intensity maps recorded during the deposition of a Ta₂O₅ layer, on the top, for $d_H = 0$ nm and on the bottom, for $d_H \sim 100$ nm [shape in m, phase in radians, intensity in arbitrary units].

The three top graphs correspond to the shape of the bottom face of the substrate (left graph), and to the corresponding phase and intensity maps (middle and right graphs) recorded just before deposition. The substrate holder is rotating and the deposition chamber is under vacuum. The two ion beams (sputtering and assistance) are ready to be activated. The three bottom graphs correspond to the same maps, but after deposition of a 100 nm thick Ta₂O₅ layer. Note that the initial shape of the substrate is not a plane but is close to a sphere with a radius of curvature about 2 m. For each acquisition, this radius of curvature is determined using only the uncoated annular zone and this information is used to correct the data in the central zone. Note also the uniformity of the phase data recorded over both the central and annular zones, and the level variation of the intensity recorded over the surface of the sample, that reveals the Gaussian shape of the probe beam as well as its relatively narrow spectral bandwidth (speckle pattern). To overcome this difficulty, the modulus of the reflection coefficient is calculated using the following formula:

$$|r| = \frac{\langle S_1 \rangle_C}{\langle S_1 \rangle_A} \times \frac{\langle S_1 \rangle_{A,0}}{\langle S_1 \rangle_{C,0}} |r|_0 = \frac{\langle S_1 \rangle_C}{\langle S_1 \rangle_A} \times \frac{\langle S_1 \rangle_{A,0}}{\langle S_1 \rangle_{C,0}} \cdot \frac{n_s - 1}{n_s + 1} \quad (14)$$

where the quantities with subscript 0 correspond to the values recorded just before the start of deposition.

Figure 12 shows the change in the modulus and phase of the reflection coefficient with respect to time during the deposition of a half-wave silica layer onto a silica substrate.

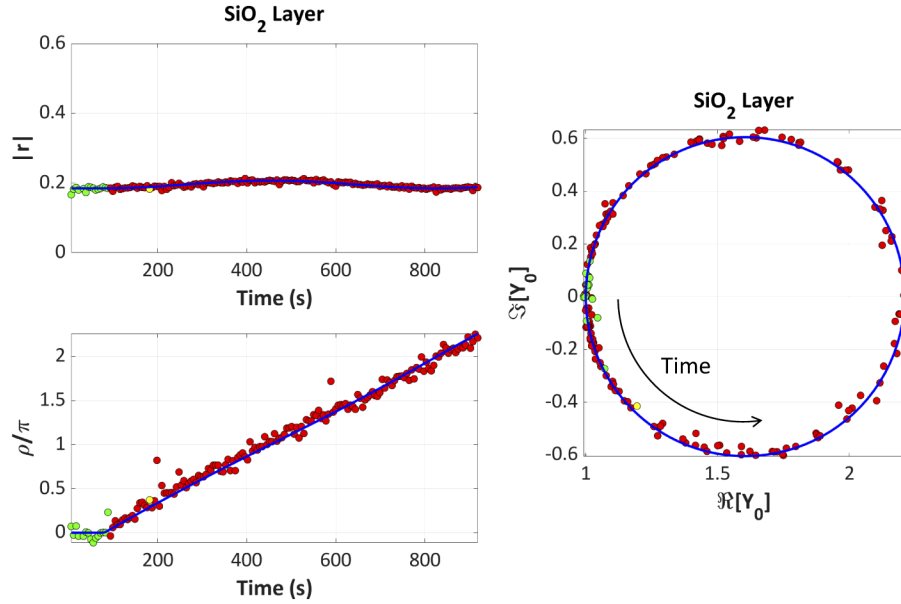


Fig. 12. Experimental data recorded during the deposition of a half-wave silica layer onto a silica substrate (see text for more details).

The red dots correspond to measurement results, namely the modulus of r and its argument ρ divided by π . The green dots also correspond to experimental results, but the color change is used simply to identify the acquisitions performed before the start of the layer deposition. Moreover, by inverting relation (7), the admittance Y_0 can be derived from the reflection coefficient r , i.e.

$$Y_0 = n_s \left(\frac{1-r}{1+r} \right). \quad (15)$$

The result of this calculation is presented on the right of Fig. 12 as a trajectory in the complex plane (admittance locus). Finally, on these three graphs the blue line corresponds to a theoretical fit, based on relation (8), in which the only free parameters are the refractive index of the layer (n_1), the deposition rate (v), assumed constant, and the time value t_0 corresponding to the start of the layer deposition. Consequently, we have:

$$d_1(t) = \begin{cases} 0 & \text{if } t \leq t_0 \\ v(t - t_0) & \text{if } t \geq t_0 \end{cases}. \quad (16)$$

The fitting process provides the following results: $t_0 = 80$ s, $v = 0.374 \pm 0.015$ nm/s, and $n_1 = 1.4865 \pm 0.005$; the agreement between experimental data and theoretical fit is excellent. Moreover, the deposition rate and the refractive index are comparable with those obtained a few months ago [$v = 0.3364$ nm/s, $n_1 = 1.4837$] on the same deposition machine using another method [18].

The results obtained with the same approach during the deposition of a half-wave tantala layer on a silica substrate are shown in Fig. 13. Again, the agreement between experimental results

and theoretical fit for the modulus of the reflection coefficient is very satisfactory, even if there is also a discrepancy in the phase term (about 0.25 radians). This difference is notably visible on the admittance locus graph (right of Fig. 13) where the center of the blue circle clearly does not appear to be in the right place, even though its radius seems correct. Adding 0.25 radians to the theoretical phase values shifts the model data (thin black circle) to the right place with respect to the experimental data. We still have no satisfactory explanation for this discrepancy. Note that the refractive index and deposition rate values (respectively, 2.1137 ± 0.02 and 0.255 ± 0.007 nm/s) are in good agreement with the results of previous measurements [7].

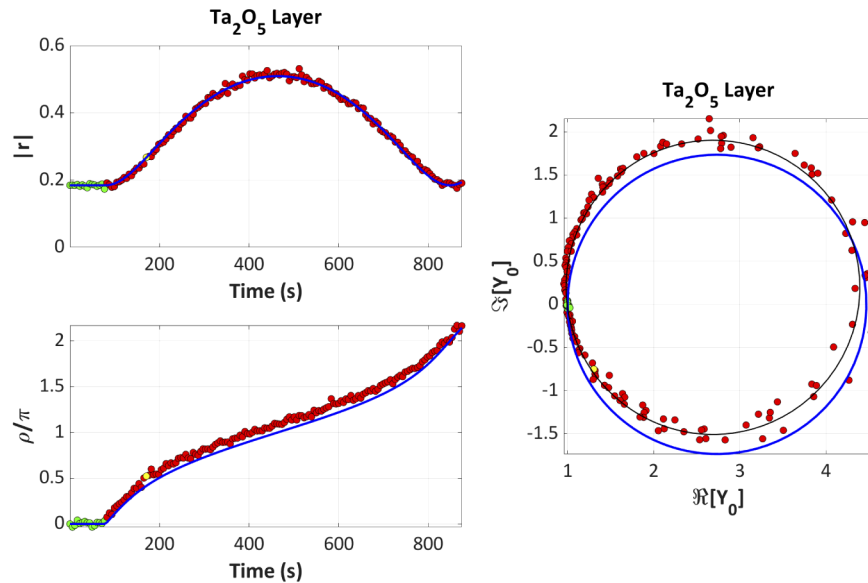


Fig. 13. Experimental data recorded during the deposition of a half-wave tantalum layer on a silica substrate (see text for more details).

5. Discussion and conclusion

5.1. Discussion

This interferometric approach allows the growth of a single layer to be monitored through the temporal change of the admittance Y_0 in the complex plane. The trajectory shape shows that the accuracy of the material change should be nearly independent of the layer thickness. The obtained results are promising and should permit to satisfy one of our objective, namely to monitor the deposition of matching layers between stacked Fabry-Perot cavities.

The implementation of this interferometric scheme for the monitoring of the deposition of complete stacks, such as an 8-layer antireflective coating can be also envisaged, although more challenging. Indeed, the corresponding phase variations (see Fig. 14) are mostly linear throughout the stack deposition, while the dimensions of the admittance locus are approximately the same as those recorded during the deposition of a half-wave silica layer. However, the actual performance of our set-up (optical path difference noise about 10 nm in dynamic configuration) has to be improved to allow very thin layers with thicknesses less than 25 nm to be accurately monitored.

In addition, our method gives access to an estimation of the change in the radius of curvature of the front face of the substrate during the deposition of a stack (see section 4.2). The order of magnitude is correct, but the instantaneous fluctuations are today too large to allow the time evolution of the layers' stresses to be determined with a sufficient accuracy.

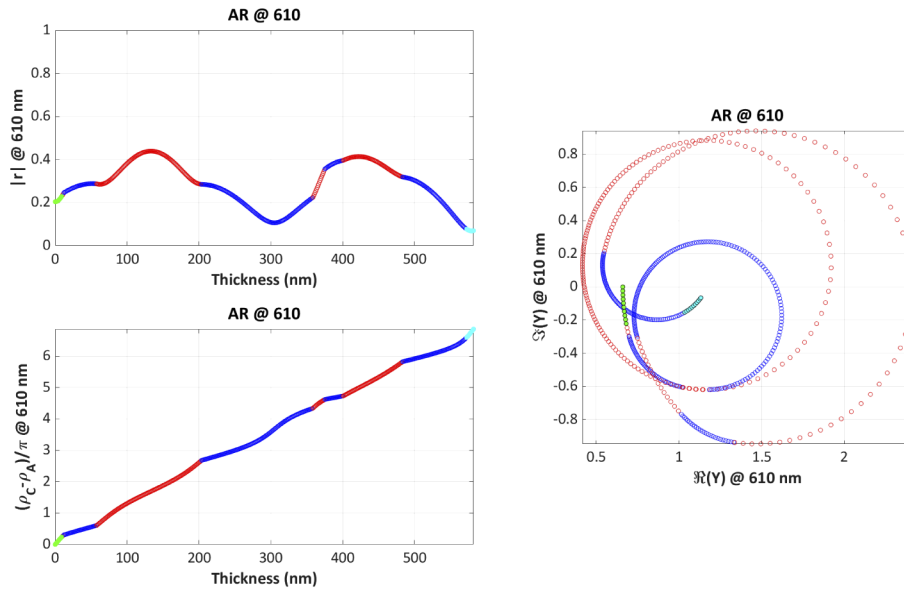


Fig. 14. Theoretical data recorded during the deposition of an 8-layer antireflective coating onto an N-BK7 substrate.

To improve the performance of our set-up, several changes can be envisaged, namely:

- to decrease the focal length of the photographic lens used to image the bottom surface of the sample on the CCD matrix; this will allow to record the interferogram with a better spatial resolution and to increase the number of pixels used for the calculation of the phase difference $\phi_C - \phi_A$,
- to increase the peak power of the light pulse provided by the superluminescent diode, and to decrease the duration of this pulse (better cancellation of the vibrations effect),
- to select a CCD camera with upgraded performance (16 bits),
- to add a motorized sub-assembly using e.g. a Risley prism pair to provide a dynamic alignment capability of the probe beam with respect to the substrate (as stressed in section 3.2, the tilt angle between the reference mirror and the substrate must remain between 0.005 radians and 0.01 radians).

5.2. Conclusion

We have demonstrated that the use of an interferometric approach can provide useful information for the *in situ* monitoring of the deposition of transparent layers. The implementation of a self-referenced scheme allows accurate measurements to be obtained despite the severe constraints created by the thermal and vibrational environment. Moreover, it is surely possible to implement simultaneously optical broadband monitoring (we have successfully carried out some preliminary tests in this direction) so as to mix intensity and phase measurements in this way.

In addition, the use of low coherence interferometry allows easy implementation of some other on-line measurements, such as a real time measurement of the temperature of the substrate.

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Disclosures

The authors declare no conflicts of interest.

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