## Supplemental Materials: Intermolecular interactions in optical cavities: an ab initio QED study

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## I. ADDITIONAL DATA FOR VAN DER WAALS BONDS

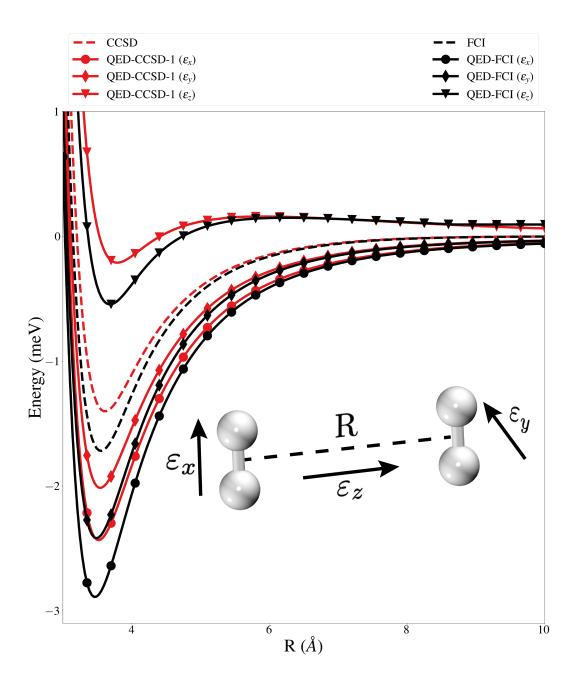


FIG. 1.  $(H_2)_2$  polarization along H-H bond, orthogonal and along the chain.

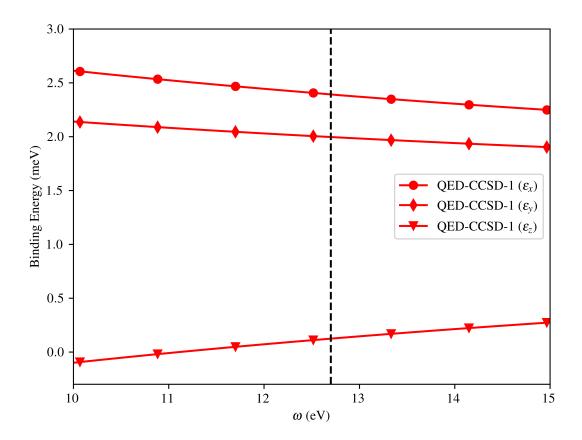


FIG. 2. Binding energy of two parallel  $H_2$  molecules as a function of the photon frequency. Binding energies are calculated as energy differences between the value at 20 Å and 3 Å. The coupling value is set to  $\lambda = 0.1$  and all three polarization directions have been presented. The black dashed line is the resonance frequency (12.7 eV).

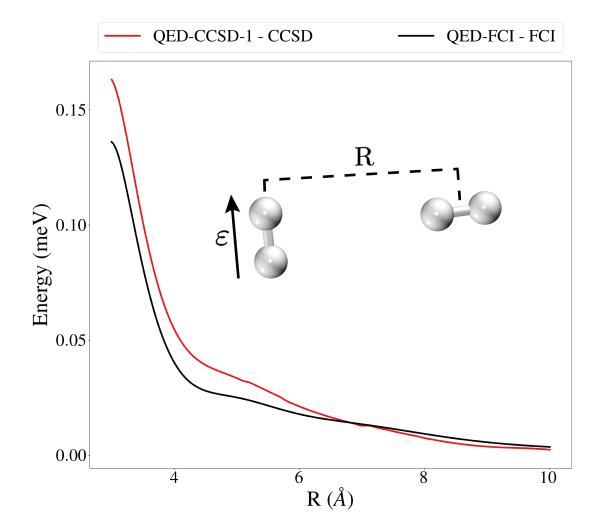


FIG. 3. Cavity induced effects on potential energy curves for two  $H_2$  molecules in  $C_{2v}$  configuration stretching the distance between them. The polarization has equal components along the bond, chain and orthogonal directions with coupling  $\lambda=0.1$  and frequency  $\omega=12.7$  eV. The value at 200 Å has been subtracted.

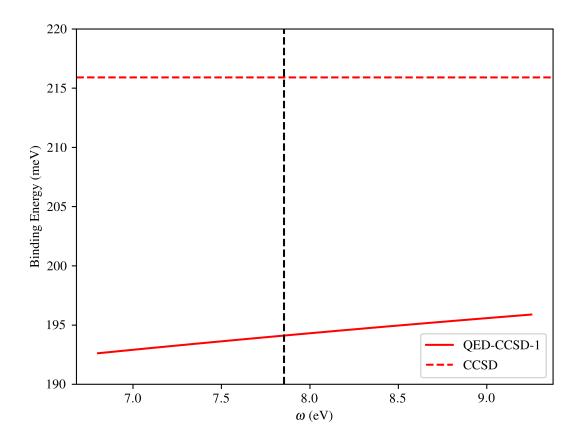


FIG. 4. Binding energy of the  $H_2O$  dimer as a function of the photon frequency. Binding energies are calculated as energy differences between the value at 20 Å and 3 Å distance between the oxygen atoms. The coupling value is set to  $\lambda = 0.1$  and the polarization is parallel to the oxygens. The black dashed line is the resonance frequency (7.86 eV).