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Different types of spin currents in the comprehensive materials database of nonmagnetic spin Hall effect

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Spin Hall effect (SHE) has its special position in spintronics. To gain new insight into SHE and to identify materials with substantial spin Hall conductivity (SHC), we performed high-precision high-throughput ab initio calculations of the intrinsic SHC for over 20,000 nonmagnetic crystals. The calculations revealed a strong relationship between the magnitude of the SHC and the crystalline symmetry, where a large SHC is typically associated with mirror symmetry-protected nodal line band structures. This database includes 11 materials with an SHC comparable to or even larger than that of Pt. Materials with different types of spin currents were additionally identified. Furthermore, we found that different types of spin current can be obtained by rotating applied electrical fields. This improves our understanding and is expected to facilitate the design of new types of spin-orbitronic devices.

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INTRODUCTION

Even though the extrinsic spin Hall effect (SHE) was predicted almost 50 years ago^{1,2}, the SHE did not receive extensive attention until the last decade, after theoretical studies of its intrinsic mechanism^{3,4} and its experimental observation^{5–7}. The SHE gives rise to an electrical current to generate a transverse spin current^{1,2,8}, and vice versa^{9–11}. The advantages of strong SHE materials, which are of central importance for the detection, generation, and manipulation of spin currents suggested the necessity of performing large-scale screening to identify the most suitable materials for spintronics devices. Experimentally, however, such large-scale screening would be highly impractical, as quantitative determination of the spin Hall conductivity (SHC) by electrical measurement requires integrating each material separately into a complex multicomponent microscopic transport device^{9–11}. In contrast, theoretically and computationally the situation is in principle much more straightforward. An additional advantage of high-throughput calculations is that they can provide further insight into the physics of the SHE and suggest general guidelines for designing new SHE materials.

In general, the SHE has two origins: an extrinsic contribution from scattering and intrinsic contributions from electronic band structures. In this study, we focus only on the intrinsic contribution for two reasons. First, the intrinsic contribution is typically dominant in systems with strong spin-orbit coupling (SOC)⁸. Second, the SHE can be accurately predicted theoretically as long as the calculation of the electronic structure is sufficiently precise^{3,4,8,12–14}. Contrary to this, the extrinsic contributions are much more difficult to predict and strongly depend on the type of scattering. In many cases, the calculated intrinsic SHE is in good qualitative agreement with the experimental measurements^{8,15}. For example, the large intrinsic SHC of Pt^{16–19} or the predicted sign change of the SHC from Pt to Ta were experimentally observed^{20,21}. Therefore, this database is anticipated to be helpful for selecting new materials with a spin-to-charge conversion, even if the predicted values are not expected

to be precisely reproducible in experiments. Apart from the SHC, other parameters could also be used to determine the usefulness of material for spin-to-charge conversion, in particular the spin Hall angle (SHA)^{8,22}. Although we did not attempt to evaluate these parameters in this study, we note that the charge conductivity is straightforward to measure experimentally; thus, the SHAs can be easily obtained from our calculations for materials for which the conductivity is experimentally known.

RESULTS AND DISCUSSION

Workflow

We developed automatic Wannier function (WF) generating code to enable us to conduct high-throughput simulations and calculations. The workflow of the procedure we followed to build a collection of suitable materials for inclusion in our database is shown in Fig. 1. Most of the materials we studied are in the ICSD database²³, which contains details of real materials that have been experimentally characterized. In addition, we also considered computational materials from the Materials Project^{24,25} (MP), because they were extracted from alloys or similar structures on the basis of experimentally known materials and could thus possibly be synthesized. Owing to the limited accuracy of the density functional theory (DFT) for strongly correlated systems, we did not consider computational materials from the MP that contain V, Mn, Fe, Co, Ni, N, O, F, Cl, or f-electron atoms. This is because these materials are often strongly correlated and the predicted structures may thus be less accurate (see Fig. 1). We did not remove the materials that are possibly strongly correlated from the ICSD database, as it is almost impossible to accurately estimate the strength of these correlations from high-throughput calculations. Furthermore, generalized gradient approximation (GGA)-level calculations would be useful even for those materials characterized by strong correlations. However, we did remove all

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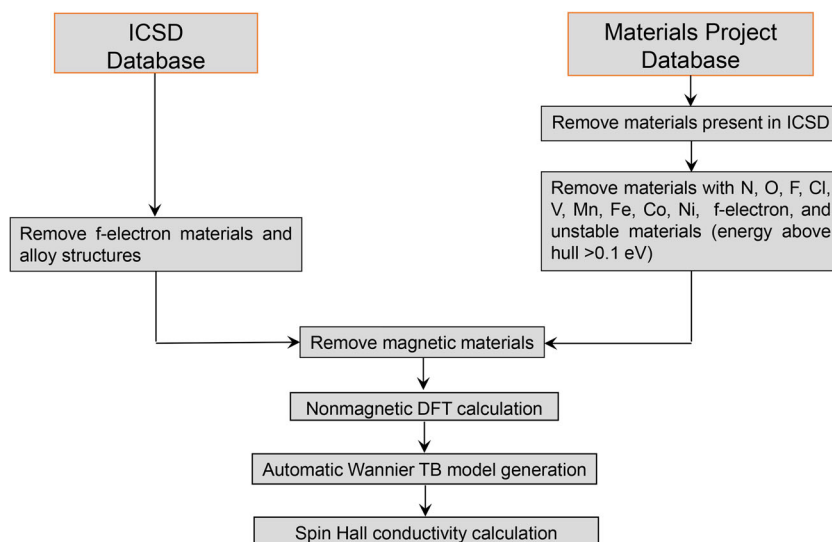


Fig. 1 Workflow to obtain the dataset of materials for the high-throughput calculations of intrinsic SHC.

f-electron systems. We then used the MP database to identify materials that were likely to be magnetic. After excluding these materials, 17,682 real materials from the ICSD database and 2486 computational materials from the MP remained.

These lattice structures were then loaded into the full-potential local-orbital minimum-basis code of FPLO for DFT calculations^{26,27}. We then projected the Bloch wavefunctions into highly symmetric atomic-orbital-like WFs, and generated the corresponding tight-binding model Hamiltonians. The symmetry of the tight-binding model Hamiltonian is essential to determine the SHC accurately. Based on the tight-binding model Hamiltonian, the intrinsic SHCs were computed by the Kubo formula approach^{4,12,14}. The accuracy of the calculated SHCs was doubly checked by the symmetry analysis^{28,29}. All of the SHC calculations were based on DFT calculations for nonmagnetic materials. A few of the materials we considered could have been magnetic; however, the SHC calculation for these materials would not be accurate. We thus checked the magnetic states of materials with large SHC (>500 (\hbar/e)(S/cm)) using spin-polarized DFT calculations to eliminate the remaining magnetic materials.

Data overview

The distribution of the calculated SHC for the full set of materials is shown in Fig. 2. (Details of each of these compounds can be found on our website). Among the $>20,000$ materials, we identified only 1048 with an SHC larger than 500 (\hbar/e)(S/cm), and only 169 for which the value was above 1000 (\hbar/e)(S/cm). We identified eleven materials with an SHC comparable to or even larger than that of Pt: IrN, In_5Bi_3 , Tl_3Ru , Pt_3Rh , $CuPt_7$, $LiPt_7$, Bi_2OsAu , Bi_3In_4Pb , $HgOsPb_2$, $Lilr$, and $PtRh_3$. Of these materials, In_5Bi_3 , $CuPt_7$, $LiPt_7$, and $Lilr$ were already synthesized in experiments (details appear in the SI). The compound with the largest SHC is IrN, which has an SHC larger than 2900 (\hbar/e)(S/cm) in σ_{zx}^y ; however, we note that this is for a theoretically proposed phase of IrN^{30,31}. The next largest is In_5Bi_3 , which, unlike the other compounds with large SHC that contain $5d$ elements, is a pure p -orbital metal with an SHC above 2500 (\hbar/e)(S/cm) in the σ_{xy}^z component. Apart from the record-breaking in In_5Bi_3 , the high-throughput calculations identified four other non-transition metal compounds (InBi, In_2Bi , In_5Bi_2Pb , and the element Tl) with a large SHE. The fact that only a handful of the $20,000$ crystals we studied has an SHC larger than that of Pt and none has a significantly higher value, suggests that we may have approached the realistic limit of the intrinsic SHC in our calculations.

Giant SHC

To analyze the origin of the large SHC, we considered the spin Berry curvature (SBC) distribution in the Brillouin zone (BZ) of the top 12 compounds with $SHC > 2000$ (\hbar/e)(S/cm). We discovered that in most of these materials, the large SHC is associated with nodal lines protected by the mirror symmetry, see Fig. 2c. The nodal lines are one-dimensional band crossings, which exist in the absence of SOC protected by the mirror (or other) symmetry³². With SOC, the nodal lines are split, which gives rise to a large SBC if the nodal lines cross the Fermi level. Particulars for two selected materials, In_5Bi_3 and Pt, are shown in Fig. 3 and those of the others are included in the SI. The giant SHC in In_5Bi_3 is related to the mirror planes m_{100} and m_{110} , which cause two independent nodal lines in the $k_x = 0$ and $k_x + k_y = 0$ planes, respectively. In addition to these mirror symmetry-protected nodal lines, In_5Bi_3 also contains special PT symmetry-protected nodal rings away from high-symmetry planes. It is clear from Fig. 3a that the hotspots of SBC are dominated by these nodal lines.

A similar symmetry analysis of Pt indicated that also in this well-known SHE material, the large SHC originates from mirror symmetry: it protects the nodal rings of which the SBC distribution is shown in Fig. 3c. We also created a local integral of the SBC in the spheres with centers of high-symmetry points of L and X and diameters of $1/10$ of the reciprocal lattice vectors. Interestingly, the contribution to the SBCs by the high-symmetry points of L and X is $<15\%$ of the contribution by the nodal lines. Even if the SBC was very large around the two high-symmetry points of L and X , their volumes were much smaller than those of the nodal lines. This suggests the important advantage of the nodal rings in the context of SHE: their significant dispersion in energy space indicates the existence of a large possibility of crossing the Fermi level and contributing strongly to the SHC. This understanding clearly explains the strong SHC in the classical martial Pt, which was ignored in the past.

The SBC analysis for the other ten compounds also showed the importance of nodal line band structures, see SI. In 9 of the 12 materials (IrN, Tl_3Ru , Pt_3Rh , $CuPt_7$, $LiPt_7$, Bi_2OsAu , Bi_3In_4Pb , $HgOsPb_2$, $Lilr$, and $PtRh_3$) the main contributions to the SBC originate from mirror symmetry-protected nodal lines. As mentioned above, in In_5Bi_3 the main contributions originate from nodal lines protected by both mirror symmetry and PT symmetry. In $Lilr$ and IrN both, mirror symmetry-protected nodal lines and other hotspots contribute (see the SI for more details).

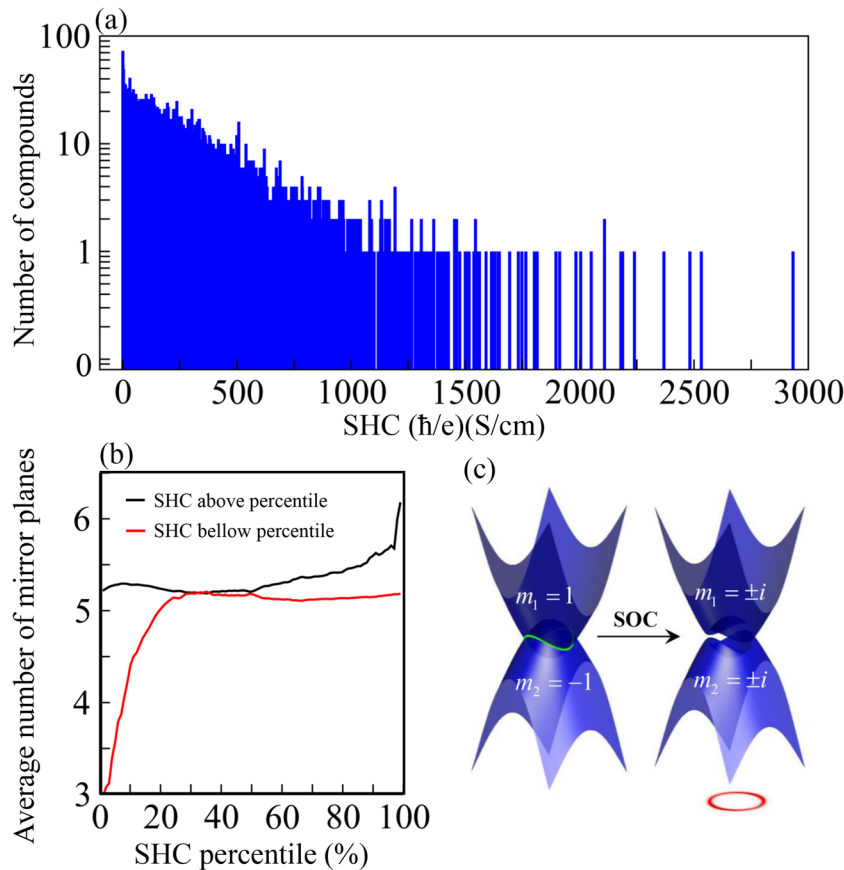


Fig. 2 Calculated intrinsic SHC. **a** Histogram of SHC values for all calculated materials. **b** Average number of mirror planes for materials with an SHC above a percentile of mirror planes and below a percentile of mirror planes as a function of the percentile. For example, the red curve shows the average number of mirror planes for 80% of the materials with the lowest SHC, whereas the black curve shows the average for the top 20% of the materials. **c** Illustration of the nodal line mechanism. The splitting of the bands from SOC results in a large SBC along the original nodal line, as illustrated by the red circle.

In addition to materials with large native SHCs, it is also possible to obtain a strong SHE by tuning the chemical potential in a given compound if it has large peak values near the Fermi level. We found that the addition of a dopant to fill the holes can increase the SHC from ~ 1200 to ~ 2300 (\hbar/e)(S/cm) in IrN_2 , from ~ 1100 to ~ 2000 (\hbar/e)(S/cm) in NaIrPb , and from ~ 400 to ~ 2000 (\hbar/e)(S/cm) in TaAsPb_2 . Electron doping can increase the SHC from ~ 800 to ~ 2000 (\hbar/e)(S/cm) in BeReB and from ~ 500 to ~ 1500 (\hbar/e)(S/cm) in TaBe_3 , etc. Details can be found on the website. Using the energy-dependent SHC for guidance, intrinsic or extrinsic doping by tuning the chemical potential to the peak value can increase the SHC to meet the experimental requirements.

Microscopic analysis suggests that mirror symmetry has an important role in generating a large SHC. Similarly, we found that materials with many mirror planes have a larger SHC on average than materials without mirror planes. The mean value of the SHC in materials with at least three mirror planes is 28% larger than the mean value in materials without mirror planes. In materials without mirror planes, the mean value is 212 at the 95% confidence interval (189,233), whereas in materials with at least three mirror planes, the mean value is 271 at the 95% confidence interval (264,277). The confidence intervals were estimated using the empirical bootstrapping method. The effect is the most pronounced in materials with large SHC. Among all the materials, 16% of materials have less than three mirror planes, among the top 500, the corresponding percentage is only 8%, and among the top 50 materials, it is only 2%. This is also illustrated in Fig. 2b, which shows that the materials with the largest SHC have more mirror planes on average than the other materials. We note that

for the statistical analysis we excluded insulating materials (materials with a density of states at the Fermi level of lower than 0.01). Our results show that mirror symmetry is one of the key factors that influence the magnitude of the SHC. Although it does not exert any effect on average, it seems to be crucial for generating a very large SHC.

Importantly, an analogous relation between the SHC and mirror symmetry is likely to exist in other effects that have a similar origin to the intrinsic SHE, such as the anomalous Hall effect, or antidamping spin-orbit torque. Thus, our results have quite a fundamental significance: it shows that the symmetry determines not only the presence or absence of transport phenomena, as previously thought, but can also have a strong influence on their magnitude.

Different types of spin currents

In commonly used materials, the symmetry of the SHE is such that the spin polarization of the spin current is perpendicular to both the spin current and the charge current. This is not a general rule, however. In materials with low crystalline symmetry, other types of spin current are allowed³³. This includes a spin current that flows in the transverse direction to the charge current, similar to normal SHE but has spin polarization along the direction of the spin current flow, the electric field, or longitudinal spin currents, that is, spin currents that flow in the same direction as the charge current, as illustrated in Fig. 4. These types of spin currents could allow for new functionalities in spintronic devices; however, they have not received much experimental attention because materials

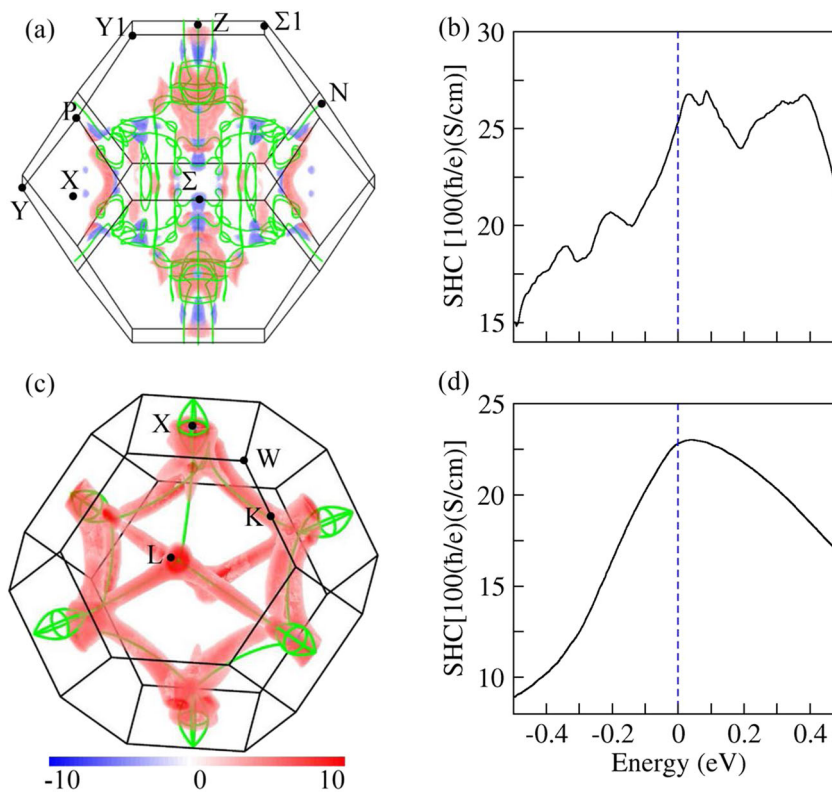


Fig. 3 Microscopic analysis for selected materials. SBC and nodal line distributions for (a) In_5Bi_3 with point group $4/m\bar{m}m$, and (c) Pt with point group $m\bar{3}m$, respectively. The green lines represent nodal lines. The color bar is in arbitrary units. Fermi-level-dependent SHC for (b) In_5Bi_3 and (d) Pt, respectively.

in which they are allowed are quite rare. A theoretical screening to identify promising materials is thus essential. We note that the SHE normally refers to a spin current flowing in the transverse direction to the charge current; thus, it is not clear whether longitudinal spin currents should be referred to as SHE. Nevertheless, we stress that the longitudinal spin currents have the same origin as the conventional SHE.

The existence and magnitude of such unusual symmetry spin currents, which are not perpendicular to the flow of the spin current, the spin polarization, and the electrical field depend on the orientation of the applied electrical field. For an electric field applied in high-symmetry directions, such spin currents are allowed only in several Laue groups. For an electric field applied in an arbitrary direction, we find that unusual symmetry spin currents can be present in all the Laue groups, except for those with $m\bar{3}m$ symmetry. All the materials from our database that have spin currents with an unusual symmetry larger than $100 (\hbar/e)(S/cm)$ are listed in the SI.

The SHE, which flows in the transverse direction to the charge current and has a spin polarization along the spin current flow direction, is of great interest for spin-orbit torques in heavy metal-ferromagnet bilayer systems (or other similar systems)³⁴ (see Fig. 4b). In these structures, the SHE from the heavy metal layer flows into the ferromagnetic layer and thus exerts a torque on the magnetization³⁵. For scalability, it is preferential to utilize a ferromagnet with a perpendicular magnetic anisotropy (PMA). However, for deterministic field-free switching of PMA systems, it is necessary to have a spin current with spin polarization perpendicular to the interface (and thus parallel to the direction of the spin current flow). This is not allowed by the symmetry of the materials commonly used in these systems, such as Pt; thus, materials with lower symmetry are needed. Our calculations

revealed that a large SHC with spin polarization along the spin current can occur, but is relatively rare. Considering the arbitrary direction of the electric field, we found 58 materials with an SHC above $500 (\hbar/e)(S/cm)$ with the largest value, $\sim 900 (\hbar/e)(S/cm)$, exhibited by BiTe_3 . When we considered the electric field along the high-symmetry directions, we found only two materials with values above $500 (\hbar/e)(S/cm)$: $\text{Ni}_2\text{P}_6\text{W}_4$ and $\text{Ba}_2\text{C}_4\text{S}_4\text{N}_4$.

The longitudinal spin currents in ferromagnetic systems were experimentally studied, where the origin of these currents lies in the ferromagnetic order. In our database, we identified a number of materials that exhibit large longitudinal spin currents with their spin polarization parallel or perpendicular to the spin current flow, as shown in Fig. 4c. In the case of an electric field with an arbitrary direction, we found seven materials with longitudinal spin currents larger than $500 (\hbar/e)(S/cm)$ with the largest being $\sim 1010 (\hbar/e)(S/cm)$ in LiIr . For an electric field along with the high-symmetry directions, the largest longitudinal spin current is $\sim 610 (\hbar/e)(S/cm)$ at σ_{zz}^z in $\text{P}_7\text{Ru}_{12}\text{Sc}_2$. The longitudinal spin current in nonmagnetic crystals may offer a new platform for the study and utilization of the spin current in nonmagnetic materials.

Another type of spin current is one that flows in the transverse direction to the electric field and has a spin polarization along the direction of the electric field, as shown in Fig. 4d. The study of the non-orthogonal SHE^{36,37} via manipulation of the crystalline symmetry opens an avenue to study the spin current and spin-orbital torque based on nonmagnetic materials. In our database, we identified 67 materials with this type of spin current larger than $500 (\hbar/e)(S/cm)$.

Our calculations revealed that the origin of the large SHC is usually associated with mirror symmetry-protected nodal lines in the band structure, which results in a strong correlation between the crystalline symmetry and magnitude of the SHC. This suggests

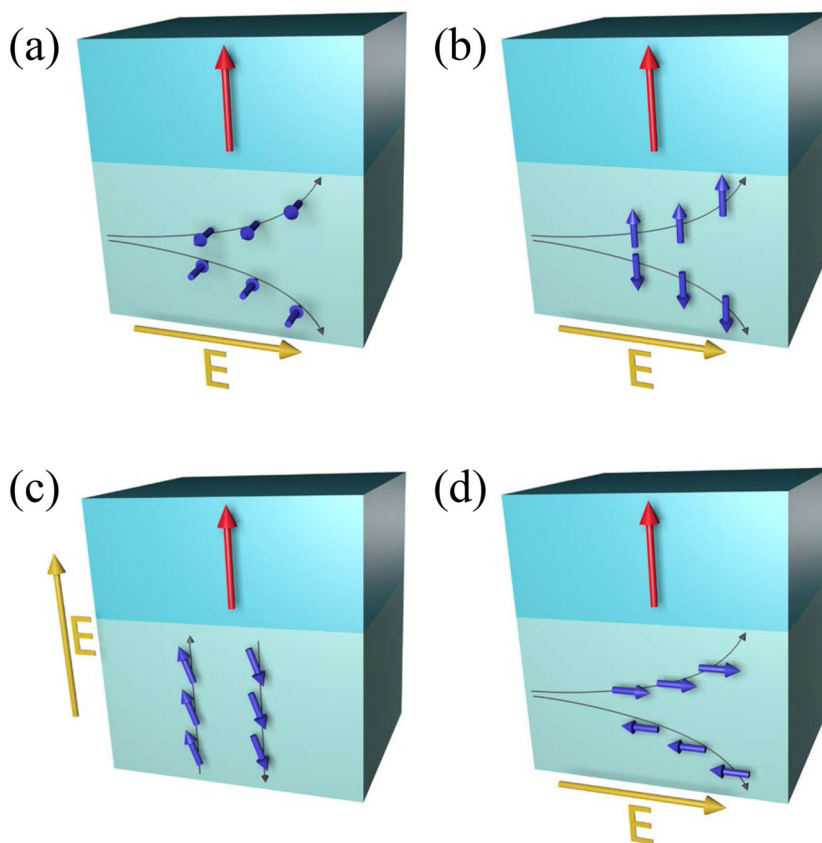


Fig. 4 Heterojunction of ferromagnets and non-magnets with four types of spin current included in this database. The top and bottom layers are ferromagnetic and non-ferromagnetic, respectively. **a** Traditional SHE with the spin polarization of the spin current perpendicular to both the spin current and the charge current. **b** Spin current flowing in the direction transverse to the electric field with the spin polarization orientated in the direction of the flow. **c** Longitudinal spin current flowing in the direction of the electric field. **d** Spin current flowing in the direction transverse to the electric field with the spin polarization existing along the direction of the electric field.

that for the design of new SHC materials, it is beneficial to consider high-symmetry materials with a large number of mirror planes. In addition, we determined that, apart from the obvious requirement for the presence of heavy elements with a strong SOC, the presence of *5d* transition metal elements is advantageous, but not decisive. We identified a number of promising spin-to-charge conversion materials, including 169 materials with an SHC above $1000 (\hbar/e)(S/cm)$, 11 materials with an SHC comparable or even larger than that of the existing record holder, Pt, and materials in which the symmetry of the SHE is lower thus allowing for different types of spin currents. These different types of spin current can also be obtained by adjusting the orientation of the applied electrical field. With these general design principles on the one hand, and the specific information on each separate compound, on the other hand, our high-throughput database is a powerful tool for the experimental design of spintronic devices.

METHODS

Automatic WF Setup

The *ab initio* calculations were carried out on the basis of DFT by using the FPLO code²⁶. The exchange and correlation energies were considered in the GGA²⁷. The *k*-point grid in the DFT calculation was set to $12 \times 12 \times 12$, and the criterion for total energy convergence below 10^{-6} eV. To perform the SHC, we projected the Bloch wavefunctions to atomic-orbital-like WFs by an automatic procedure. To ensure the Wannier projection is automatic and accurate, we set the constraint of the mean error between the DFT and tight binding below 0.02 eV in the energy window of $E_f - 2.0$ eV to $E_f + 2.0$ eV. The symmetry of the WFs is

well restored by the FPLO DFT code, where these WFs are directly mapped from the atomic orbitals without a maximum localization process.

We design the automatic Wannierization workflow by fixing two crucial parameters: (1) Wannier orbital basis set, (2) projected energy window for Wannier tight-binding model. Initially, the *s* orbitals of alkaline-earth metal elements, *d* orbitals of transition metal elements, and *s* + *p* orbitals of *p*-block elements are selected as the minimum Wannier orbital basis. After the band structure calculations, we further calculate the weights of the selected Wannier orbitals in the DFT Kohn–Sham wavefunctions and check whether the Wannier orbitals are disentangled from the inner valence orbitals.

When there is a global gap between the selected Wannier orbital basis set and the inner valence orbitals, we fix the bottom of the projected energy window in the gap. We then choose the up projected energy window by every 0.1 eV step and construct the Wannier tight-binding models correspondingly. The chosen Wannier orbitals are accepted until the mean absolute error between the DFT and Wannier band structures around the Fermi level is smaller than 0.02 eV.

When the minimum Wannier orbital basis set is entangled with the inner valence orbitals, we employ the maximum Wannier orbital basis set including all the local orbitals used in DFT calculations. Such a maximum Wannier orbital basis set automatically ensures the highly accurate Wannier tight-binding model, at the expense of relatively large Hilbert space, namely, 18 orbitals per atom. Because FPLO is a DFT code based on a localized basis, it makes this procedure convenient²⁸.

SHC calculation

Starting from the tight-binding model Hamiltonian, the SHC was calculated by using the linear response Kubo formula approach with a constant Γ

approximation^{8,14}:

$$\begin{aligned} \sigma_{ij}^k &= e \int_{BZ} \frac{d\vec{k}}{(2\pi)^3} \sum_n f_{n\vec{k}} \Omega_{n,ij}^{S,k}(\vec{k}), \Omega_{n,ij}^{S,k}(\vec{k}) \\ &= -2Im \sum_{n \neq n'} \frac{\langle n\vec{k} | J_i^k | n'\vec{k} \rangle \langle n'\vec{k} | v_j | n\vec{k} \rangle}{(E_{n\vec{k}} - E_{n'\vec{k}})^2 + \Gamma^2}, \end{aligned} \quad (1)$$

where $f_{n\vec{k}}$ is the Fermi–Dirac distribution for the n th band, $J_i^k = \frac{1}{2} \{v_i, s_k\}$ is the spin current operator with the spin operator s , velocity operator v_i , and $i, j, k = x, y, z$. Further, $|n\vec{k}\rangle$ is the eigenvector for the Hamiltonian H at eigenvalue $E_{n\vec{k}}$. In addition, $\Omega_{n,ij}^{S,k}(\vec{k})$ is referred to as the

SBC for the n th band at point \vec{k} , as an analogy to the ordinary Berry curvature. We calculated the intrinsic contribution which is independent of any scattering and that we only include very small broadening $\Gamma = 0.1$ meV for numerical reasons. After checking the convergence of the k -grid for 2,000 randomly chosen compounds, we find that the change in the SHE is below 5% by increasing the k -grid from $150 \times 150 \times 150$ to $250 \times 250 \times 250$. The changes in the cases with SHC > 500 (\hbar/e)(S/cm) are even smaller. Here, we chose $250 \times 250 \times 250$ k -grid for all SHC calculations. One point we need to emphasize is that the calculation of the SHC needs to consider the real position of Wannier orbitals in the phase factors; otherwise, the calculated SHC would differ markedly for some compounds. All the calculated results were doubly verified by symmetry analysis.

DATA AVAILABILITY

All data generated and/or analyzed during this study are included in this article, its Supplementary Information file, and the corresponding website: <https://shc-db.fw-dresden.de/index>. The data are available from the corresponding author upon reasonable request.

CODE AVAILABILITY

All code used to calculate the presented results is available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

Y.Z., Q.X., J.Ž., and Y.S. carried out all calculations. K.K. made the code for WF projection. R.R., O.J., and J. van den B. setup the database webpage. T.J., C.F., J. van den B., and Y.S. supervised this work. Y.Z. and Q.X. wrote the first version of the manuscript. All authors discussed the results and commented on the paper.

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