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Perspective: multi-dimensional coherent spectroscopy of perovskite nanocrystals

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**Abstract**

Recently, colloidal perovskite nanocrystals (PNCs) have emerged as an exciting material platform for optoelectronic applications due to their combination of facile synthesis routes, quantum size effects, and exceptional optical properties among other favorable characteristics. Given the focus on their optoelectronic properties, spectroscopic characterization of PNCs is crucial to rational design of their structure and device implementation. In this Perspective, we discuss how multi-dimensional coherent spectroscopy (MDCS) can resolve exciton dynamics and circumvent inhomogeneous broadening to reveal underlying homogeneous spectral lineshapes. We highlight recent applications of MDCS to PNCs in the literature, and suggest compelling problems concerning their microscopic physics to be addressed by MDCS in the future.

1. Introduction

The systematic synthesis and study of semiconductor nanocrystals spans four decades to early studies at the end of the 20th century [1–4]. Today the field continues to flourish, with new nanocrystal synthesis routes and architectures being discovered at a rapid pace. Among the most exciting recent developments is the synthesis of colloidal lead-halide perovskite nanocrystals (PNCs) [5], which have a perovskite lattice structure with an APbX_3 composition (where A is an organic or inorganic cation and $\text{X} = \text{Cl}, \text{Br}, \text{or I}$). PNCs combine the properties of colloidal nanocrystals, such as quantum size effects and versatile surface chemistry, with advantages inherited from their bulk counterparts. For example, the ionic bonding character [6] and defect-tolerant nature [7] of bulk lead-halide perovskites have translated to quantum efficiencies in PNCs nearing unity without the complication of shell over-coatings (necessary for comparable quantum efficiencies in traditional metal chalcogenide and pnictide nanocrystals [8]).

Despite their unique characteristics PNCs are not immune to many drawbacks of colloidal nanocrystals, most notably size and shape dispersion in ensembles. Because their exciton energy level structure is affected by quantum confinement, variation in nanocrystal geometry results in a concomitant variation of absorption and emission wavelength of electronic transitions. In such a situation optical lineshapes are broadened beyond the single-particle (homogeneous) linewidths, a phenomenon termed inhomogeneous spectral broadening. Inhomogeneous broadening is not only deleterious in many practical applications of PNCs, for example in lasing [9] and transport in superlattices [10], but also hampers study of their fundamental optoelectronic properties that manifest in homogeneous optical lineshapes.

To circumvent inhomogeneous broadening in spectroscopic studies of PNCs, single-nanocrystal spectroscopies are most commonly employed [11]. Such techniques isolate the homogeneous luminescence spectra of individual nanocrystals, albeit with significant drawbacks such as spectral diffusion and limited signal-to-noise ratio. Perhaps the most limiting aspect of single-nanocrystal spectroscopies however, is that lineshapes can vary dramatically between individual particles of an ensemble. A technique capable of

resolving *ensemble-averaged* homogeneous lineshapes is multi-dimensional coherent spectroscopy (MDCS) [12], an optical analogue of nuclear magnetic resonance spectroscopy that has found applications in numerous disordered systems ranging from molecular liquids [13, 14] to atomic gases [15, 16], and even photosynthetic bacteria [17, 18].

The experimental implementations of MDCS and its application to semiconductor nanostructures have been previously discussed in dedicated reviews on these subjects [19–23]. However, it is only recently that MDCS has been applied to PNCs. The purpose of this Perspective is therefore to highlight some of the first studies on PNCs by MDCS in recent years and to outline some compelling questions that MDCS is uniquely poised to answer, with the hope of stimulating further activity in this burgeoning field.

2. Multi-dimensional coherent spectroscopy

Multi-dimensional coherent spectroscopy (MDCS) is a general class of nonlinear spectroscopic techniques that resolves a cross-section of, or even an entire, (complex-valued) nonlinear optical response $S^{(n)}$ of order n . Below, we describe some experimental implementations of MDCS and two common types of multi-dimensional spectra that are useful in the context of colloidal nanocrystals.

2.1. Experimental implementation

In general, measurement of a system's optical response function requires excitation by light. Measurement of a frequency-domain response function may be accomplished by excitation with continuous-wave light sources of variable frequency or by excitation with pulsed light sources of variable time-delays. Fourier transform spectroscopy methods with pulsed excitation are far more commonplace, which are therefore assumed below.

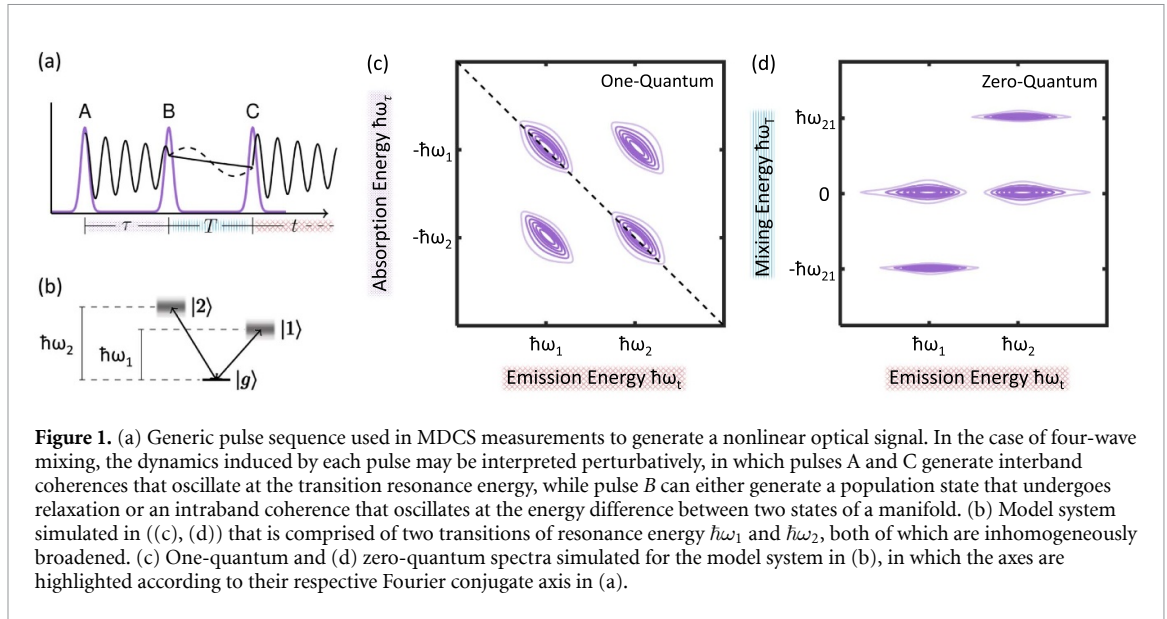
There are two general requirements for experimental implementations of MDCS. First, inter-pulse time-delays that involve coherence evolution must be stable to within a fraction of the excitation light period. Second, a nonlinear optical response must be separated from the linear optical response, which is stronger at low excitation fluences. This second requirement may be accomplished in either a non-collinear excitation geometry by wave-vector phase-matching (see supplemental information available online at stacks.iop.org/JPMATER/5/021002/mmedia) [24] or in a collinear excitation geometry by phase-cycling [20].

Most commonly, MDCS measures a third-order optical response $S^{(3)}$ by using three excitation fields to generate a four-wave mixing signal. The dynamics induced by each excitation pulse are usually interpreted in a perturbative framework, in which each field interaction induces a change in a system's density matrix. These changes altogether constitute so-called quantum pathways, which provide a physical interpretation of the peaks observed in multi-dimensional spectra. As illustrated in figure 1(a), the first pulse (A) generates a coherent superposition between the ground and an optically active excited state, which oscillates at the transition energy $\hbar\omega_\tau$. The second pulse (B) then converts this interband coherence into either a population state that decays according to its relaxation rate or an intraband coherence between two neighboring states within a ground or excited state manifold [25] that oscillates at the intraband energy splitting $\hbar\omega_T$. The last pulse (C) then generates a final interband coherence that oscillates at its respective transition energy $\hbar\omega_t$ and radiates an FWM signal. We leave further description of the analytical expressions to other more detailed texts [26].

If the phase-stability criteria introduced above is satisfied, the time-domain four-wave mixing signal may be measured and Fourier transformed along two or more time axes to generate a multi-dimensional spectrum. Although many different multi-dimensional spectra are possible depending on both the chosen pair of time axes and the pulse time-ordering, we describe below two types of spectra that have proven particularly useful in the study of PNCs, termed one-quantum and zero-quantum spectra. A model system comprised of two coupled inhomogeneously broadened transitions, one of resonance energy $\hbar\omega_1$ and another of resonance energy $\hbar\omega_2$ (shown in figure 1(b)), is simulated to demonstrate the basic features in multi-dimensional spectra of disordered level systems.

2.2. One-quantum spectra

One-quantum spectra are obtained by Fourier transform along the time-delays $\{\tau, t\}$. Interband coherence evolution occurs along these two delays, as represented by the high-frequency oscillations in figure 1(a), and therefore one-quantum spectra correlate absorption and emission dynamics of a given material system. In the case of rephasing one-quantum spectra [19, 23], coherences evolve with inverse phase between delays τ and t (reflected in negative absorption energy $\hbar\omega_\tau$), which is assumed henceforth. A schematic one-quantum spectrum (simulated for the model system in figure 1(b)) is shown in figure 1(c), which illustrates two unique capabilities:



- Two peaks are present at $|\hbar\omega_\tau| = |\hbar\omega_t|$ (indicated by the dashed black line), which correspond to absorption and emission involving identical photon energies. Two additional peaks are present at $|\hbar\omega_\tau| \neq |\hbar\omega_t|$, which then correspond to absorption and emission involving different photon energies. One-quantum spectra therefore reveal coupling between different optical transitions through the presence of the latter so-called cross-peaks.
- The peaks are elongated along the $|\hbar\omega_\tau| = |\hbar\omega_t|$ direction, which illustrates the presence of two distinct broadening mechanisms. Namely, homogeneous broadening due to the single-particle oscillator damping and inhomogeneous broadening due to disorder (see figure 1(b)) are projected in orthogonal directions in a one-quantum spectrum [27]. In contrast, a homogeneously-broadened resonance (absent of disorder) would manifest as a completely symmetric peak along both axes. It should also be noted that, unlike the homogeneous lineshapes measured by single-nanocrystal photoluminescence, the lineshapes measured by MDCS for time-delay $T \approx 0$ reflect the exciton transition in the absence of population dynamics (such as Stokes shift and spectral diffusion) following optical absorption.

We remark that a one-quantum spectrum, which plots the optical response cross-section $S^{(3)}(\omega_t, T, \omega_\tau)$, may be viewed as a generalized pump-probe response that resolves both quadratures of the complex optical response with pump spectral resolution limited only by Fourier transform parameters. For example, a transient absorption measurement is expressed in terms of the optical response function as [28, 29]:

$$\Delta A(\omega_t, T) \approx \text{Re} \int_{-\infty}^{\infty} E_{\text{pump}}(\omega_\tau) S^{(3)}(\omega_t, T, \omega_\tau) d\omega_\tau, \quad (1)$$

where the only approximation is that of an infinitely broad probe pulse spectrum (which approximates the usual case of a white-light continuum probe pulse). An equivalent transient absorption spectrum may therefore be extracted from a one-quantum spectrum by windowing the optical response along the vertical absorption axis by the excitation spectrum E_{pump} and subsequent projection onto the horizontal emission axis.

2.3. Zero-quantum spectra

Zero-quantum spectra are obtained by Fourier transform along the time-delays $\{T, t\}$. Both population relaxation and intraband coherence evolution occurs along the delay T , as represented by the solid and dashed curves in figure 1(a), and therefore zero-quantum spectra correlate these dynamics with subsequent optical emission along the delay t . A zero-quantum spectrum (simulated for the same model system in figure 1(b)) is shown in figure 1(d), which illustrates how population dynamics and intraband coherences manifest in frequency space.

- Population relaxation manifests as peaks at zero mixing energy ($\hbar\omega_T = 0$). The widths of each peak along the horizontal emission energy direction reflect the resonance energy distribution of each respective resonance, while the widths along the vertical mixing energy direction reflect their population relaxation times.

- Intraband coherence evolution manifests as peaks at non-zero mixing energy ($\hbar\omega_T \neq 0$), specifically at the energy splitting between the two states involved. The width along the vertical mixing energy direction reflects the intraband coherence dephasing time while tilt of a sideband (in the inhomogeneously broadened case) may reveal dispersion of an intraband energy splitting.

We note that the spectrum in figure 1(d) is simulated for perfectly correlated inhomogeneity between the two transitions (a good assumption for most nanocrystal systems). If this is not the case, vertical mixing energy width then gains a contribution from disorder of the intraband energy splitting $\hbar\omega_{12}$.

2.4. MDCS of colloidal nanocrystals

MDCS of colloidal nanocrystals may, at the most basic level, be understood in terms of dipole transitions between discrete energy levels arising from three-dimensional quantum confinement. While this suggests a close correspondence between electronic excitations in molecular systems and excitons in colloidal nanocrystals, the physics revealed in multi-dimensional spectra suggest a more nuanced description.

Indeed, much of the physics of colloidal nanocrystals is inherited from their bulk parent compounds. Acoustic [30] and optical phonon modes [31] of a crystal lattice couple to excitons in nanocrystals, just as in bulk semiconductors. Especially for colloidal nanocrystals of extended dimensions such as nanoplatelets, many-body effects can also play a primary role in their optical properties [32].

It should be emphasized however, that most of the new physics introduced in colloidal nanocrystals possess direct analogues in the physics of molecular systems. For example, the limited size of nanocrystals gives rise to discrete vibrational modes confined to their geometry [33], reminiscent of molecular bond vibrations. Excitons in nanocrystals also experience a fluctuating energetic environment as in molecular liquids, whether due to solvation dynamics [34] or charge migration [11]. Multi-dimensional spectra of colloidal nanocrystals may therefore be understood using intuition borrowed from the physics of both bulk semiconductors and molecules.

2.5. Limitations of MDCS

We conclude this section by discussing possible limitations of MDCS compared to conventional linear spectroscopies.

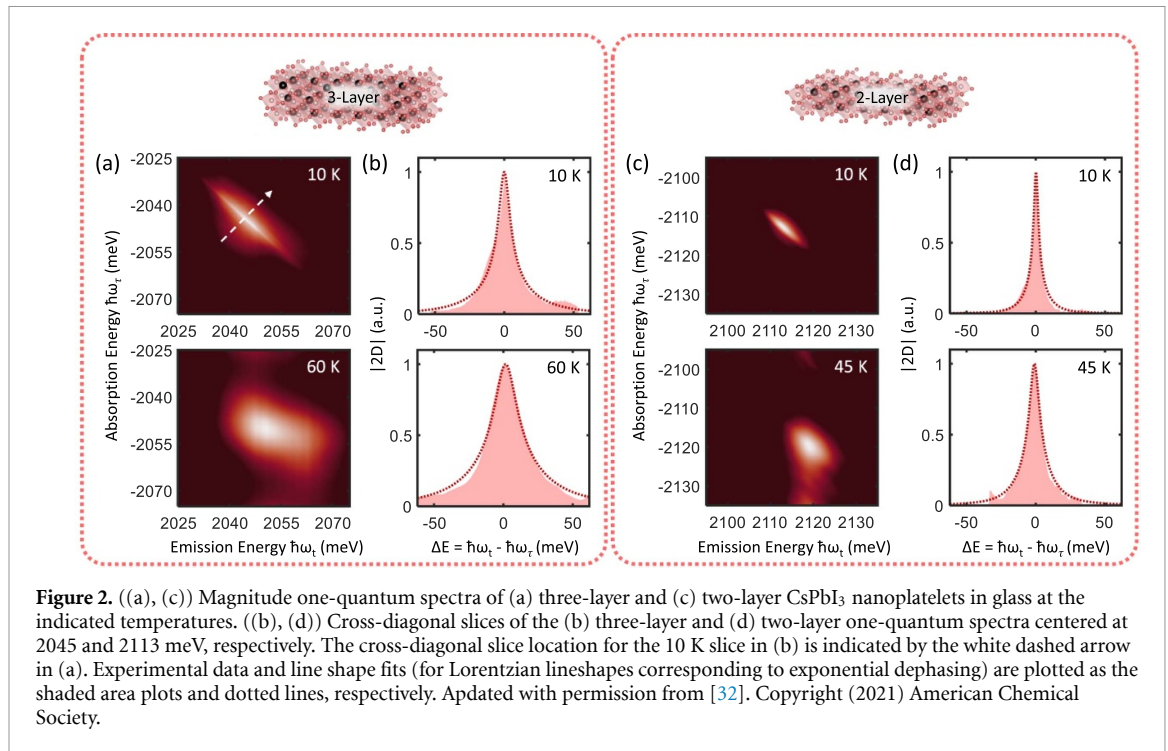
- To perform linear spectroscopies only a single excitation light source and direct, incoherent signal measurement by a photodetector is required. Experimental realization of MDCS is more complex, as two/three excitation pulses must be guided to the sample with variable, phase-stable time-delays, and the generated nonlinear optical signal is then combined with a separate local-oscillator pulse for phase-sensitive detection.
- Excitation fields that are sufficiently high to generate a nonlinear optical response are required, which may near damage thresholds for certain materials.
- The spectral content of each excitation pulse determines possible features in resultant multi-dimensional spectra. Sufficient spectral bandwidth is therefore required for broad peak linewidths or large energy separations between resonances.

3. Interband dynamics

Interband dynamics play a primary role in optoelectronic applications of PNCs, which encompass optical absorption/emission as well as charge/energy transfer following photoexcitation. As discussed in the previous section, one-quantum spectra probe these dynamics by correlating the photon energy of initial optical absorption with the photon energy of subsequent optical emission. In this section we discuss some representative studies of interband dynamics in PNCs using MDCS.

3.1. Exciton homogeneous linewidth

In one-quantum spectra, homogeneous and inhomogeneous resonance lineshapes are projected in orthogonal directions [27]. MDCS is therefore capable of extracting the ensemble-averaged homogeneous linewidth of exciton resonances in PNCs, even in the presence of strong inhomogeneous broadening. To this end, Liu *et al* recently applied MDCS to CsPbI₃ nanoplatelets at cryogenic temperatures [32]. As shown in figure 2, one-quantum spectra of 2-layer and 3-layer nanoplatelets exhibit Lorentzian homogeneous lineshapes reflecting Markovian (memory-less) exponential dephasing with dramatically different homogeneous and inhomogeneous linewidths. Extrapolating the homogeneous linewidth to room-temperature, these measurements [32] suggested that thin (2-layer) nanoplatelets were homogeneously-broadened at room-temperature while increasing out-of-plane thickness violates this



common assumption in nanoplatelets [35, 36]. In addition to elucidating homogeneous broadening mechanisms via temperature- and excitation fluence-dependent measurements, the homogeneous linewidth was further resolved as a function of exciton resonance energy to inform the effect of variations in nanoplatelet geometry. Such an analysis provides a unique view into the effects of quantum confinement on excitons in PNCs, a contentious topic in itself [37].

Similar measurements have also been performed by Yu *et al* [38] on CsPbBr₃ nanocubes, which revealed exciton-phonon coupling to acoustic vibrational modes to be the dominant homogeneous line-broadening mechanism. This conclusion is similar to what was found for CsPbI₃ nanoplatelets [32]. In contrast, increasing excitation fluence was found to have a minimal effect on the measured homogeneous linewidth, which is not the case for CsPbI₃ nanoplatelets [32], highlighting the importance of nanocrystal dimensionality on exciton-exciton scattering in PNCs.

3.2. Exciton fine-structure

Exciton fine-structure states in PNCs share a common ground state, and therefore lead to cross-peaks in one-quantum spectra. For inhomogeneously-broadened ensembles, these cross-peaks are elongated into sidebands that inform the fine-structure energy splittings and dephasing rates.

An interesting aspect of the exciton fine-structure of PNCs lies in their orthogonal linear transition dipole moments, which allow for polarization-selective excitation of individual states in the triplet manifold. Thus far, polarized fine-structure emission has primarily been observed in single-nanocrystal spectroscopies [39, 40], which suffer from limited signal-to-noise ratio and variation between individual nanocrystals. With polarization-resolved MDCS however, the fine-structure selection rules are preserved in ensemble measurements even in the presence of nanocrystal orientation disorder [41]. Such an experiment was recently performed by Liu *et al* on CsPbI₃ nanocubes, in which one-quantum spectra were acquired with two different excitation polarization schemes termed co-linear and cross-linear (shown in figure 3(a)). In the spectra shown in figure 3(b), dramatically different lineshapes are observed between the two polarization schemes due to enhancement and suppression of different fine-structure transitions. The polarization-dependent lineshapes were then used to fit dephasing times between the different triplet state transitions and to infer a partially-bright triplet exciton band-edge [42].

We finally mention that exciton fine-structure may also manifest in one-quantum spectra as coherent dynamics during the time-delay T . In exemplary measurements of MAPbBr₃ nanocrystals in a strongly quantum-confined size regime, Wang *et al* reported coherent oscillations of one-quantum spectra with varying delay T [43]. Though the nature of these oscillations could not be ascertained as vibronic or purely electronic, low-temperature measurements were proposed as a potential route to resolve this ambiguity.

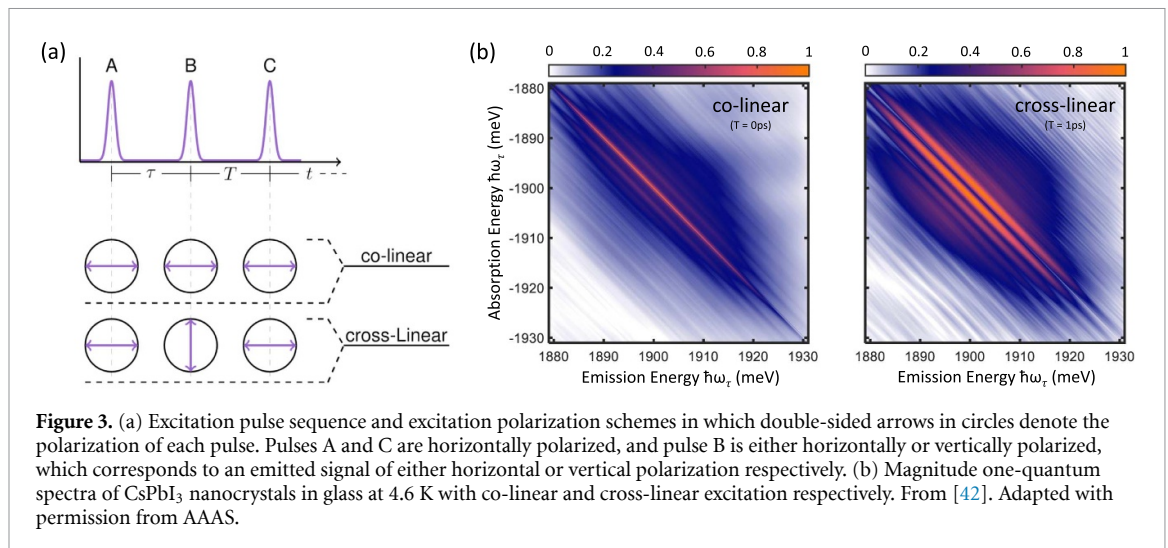


Figure 3. (a) Excitation pulse sequence and excitation polarization schemes in which double-sided arrows in circles denote the polarization of each pulse. Pulses A and C are horizontally polarized, and pulse B is either horizontally or vertically polarized, which corresponds to an emitted signal of either horizontal or vertical polarization respectively. (b) Magnitude one-quantum spectra of CsPbI₃ nanocrystals in glass at 4.6 K with co-linear and cross-linear excitation respectively. From [42]. Adapted with permission from AAAS.

3.3. Exciton–phonon coupling

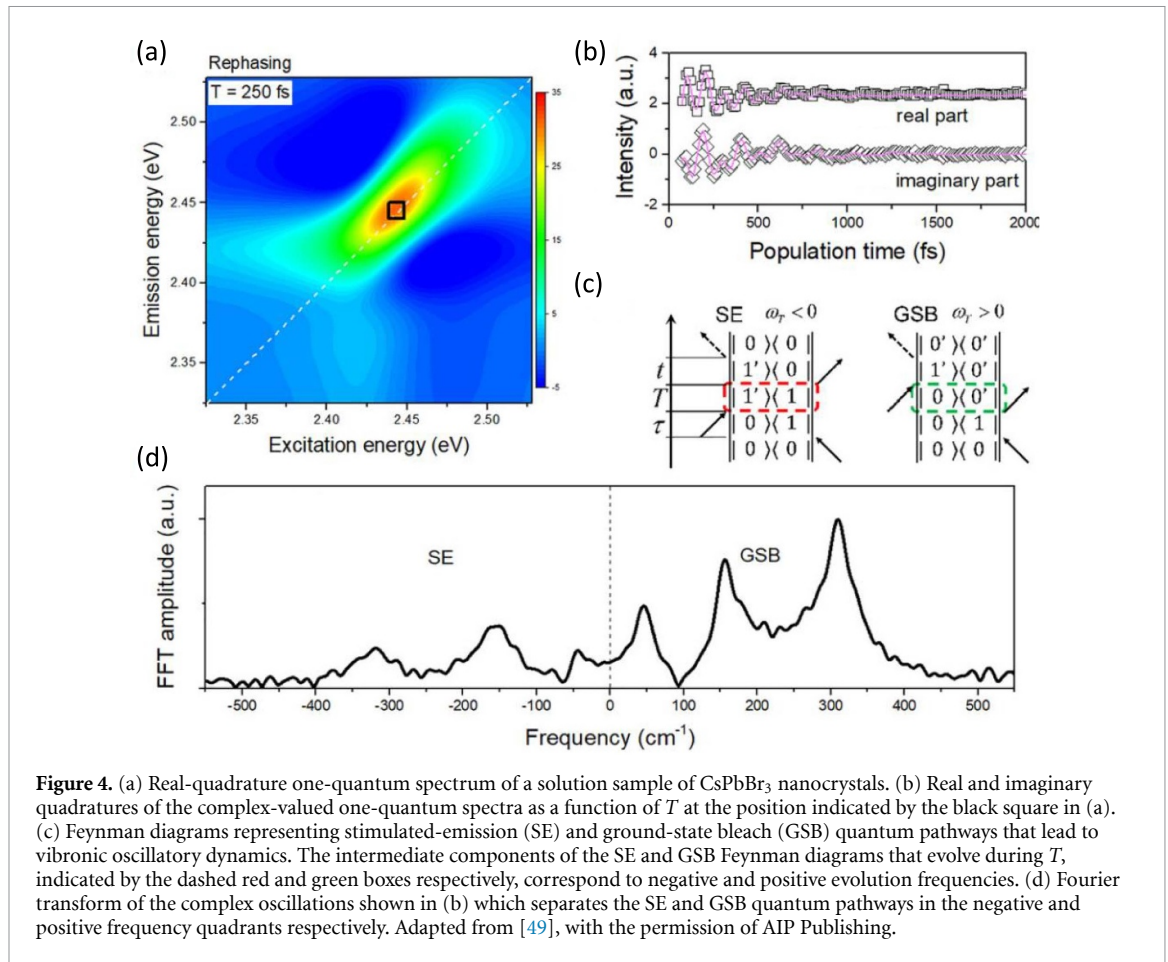
In both PNCs and nanocrystals more broadly, exciton-phonon coupling constitutes a primary mechanism of coherence dephasing [44] and energy transfer [45]. From a spectroscopic perspective exciton-phonon coupling manifests in two primary ways, namely in homogeneous spectral lineshapes and oscillatory dynamics due to coherent nuclear motion [46].

To be more precise, homogeneous lineshapes of exciton resonances are comprised of three components: (1) zero-phonon lines representing an exciton resonance without phonon involvement [44, 45], (2) non-Lorentzian phonon pedestals due to inelastic scattering with phonons spanning a continuous range of eigenenergies (i.e. acoustic vibrations) [30], and (3) phonon sidebands (replicas) due to inelastic scattering with phonons of discrete eigenenergies (i.e. optical or quantum-confined vibrations) [47]. Broadening of the zero-phonon line with temperature then informs elastic scattering with phonons of both discrete and continuum eigenenergies. Indeed, recent publications by Yu *et al* [38] and Liu *et al* [32] have reported zero-phonon line broadening dominated by acoustic-phonon scattering in CsPbBr₃ nanocubes and CsPbI₃ nanoplatelets respectively. While no clear signatures of acoustic phonon pedestals or sidebands were observed in the nanoplatelet spectra [32], more complex lineshapes are evident in the one-quantum spectra of both CsPbBr₃ [38] and CsPbI₃ [42] nanocubes that indicate inelastic scattering channels involving many vibrational modes. Dimensionality thus plays a primary role in determining exciton-phonon coupling in PNCs [48].

Complementary information may also be obtained by MDCS about the electronic dynamics that arise from exciton-phonon coupling. During the intermediate time-delay T , exciton-phonon coupling can give rise to coherent oscillations at characteristic vibrational frequencies. These oscillations may be thought of as vibrational coherences on either a ground or an excited electronic potential energy surface, with their own vibronic dephasing times. Recently Zhao *et al* reported T -dependent one-quantum spectra of CsPbBr₃ nanocubes, in which coherent oscillations were observed of the exciton resonance at room temperature [49]. As shown in figure 4, vibrational coherences on the ground and excited electronic potential energy surfaces were separated in frequency space according to their ground-state bleach and stimulated-emission quantum pathways respectively. We emphasize that this separation of ground and excited state coherences would not be possible via other techniques such as transient absorption spectroscopy [50], and requires the full complex-valued optical response.

3.4. Excited-state dynamics

The dynamics that evolve along the T time-delay also include incoherent processes such as spectral diffusion and population relaxation. Spectral diffusion dynamics, which refer to resonance energy fluctuations in time [11], are of particular interest on the ultrafast timescale as a microscopic origin of coherence dephasing [31] and spectral line-broadening. In an interesting report from Seiler *et al* [51] the spectral dynamics of CsPbI₃ nanocrystals were resolved as a function of T and compared with those of conventional CdSe nanocrystals and a molecular dye (shown in figure 5). Broadening of the homogeneous linewidth with increasing T , a direct measure of spectral diffusion [52, 53], was then used to quantify the polaronic dynamics in PNCs. While the diffusive dynamics were dissimilar to those of covalently-bonded CdSe nanocrystals, in which the homogeneous linewidth was coherently modulated at the LO-phonon frequency, they were reminiscent of



spectral diffusion in the molecular dye Nile Blue. Time-resolved measurements of the homogeneous linewidth enabled by MDCS thus provide an interesting conceptual analogy between polaron formation and solvation dynamics.

Beyond spectral diffusion dynamics, dynamically-varying spectral weight of peaks in one-quantum spectra may be ascribed to incoherent charge or energy transfer between resonances. In a recent report by Yu *et al* the incoherent relaxation dynamics of hot carriers to the band-edge exciton state were measured in this way with femtosecond (< 10 fs) time-resolution [54]. Relaxation times were measured for a range of nanocrystal sizes, through which phonon-bottlenecking [55] was directly inferred with increasing quantum confinement. Crucial to this observation was also the combination of high temporal and energy resolution possible in Fourier transform spectroscopies such as MDCS. In contrast, conventional pump-probe techniques such as transient absorption spectroscopy suffer from a trade-off between temporal and energy resolution due to the Fourier transform limit of excitation pulses.

4. Intraband dynamics

In the previous section, we have described how one-quantum spectra exhibit both coherent and incoherent dynamics along the time-delay T . If these dynamics are of particular interest, it is often advantageous to acquire zero-quantum spectra (rather than a full three-dimensional dataset) to correlate the dynamics during T with the subsequent optical emission. In this section we focus specifically on studies of intraband coherences in PNCs using MDCS, which can be of either vibrational or electronic origin.

4.1. Vibrational intraband coherences

It is shown in figure 4 that electron-phonon coupling involving vibrations of discrete energy may give rise to coherent oscillations along T , a form of vibrational intraband coherence. In zero-quantum spectra, these oscillations manifest as sidebands that correlate the vibronic energy and lifetime with the exciton emission energy. In figure 6(a), a zero-quantum spectra of CsPbI₃ nanocrystals is shown for co-linear excitation, in which three sidebands are observed at mixing energies $\hbar\omega_T = -3.3, -5.5,$ and -14.9 meV due to coupling to three distinct vibrational modes. We note that the asymmetry of these sidebands, referring to a lack of

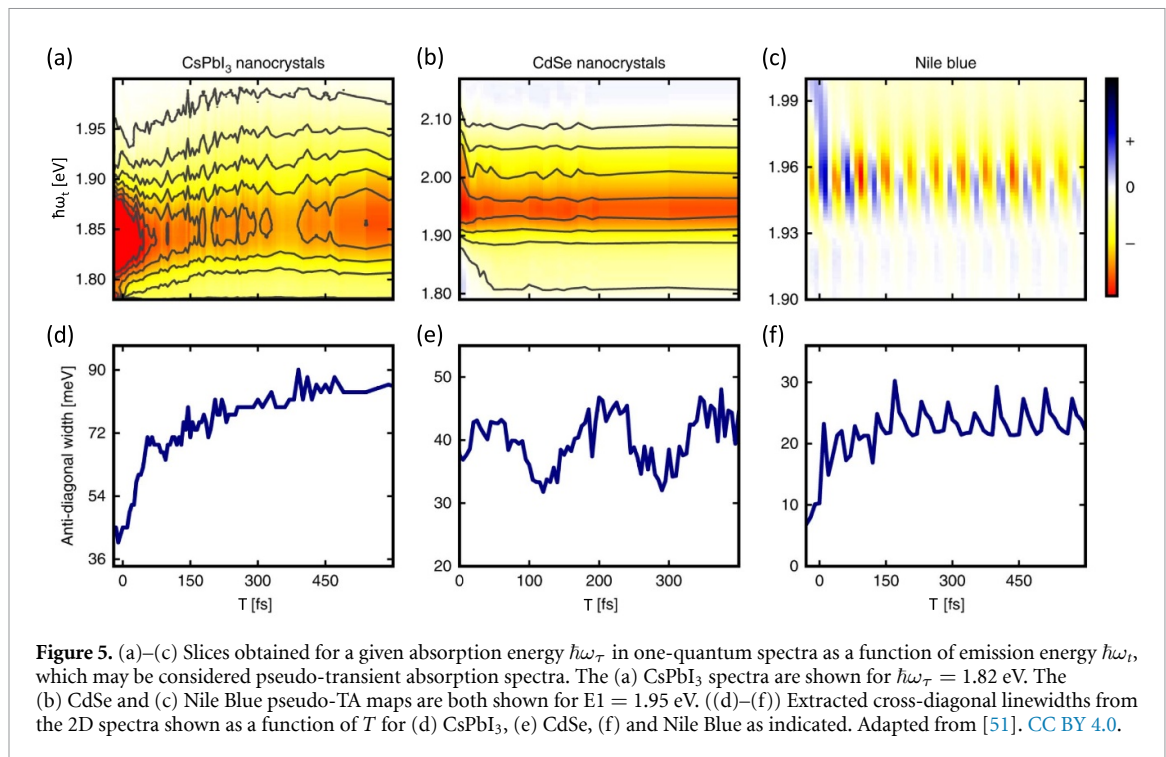


Figure 5. (a)–(c) Slices obtained for a given absorption energy $\hbar\omega_\tau$ in one-quantum spectra as a function of emission energy $\hbar\omega_t$, which may be considered pseudo-transient absorption spectra. The (a) CsPbI₃ spectra are shown for $\hbar\omega_\tau = 1.82$ eV. The (b) CdSe and (c) Nile Blue pseudo-TA maps are both shown for $E_1 = 1.95$ eV. ((d)–(f)) Extracted cross-diagonal linewidths from the 2D spectra shown as a function of T for (d) CsPbI₃, (e) CdSe, (f) and Nile Blue as indicated. Adapted from [51]. CC BY 4.0.

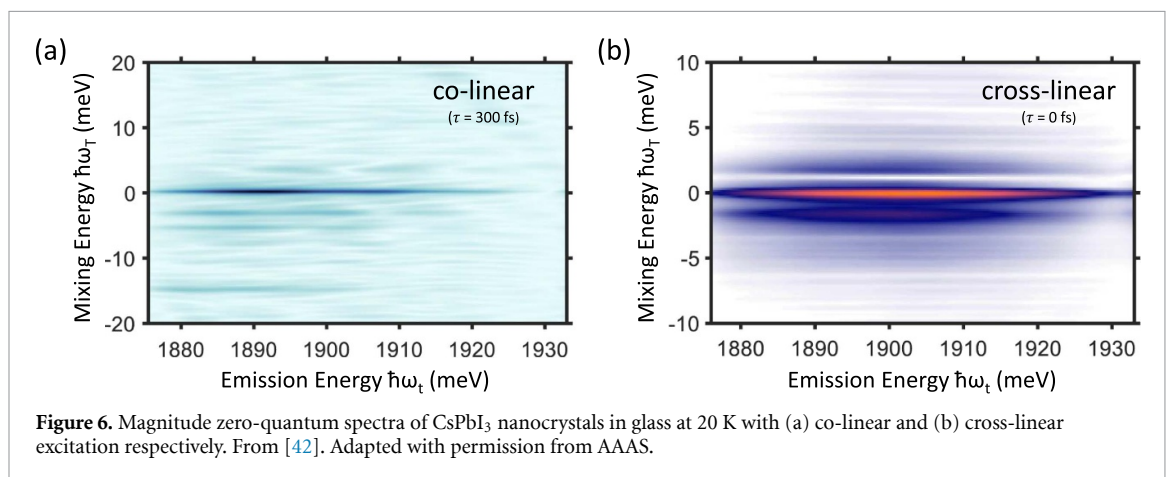
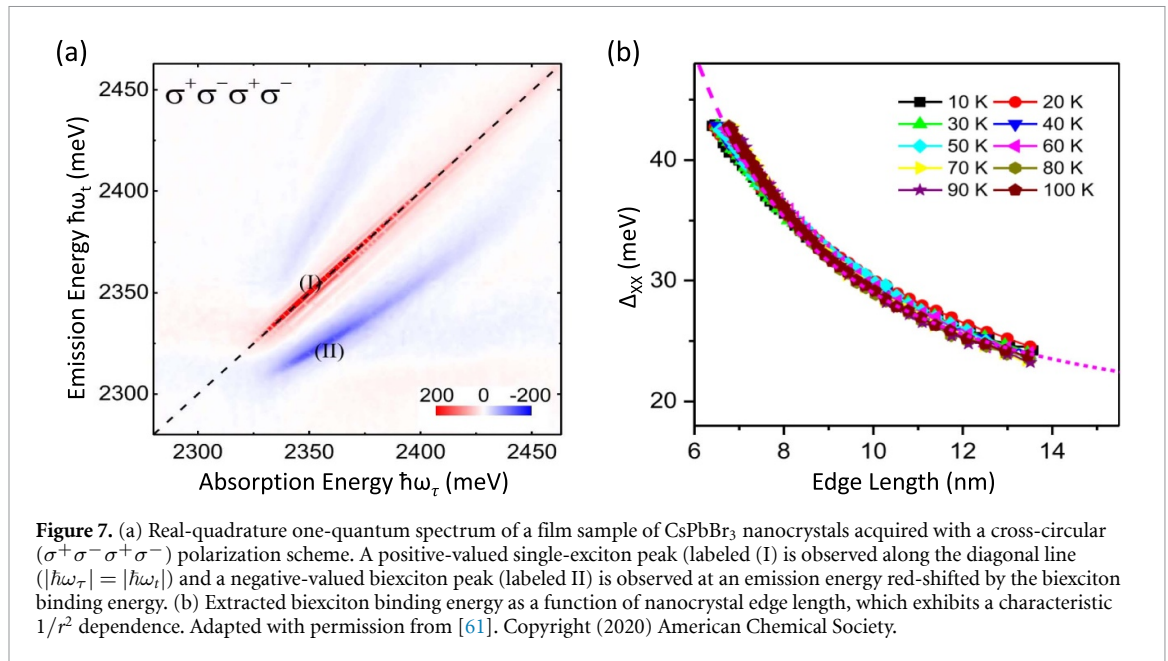


Figure 6. Magnitude zero-quantum spectra of CsPbI₃ nanocrystals in glass at 20 K with (a) co-linear and (b) cross-linear excitation respectively. From [42]. Adapted with permission from AAAS.

sidebands at positive mixing energy, is a signature of their vibrational nature [31, 46, 56]. Intraband coherences of purely electronic origin would instead exhibit symmetric sidebands of both oscillation polarities, which is discussed below.

4.2. Electronic intraband coherences

In PNCs, structural phase transitions away from the high-temperature cubic phase lift the degeneracy of the triplet exciton states [57]. Superpositions of these non-degenerate fine-structure states, a form of electronic intraband coherence, is of primary importance for many quantum coherent applications of PNCs such as single-photon emission [58]. In figure 6(b), a zero-quantum spectra of the same CsPbI₃ nanocrystals is shown for cross-linear excitation, in which symmetric sidebands at ± 1.6 meV are observed that arise from intraband coherences between two non-degenerate triplet exciton states. By measuring zero-quantum spectra as a function of temperature and fitting the resultant lineshapes, Liu *et al* showed that these intraband triplet coherences exhibit both a long coherence time of 1.36 ps (at a temperature of 20 K) and minimal thermal dephasing [42]. These properties compare favorably to those of candidate materials [59] for valleytronic applications [60], thus suggesting PNCs as a potential material platform for quantum information processing.



5. Higher-order exciton complexes

In third-order MDCS that measures a four-wave mixing signal, certain quantum pathways termed excited-state absorption involve emission from doubly-excited states. Biexciton resonances in PNCs thus manifest in one-quantum spectra, specifically as negative peaks in the real-quadrature component [62]. This was observed in a recent study by Huang *et al* which applied MDCS to CsPbBr₃ PNCs in order to extract the biexciton binding energy as a function of nanocrystal size and temperature [61]. As shown in the real-quadrature one-quantum spectrum plotted in figure 7(a), a negative peak is observed that is red-shifted along the emission energy axis (relative to the positive single-exciton peak located at $|\hbar\omega_\tau| = |\hbar\omega_t|$) by a value identical to the biexciton binding energy. This binding energy is plotted in figure 7(b) as a function of nanocrystal size, which exhibits a characteristic $1/r^2$ dependence that is largely independent of temperature. Finally, we note a related study by Zhao *et al* that revealed the mechanisms of optical gain in CsPbBr₃ PNCs [49].

6. Final remarks

We have performed a brief overview of multi-dimensional spectroscopy (MDCS), and surveyed the literature thus far applying MDCS to PNCs. Even as a burgeoning field, MDCS of PNCs has provided unique insights into their microscopic physics such as intrinsic linewidths, triplet exciton fine-structure, polaron formation, and biexciton resonances. However, these studies give merely a glimpse into the potential breadth of physics in PNCs to be explored by this technique.

From our point of view, among the most interesting physics reveal themselves at cryogenic temperatures. For example, population transfer between the triplet exciton states as well as between the neighboring dark singlet state may be resolved in time using MDCS. At sufficiently low temperatures the coherence dephasing dynamics also become non-Markovian, resulting in spectral lineshapes that reflect the spectral density of exciton-acoustic phonon coupling [30].

Another interesting direction is in terms of action-based MDCS techniques that detect signals other than coherent optical emission. For example, photoluminescence-detected MDCS [63] isolates the quantum pathways leading to incoherent luminescence and can inform the mechanisms that limit the performance of light-emitting devices. Photocurrent-detected MDCS [64] could also address many interesting questions concerning transport and other collective phenomena in PNC superlattices [10, 65].

Lastly, the unique insight into multiple-exciton dynamics afforded by MDCS yields a rich area of investigation. Biexciton fine-structure, and even higher-order exciton species such as triexcitons may be directly characterized by MDCS [66]. The addition of an incoherent pre-pulse prior to each MDCS measurement also introduces a host of new multiple-exciton phenomena that manifest in multi-dimensional spectra. For example, a high-photon energy pre-pulse could excite hot-carriers which undergo impact

ionization to generate multiple excitons. Varying a time-delay between this pre-pulse and a subsequent MDSCS measurement would then constitute a direct measurement of carrier multiplication in PNCs [67].

Data availability statement

No new data were created or analysed in this study.

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