

# A rapid optical and X-ray timing study of the neutron star X-ray binary Swift J1858.6–0814

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## ABSTRACT

We present a rapid timing analysis of optical (HiPERCAM and ULTRACAM) and X-ray (NICER) observations of the X-ray transient Swift J1858.6–0814 during 2018 and 2019. The optical light curves show relatively slow, large amplitude ( $\sim 1$  mags in  $g_s$ ) ‘blue’ flares (i.e. stronger at shorter wavelengths) on time-scales of  $\sim$ minutes as well as fast, small amplitude ( $\sim 0.1$  mag in  $g_s$ ) ‘red’ flares (i.e. stronger at longer wavelengths) on time-scales of  $\sim$ seconds. The ‘blue’ and ‘red’ flares are consistent with X-ray reprocessing and optically thin synchrotron emission, respectively, similar to what is observed in other X-ray binaries. The simultaneous optical versus soft- and hard-band X-ray light curves show time- and energy dependent correlations. The 2019 March 4 and parts of the June data show a nearly symmetric positive cross correlations (CCFs) at positive lags consistent with simple X-ray disc reprocessing. The soft- and hard-band CCFs are similar and can be reproduced if disc reprocessing dominates in the optical and one component (disc or synchrotron Comptonization) dominates both the soft and hard X-rays. A part of the 2019 June data shows a very different CCFs. The observed positive correlation at negative lag in the soft-band can be reproduced if the optical synchrotron emission is correlated with the hot flow X-ray emission. The observed timing properties are in qualitative agreement with the hybrid inner hot accretion flow model, where the relative role of the different X-ray and optical components that vary during the course of the outburst, as well as on shorter time-scales, govern the shape of the optical/X-ray CCFs.

**Key words:** accretion, accretion discs – X-rays: binaries – X-rays: individual: Swift J1858.6-0814 – stars: neutron

## 1 INTRODUCTION

The low-mass X-ray binary Swift J1858.6–0814 was discovered as an X-ray transient on 2018 October (Krimm et al. 2018) with the Burst Alert Telescope (BAT) aboard the Neil Gehrels *Swift* Observatory (Gehrels et al. 2004). Subsequent multi-wavelength observations detected the source at longer wavelengths. The Ultraviolet and Optical Telescope (*Swift*-UVOT) on-board *Swift* detected a variable UV source which was coincident with a previously detected UKIRT Infrared Deep Sky Survey (UKIDSS) and Pan-STARRs source (Kennea & Krimm 2018). Optical follow-up observations revealed that the source had brightened by  $\sim 2.5$  magnitudes (Vasilopoulos et al.

2018). The source was also detected in the radio by the Arcminute Microkelvin Imager Large Array having a variable flux density of 300–600  $\mu$ Jy at 15.5 GHz (Bright et al. 2018). At X-ray wavelengths, the outburst was relatively faint, with a flux of  $\sim 10^{-11}$  erg s<sup>-1</sup> cm<sup>-2</sup> at 0.5–10 keV and a hard spectrum with a photon index of  $\Gamma = 2$  (Reynolds et al. 2018).

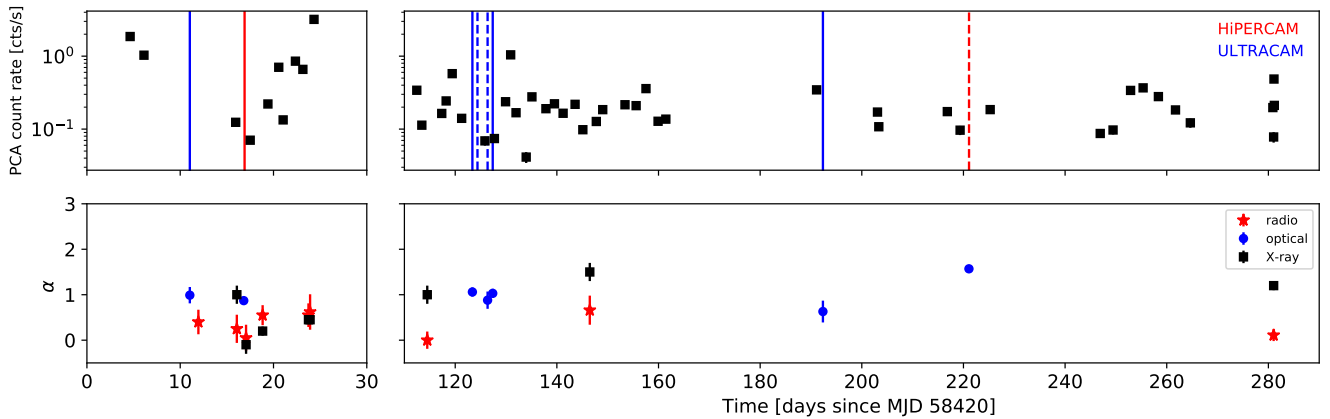
Superimposed on the outburst were bright, short X-ray flare events (Ludlam et al. 2018; Hare et al. 2019) where the observed flux increased by more than an order of magnitude in a few seconds (Hare et al. 2020). Optical flares were also identified (Vasilopoulos et al. 2018; Baglio et al. 2018; Rajwade et al. 2018, 2019; Paice et al. 2018) with wavelength-dependent optical variability on time-scales of minutes, and sporadic, fast ‘red’ flares on time-scales of seconds (Paice et al. 2018). The timing characteristics were reminiscent of

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**Table 1.** Log of ULTRACAM, HiPERCAM & NICER observations for Swift J1858.6–0814.

UT date	UT Start	UT End	Instrument	Filters	Cadence <sup>1</sup>	Comments
2018/11/14	19:24:22	19:50:15	HiPERCAM	$u_s, g_s, r_s, i_s, z_s$	46.6 ms	
2018/11/09	00:42:59	01:18:33	ULTRACAM	$u', g', i'$	0.93 (4.63) s	
2019/03/01	09:14:15	09:49:19	ULTRACAM	$u_s, g_s, i_s$	1.00 (3.01) s	
2019/03/02	09:07:00	09:39:20	NICER	0.2–12 keV	40 ns	ObsId 2200400101
2019/03/02	09:05:22	09:45:14	ULTRACAM	$u_s, g_s, i_s$	0.28 s (0.29) s	Simultaneous with NICER
2019/03/04	08:54:22	09:48:59	ULTRACAM	$u_s, g_s, i_s$	0.50 s (4.01) s	Simultaneous with NICER
2019/03/04	09:05:25	09:36:20	NICER	0.2–12 keV	40 ns	ObsId 2200400103
2019/03/05	09:06:26	09:26:49	ULTRACAM	$u_s, g_s, i_s$	0.58 s (1.17) s	
2019/05/09	08:13:38	10:23:17	ULTRACAM	$u_s, g_s, i_s$	0.25 s (1.26) s	
2019/06/07	01:52:25	02:39:45	HiPERCAM	$u_s, g_s, r_s, i_s, z_s$	47.9 ms	Simultaneous with NICER
2019/06/07	01:53:20	02:33:43	NICER	0.2–12 keV	40 ns	ObsId 2541030101
2019/06/07	03:23:09	04:17:27	HiPERCAM	$u_s, g_s, r_s, i_s, z_s$	47.9 ms	

<sup>1</sup>Numbers in brackets is the  $u_s$ -band cadence, if different from the other wave-bands.



**Figure 1.** The long-term X-ray light curves and the radio and X-ray spectral index light curves of Swift J1858.6–0814 during its 2018 and 2019 outburst. The top panel shows the Swift/XRT PC mode X-ray data (black squares), where the vertical lines mark the times of our ULTRACAM (blue) and HiPERCAM (red) optical observations. The dashed lines show the times when the optical observations were simultaneous with NICER. The bottom panel show the radio (red stars; 4.5 GHz) and X-ray (black squares; 0.2–10 keV) spectral indices ( $F_\nu \propto \nu^\alpha$ ) taken from van den Eijnden et al. (2020). The blue squares show the spectral index of the optical flares observed with ULTRACAM and HiPERCAM determined in this paper (see Section 4).

those seen in the black hole X-ray binary V404 Cyg, which showed long-term ‘blue’ flaring and short-term sporadic ‘red’ flaring during its 2015 outburst (Kimura et al. 2016; Gandhi et al. 2016). The radio emission from Swift J1858.6–0814 showed variability by up to a factor of  $\sim 8$  on time-scales of minutes due to mass accretion rate fluctuations consistent with a compact jet (Bright et al. 2018; van den Eijnden et al. 2020). The X-ray spectrum showed evidence for significant intrinsic local absorption (Reynolds et al. 2018; Hare et al. 2020) and the P-Cygni profile observed in the optical spectrum (Muñoz-Darias et al. 2020), suggested that a significant amount of mass was ejected from the inner accretion flow.

Although Swift J1858.6–0814 entered the Sun constraint for most X-ray telescopes in 2019 November, it was detected again with the Monitor of the All-sky X-ray Imager (MAXI) in 2020 February in a previously unobserved X-ray state, with significantly less variability and enhanced soft X-ray emission, implying a transition to a soft state (Negoro et al. 2020; Buisson et al. 2020b). During 2020 March several Type I X-ray bursts were detected with the Neutron star Interior Composition Explorer (NICER) and the Nuclear Spectroscopic Telescope Array (NuSTAR), identifying Swift J1858.6–0814 as a neutron star binary system despite the fact that pulsations were not detected (Buisson et al. 2020a). These bursts exhibited photospheric radius

expansion allowing a distance estimate of  $\sim 12.8$  kpc. Strong periodic drops in X-ray flux were also detected, consistent with eclipses by the secondary star and variable obscuration due to the thickness of the disc/accretion stream which is also responsible for the strong variability (Buisson et al. 2021).

Here we report on high time-resolution HiPERCAM and ULTRACAM optical observations of Swift J1858.6–0814 some of which are simultaneous with NICER observations, taken in 2018 and 2019. We comment on the observed optical flaring and on the optical/X-ray flux correlations and timing properties of the light curves.

## 2 OBSERVATIONS

In Fig. 1 we show the long-term X-ray light curve of Swift J1858.6–0814 during its 2018 and 2019 outburst and mark the optical and X-ray observations presented in this paper.

## 2.1 NICER – X-rays

Swift J1858.6–0814 was observed with NICER in an intensive monitoring program during its 2018 and 2019 X-ray outburst. NICER is an X-ray instrument on board the International Space Station (ISS) where individual photons with energies in the range 0.2–12 keV can be detected with a time resolution of 40 ns (Gendreau et al. 2016). The data reduction was carried out using the collection of NICER-specific tools `NICERDAS` which is part of HEASARC<sup>1</sup>. Full Level2 calibration and screening was conducted with `NICERL2`, which calibrated, checked for good time intervals, merged, and cleaned the data. The barycentric correction was carried out using `BARYCORR`, and finally the photon events were binned to the times of the optical light curves as described in the following sections. We produced a light curve in the 0.2–12 keV energy band for each data segment using `XSELECT` and then applied the background correction. In order to calculate the hardness ratio, we extracted light curves in the 0.5–3.0 keV and 3–10 keV bands. For these light curves, we normalised each incoming photon with respect to the effective area of the telescope at that energy. We define the hardness ratio of the X-rays as  $(\text{hard-soft})/(\text{hard+soft})$ , where the hard and soft X-ray rates are in the 3–10 keV and 0.5–3.0 keV range, respectively. The errors on the hardness ratio were calculated by using  $1-\sigma$  Poisson errors (following the example of Gehrels 1986) to simulate maximum and minimum values of the individual X-ray bands, and then calculating the hardness ratio at each extreme. We note that these errors are an approximation only and may underestimate any outliers.

## 2.2 ULTRACAM/NTT – Optical

High-speed multi-colour photometry of Swift J1858.6–0814 was carried out using ULTRACAM instrument (Dhillon et al. 2007) on the 3.5 m New Technology Telescope (NTT) in La Silla, Chile. ULTRACAM uses dichroic beamsplitters to simultaneously image three custom made Sloan Digital Sky Survey (SDSS) filters, and can observe at frame-rates well above 100 Hz due to the frame-transfer CCDs and the lack of a physical shutter (Dhillon et al. 2007). We used ULTRACAM to observe Swift J1858.6–0814 during 2018 November, 2019 March and 2019 May. The 2018 observations were carried out simultaneously with the  $u'$ ,  $g'$ , and  $i'$  SDSS filters (Doi et al. 2010), whereas the 2019 observations were performed using the higher throughput  $u_s$ ,  $g_s$ , and  $i_s$  Super-SDSS filters (Dhillon et al. 2021) which use multi-layer coatings rather than coloured glass to define the filter bandpasses, with the cut-on/off wavelengths designed to match higher throughput the original SDSS filters. Unlike most observations of this type, the times were not explicitly chosen to coincide with X-ray observations. Some of the observations did overlap with the X-ray observations performed with the NICER instrument and such simultaneity was purely serendipitous (see Section 2.1). On different nights, ULTRACAM was used in windowed mode (one window containing the target and the other containing multiple comparison stars) with  $1\times 1$  binning. Typically, compact binaries are faint in the  $u_s$ -band, and so ULTRACAM's on-chip co-adding feature was used, which provides a longer exposure time in the  $u$ -band so as to increase the signal-to-noise ratio. The details of the observing setup for each night are given in Table 1.

We used the HiPERCAM pipeline software<sup>2</sup> to debias, flat-field and extract the target count rates using aperture photometry with

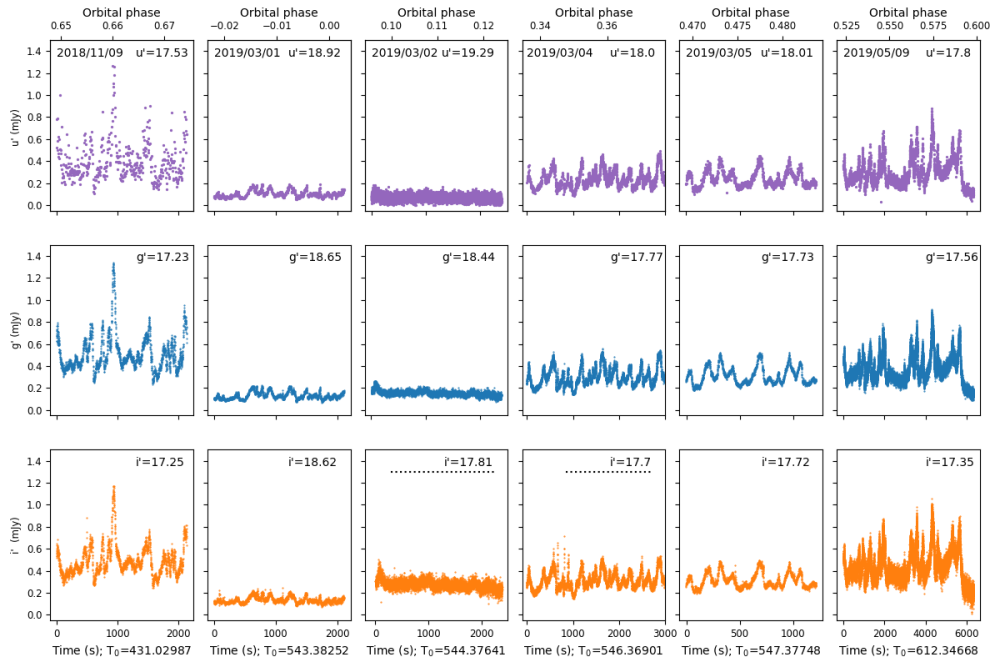
a seeing-dependent circular aperture tracking the centroid of the source. The sky background was computed using the clipped mean of an annular region around the target and relative photometry of Swift J1858.6–0814 was carried out with respect to the local standard star (PSO J185832.982-081400.913). For the  $r_s$ -band and  $g_s$ -band, the field is covered by the Pan-STARRS survey and so the calibrated  $r_s$ -band and  $g_s$ -band magnitudes are listed in DR1 catalog (Magnier et al. 2020). These were transformed to SDSS magnitudes (Finkbeiner et al. 2016) and then used to calibrate the target light curves. Since the field is not covered by any archival optical survey in the  $u_s$ -band, calibrating these data was less straightforward. Flux standards were observed on various nights during the ULTRACAM observations in 2019 March. These flux standards were used to determine the  $u_s$ -band instrument zero-point. The local standards were then calibrated which in turn were used to calibrate the target light curve. For the nights when no flux standard was observed, we assume that the  $u_s$ -band zero-point measured during the March observing runs was still valid. The difference between the ULTRACAM Super-SDSS and SDSS filters leads to an uncertainty in the flux calibration of  $< 3$  per cent (Wild et al. 2022). The observed ULTRACAM light curves are shown in Fig. 2a.

## 2.3 HiPERCAM/GTC – Optical

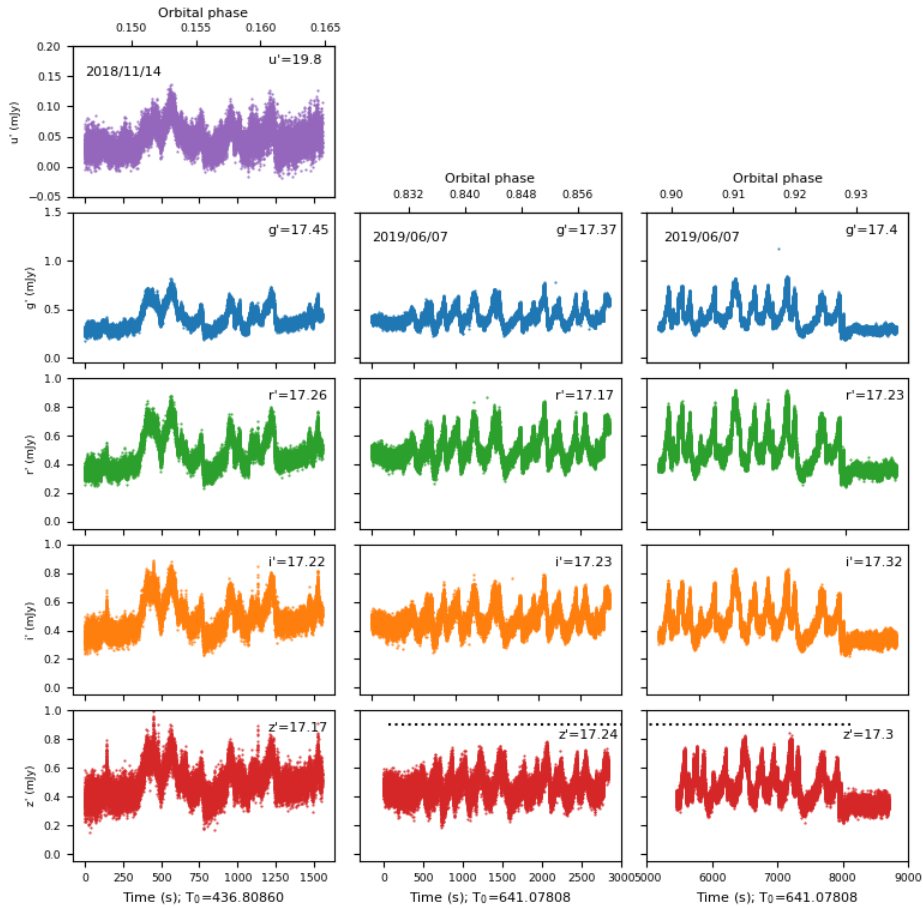
Sub-second optical imaging was carried out in 2018 November and 2019 June using HiPERCAM on the 10.4 m Gran Telescopio Canarias (GTC) in La Palma, Spain. HiPERCAM uses dichroic beamsplitters to simultaneously image the custom made Super-SDSS  $u_s$ ,  $g_s$ ,  $r_s$ ,  $i_s$  and  $z_s$  filters. Similar to ULTRACAM, HiPERCAM can observe at frame-rates well above 1000 Hz which is achieved by the lack of a physical shutter and the frame-transfer CCDs that can rapidly shift charge into a storage area for reading out, freeing up the original pixels for observation and thereby achieving low (7.8 ms) dead-times (Dhillon et al. 2021). The CCDs were binned by a factor of 4 and drift mode was used with four windows (336 $\times$ 200 pixels each) for all the observations. The instrument was orientated so that one window was centered on Swift J1858.6–0814 and another window on a local standard star. We used an exposure time of 43.6 ms and 44.9 ms which resulted in a cadence of 46.6 ms and 47.9 ms, for the 2018 and 2019 observations, respectively (see Table 1 for details). Observations were obtained on two nights, 2018 November 14 and 2019 June 7. The observations taken in 2019 were coordinated with the X-ray instrument NICER. A log of the observations is given in Table 1. Similar to the ULTRACAM data, we used the HiPERCAM pipeline software to debias, flat-field and extract the photon counts for the target and local standard using aperture photometry with a seeing dependent circular aperture. The local standard stars used are listed in the Pan-STARRS survey DR1 catalog (Magnier et al. 2020) and have  $g'$ ,  $r'$ ,  $i'$  and  $z'$  magnitudes which were transformed to SDSS magnitudes (Finkbeiner et al. 2016) and then used for the photometric calibration of Swift J1858.6–0814. For the 2018 data the  $u'$ -band calibration was determined using the local standard star PSO J185827.968-081329.815 and the full-frame acquisition images which was calibrated by determining the instrument zero-point. As a check we also determined the  $g_s$ ,  $r_s$ ,  $i_s$  and  $z_s$  magnitudes and found that they agreed with the Pan-STARRS magnitudes at the  $< 10$  per cent level. Unfortunately, the local standard star PSO J185826.795-081357.216 used in the 2019 observations was not detected in the  $u_s$ -band images, and so it could not be flux calibrated. The difference between the HiPERCAM Super-SDSS and SDSS filters leads to an uncertainty in the flux calibration of  $< 3$  per cent (Brown et al. 2022). Finally we convert from SDSS magnitudes to flux density, where we

<sup>1</sup> <https://heasarc.gsfc.nasa.gov>

<sup>2</sup> <https://github.com/HiPERCAM/hipercam>

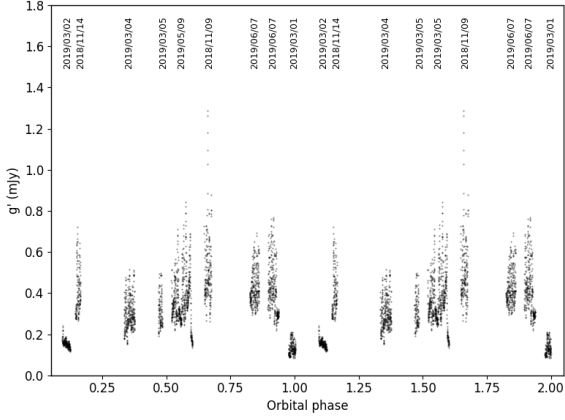


(a) The ULTRACAM light curves



(b) The HiPERCAM light curves

**Figure 2.** The observed ULTRACAM (top) and HiPERCAM (bottom) light curves of Swift J1858.6–0814. The black dotted horizontal line shows the time of NICER observations. The mean magnitude of Swift J1858.6–0814 is shown in each panel. A MJD time offset of  $T_0 + 58000.0$  ( $T_0$  is in days) is applied and we use the orbital ephemeris given in [Buisson et al. \(2021\)](#).



**Figure 3.** ULTRACAM and HIPERCAM  $g_s$ -band light curves of Swift J1858.6–0814 as a function of orbital phase using the orbital ephemeris given in Buisson et al. (2021), where phase 0.0 is defined as superior conjunction of the compact object. For clarity two orbital phases are plotted and the light curves have been rebinned to a time resolution of 10 s.

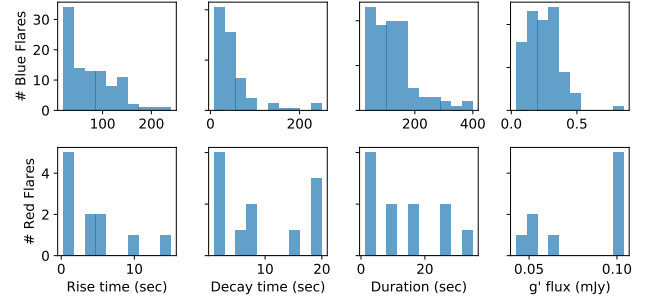
propagate the uncertainty in the local standard. The observed HiPERCAM light curves are shown in Fig. 2b.

### 3 REDDENING

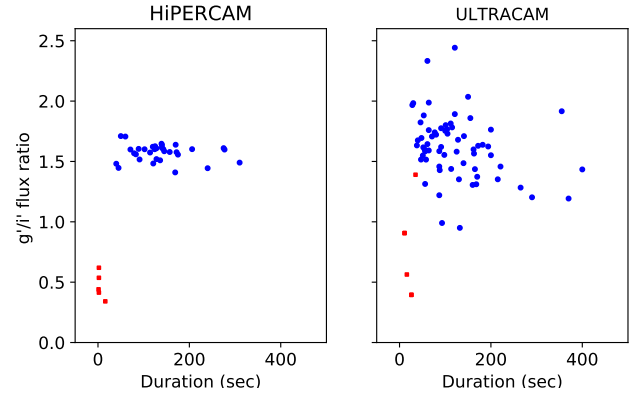
Swift J1858.6–0814’s position in the sky allows us to estimate the line of sight interstellar reddening. The Galactic neutral atomic hydrogen (H I) column density to the target is  $N_{\text{H}} \sim 1.84 \times 10^{21} \text{ cm}^{-2}$  (HI4PI Collaboration et al. 2016). Using the relation between the Galactic hydrogen absorption column density and optical extinction (Foight et al. 2016) along with the galactic extinction law (Cardelli et al. 1989) we determine a colour excess of  $E(B - V) = 0.21$  mag. We can also estimate  $N_{\text{H}}$  from spectral fits to the NICER data. Using the XSPEC (Arnaud 1996) software package, a blackbody and power-law model fit to the 2018 November data gives  $N_{\text{H}} \sim 2.0 - 2.5 \times 10^{21} \text{ cm}^{-2}$ , whereas fits to the 2019 June data gives  $N_{\text{H}} \sim 1.6 - 1.7 \times 10^{21} \text{ cm}^{-2}$ . The value for  $N_{\text{H}}$  determined from the NICER data is consistent with the value determined from the H I maps and we assume a colour excess of 0.21 mag for the rest of this paper.

### 4 OPTICAL FLARES

In Figs. 2a and 2b we show the observed HiPERCAM and ULTRACAM light curves, respectively, where wavelength dependent flaring activity is clearly seen. Flaring is superimposed on a sinusoidal modulation, which is due to a combination of the secondary star’s ellipsoidal modulation, X-ray heating and other possible sources of light in the system (see Fig. 3). To determine the properties of the flares first use the colour excess of  $E(B - V) = 0.21$  mag determined in Section 3 with the interstellar extinction law (Cardelli et al. 1989) to deredden the observed fluxes. We identify and isolate the flare events by determining the start and end of the same flare event in each waveband. We then subtract the interpolated flux underneath the flare event which in effect subtracts the contribution of the non-variable component. We assume during the actual flare event that the other components that contribute to the observed flux do not vary. We define small and large flares as events with  $g_s$ -band amplitudes of  $\sim 0.1$  mag and  $\sim 1$  mag, respectively. A total of 102 large



**Figure 4.** The rise, decay time-scales, duration and flux histograms of the dereddened flare events.



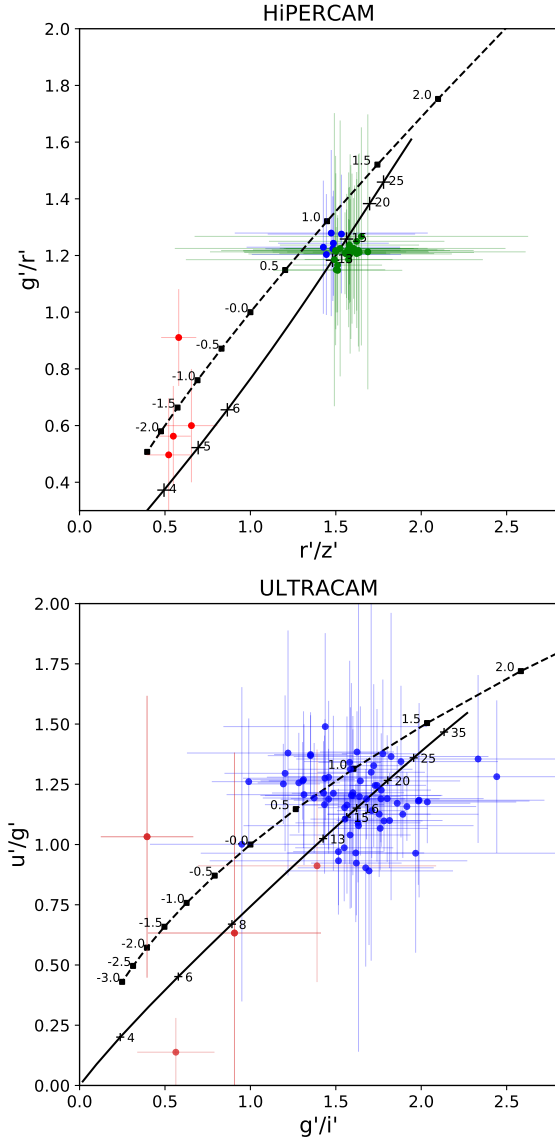
**Figure 5.** The flare duration versus colour of the dereddened small (red points) and large flare (blue points) events.

and 5 small flare events were isolated, respectively. Fig. A1 of the Appendix shows some examples of the isolated flare events where flares on different time-scales, amplitude and colour are clearly seen. For the flare events we also determine the peak flare flux in each waveband and flux ratio.

In Fig. 3 we show the observed  $g_s$ -band light curve of Swift J1858.6–0814 as a function of orbital phase, using the orbital ephemeris given in Buisson et al. (2021) where phase 0.0 is defined as superior conjunction of the compact object. Although our orbital phase coverage is relatively poor ( $\sim 33$  per cent), we observe flares at all orbital phases. Buisson et al. (2021) find that the bright flares occur preferentially in the post-eclipse phase of the orbit, around orbital phase  $\sim 0.3$ , most likely due to increased thickness at the disc-accretion stream. We do not find any evidence for this in our optical data, but note our poor phase coverage. We find that the mean flux and the intrinsic source fractional RMS variability defined as  $\sigma_{\text{source}}^2 = \sigma_{\text{total}}^2 - \sigma_{\text{noise}}^2$  (Vaughan et al. 2003) are strongly linearly correlated with a Pearson’s correlation coefficient of 0.84. The low RMS observed at phase 0.0 (2019 March 01) which has the lowest flux of our observations and very little flaring is consistent with a system at a high binary inclination angle (Buisson et al. 2021; Knight et al. 2022).

#### 4.1 Time-scales

We determine the rise, decay and duration of the dereddened flares which are shown in Fig. 4. As one can see, the ‘red’ flares (more flux at longer wavelengths) have a much shorter time-scale and amp-



**Figure 6.** Colour–colour diagram for the ULTRACAM and HiPERCAM large and small dereddened flare events. The dashed line shows a power-law model of the form  $F_\nu \propto \nu^\alpha$ , where the black squares mark the value of  $\alpha$  ranging from  $-2.0$  to  $+2.0$  in units of  $0.5$ . The solid black line is a blackbody model where the crosses show the temperature in units of  $1000\text{ K}$ . In the top panel the red circles show the HiPERCAM small flares, whereas the blue (2018 November 14) and green circles (2019 June 7) show the HiPERCAM large flare events. In the bottom panel the red and blue circles show the ULTRACAM small and large flares events, respectively.

litude compared to the ‘blue’ flares (more flux at shorter wavelengths) events. The ‘red’ and ‘blue’ flares have median  $g_s$ -band amplitudes of  $\sim 0.1$  mag and  $\sim 1$  mag, respectively. In Fig. 5 we show the flare duration versus colour. The flares are separated into two regions: short-duration ‘red’ flares and long-duration ‘blue’ flares. Small amplitude ‘red’ flares are observed on 2018 November 14 (HiPERCAM) and 2019 February 2 (ULTRACAM), whereas large ‘blue’ flares are present in all observations, except on 2019 March 2 where no flares are observed. The different time-scales and amplitudes of the flares indicate that they arise from different emission processes.

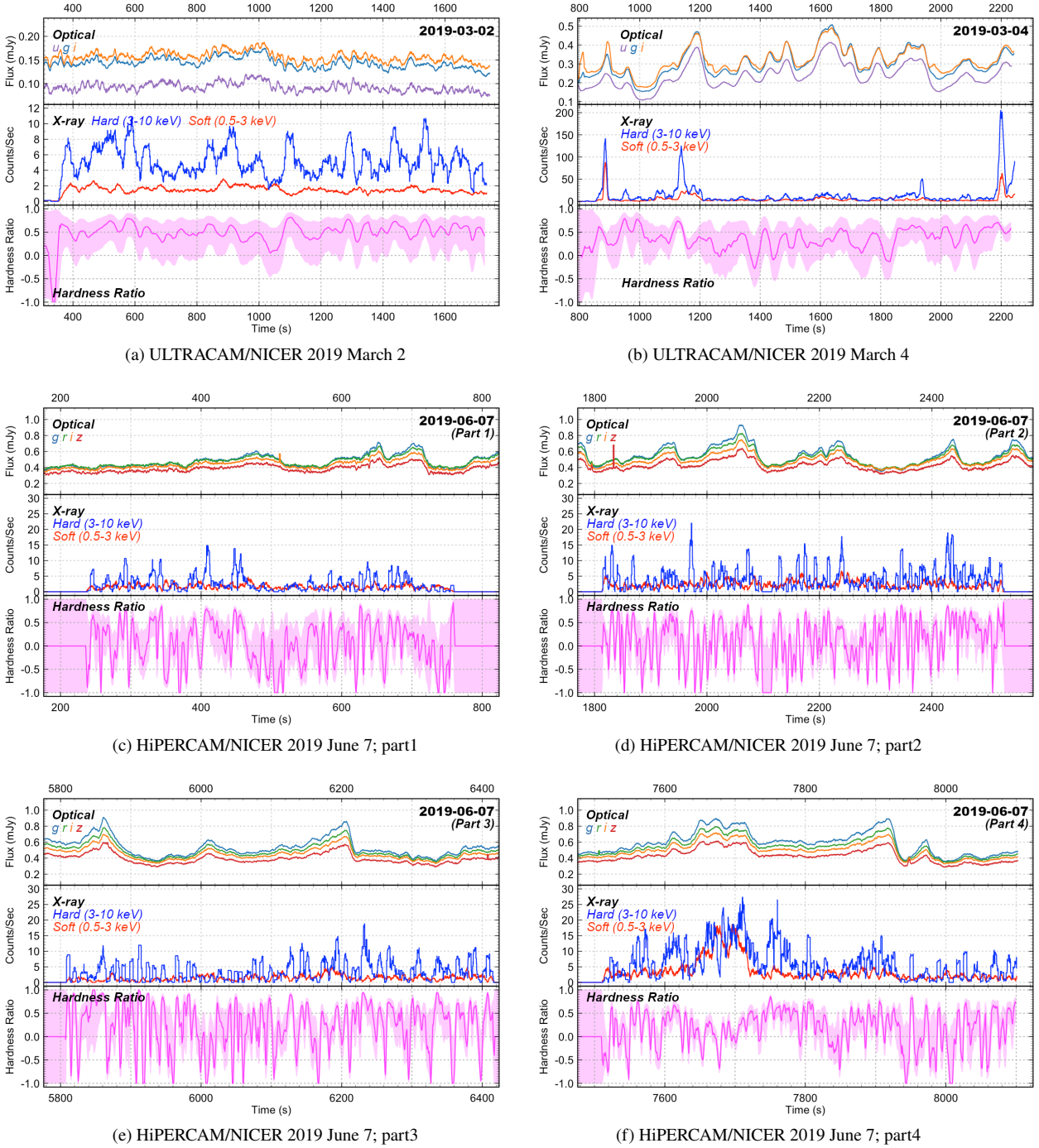
## 4.2 Spectral energy distribution

In an attempt to interpret the broad-band spectral properties of the flares, we compare the observed fluxes with the prediction for different emission mechanisms, namely synchrotron emission and blackbody. The latter has an approximately power-law form on the Rayleigh–Jeans tail and so we characterise the synchrotron and blackbody emission with a power-law form  $F_\nu \propto \nu^\alpha$ , where  $\nu$  is the frequency and  $\alpha$  is the spectral index. We compute the given emission spectrum and then calculate the expected flux density ratios in the relevant filters using the synthetic photometry package `SYNPHOT` in `IRAF/STSDAS`. For the blackbody emission, given the intrinsic model flux we then determine the corresponding radius of the region that produces the observed dereddened flux at a given distance.

In Fig. 6 we show the HiPERCAM and ULTRACAM individual peak flare flux ratios and the expected results for different emission models. We show the  $g_s$ ,  $r_s$  and  $z_s$  fluxes common to the HiPERCAM 2018, 2019 and ULTRACAM 2019 data sets and the  $u'$ ,  $g'$  and  $i'$  fluxes for the ULTRACAM 2018 data set. Fig. A2 of the Appendix shows some example fits to the individual dereddened flare events observed on 2018 November 14 (HiPERCAM) and 2019 May 9 (ULTRACAM). The power-law indices obtained by fitting the broad-band spectral energy distribution of the individual large and small flare events are in the range  $\alpha \sim -1.0$  to  $-2.0$  (with a mean of  $\alpha \sim -1.5$ ) for the ‘red’ flares. In contrast the ‘blue’ flares can be represented with a power-law of  $\alpha \sim 1.0$  (range of  $\alpha \sim 0.6$  to  $1.2$ ) or a  $\sim 14,000 \pm 2000\text{ K}$  blackbody which with a mean  $g_s$  peak flare flux of  $\sim 0.45\text{ mJy}$  (out of eclipse) corresponds to a radius of  $\sim 1.0 \pm 0.2 R_\odot$ , assuming a distance of  $12.8\text{ kpc}$  (Buisson et al. 2020a). Although a single temperature blackbody has limited physical significance and is likely a very poor description of a flare event, it is useful for comparison with other works. The 2019 data was taken at orbital phase  $\sim 0.9$  which is outside the start of eclipse ingress (Buisson et al. 2021) and so we can rule out a decrease in  $N_{\text{H}}$  due to the absorption in the atmosphere of the secondary star. However, Castro Segura et al. (2022) have detected disc winds in the hard state and the associated variable obscuring columns that contribute to  $N_{\text{H}}$  might explain the differences we observe.

## 5 TIMING AND CORRELATION ANALYSIS

The auto-correlation function (ACF) analysis of the individual optical and X-ray light curves and the cross-correlation function (CCF) of the simultaneous optical and X-ray light curves can also be used to constrain the emission processes and location, respectively. We perform such a timing analysis on the simultaneous optical and X-ray data using the same methods/techniques outlined in Paice et al. (2019). We use the NICER X-ray light curves and the dereddened ULTRACAM and HiPERCAM optical light curves determined in Sections 2.1 and 4, respectively. To create the simultaneous light curves we first corrected the times of both datasets to the solar system barycentre and then binned the X-ray photons directly to the optical time bins. Since the optical light curves have a constant dead-time, the X-ray photons observed during these times are not used. For the 2019 June 7 HiPERCAM data, we show the four different simultaneous sections, whereas for the ULTRACAM dataset we show the two simultaneous sections taken in 2019 March 2 and 4.

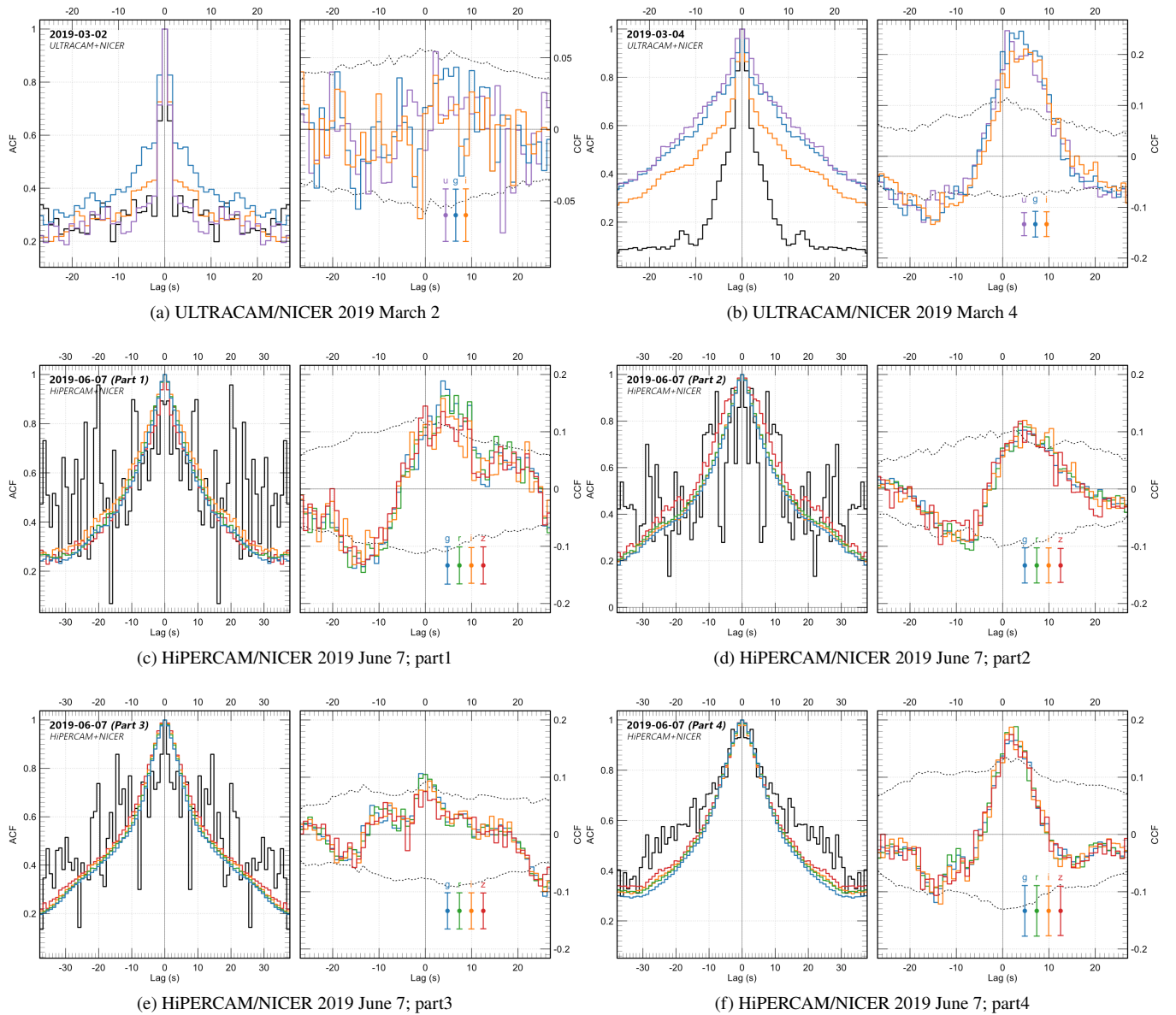


**Figure 7.** The simultaneous optical and X-ray light curves of Swift J1858.6–0814. From top to bottom, the optical light curves, the hard (3–10 keV; blue) and soft (0.5–3.0 keV; red) X-ray light curves and the X-ray hardness ratio defined as the ratio of the rates (hard-soft)/(hard+soft). The X-rays and hardness ratio light curves have been binned with a moving average of 100 points for readability (except for 2019 March 4 where a 20 point moving average was used due to the much higher count rates). A barycentered MJD time offset of 58544.37641329, 58546.36898883 and 58641.08379497 has been applied to the 2019 March 2, March 4 and June 7 data, respectively.

### 5.1 Optical/X-ray correlations

In Fig. 7 we show the simultaneous optical and X-ray light curves taken on 2019 March 2, 4 and June 7. For the X-ray data we also show the hardness ratio of the X-ray count rates. The CCF shows the response of the optical light curves to variations in the X-ray light curve as a function of time lag. Positive time lags indicate a

net correlation in which the optical flux lags the X-ray flux. The CCF is produced by splitting and detrending the simultaneous light curves into segments of equal length. We determine the CCF for each segment and calculate the mean CCF and standard error in each bin. We also compute the auto-correlation functions (ACFs) of the X-ray/optical light curves. The Poisson noise dominating the X-ray ACFs at zero lag is corrected by making use of the Wiener–Khinchin



**Figure 8.** The ACF (left plot) and CCF (right plot) of the simultaneous optical and X-ray light curves of the 2019 March 2 (a), 2019 March 4 (b) and 2019 June 7 (c to f) data. A positive lag implies that the optical flux lags the X-ray flux. For the 2019 June 7 data (c to f) we show the corresponding ACFs and CCFs of the data split into four sections, corresponding to the sections when the data were simultaneous. In the left panel, the ACF of the X-ray data is shown in black and the ACF of the  $g_s$ ,  $r_s$ ,  $i_s$ , and  $z_s$  data are shown in blue, green, orange and red, respectively. In the right panel the CCF of the X-ray data with respect to the  $g_s$ ,  $r_s$ ,  $i_s$  and  $z_s$  data are shown in blue, green, orange and red, respectively. The black dashed lines represent the 5 and 95 percent confidence intervals.

theorem, which states that the power spectrum of a random process and its ACF are Fourier pairs. Therefore, we can subtract the white noise from the X-ray power spectrum and then compute the inverse Fourier transform to determine the ACF. In Fig. 8 we plot the corresponding ACF and CCFs for all our simultaneous optical/X-ray light curves. To determine the confidence levels in the CCFs we simulate 1000 similar (yet uncorrelated) optical light curves, compute the cross-correlation function with respect to the X-ray light curve and then determine the 5 and 95 percent boundaries in each bin of the CCF lag. We create the optical light curves by first computing the Fourier transform of the optical light curve, randomising the arguments and then performing the inverse Fourier transform to create a lightcurve with an identical power spectrum. In the following, for

each simultaneous dataset we summarise the observed characteristic of the light curves and average ACFs and CCFs.

- For the 2019 March 2 data the mean X-ray count rate is  $2.6 \text{ counts s}^{-1}$  over the length of the simultaneous ULTRACAM observation. Low optical and X-ray variability is observed with no significant flaring behaviour, compared to what is observed on other nights. In general the X-ray light curve has a strong hard component. The optical ACF is broader than the X-ray ACF which is what one expects if the optical flux arises from X-ray reprocessing. No significant features are observed in the CCFs.

- For the 2019 March 4 data, the mean count rate is relatively high at  $7.9 \text{ counts s}^{-1}$  over the length of the simultaneous ULTRACAM observation. A few relatively strong X-ray flare events are observed



which have a strong hard component. The optical ACF is broader than the X-ray ACF, consistent with X-ray reprocessing. One can clearly see that the optical and X-ray fluxes are correlated, which provides a visual confirmation of the CCF observed. The CCF of this observation shows the strongest positive correlation of any of our epochs, with a peak at a time lag of  $\sim 5$  s in every band (a coefficient of  $\sim 0.3$  is a significant value in fast-timing studies of X-ray binaries; see e.g. Gandhi et al. 2010, 2017; Paice et al. 2019). A weak negative correlation at negative lags is also seen at  $\sim -5$  s. Furthermore, there appears to be a repeated phenomenon in the light curves - the hard X-rays increase first and then give way to softer X-rays. This is more clearly seen in the flare at time  $\sim 1100$  s. In the CCFs, there appears to be a correlation between the optical delay and wavelength, in which the  $u_s$ -band delay is shorter than the  $g_s$ -band delay, which is shorter than the  $i_s$ -band delay. This implies that reprocessing is dominant.

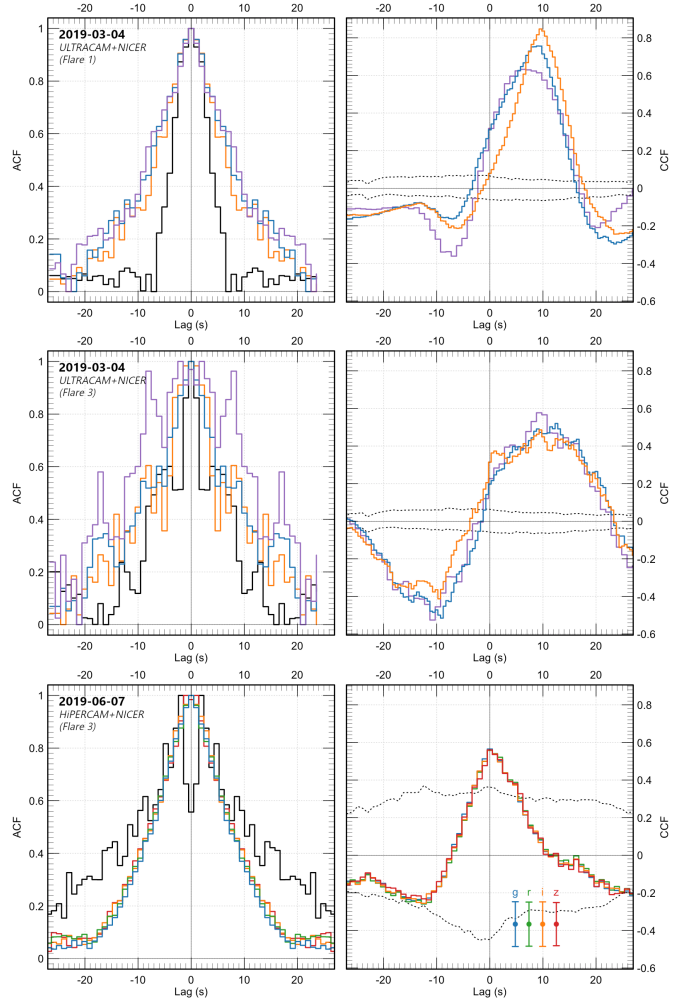
- Finally, the 2019 June 7 data has a relatively low mean count rate of  $0.65 \text{ counts s}^{-1}$  coincident with the HiPERCAM observations. Although the X-ray variability is much lower, several optical peaks do have slight increases in X-ray count rates, where the increase seems to be slightly greater in the hard X-rays. In general the X-ray light curve has a hard component but slightly softer than other epochs and is dominated by a large flare event in part 4 at 7700 s, which has a strong soft component as noted by the change in the X-ray hardness ratio. This is in contrast to the other short-term X-ray flare events which seem to have a hard component. The ACF and CCF properties in sections 1 to 3 are very similar. The parts 1 to 4 data show the optical ACF and X-ray ACF to be similar in shape. A relatively strong positive correlation in the CCF with a peak at a time lag of  $\sim 5$  s is observed in every band for parts 1, 2 and 4, and at a time lag of  $\sim 0$  s in the part 3 data. A weak negative correlation at negative lags is also observed between  $\sim -20$  s and  $-10$  s.

## 5.2 Optical/X-ray correlations of flaring Events

In order to further investigate the flaring events we determine the ACFs and CCF for three clearly defined flare events on 2019 March 4. We compute the optical and X-ray ACFs and well as the optical/X-ray CCF using a 100 s window (see Fig. 9). As one can see, the CCFs of the flare events share many characteristics, including a high CCF correlation ( $0.4\text{--}0.8$ ) with lags between  $0\text{--}5$  s and a precognition dip. The 2019 March 4 and 2019 June 9 data are taken at orbital phase  $\sim 0.35$  and  $\sim 0.93$ , respectively. Indeed, the flare events taken at different orbital phases have time delays consistent with arising from reprocessing in the secondary star. One expects the longest time delay to arise at orbital phase quadrature (phase 0.25) and the shortest at superior conjunction of the secondary star (phase 0.0). Indeed, if one had sufficient flare events across the binary orbit one could perform echo-mapping in order to extract the fundamental binary parameters (O’Brien et al. 2002).

## 5.3 Fourier Analysis

In order to understand the nature of the different components contributing to the CCF, we decomposed the observed variability into different time-scales using Fourier techniques. We performed a Fourier analysis of the light curves using the X-ray spectral-timing software package STINGRAY<sup>3</sup> (Huppenkothen et al. 2019). The coherence and corresponding errors were determined using the method described in Vaughan & Nowak (1997). We computed the Fourier transform

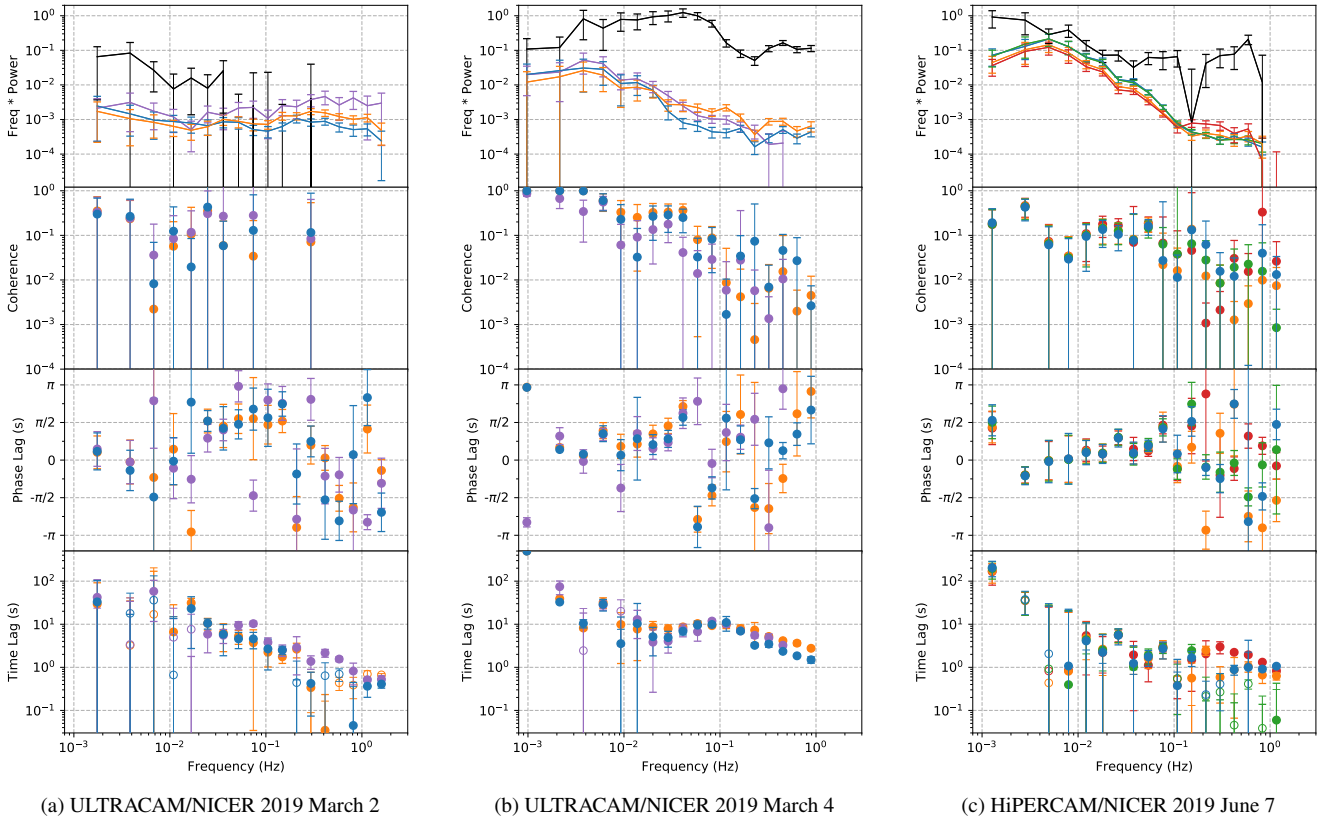


**Figure 9.** Same as Fig. 8 but for the clear flare events on 2019 March 4 and 2019 June 7.

of the light curves and then analysed them at each frequency. The power spectra represent the amplitude of the variability at each Fourier frequency, the coherence shows how the variability in the power of the correlated signal is distributed over the Fourier frequencies, and the phase lags represent a measure of the lag between the bands at each frequency as a function of phase. Sometimes, the time lags are a more intuitive representation of the delays, which are connected to the phase lags through  $\Delta t = \Delta\phi/2\pi f$ , where  $f$  is the frequency of the bin and  $\phi$  is the phase lag. Positive phase lags correspond to the delay of the optical light curve with respect to the X-rays.

Good Time Intervals (GTIs) are used based on the individual epoch of the X-ray observations and the average cross-spectrum is computed over independent light curve segments with 2048 bins in length. We use 2, 1, and 6 segment(s) for the 2019 March 2, 2019 March 4 and 2019 June 7 data, respectively, where the white noise is fitted to each power spectrum and removed prior to the calculation of coherence. The standard root-mean-squared (RMS) normalisation is applied (Belloni & Hasinger 1990). In Fig. 10 we show the frequency-dependent products binned logarithmically in frequency. The HiPERCAM data were binned by a factor of 8, and then all data were averaged over segments of 2048 bins, or  $\sim 572$ , 1028, and 784 s respectively (except for the  $u_s$  band data in March 4, which was co-added and thus sampled differently; this was averaged over segments of 1024 bins, or 1028 s).

<sup>3</sup> <https://github.com/StingraySoftware/stingray>



**Figure 10.** Results of the Fourier analysis of the simultaneous optical and X-ray light curves of Swift J1858.6–0814. From top to bottom: the X-ray and optical power spectra where the white noise has been removed, coherence spectrum, phase lags and time lags. For the bottom two panels, a positive lag mean that the optical lags the X-rays. We use a logarithmic rebinning of a factor of 1.4 to display the data. In each plot, the X-ray data are shown in black, whereas the purple, blue, green, orange and red show the  $u_S$ ,  $g_S$ ,  $r_S$ ,  $i_S$ - and  $z_S$ -band data, respectively.

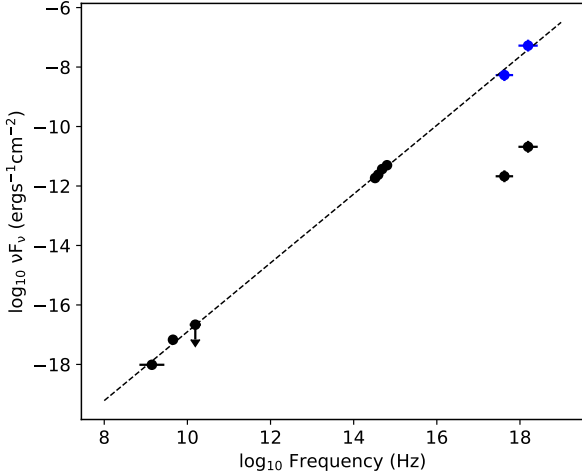
For Swift J1858.6–0814 on the nights where there is significant optical and X-ray variability (2019 March 4 and June 7), the power spectra for the optical and X-ray light curves are very similar. However, there is consistently higher power in the X-ray variability compared to the optical, which suggests that the optical variability is a result of reprocessing of faster X-ray variations at frequencies above the optical power spectrum peak.

In the 2019 March 4 and June 7 data, the coherence function shows a linear decline with increasing frequency. The declining absolute value of the optical/X-ray coherence means that a single component is not a good representation of the broad-band variability. In the 2019 March 4 and June 7 data there is a plateau in the coherence between 0.01–0.1 Hz at  $\sim 10$  s (most notable in the March 4 data), during which a rise in phase lags is observed. Beyond  $\sim 0.1$  Hz, the data become white-noise dominated, and it is not possible to find meaningful results. Frequency-dependent time-lags are also observed. Below  $\sim 0.01$  Hz, the time lags rise towards low Fourier frequencies and a plateau is observed between 0.01–0.1 Hz. Beyond  $\sim 0.1$  Hz the time-lags are observed to decrease with frequency, a natural consequence of the large scatter and randomly distributed phase lags. The time lag observed at  $\sim 0.1$  Hz on March 4 is longer than what is observed in the CCFs; this is likely because the lower frequency lags contribute more to the CCF than the high frequency lags, as evidenced by the higher coherence below 0.05 Hz, and the sharp drop thereafter with time lags between 3–10 s. This combination gives rise to a culmination of many frequencies which results in the time-lag of  $\sim 5$  s observed in the CCFs.

## 6 DISCUSSION

### 6.1 Flare spectra

Generally, in the optical/near-IR region, a negative power-law index is expected if there is an optically-thin synchrotron spectrum from a flow/jet, whereas a positive power-law index is expected (with spectral index  $\sim 1$ ) if the optical emission is dominated by blackbody emission from regions in the accretion disc (Hynes 2005). The fast, ‘red’ optical flares observed in the ULTRACAM and HiPERCAM data have a power-law index of  $\alpha \sim -1.3$ , steeper than what is typically observed in XRBs,  $\alpha \sim -0.7$  (Hynes et al. 2003; Gandhi et al. 2011; Russell et al. 2013). However, it should be noted that flares with similarly steep spectral properties have been observed before with a power-law in the range  $-1.3$  to  $-1.5$  (Russell et al. 2010, 2013; Shahbaz et al. 2013; Gandhi et al. 2016) and indeed the fast ‘red’ flares are reminiscent of the ‘red’ flares observed during the outburst of V404 Cyg (Gandhi et al. 2016). Indeed, for V404 Cyg, based on the cooling timescales of the flaring events the emission has been attributed to synchrotron processes (Dallilar et al. 2017). For optically thin synchrotron emission, the only parameter which changes the spectral index is the particle energy distribution ( $p$ ) of the emitting electrons, which is related to the observed spectral slope in the optically thin plasma;  $\alpha_{\text{thin}} = (1 - p)/2$ . If the observed quiescent power-law index of  $\alpha \sim -1.3$  is interpreted as optically thin synchrotron, then  $p = 3.6$ , which is steeper than  $p \sim 2.4$  (or  $\alpha \sim -0.7$ ), which is typical for optically thin synchrotron in XRBs. A mixture of thermal and non-thermal particle energies could potentially explain such a steep



**Figure 11.** The absorption-corrected spectral energy distribution of Swift J1858.6–0814 on 2019 June 7 (black points). The NICER (0.5–3.0 keV and 3.0–10.0 keV) and optical ( $g_s$ ,  $r_s$ ,  $i_s$ ,  $z_s$ ) data are simultaneous, whereas the radio data (1.4, 4.5, and 15.5 GHz) are interpolated values taken within  $\sim 2$  months (Bright et al. 2018; van den Eijnden et al. 2020; Rhodes et al. 2022). We assume a distance of 12.8 kpc. (Buisson et al. 2021). The blue points are the scaled X-ray luminosities according to the  $L_{\text{OIR}} - L_X$  relation of Russell et al. (2006). The radio–X-ray spectral energy distribution can be described with a power-law of the form  $F_\nu \propto \nu^\alpha$  with an index of  $\alpha = -0.84 \pm 0.02$  (dashed line).

slope observed in Swift J1858.6–0814. In contrast, slow, large ‘blue’ flares are observed with a power-law index  $\sim 1.0$ , consistent with blackbody emission from an irradiated accretion disc (Hynes 2005); the spectrum from an irradiated accretion disc has a power-law index of 1.2 in the  $g_s$  to  $i_s$  bands.

We estimate the binary separation to be  $\sim 5.1 R_\odot$  ( $M_1=2.0 M_\odot$ ,  $M_2=0.25 M_\odot$ ,  $P_{\text{orb}}=0.883$  d) assuming that the accretion disc extends to its tidal truncation radius ( $R_d = 0.9 R_{L1}$ , where  $R_{L1}$  is the equivalent radius of the Roche lobe of a sphere with the same volume), we find  $R_d < 2.5 \pm 0.2 R_\odot$ . The large flare events can be represented by a  $\sim 14,000 \pm 2,000$  K blackbody and an equivalent blackbody radius of  $\sim 1.0 \pm 0.2 R_\odot$  (see Section 4.2) which is consistent with arising from regions in the accretion disc or from an extended disc atmosphere or wind (Buisson et al. 2021). The optical multi-wavelength spectral properties are reminiscent of those observed in the black hole X-ray binary V404 Cyg, where slow, ‘blue’ as well as fast, ‘red’ flares were observed during its 2015 outburst (Kimura et al. 2016; Gandhi et al. 2016). From the strongest observed flare on 2019 June 6 we estimate the optical ( $u_s - z_s$ ) and X-ray (0.5–10 keV) unabsorbed flare power to be  $\sim 0.1\%$  and  $\sim 0.33\%$  of the Eddington luminosity, assuming a  $1.8 M_\odot$  neutron star and a distance of 12.8 kpc (Buisson et al. 2020a). The optical flare in Swift J1858.6–0814 is a factor  $\sim 5$  less powerful compared to the optical flares in GX 339–4 (Gandhi et al. 2010) and V404 Cyg (Gandhi et al. 2016).

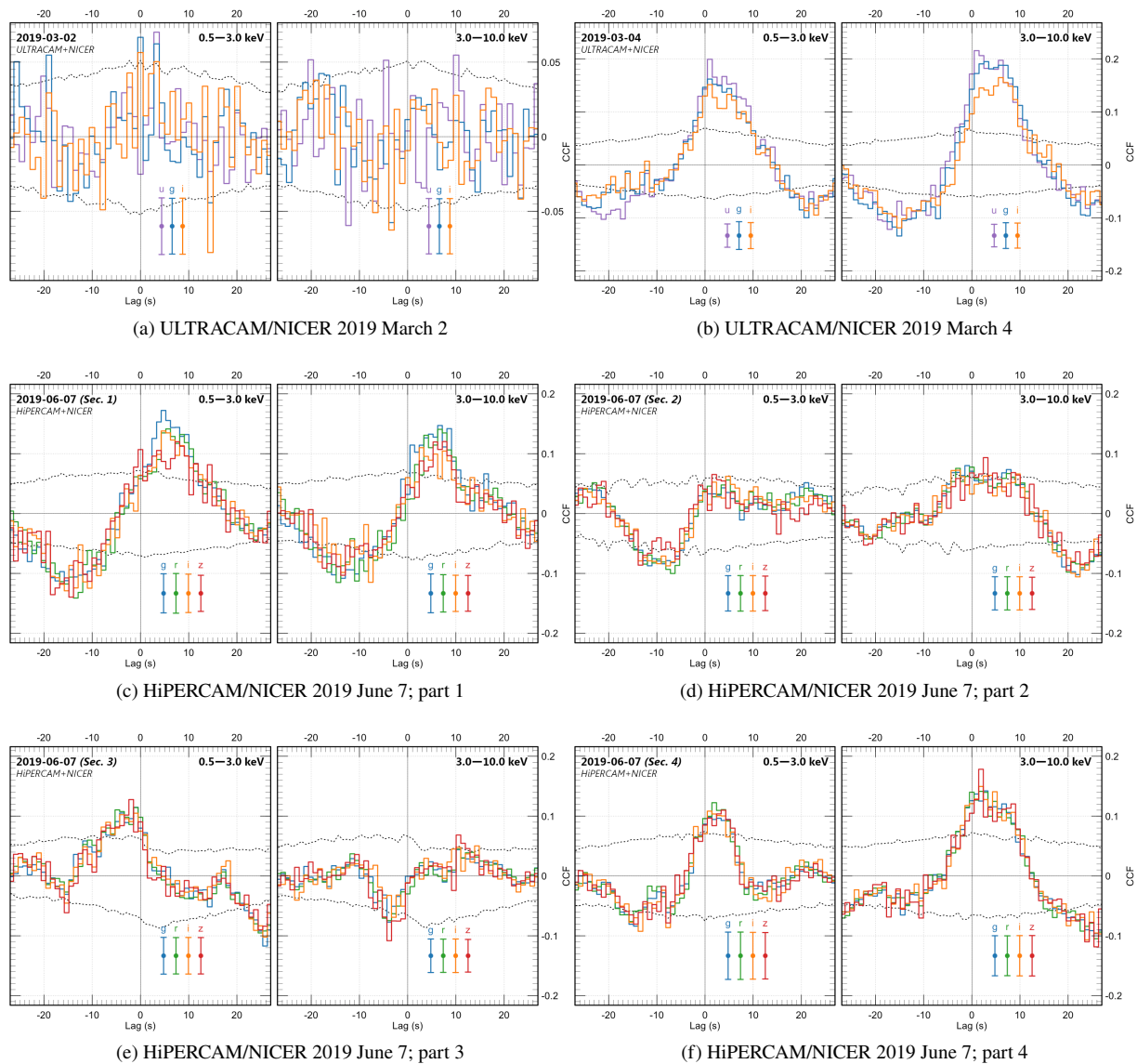
## 6.2 Spectral energy distribution

The radio–X-ray spectral energy distribution of the X-ray binary systems GX 339–4 (Gandhi et al. 2010), MAXI J1820+070 (Rodi et al. 2021) and GRS 1716–249 (Bassi et al. 2020), can be described by a combination of non-thermal emission of electrons accelerated in the jet by internal shocks (Malzac 2013, 2014) and

emission from the irradiated disc and hot corona (Gierliński et al. 2009). In Fig. 11 we show the absorption-corrected spectral energy distribution of Swift J1858.6–0814 observed on 2019 June 7 using  $N_{\text{H}} = 1.84 \times 10^{21} \text{ cm}^{-2}$ . The absorption-corrected NICER soft- and hard-band fluxes were determined using the XSPEC software package (Arnaud 1996) with the TBABS(DISKBB+BBODY) model with  $\Gamma = 1.6$ . The mean absorption-corrected optical ( $g_s$ ,  $r_s$ ,  $i_s$ ,  $z_s$ ) data were determined using the light curves in Section 2.3. There are not many radio measurements in 2019, so we interpolate the radio flux values at 1.4, 4.5, 15.5 GHz given in Rhodes et al. (2022), van den Eijnden et al. (2020) and Bright et al. (2018), respectively. From the mean optical ( $u_s - z_s$ ) and X-ray (0.5–10 keV) unabsorbed fluxes on 2019 June 7 we estimate luminosities of  $\sim 2.5 \times 10^{35} \text{ erg s}^{-1}$  and  $\sim 4.5 \times 10^{35} \text{ erg s}^{-1}$ , respectively, assuming a distance of 12.8 kpc (Buisson et al. 2020a). The optical to X-ray luminosity ratio  $L_{\text{opt}}/L_X$  ratio is  $\sim 0.6$ , which is much higher than what is typical of X-ray binaries in outburst. In neutron star X-ray binaries the optical and X-ray luminosity’s are described by  $L_{\text{OIR}} = 10^{10.8} L_X^{0.63}$ , where the optical luminosity is dominated by X-ray reprocessing with an additional contributions from a jet and the viscously heated accretion disc. (Russell et al. 2006). We find that either the optical luminosity in Swift J1858.6–0814 is a factor of  $\sim 140$  more than what is expected or that X-ray luminosity is a factor of  $\sim 2530$  under-luminous. Note that the 2019 June 7 observations were taken at orbital phase  $\sim 0.93$  and given the high binary inclination angle (Buisson et al. 2021; Knight et al. 2022) the low X-ray luminosity can be explained by optically thick material in the outer regions of the accretion disc or secondary star blocking most of the direct X-ray emission. So what we observe is scattered X-rays and the intrinsic X-rays is much higher. If we scale the X-rays using the  $L_{\text{OIR}} - L_X^{0.63}$  relation (Russell et al. 2006), we find that the radio–X-ray spectral energy distribution can be described with a power-law of the form  $F_\nu \propto \nu^\alpha$  with an index of  $\alpha \sim 0.16$ . Indeed, this is similar to what is observed in the mean spectrum of GX 339–4 (Gandhi et al. 2010) and XTE J1118+480 (Hynes et al. 2003), where the spectral energy distribution is attributed to a mixture of optically thin synchrotron emission from a jet and the irradiated accretion disc/corona.

## 6.3 Optical/X-ray correlations

In the optical waveband, many components can potentially contribute to the optical emission e.g. the irradiated secondary star, the cold optically-thick accretion disc, the hot optically-thin X-ray emitting medium and hot flow/jet (Poutanen & Veledina 2014). Whereas in the X-rays, two separate components are present, a soft component arising from Comptonization of disc photons and a harder component arising from synchrotron Comptonization in the hot flow (Veledina 2016). Indeed, this results in optical/X-ray correlations that show complex patterns, with both positive and negative correlations. The CCFs show a variety of shapes: some show positive correlations with optical photons lagging the X-rays, consistent with simple reprocessing (O’Brien et al. 2002; Hynes et al. 2009; Paice et al. 2018; Kajava et al. 2019); some show a very broad and nearly symmetric positive cross-correlation (Casella et al. 2010); some show a more complex structure containing a narrow ‘precognition’ dip at negative lags (optical photons leading X-rays) superimposed on a very broad positive cross-correlation (Kanbach et al. 2001; Gandhi et al. 2008; Durant et al. 2008, 2011; Lasso-Cabrera & Eikenberry 2013); and some show only a strong broad anti-correlation (Motch et al. 1983; Pahari et al. 2017) or a narrow positive correlation superimposed on a very broad positive cross-correlation (Hynes et al. 2019). Cyclo-synchrotron optical photons undergoing Compton upscatter-



**Figure 12.** The HiPERCAM/NICER CCFs. The left plot shows the CCF of the optical bands versus soft X-rays (0.5–3.0 keV) and the right plot shows the CCF of the optical bands versus hard X-rays (3.0–10.0 keV). The black dashed lines represent the 5 and 95 percent confidence intervals.

ing to X-rays in a hot flow can also reproduce both the observed optical/X-ray anti-correlation and QPOs (Veledina et al. 2011, 2013, 2015). In some cases the observed features can be explained by synchrotron emission from internal shocks within a relativistic compact jet (Malzac 2013; Hynes et al. 2019; Paice et al. 2019). Finally, in some sources a fast optical delay component at  $\sim 100$  ms is observed which is associated with the base of the optically-emitting jet close to the compact object (Gandhi et al. 2008, 2017; Paice et al. 2019).

Although there are some strong similarities in the timing behaviour of Swift J1858.6–0814 with well-studied XRBs, one notable difference is the lack of a  $\sim 100$  ms positive optical time lag with respect to X-rays. This feature has been seen in the cross-correlated timing behaviour of three sources now: GX 339–4 (Gandhi et al. 2008), V404 Cyg (Gandhi et al. 2017) and MAXIJ1820–070 (Paice et al. 2019). Both timing and multi-wavelength spectral properties support an origin of this feature in the inner jets of hard state binaries, in a compact region no larger than a few thousand Schwarzschild Radii. Malzac (2014) has shown that flicker noise Lorentz factor plasma

variations within a compact jet can naturally produce such timing lags. The fact that Swift J1858.6–0814 does *not* show this feature then implies some difference between its internal jet structure with respect to other systems. Whether this is related to a difference in jet plasma Lorentz factors during the state when it was observed, or perhaps even a difference in compact object types (all three systems named above host black holes whereas Swift J1858.6–0814 does not), remains to be investigated.

In the standard reprocessing model, X-rays arising from the inner accretion disc photoionize and heat the surrounding regions, which later recombine and cool producing lower energy (optical/near-IR) photons. The observed optical/near-IR flux is thus delayed relative to the X-rays due to the light travel time between the X-ray source and the reprocessing region. The corresponding CCF arising from X-ray reprocessing has a characteristic orbital phase-dependent shape, where the CCF rises from negative lags, peaks, and subsequently falls off (Hynes et al. 1998; O’Brien et al. 2002). Depending on the orbital phase the CCF can be very symmetric, but sometimes

an extended positive delay is observed, especially near quadrature (O’Brien et al. 2002; Hynes et al. 2009). The shapes of the CCFs observed in Swift J1858.6–0814 are more consistent with the shape of the CCFs in Sco X–1, Cyg X–2 (Durant et al. 2011), rather than other XRBs such as XTE J1118+480 (Kanbach et al. 2001), Swift J1753.5–0127 (Durant et al. 2008) and GX 339–4 (Gandhi et al. 2008) and MAXI J1820+70 (Paice et al. 2019), where ‘pre-recognition’ dips are observed and X-ray reprocessing is not thought to be dominant. The time delay between the optical/near-IR and X-ray flux can be up to twice the binary separation ( $a$ ) and can be obtained from Kepler’s third law:  $a/c = 9.77 M^{1/3} P_d^{2/3}$  s (where  $c$  is the speed of light,  $M$  is the sum of the binary masses in solar units and  $P_d$  is the orbital period in days). Although the binary parameters for Swift J1858.6–0814 are not fully known, the orbital period of 21.2 hr together with estimates of the binary masses allows one to estimate the binary separation to be  $a/c \sim 12$  s. Indeed, we observe CCFs with time delays of  $\sim 5$ –15 s which suggests that the delays are consistent with arising from regions in the accretion disc.

As mentioned earlier, in the hybrid hot inner flow model of Veledina (2016) two X-ray components, one arising from disc Comptonization and the other from synchrotron Comptonization, as well as two optical components due to synchrotron self-Compton emission from the hot inner accretion flow and disc reprocessing are present. In the X-rays, the seed photons for Comptonization are provided by the accretion disc (disc Comptonization) which dominates in the hard state. However, the hot flow itself also produces synchrotron radiation that can contribute or even dominate the seed photon flux for Comptonization (synchrotron Comptonization). In the optical, the flux can arise from X-ray reprocessing or from synchrotron emission in the hot inner accretion flow. An anti-correlation and negative lags between the optical and X-ray flux is expected because the increase in the mass accretion rate leads to an increased X-ray flux and a higher level of synchrotron self-absorption, leading to a drop in the optical emission (Veledina et al. 2011). Furthermore, the optical is expected to have a stronger anti-correlation with the hard X-rays compared to with the soft X-rays, characteristics that are expected if the source transitions from a hard to soft state. During the initial stages of the outburst of Swift J1858.6–0814 (in the hard state) we observe CCFs with a positive peak at a time delay of  $\sim 5$ –15 s and optical ACFs which are broader than the X-ray ACFs (see Fig. 8a,b). This implies some underlying connection between the optical and X-ray fluxes and is consistent with optical flux arising from X-ray reprocessing in the outer regions of the accretion disc. For example, the 2019 March 4 CCF shows a nearly symmetric positive correlations at positive lags which is consistent with X-ray reprocessing, supported by the wavelength dependant optical/X-ray delays in the CCFs, in which the longest wavelength delay has the longest delay. On the other hand, the 2019 June 7 data taken during a softer state cannot be described within the simple reprocessing scenario. The narrow optical ACF (comparable with the X-ray ACF) and the negative correlation in the optical/X-ray CCFs (see Fig. 8c–f) are the characteristics of the synchrotron self-Compton mechanism operating in a hot accretion flow (Veledina et al. 2011). The presence of both synchrotron and reprocessed X-ray emission in the optical is in line with the spectral energy distributions of the observed fast ‘red’ flares (see Section 4.2).

The CCFs of the 2019 June 7 parts 1 and 4 data have similar shapes, with anti-correlations at negative lags and positive correlation at positive lags. The shape can be explained by the presence of two emission components in the optical, with the X-rays being dominated by the synchrotron Comptonization continuum (Veledina et al. 2017). The CCF of the 2019 June 7 part 3 data shows a hint of positive correlation at negative lags. It looks very similar to the CCF

observed in MAXI J1820+070 (see epoch 6 in Paice et al. 2021). To explain this shape, one requires an additional source of X-ray photons arising from the disc Comptonization. Indeed, the hard-to-soft spectral state transition involves the motion of the cold accretion disc towards the compact object. As the role of the disc increases with the overall increase in the mass accretion rate, the power dissipated in the hot accretion flow increases, so the whole spectrum of this component increases (similar to ADAFs) resulting in the enhancement of the synchrotron emission. The simultaneous presence of two X-ray components, synchrotron Comptonization and disc Comptonization, leads to the complex shape of the optical/X-ray CCF and manifests itself through the different correlations with the soft and hard X-ray bands.

To investigate this possibility further, we separate the X-ray range into soft (0.5–3.0 keV) and hard (3.0–10.0 keV) energy bands and show the CCFs with respect to only one optical band ( $g_s$ ) for clarity (see Fig. 12). We systematically observe different correlations between the optical and soft/hard-X-rays, supporting the assumption of two X-ray components. In Appendix B we attempt to reproduce the timing and correlation properties observed in Swift J1858.6–0814 in the context of the hot inner flow-disc Comptonization and reprocessing model (Veledina et al. 2011; Veledina 2018). The low absolute value of the optical/X-ray coherence of  $\sim 0.1$ –0.2 means that multiple components are required to explain the broad-band variability. We clearly observe correlations between some optical and X-ray flares which shows that they are indeed related, some flares events have weak correlations and so may not be related. In general, we find good qualitative agreement between the data and the multi-component hot inner flow-disc Comptonization and reprocessing model, and find that the relative role of the different X-ray and optical components vary during the course of the outburst as well as on shorter time-scales.

## 7 CONCLUSIONS

We present a rapid timing analysis of simultaneous optical (HiPER-CAM and ULTRACAM) and X-ray (NICER) observations of the X-ray transient Swift J1858.6–0814 during 2018 and 2019. The optical light curves show rapid, small amplitude ( $\sim 0.1$  mag in  $g_s$ ) ‘red’ flares (i.e. stronger at longer wavelengths) on time-scales of  $\sim$ seconds which have a power-law index consistent with optically thin synchrotron emission. The optical light curves also show relatively slow, large amplitude ( $\sim 1$  mag in  $g_s$ ) ‘blue’ flares (i.e. stronger at shorter wavelengths) on time-scales of  $\sim$ minutes, with a spectral energy distribution consistent with X-ray reprocessing in the accretion disc.

We present a Fourier time- and energy-dependant timing analysis of the simultaneous optical/X-ray light curves. The simultaneous optical and X-ray data show correlated variability that has a strong hard-energy component on 2019 March 2 and 4, and a strong soft-energy X-ray component on 2019 June 7, suggesting a spectral state change. We find that the optical ACF is broader than the X-ray ACF during the initial outburst stages, which can be explained by simple X-ray reprocessing. The coherence function shows a linear decline with increasing frequency. There is also a plateau in the time lags between 0.01–0.1 Hz at  $\sim 10$  s. These characteristics can be attributed to thermal reprocessing of X-ray emission in the outer regions of the accretion disc.

We find that relative roles of the different X-ray and optical components governs the shape of the optical/X-ray CCFs and vary on shorter time-scales. The CCFs of the simultaneous optical versus soft- and hard-band X-ray light curves show time- and energy de-

pendent correlations. The 2019 March 4 and 2019 June parts 1 and 4 CCFs show a nearly symmetric positive correlations at positive lags consistent with simple X-ray disc reprocessing. The soft- and hard-band CCFs are similar and can be reproduced if disc reprocessing dominates in the optical and one component (disc or synchrotron Comptonization) dominates both the soft and hard X-rays. The 2019 June 7 part 3 data obtained between parts 1 and 4, shows a very different CCFs. The observed positive correlation at negative lags in the soft X-ray band can be reproduced if the optical synchrotron emission is correlated with the hot flow X-ray emission. The observed timing properties are in qualitative agreement with the inner hot accretion flow model, where X-rays are produced by both synchrotron and disc Comptonization and the optical emission arises from the hot flow synchrotron and irradiated disc components.

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*Facilities:* GTC (HiPERCAM), NTT (ULTRACAM), NICER

## DATA AVAILABILITY

The ULTRACAM and HiPERCAM data can be obtained by contacting the ULTRACAM team. The NICER data are available in the HEASARC Data Archive (<https://heasarc.gsfc.nasa.gov/docs/archive.html>). The data used in this paper will be shared on reasonable request to the corresponding author.

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## Appendices

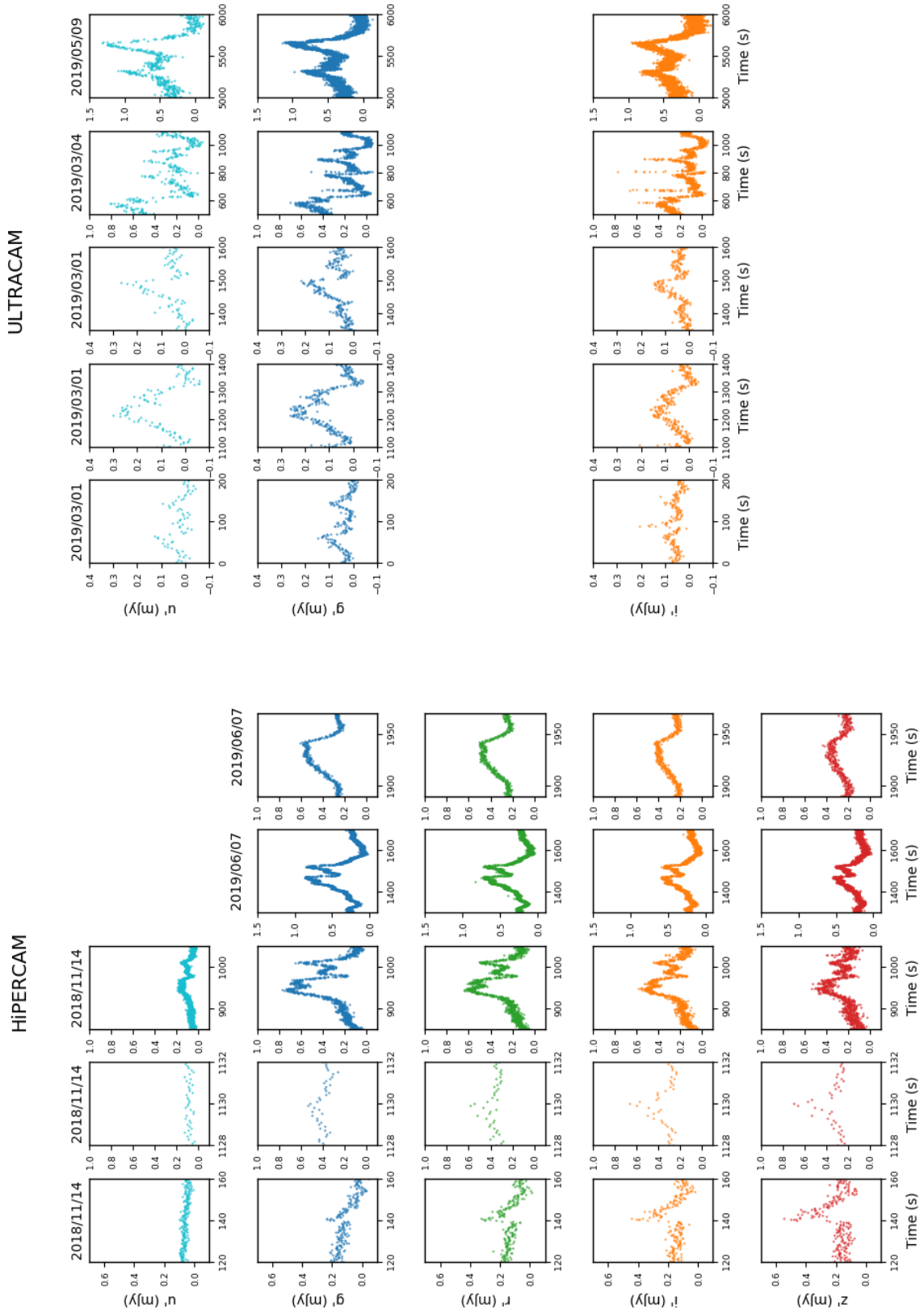
### APPENDIX A: OPTICAL LIGHT CURVES PROPERTIES

In Fig. A1 we show examples of the HiPERCAM and ULTRACAM small and large flare events. As one can see, flares on different time-scale, amplitudes and colour are present. We also show examples of fits to the broad-band dereddened spectral energy distribution of the observed flaring events (see Fig. A2).

### APPENDIX B: MODELLING THE TIMING PROPERTIES IN THE CONTEXT OF THE HYBRID HOT INNER FLOW MODEL

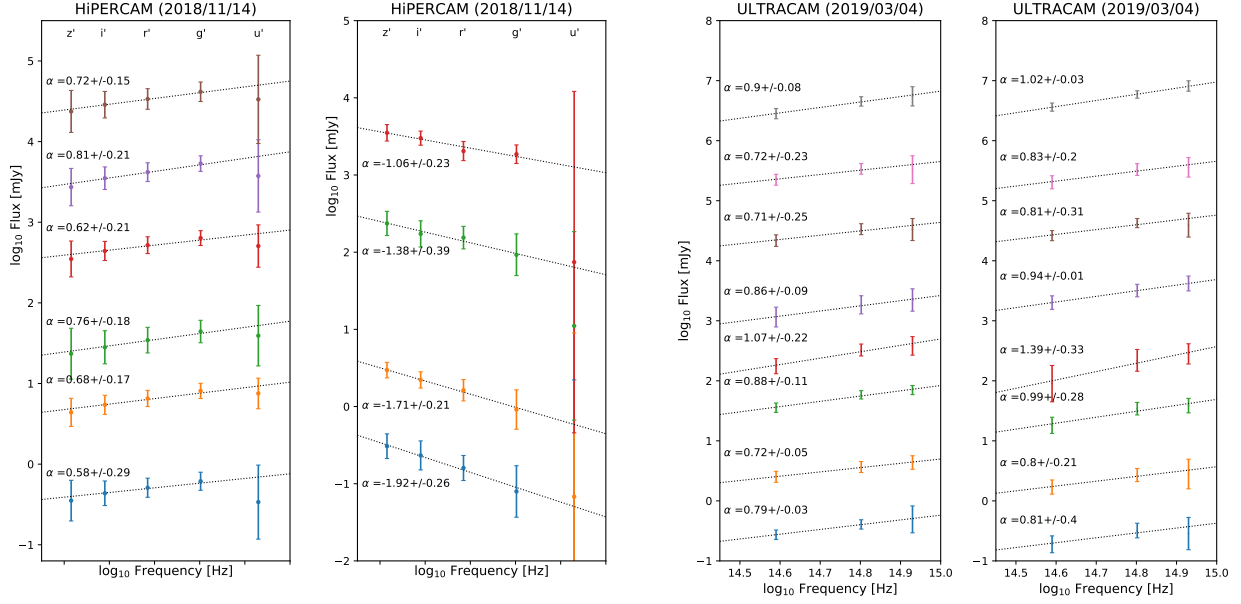
The observed complex shape of the CCFs can be explained via an interplay between different optical emission components, namely, reprocessing in the accretion disc, synchrotron emission from the jet and emission from the hot inner accretion flow (see e.g. Veledina et al. 2013; Malzac et al. 2018; Paice et al. 2021). The systematically different correlations of the optical/hard X-rays versus optical/soft X-rays indicate the presence of at least two sources of X-ray photons, one dominating at soft energies and the other dominating at hard energies. Indeed, studies of the broad-band spectral and timing properties of many black hole X-ray binaries reveal several emission components in the X-rays. A standard and irradiated accretion disc dominates the soft X-rays, as demonstrated by the covariance spectra and the soft X-ray time lags (see e.g. Uttley et al. 2011; Cassatella et al. 2012; De Marco et al. 2015, 2021); a disc Comptonization and/or synchrotron Comptonization components stratified in a hot medium contribute to the hard X-rays, as shown by the hard X-ray time lags (see e.g. Kotov et al. 2001; Veledina et al. 2013; Mahmoud & Done 2018), as well as a complex reflection feature appearing at hard X-ray energies, studied via frequency-resolved spectroscopy and reverberation lags (Revnivtsev et al. 1999; Fabian & Ross 2010; Uttley et al. 2014; Axelsson & Veledina 2021). When the different components contribute approximately equally, the interplay between these components is observed in terms of complex shapes in the X-ray power spectra and the cross-correlation function between the optical and X-ray bands (Veledina 2016, 2018).

To reproduce the shapes of the observed CCFs in Swift J1858.6–0814, we investigate the scenario of the simultaneous presence of two X-ray components, one arising from disc Comptonization and the other from synchrotron Comptonization, as well as two optical components due to synchrotron emission from the hot inner accretion flow and disc reprocessing. The variability of both components are caused by accretion rate fluctuations (Lyubarskii 1997) and the power spectra are modelled through zero-centered Lorentzian functions. The accretion disc is assumed to be truncated at some radius away from the compact object. The synchrotron Comptonization continuum is assumed to be delayed with respect to the disc Compton-



**Figure A1.** Examples of the HiPERCAM (left) and ULTRACAM (right) small and large flare events.





**Figure A2.** Examples of the broad-band dereddened spectral energy distribution of the flaring events observed in Swift J1858.6–0814. The dotted lines show a power-law fit to the data of the form  $F_\nu \propto \nu^\alpha$ . The left panel shows the HiPERCAM data taken on 2018 November 14 and the right panel shows the ULTRACAM data taken 2019 May 9.

ization by the time it takes the fluctuations to propagate from the radius of truncated disc to the place where the synchrotron is effectively Comptonized. The spectral shape of the synchrotron and disc Comptonization emission change under the changing mass accretion rate with two major patterns: (i) an increase and decrease in flux with a constant spectral slope and (ii) spectral pivoting. Depending on the relative amplitudes of these variations, the number of photons in a given X-ray band may correlate or anti-correlate with the mass accretion rate fluctuations. This can be parameterised through the simple relation

$$x_h(t) = \varepsilon_h \dot{m}(t + t_0) * g(t) + \dot{m}(t) \quad (\text{B1})$$

$$x_s(t) = \varepsilon_s \dot{m}(t + t_0) * g(t) + \dot{m}(t), \quad (\text{B2})$$

where  $x_h(t)$  and  $x_s(t)$  are the hard- and soft X-ray light curves, respectively,  $\dot{m}$  is the mass accretion rate,  $t_0$  is the time delay and  $g(t)$  is the low-pass filter (see [Veledina 2018](#), for further details). The variables  $\varepsilon_h$  and  $\varepsilon_s$  parameterise the contribution of the disc and synchrotron Comptonization components, and their signs indicate the correlation (plus) or anti-correlation (minus) with the accretion rate fluctuations. The optical light curve is given by

$$o(t) = -\dot{m}(t) + \varepsilon_{ds} x_s(t) * r(t), \quad (\text{B3})$$

where the first term gives the synchrotron contribution and  $r(t)$  is the disc response function whose contribution is parameterised by  $\varepsilon_{ds}$  ([Veledina et al. 2011](#)). An implicit parameter of the model is the assumed shape of the accretion rate power spectrum, which greatly affects the exact shape (and width) of the features in the CCF. We take a single zero-centered Lorentzian for each model. The resulting soft- and hard-band CCFs are shown in Figure B1.

We do not attempt to fit the 2019 March 2 and 2019 June 7 part 2 observations because the CCFs are at the noise level. However, the 2019 March 4 and 2019 June parts 1 and 4 CCFs show a nearly symmetric positive correlations at positive lags consistent with simple

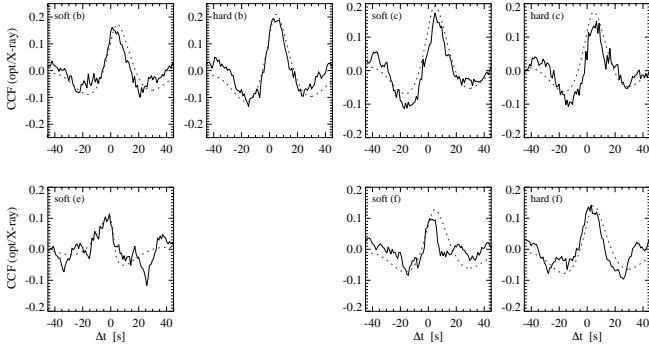
X-ray disc reprocessing. The soft- and hard-band CCFs from 2019 March 4, June 7 parts 1 and 4 are similar in shape indicating that one component dominates both the soft and hard X-rays. These CCFs can be reproduced if disc reprocessing dominates in the optical ( $\varepsilon_{ds} = 3$ ) and when Comptonization of either synchrotron or disc photons dominate in the X-rays. We find that the resulting CCFs (Fig. B1a) can be reproduced with both  $\varepsilon_h = \varepsilon_s \gg 1$  and  $\varepsilon_h = \varepsilon_s \ll 1$ , hence the data do not allow us to distinguish between these components. We assume  $\varepsilon_h = \varepsilon_s = 0.01$ .

We note that the 2019 June 7 part 3 data was observed between parts 1 and 4 in time, but shows a very different soft- and hard- X-ray CCF. It shows a positive correlations at negative lag in the soft-band, while in the hard X-ray band the correlation amplitudes are not significant. To reproduce the positive correlation at negative lags we consider an alternative scenario where the optical synchrotron emission is correlated with the hot flow X-ray emission, which translates to the formal description

$$o(t) = \dot{m}(t) + \varepsilon_{ds} x_s(t) * r(t). \quad (\text{B4})$$

This corresponds to the case when the fluctuations in the magnetic field (as response to the mass accretion rate variations) dominates the fluctuations in the number density and the emission in the optical band falls below the synchrotron self-absorption frequency (see Fig. 1b of [Poutanen & Vurm 2009](#)). The resulting CCF is shown in Fig. B1e and is obtained assuming the parameters ( $\varepsilon_{ds}$ ,  $\varepsilon_s$ ) to be (0, -0.8), i.e. assuming contribution of the synchrotron alone to the optical band. The parameter  $\varepsilon_h$  is not constrained, as the hard-band CCF does not show any significant correlations. The parameter  $t_0$  mildly affects the fit; we assume  $t_0 = 4$ .

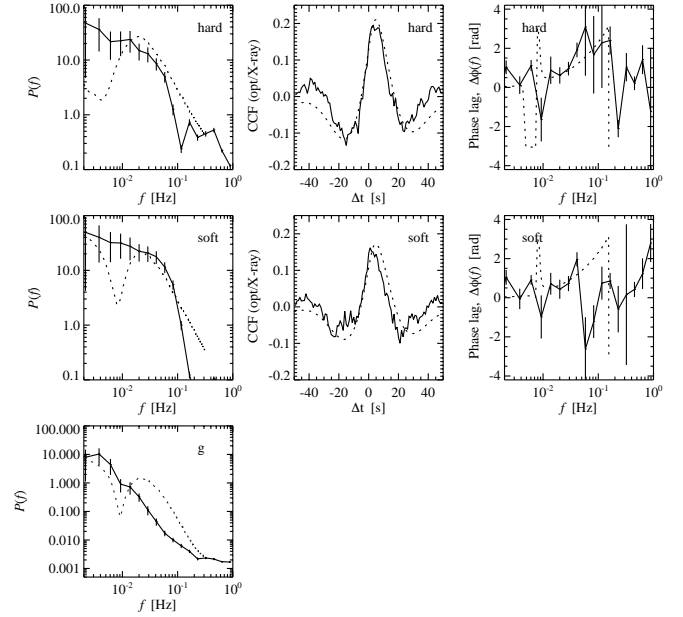
Overall, we see a general trend in the short-term variability. In the 2019 March and parts 1 and 4 of the June data, we find the optical flux is dominated by a reprocessing component (with possible minor contribution from the hot flow synchrotron emission), and the X-rays are also dominated by one component – either synchrotron- or disc



**Figure B1.** We show the ULTRACAM or HiPERCAM optical versus NICER X-ray CCFs. The optical ( $g_s$ -band) versus soft (0.5–3.0 keV) and hard X-rays (3.0–10.0 keV) are shown. We only show the data where the CCFs are significantly above the noise level. The data taken on 2019 March 4 (b), 2019 June 7 parts 1 (c), 3 (e) and 4 (f) are shown. The solid line shows the data whereas the dashed line shows the hybrid hot inner flow model.

Comptonization. For the 2019 June 7 part 3 data we see an indication of a positive correlation at negative lags in the optical/soft-band X-ray CCF (see Fig. 12e). The lack of a significant correlation in the optical/hard X-rays may be explained by the competing role of two anti-correlated spectral components in the X-rays, which we attribute to disc and synchrotron Comptonization. We find that the role of synchrotron emission in the optical band increases. This scenario can also explain the changing width of the ACFs. The 2019 March 4 data taken during the hard state have optical ACFs that are broader than the X-ray ACFs, consistent with X-ray reprocessing. The soft- and hard-band X-ray CCFs are similar implying that a single component dominates the X-rays. In contrast, the 2019 June part 3 data has a strong soft X-ray component with comparable optical and X-ray ACFs. This is indicative of the interplay between two anti-correlating components. The optical/soft- and optical/hard X-ray CCFs are very different reflecting the comparable role of disc Comptonization and synchrotron Comptonization.

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**Figure B2.** We show the power spectrum, CCF and phase lags for the 2019 March 4 (b) data (solid line) with the corresponding hybrid hot inner flow model (dashed line).