

Software Toolbox



# ACID: A comprehensive toolbox for image processing and modeling of brain, spinal cord, and ex vivo diffusion MRI data

Gergely David<sup>a,b,\*</sup>, Björn Fricke<sup>a,c,\*</sup>, Jan Malte Oeschger<sup>a,c</sup>, Lars Ruthotto<sup>d</sup>, Francisco J. Fritz<sup>a,c</sup>, Ora Ohana<sup>e</sup>, Laurin Mordhorsta.c, Thomas Sauvigny', Patrick Freundb.g.h, Karsten Tabelowi, Siawoosh Mohammadia.c.h.j

a Department of Systems Neuroscience, University Medical Center Hamburg-Eppendorf, Hamburg, Germany

**bSpinal Cord Injury Center, Balgrist University Hospital, University of Zurich, Zurich, Switzerland** 

c Department of Neuroradiology, University of Lübeck, Lübeck, Germany

dDepartment of Mathematics, Emory University, Atlanta, GA, United States

e Center for Molecular Neurobiology Hamburg, University Medical Center Hamburg-Eppendorf, Hamburg, Germany

f Department of Neurosurgery, University Medical Center Hamburg-Eppendorf, Hamburg, Germany

gWellcome Trust Centre for Human Neuroimaging, UCL Queen Square Institute of Neurology, University College London, London, United Kingdom

hDepartment of Neurophysics, Max Planck Institute for Human Cognitive and Brain Sciences, Leipzig, Germany

i Weierstrass Institute for Applied Analysis and Stochastics, Berlin, Germany

j Max Planck Research Group MR Physics, Max Planck Institute for Human Development, Berlin, Germany

\*Shared first authors

Corresponding Author: Siawoosh Mohammadi ([mohammadi@mpib-berlin.mpg.de](mailto:mohammadi@mpib-berlin.mpg.de))

#### ABSTRACT

Diffusion MRI (dMRI) has become a crucial imaging technique in the field of neuroscience, with a growing number of clinical applications. Although most studies still focus on the brain, there is a growing interest in utilizing dMRI to investigate the healthy or injured spinal cord. The past decade has also seen the development of biophysical models that link MR-based diffusion measures to underlying microscopic tissue characteristics, which necessitates validation through ex vivo dMRI measurements. Building upon 13 years of research and development, we present an opensource, MATLAB-based academic software toolkit dubbed ACID: A Comprehensive Toolbox for Image Processing and Modeling of Brain, Spinal Cord, and Ex Vivo Diffusion MRI Data. ACID is an extension to the Statistical Parametric Mapping (SPM) software, designed to process and model dMRI data of the brain, spinal cord, and ex vivo specimens by incorporating state-of-the-art artifact correction tools, diffusion and kurtosis tensor imaging, and biophysical models that enable the estimation of microstructural properties in white matter. Additionally, the software includes an array of linear and nonlinear fitting algorithms for accurate diffusion parameter estimation. By adhering to the Brain Imaging Data Structure (BIDS) data organization principles, ACID facilitates standardized analysis, ensures compatibility with other BIDS-compliant software, and aligns with the growing availability of large databases utilizing the BIDS format. Furthermore, being integrated into the popular SPM framework, ACID benefits from a wide range of segmentation, spatial processing, and statistical analysis tools as well as a large and growing number of SPM extensions. As such, this comprehensive toolbox covers the entire processing chain from raw DICOM data to group-level statistics, all within a single software package.

Keywords: diffusion MRI, brain and spinal cord, SPM12, artifact correction, biophysical modeling, BIDS

Received: 9 February 2024 Revision: 12 July 2024 Accepted: 14 August 2024 Available Online: 29 August 2024

## 1. INTRODUCTION

Diffusion MRI (dMRI) exploits the self-diffusion of water molecules to produce images that are sensitive to tissue microstructure by measuring the diffusion along various spatial directions ([Callaghan et al., 1988](#page-19-0); [Le Bihan et al.,](#page-21-0) [1988](#page-21-0); [Stejskal & Tanner, 1965\)](#page-23-0). dMRI has been applied to study a number of phenomena including normal brain development ([Dubois et al., 2014;](#page-20-0) [Miller et al., 2002\)](#page-22-0), aging ([Draganski et al., 2011;](#page-20-1) [Sullivan et al., 2010\)](#page-23-1), training-induced plasticity [\(Scholz et al., 2009\)](#page-23-2), and monitoring progression of and recovery from neurological diseases ([Farbota et al., 2012;](#page-20-2) [Meinzer et al., 2010](#page-22-1)). Clinical applications of dMRI include the diagnosis of ischemic stroke ([Urbach et al., 2000](#page-24-0)), multiple sclerosis [\(Horsfield](#page-21-1) [et al., 1996](#page-21-1)), cancer and metastases [\(Gerstner &](#page-21-2) [Sorensen, 2011\)](#page-21-2), and surgical planning of brain tumors [\(Chun et al., 2005](#page-19-1)). Although the vast majority of dMRI applications has focused on the brain, there is a growing interest in spinal cord dMRI, as researchers seek sensitive and predictive markers of spinal cord white matter damage ([Cohen et al., 2017](#page-20-3); [Martin et al., 2016\)](#page-22-2). Furthermore, an increasing number of studies utilize dMRI on ex vivo specimens for comparative analysis with other imaging modalities, such as electron microscopy [\(Barazany](#page-19-2) [et al., 2009](#page-19-2); [Kelm et al., 2016;](#page-21-3) [Papazoglou et al., 2024\)](#page-22-3).

To fully utilize the sensitivity of dMRI to tissue microstructure, expert knowledge is required to minimize artifacts both during acquisition, for example, by cardiac gating or twice-refocused spin-echo sequences, and through dedicated retrospective correction methods. Commonly used retrospective correction techniques include motion and eddy-current correction [\(J. L. R.](#page-19-3) [Andersson & Sotiropoulos, 2016](#page-19-3); [Mohammadi et al.,](#page-22-4) [2010](#page-22-4)), susceptibility distortion correction [\(Gu & Eklund,](#page-21-4)  [2019](#page-21-4); [Ruthotto et al., 2012\)](#page-23-3), denoising ([Becker et al.,](#page-19-4)  [2014](#page-19-4); [Veraart et al., 2016\)](#page-24-1), Rician bias correction [\(Oeschger et al., 2023a;](#page-22-5) [Sijbers et al., 1998\)](#page-23-4), and robust tensor fitting techniques ([Chang et al., 2005;](#page-19-5) [Mohammadi,](#page-22-6) [Freund, et al., 2013](#page-22-6)). Retrospective artifact correction techniques, along with diffusion signal modeling capabilities, are widely available in open-source toolboxes such as FSL-FDT [\(Smith et al., 2004\)](#page-23-5), DiPY [\(Garyfallidis et al.,](#page-20-4) [2014](#page-20-4)), DESIGNER ([Ades-Aron et al., 2018](#page-19-6)), ExploreDTI [\(Leemans et al., 2009](#page-21-5)), MRtrix3 ([Tournier et al., 2019\)](#page-24-2), TORTOISE ([Pierpaoli et al., 2010\)](#page-22-7), AFNI-FATCAT ([Taylor &](#page-23-6) [Saad, 2013](#page-23-6)), and others.

While the majority of toolboxes have been designed for brain dMRI, ACID has introduced several features and utilities that make it particularly suitable for spinal cord and ex vivo dMRI as well. Specifically, ACID addresses the higher level and different nature of artifacts in spinal cord dMRI [\(Barker, 2001](#page-19-7); [Stroman et al., 2014\)](#page-23-7), and the

highly variable geometry and diffusion properties in ex vivo dMRI (see Sé[bille et al., 2019](#page-23-8) for a list of ex vivo/ postmortem dMRI studies). Although there are some software options available for processing spinal cord images, most notably the Spinal Cord Toolbox [\(De Leener](#page-20-5)  [et al., 2017\)](#page-20-5), these tools lack comprehensive artifact correction and biophysical modeling capabilities for estimation of dMRI-based metrics related to microscopic tissue properties. Biophysical modeling estimates microstructural properties, such as axonal water fraction and orientation dispersion, as aggregated measures on the voxel level, providing greater specificity than standard diffusion tensor (DTI) or diffusion kurtosis imaging (DKI). Toolboxes dedicated for biophysical modeling of the dMRI signal, such as the NODDI [\(Zhang et al., 2012](#page-24-3)) or SMI toolbox [\(Coelho et al., 2022](#page-19-8)), typically do not include a comprehensive processing pipeline to correct for artifacts in dMRI data. In addition, to date, only a few of the dMRI toolboxes support the Brain Imaging Data Structure (BIDS; [Gorgolewski et al., 2016\)](#page-21-6) standard for organizing and annotating raw and processed dMRI data. The lack of standardization not only complicates the sharing and aggregation of processed dMRI data but also the application of automated image analysis tools designed for big data, such as machine learning techniques. Over the past two decades, tens of thousands of dMRI datasets have been made openly available in large neuroimaging databases (e.g., HCP ([Van Essen et al., 2013\)](#page-24-4) and the UK Biobank [\(Littlejohns et al., 2020\)](#page-21-7)), underscoring the importance of consistent data storage practices.

Building upon 13 years of research and development, we introduce an open-source MATLAB-based extension to the Statistical Parametric Mapping (SPM) software, the ACID toolbox: A Comprehensive Toolbox for Image Processing and Modeling of Brain, Spinal Cord, and Ex Vivo Diffusion MRI Data. ACID was initially developed as a collection of artifact correction tools but has now been extended to a comprehensive toolbox for processing and modeling of dMRI data. In particular, ACID offers (i) stateof-the-art image processing tools as well as (ii) DTI, DKI, and white matter biophysical model parameter estimation methods optimized for brain, spinal cord, and ex vivo dMRI data. Additionally, (iii) ACID adheres to the BIDS standard for organizing the output, making the processed images compliant with other BIDS software and facilitating data sharing. Finally, (iv) ACID is embedded in the SPM framework to benefit from its established functions including spatial processing tools and statistical inference schemes. ACID tools can be combined with other SPM functions to create pipelines in the SPM batch system, which offers an all-in-one software solution from conversion of DICOM data to statistical group analysis. ACID also benefits from a large and growing number of SPM

Method	Publication
ECMOCO:	Mohammadi et al. (2010);
Eddy-current and	Mohammadi, Freund, et al. (2013);
motion correction	Mohammadi, Tabelow, et al. (2015)
HySCO: Susceptibility	Macdonald and Ruthotto (2018);
artifact correction	Ruthotto et al. (2012, 2013)
HySCO: Combine	Clark et al. (2021)
blip-up and blip-down	
msPOAS: Adaptive	Becker et al. (2014); Tabelow et al.
denoising	(2015)
RBC: Rician bias	Oeschger et al. (2023a)
correction	
DTI using robust	Mohammadi, Freund, et al. (2013)
fitting	
DKI and axisymmetric	Oeschger et al. (2023a, 2023b)
DKI using NLLS	
NODDI-DTI	Edwards et al. (2017)
WMTI-Watson	Oeschger et al. (2023b)*
Reliability masking	David et al. (2017)

<span id="page-2-0"></span>Table 1. Peer-reviewed methods used in the ACID toolbox.

DKI, diffusion kurtosis imaging; DTI, diffusion tensor imaging; NLLS, nonlinear least squares; NODDI, neurite orientation dispersion and density imaging; WMTI, white matter tract integrity. \*The ACID implementation is based on the method introduced by [Jespersen et al. \(2018\).](#page-21-10)

extensions. For example, ACID can be combined with the SPM12-based hMRI toolbox [\(Tabelow et al., 2019](#page-23-9)) to perform multicontrast analysis of dMRI and other quantitative MRI data, such as relaxation rates, acquired from the same subject, all within a single pipeline. Many of the methods used in the ACID toolbox have already been published in the scientific dMRI literature ([Table 1\)](#page-2-0). In this paper, we detail the design and function of the ACID modules and provide guidance on their optimal combination for brain, spinal cord, and ex vivo applications.

#### 2. METHODS

## 2.1. Overview

The ACID toolbox is a comprehensive toolbox for processing and analyzing dMRI data, built upon the following four pillars: (1) preprocessing of dMRI data (*Pre-processing* module), (2) physical models of the diffusion signal (*Diffusion tensor/kurtosis imaging* module), (3) white matter biophysical models of the diffusion signal (*Biophysical models* module), and (4) additional features referred to as *Utilities*. The *Pre-processing* module consists of state-ofthe-art methods for retrospective correction of the dMRI data. The *Diffusion tensor/kurtosis imaging* module contains tensor and kurtosis models that can be applied to dMRI data from various tissues or samples, including gray and white matter, as well as diffusion phantoms [\(Woletz et al., 2024\)](#page-24-5). In contrast, the *Biophysical models* module can only be applied to samples that fall within

their validity ranges (see [Section 4.2.2\)](#page-14-0). The *Utilities* module contains various useful tools, including masking and noise estimation. The ACID toolbox follows the BIDS convention and enables the seamless integration of external tools into its processing pipeline in a modular fashion (*External tools* module). More details about the implementation and organization of ACID are provided in [Appendix A](#page-24-6).

#### 2.2. Preprocessing

In this section, we provide brief descriptions of each artifact correction tool currently implemented in ACID. For detailed recommendations on various dMRI datasets (in vivo brain, in vivo spinal cord, ex vivo/postmortem), refer to Sections [3.2](#page-9-0) and [4.1](#page-12-0), as well as [Table 5](#page-11-0).

# <span id="page-2-1"></span>*2.2.1. Eddy-current and motion correction (ECMOCO)*

ACID uses the eddy-current and motion correction (ECMOCO) algorithm [\(Mohammadi et al., 2010\)](#page-22-4) to correct for spatial misalignments that may occur between dMRI volumes. These misalignments can be caused by motion and eddy currents induced by the rapidly varying field of the diffusion-sensitizing gradients ([Jezzard et al., 1998\)](#page-21-8), which may lead to biased diffusion estimates [\(Mohammadi,](#page-22-6)  [Freund, et al., 2013](#page-22-6)). ECMOCO aligns all source volumes to a target volume using a coregistration algorithm with an affine transformation [\(Friston & Ashburner, 1997](#page-20-6)) implemented in the SPM function *spm\_coreg*. It was previously shown that the robustness of registration can be increased by separately registering diffusion-weighted (DW) and nondiffusion-weighted (b0) volumes to their corresponding target volumes [\(Mohammadi, Carey, et al., 2015\)](#page-22-8). ECMOCO features the multitarget registration mode, where source volumes from each diffusion shell (b-value) are coregistered to their shell-specific target volume [\(Appendix Fig. B1\)](#page-26-0). ECMOCO rotates the b-vectors by the obtained rotational parameters; these rotated b-vectors can be passed on to subsequent processing steps. Of note, the affine transformation of ECMOCO can only correct for first-order eddy-current displacements. The advantages and disadvantages of ECMOCO compared with other established tools, such as FSL eddy, are discussed in [Section 4.1](#page-12-0).

In spinal cord dMRI, eddy-current and motion correction is more challenging than in brain dMRI due to the considerably lower number of voxels and lower signalto-noise ratio (SNR), particularly in volumes with high b-values (>1000 s/mm2) or with diffusion-sensitizing gradients parallel to the spinal cord. While movement of the brain can be considered approximately rigid, the spinal

cord may experience varying degrees of displacement along the rostrocaudal axis caused by factors such as breathing, pulsation of the cerebrospinal fluid, or swallowing ([Yiannakas et al., 2012\)](#page-24-7). To address this, we introduced *slice-wise* (2D) registration, which independently aligns each slice of the source volume to the corresponding slice of the target volume, thereby correcting for nonrigid, slice-dependent displacements [\(Mohammadi, Freund,](#page-22-6) [et al., 2013\)](#page-22-6). For more details on ECMOCO, including other recently introduced features (*initialized registration* and *exclusion mode*), refer to [Appendix B](#page-25-0).

#### <span id="page-3-0"></span>*2.2.2. Adaptive denoising (msPOAS)*

The Multi-shell Position-Orientation Adaptive Smoothing (msPOAS) is an iterative adaptive denoising algorithm designed to adaptively reduce noise-induced variance in dMRI data while preserving tissue boundaries, as illustrated in [Figure 3](#page-10-0) [\(Becker et al., 2012,](#page-19-10) [2014;](#page-19-4) [Tabelow](#page-23-11) [et al., 2015](#page-23-11)). The algorithm adapts to the intensity values and their distance in both voxel space and the spherical space of diffusion directions, allowing smoothing only within spatially homogeneous areas of the DW images. One of the key advantages of msPOAS is its compatibility with all diffusion models as it operates on the raw dMRI data. Adjustable parameters include *kstar* (number of iterations that define the image smoothness), *lambda* (adaptation parameter that defines the strength of edge detection), *kappa* (initial ratio of the amount of smoothing between the local space of neighboring voxels and the spherical space of diffusion gradients), and *ncoils* (the effective number of receiver coils that contributed to the measured signal). To distinguish random fluctuations from structural differences, msPOAS requires an estimate of SNR, or equivalently the noise standard deviation (*sigma*). A higher *kstar* leads to greater smoothness within homogeneous image regions, while a larger *lambda* results in weaker adaptation and more blurring at tissue edges. The optimal *kappa* depends on the number of directions per shell, while *ncoils* should be the same as the value used for noise estimation. When using msPOAS, we recommend starting with the default parameters and the *sigma* estimated with the *Noise estimation* utility function ([Table 2](#page-4-0)). In case of insufficient noise reduction, parameters should be adjusted according to [Appendix D](#page-27-0).

#### <span id="page-3-1"></span>*2.2.3. Rician bias correction*

The voxel intensities of MRI magnitude images exhibit a Rician distribution in case of a single receiver coil [\(Gudbjartsson & Patz, 1995\)](#page-21-11) and a noncentral  $\chi$  distribution in case of multiple receiver coils (Aja-Ferná[ndez et al.,](#page-19-11) [2014\)](#page-19-11). When fitting diffusion signal models ([Section 2.3\)](#page-5-0), this distribution leads to a bias, known as the Rician bias, in the estimated tensor ([Basser & Pajevic, 2000](#page-19-12); [Gudbjartsson & Patz, 1995;](#page-21-11) [Jones & Basser, 2004\)](#page-21-12) and kurtosis parameters [\(Veraart et al., 2011;](#page-24-8) [Veraart, Rajan,](#page-24-9) [et al., 2013](#page-24-9)), as well as in biophysical parameter estimates [\(M. Andersson et al., 2022;](#page-19-13) [Fan et al., 2020](#page-20-9); [Howard et al., 2022\)](#page-21-13). This Rician bias is particularly relevant in low SNR situations [\(Polzehl & Tabelow, 2016\)](#page-23-12). Two approaches of Rician bias correction (RBC) are implemented in ACID. The M2 approach, introduced in [Miller &](#page-22-11)  [Joseph \(1993\)](#page-22-11), and later extended to multichannel receiver coil (André [et al., 2014\)](#page-19-14), operates on the dMRI data and uses the second moment of the noncentral  $\chi$ distribution of the measured intensities and noise estimates to estimate the true voxel intensities. The second approach modifies the parameter estimation by considering the noncentral  $\chi$  distribution to account for the Rician bias during model fitting [\(Oeschger et al., 2023a\)](#page-22-5). Note that the latter approach assumes uncorrected data, therefore, it must not be combined with the first method and is currently only available for nonlinear least squares fitting. Both methods require an estimate of the noise standard deviation, which can be obtained using either the *standard* or the *repeated measures* method within the *Noise estimation* utility function ([Table 2\)](#page-4-0). Details on noise estimation are available in [Appendix C](#page-27-1). In addition, ACID offers the *Rician bias simulation* utility function to determine the optimal RBC method for the dMRI dataset and SNR at hand ([Table 2](#page-4-0)). An example of how RBC influences the estimation of biophysical parameters is illustrated in [Appendix Figure F1.](#page-29-0)

#### *2.2.4. Susceptibility artifact correction (HySCO)*

Hyperelastic Susceptibility Artifact Correction (HySCO) is a technique used to correct for geometric distortions caused by susceptibility artifacts ([Ruthotto et al., 2012](#page-23-3), [2013](#page-23-10)). These artifacts can occur at interfaces between tissues with different magnetic susceptibilities, such as those found near paranasal sinuses, temporal bone, and vertebral bodies. To correct for these artifacts, HySCO estimates the bias field based on a reversed-gradient spin-echo echo planar imaging (EPI) acquisition scheme. This requires the acquisition of at least one image with identical acquisition parameters as the dMRI data but with reversed phase-encoding direction, also referred to as "blip-up" or "blip-down" acquisitions. The bias field map, estimated from the blip-up and blip-down images, is applied to the entire dMRI data to unwarp the geometric distortions (see [Fig. 3](#page-10-0) for examples). For datasets that include full blip-reversed acquisition, that is, each image was acquired with two phase-encoding directions (blip-up and blip-down), the reverse phase-encoded images can

# <span id="page-4-0"></span>Table 2. List of ACID utility functions.



#### Table 2. (*Continued*)



be combined using the submodule *HySCO: combine blip-up and blip-down images*.

## <span id="page-5-0"></span>2.3. Diffusion signal models

The dependence of dMRI signal on the direction and strength of diffusion weighting is commonly described by mathematical models. Two of the most widely used models are DTI [\(Basser et al., 1994](#page-19-16)) and DKI ([Hansen](#page-21-14) [et al., 2016;](#page-21-14) [Jensen et al., 2005](#page-21-15)).

### *2.3.1. Diffusion tensor imaging (DTI)*

DTI describes the anisotropic water diffusion in the white matter by a diffusion tensor with six independent diffusion parameters. The eigenvalues of the tensor can be used to compute rotationally invariant DTI scalar metrics including fractional anisotropy (FA) and mean (MD), axial (AD), and radial diffusivities (RD). The interpretation of DTI assumes that the direction of axial diffusivity is aligned with the white matter tracts, which may not be the case in complex fiber geometry such as crossing or fanning fibers.

ACID provides four algorithms to obtain the diffusion tensor (see [Appendix E](#page-28-0) for details). Ordinary least squares (OLS) fits the tensor model by minimizing the sum of squared model-fit errors, while weighted least squares (WLS) minimizes the *weighted* sum of squared model-fit errors, accounting for the distortion of noise distribution in the linearized (logarithmic) data. Robust fitting is similar to WLS but factorizes the weights into three components to account for local and slice-specific artifacts as well, while also featuring Tikhonov regularization to handle illconditioned weighting matrices resulting from a high occurrence of outliers. Robust fitting is designed to down-weight outliers in the model fit, which can otherwise introduce a bias in the fitted model parameters

<sup>1</sup> [https://github.com/quantitative-mri-and-in-vivo-histology/axisymmetric](https://github.com/quantitative-mri-and-in-vivo-histology/axisymmetric_dki_with_rician_bias_correction_simulation_study) [\\_dki\\_with\\_rician\\_bias\\_correction\\_simulation\\_study](https://github.com/quantitative-mri-and-in-vivo-histology/axisymmetric_dki_with_rician_bias_correction_simulation_study)

[\(Mohammadi, Freund, et al., 2013\)](#page-22-6) ([Appendix Fig. E1\)](#page-28-1). Unlike the linearized models, the nonlinear least squared (NLLS) method is based on an implementation ([Modersitzki,](#page-22-12) [2009](#page-22-12)) of the Gauss-Newton algorithm and operates on the nonlogarithmic data, avoiding the distortion of the noise distribution.

#### *2.3.2. Diffusion kurtosis imaging (DKI)*

DKI expands the diffusion tensor model by the kurtosis tensor, a fourth-order tensor with 15 independent parameters, which captures the effects of non-Gaussian water diffusion. From the 15 kurtosis parameters, several kurtosis metrics can be estimated including the mean (MK), axial (AK), and radial kurtosis (RK), as well as the mean (MW), axial (AW), and radial (RW) kurtosis tensor [\(Tabesh](#page-23-13) [et al., 2011\)](#page-23-13) ([Fig. 1\)](#page-6-0). These metrics provide additional information about tissue complexity beyond what can be captured by diffusion tensor metrics alone. DKI requires the acquisition of a second diffusion shell with higher b-value (typically between 2000 and 2500 s/mm2). ACID also includes the axisymmetric DKI model, a recent modification of DKI which reduces the parameter space to eight independent parameters by imposing the assumption of axisymmetrically distributed axons ([Hansen](#page-21-14) [et al., 2016\)](#page-21-14). Currently, ACID offers the OLS and NLLS algorithms for fitting the kurtosis tensor, and the NLLS algorithm for fitting the axisymmetric kurtosis tensor. Note that the diffusion tensor parameters from DKI

might differ from standard DTI parameters. In particular, diffusivities (AD, MD, and RD) derived from the DTI model are often underestimated compared with those derived from the DKI model (referred to as kurtosis bias) ([Edwards et al., 2017\)](#page-20-7). By incorporating higher-order moments of the diffusion signal, DKI can address kurtosis bias, resulting in more accurate diffusivity estimates (see Supplementary Fig. S3 in the Supplementary Material for a comparison of MD derived from DTI and DKI).

#### 2.4. Biophysical models

Biophysical models separate the dMRI signal into distinct signal components from various tissue compartments, each with their own underlying assumptions. Biophysical models provide more specific and biologically interpretable metrics that are linked to tissue microstructure [\(Jelescu et al., 2020\)](#page-21-16). The application of biophysical models is often referred to as dMRI-based in vivo histology ([Mohammadi & Callaghan, 2021](#page-22-13); [Weiskopf et al., 2021\)](#page-24-10) or microstructural dMRI [\(Jelescu et al., 2020;](#page-21-16) [Novikov,](#page-22-14) [2021](#page-22-14); [Novikov et al., 2019\)](#page-22-15). In the following, we briefly describe the two white matter biophysical models currently implemented in ACID (WMTI-Watson and NODDI-DTI), while recommendations on their usage are provided in [Section 4.2.2.](#page-14-0) Example maps are shown in [Figure 2](#page-7-0), and specific values obtained from the brain and spinal cord are presented and discussed in Supplementary Figure S5 (Supplementary Material).



<span id="page-6-0"></span>Fig. 1. Selected maps derived from diffusion kurtosis imaging (DKI) using an in vivo brain, in vivo spinal cord, and ex vivo dMRI dataset (refer to [Table 4](#page-11-1) for details on the dataset). Shown are maps of fractional anisotropy (FA), mean diffusivity (MD), axial diffusivity (AD), radial diffusivity (RD), mean kurtosis (MK), axial kurtosis (AK), and radial kurtosis (RK).



<span id="page-7-0"></span>Fig. 2. Maps of biophysical parameters derived from the WMTI-Watson model using an in vivo brain, in vivo spinal cord, and ex vivo dMRI dataset (refer to [Table 4](#page-11-1) for details on the dataset). Shown are maps of Watson concentration parameter (κ), axonal water fraction (*f*), parallel and perpendicular extra-axonal diffusivities (*De*,! and *De*,⊥), and intra-axonal diffusivity (*D<sub>a</sub>*). Note that for the in vivo spinal cord dataset, the maximum b-value (b = 1500 s/mm<sup>2</sup>) was probably too low for an accurate estimation of *De*,!, resulting in voxels with negative (hence unphysical) values within the spinal cord. Since WMTI-Watson is a white matter biophysical model, the parameter maps were masked for the white matter in the brain dataset. For the spinal cord and ex vivo specimen, we refrained from masking for the white matter due to the difficulty of obtaining an accurate white matter mask.

#### *2.4.1. WMTI-Watson model*

The white matter tract integrity (WMTI)-Watson model as an implementation of the Standard Model assumes two nonexchanging water compartments (intra- and extraaxonal tissue water) [\(Alexander et al., 2019;](#page-19-17) [Novikov](#page-22-15)  [et al., 2019](#page-22-15)). The model characterizes the intra-axonal compartment as "sticks" of zero radius, with an intraaxonal diffusivity *Da* and axonal water fraction *f*. Axonal alignment is characterized by the Watson concentration parameter κ, where higher values indicate higher axonal alignment, and the orientation dispersion index (ODI), where higher values indicate lower alignment. While κ and ODI are mathematically related ([Mollink et al., 2017\)](#page-22-16), ACID outputs both for convenience. The extra-axonal space is modeled as a homogeneous medium, described by an axisymmetric diffusion tensor with parallel ( $D_{e,||}$ ) and perpendicular (*De*,⊥) extra-axonal diffusivities. The five biophysical parameters (*Da*, *f* , <sup>κ</sup> , *De*,!, *De*,⊥) are derived from the axisymmetric DKI tensor metrics (AD, RD, MW, AW, RW) according to the formulas described in [Jespersen et al. \(2018\)](#page-21-10) and [Novikov et al. \(2018\)](#page-22-17). Being derived from the biophysical Standard Model, the estimation of WMTI-Watson biophysical parameters is generally degenerate, which leads to two solutions: the plus branch, which assumes  $D_a > D_{e, \parallel}$ , and the minus branch, which assumes  $D_a < D_{e, \parallel}$  [\(Novikov et al., 2018](#page-22-17)). We recommend using the plus branch (default in the toolbox), as in our experience, and also reported by others [\(Jelescu](#page-21-16)  [et al., 2020;](#page-21-16) [Jespersen et al., 2018\)](#page-21-10), the minus branch is the biologically invalid solution.

#### *2.4.2. NODDI-DTI*

NODDI-DTI ([Edwards et al., 2017](#page-20-7)) is based on the neurite orientation dispersion and density imaging (NODDI) model [\(Zhang et al., 2012](#page-24-3)). While NODDI is a three-compartment biophysical model with intra- and extra-axonal space, and cerebrospinal fluid compartments, NODDI-DTI assumes that the latter compartment can be neglected in normal appearing white matter. NODDI-DTI further

Label	Description	Label	Description
<b>ECMOCO</b>	<b>Eddy-Current and Motion Correction</b>	V1	1st Eigenvector of the Diffusion Tensor
msPOAS	<b>Multi-shell Position-Orientation Adaptive</b> Smoothing	V <sub>2</sub>	2nd Eigenvector of the Diffusion Tensor
<b>RBC</b>	<b>Rician Bias Correction</b>	V3	3rd Eigenvector of the Diffusion Tensor
<b>HySCO</b>	<b>Hyperelastic Susceptibility Artifact Correction</b>	DKI	Diffusion Kurtosis Imaging
fmap	Off-Resonance Field	<b>DKlax</b>	Axisymmetric Diffusion Kurtosis Imaging
COMB-WM	Write Combined Weighted Mean	<b>MK</b>	<b>Mean Kurtosis</b>
COMB-AM	Write Combined Arithmetic Mean	AK	<b>Axial Kurtosis</b>
DTI	Diffusion Tensor Imaging	RK.	<b>Radial Kurtosis</b>
<b>OLS</b>	<b>Ordinary Least Squares</b>	<b>MW</b>	Mean Kurtosis Tensor
<b>WLS</b>	<b>Weighted Least Squares</b>	AW.	Axial Kurtosis Tensor
<b>ROB</b>	<b>Robust Tensor Fitting</b>	<b>RW</b>	<b>Radial Kurtosis Tensor</b>
<b>NLLS</b>	Non-linear Least Squares	WMTI-W	White Matter Tract Integrity - Watson
FA	<b>Fractional Anisotropy</b>	NODDI-DTI	<b>Neurite Orientation Dispersion and Density-</b>
MD	<b>Mean Diffusivity</b>		Diffusion Tensor Imaging
<b>AD</b>	<b>Axial Diffusivity</b>	<b>AWF</b>	<b>Axonal Water Fraction</b>
<b>RD</b>	<b>Radial Diffusivity</b>	DA	Intra-axonal Diffusivity
L1	1st Eigenvalue of the Diffusion Tensor	DE-PARA	Parallel Extra-axonal Diffusivity
L2	2nd Eigenvalue of the Diffusion Tensor	DE-PERP	Perpendicular Extra-axonal Diffusivity
L3	3rd Eigenvalue of the Diffusion Tensor	<b>KAPPA</b>	<b>Watson Concentration Parameter</b>
		<b>ODI</b>	Orientation Dispersion Index

<span id="page-8-0"></span>Table 3. List of labels in the output filename's desc field (not comprehensive).

assumes a fixed diffusivity of the intraneurite compartment (*Da*). In our implementation, users can either choose from two fixed values tailored for in vivo (*Da* = 1.7∙10–3 mm2/s) and ex vivo ( $\boldsymbol{D}_a = 0.6 \cdot 10^{-3}$  mm<sup>2</sup>/s) datasets, or select their own value. NODDI-DTI estimates the intraneurite (here: *f*) and extraneurite (1− *f*) signal fraction, as well as the Watson concentration parameter κ and the orientation dispersion index (ODI), from the FA and MD maps. While WMTI-Watson requires specific multishell dMRI data for robust parameter estimation, NODDI-DTI parameters can also be obtained from single-shell DTI acquisitions.

#### 2.5. Utilities

ACID utilizes SPM's utility functions, available under SPM -> Util in the SPM12 Batch Editor, for handling and manipulating NIfTI images. These functions include mathematical operations on single or multiple images, reorienting images, and concatenating 3D volumes and separating 4D volumes. Additionally, ACID provides its own set of utility functions for image manipulation, mask generation, quality assessment, and other related tasks (refer to [Table 2](#page-4-0) for more details).

#### <span id="page-8-1"></span>2.6. External tools

ACID provides the option to integrate external tools from other packages, which can be accessed directly from the ACID graphical user interface (GUI) (*External tools* module), ensuring a seamless integration into ACID pipelines. We included the following external tools in the current release: (i) FSL eddy<sup>2</sup> (J. L. R. Andersson & Sotiropoulos, [2016](#page-19-3)); (ii) FSL topup<sup>3</sup> ([Smith et al., 2004\)](#page-23-5); (iii) dwidenoise<sup>4</sup> (based on the Marchenko-Pastur principal component analysis (MP-PCA), part of the MRtrix toolbox) ([Veraart](#page-24-1)  [et al., 2016\)](#page-24-1); (iv) denoising<sup>5</sup> (based on the local principal component analysis (LPCA), part of the DWI Denoising Software) (Manjó[n et al., 2013](#page-22-18)); (v) Koay's noise estimation<sup>6</sup>; (vi) mrdegibbs<sup>7</sup> for Gibbs ringing removal, part of the MRtrix toolbox ([Kellner et al., 2016](#page-21-17)); and (vii) the WMTI model (part of the DESIGNER toolbox) [\(Fieremans et al.,](#page-20-12) [2011](#page-20-12)). ACID also allows expert users to incorporate their own external tools into the toolbox, using the aforementioned examples as a template.

#### 2.7. Output structure and BIDS naming convention

ACID supports the BIDS standard, while also being compatible with non-BIDS data*.* Following BIDS recommendations, ACID appends a label to the output filename's desc field, which indicates the applied processing step (refer to [Table 3](#page-8-0) for a list of labels used in the modules *Preprocessing*, *Diffusion tensor/kurtosis imaging*, and *Biophysical models*). For instance, after applying ECMOCO to sub01 dwi.nii, the output file becomes sub01

https://github.com/ian-martin-mri/koays-inversion

<sup>2</sup> <https://fsl.fmrib.ox.ac.uk/fsl/fslwiki/eddy>

<sup>3</sup> <https://fsl.fmrib.ox.ac.uk/fsl/fslwiki/topup>

[https://mrtrix.readthedocs.io/en/dev/dwi\\_preprocessing/denoising.html](https://mrtrix.readthedocs.io/en/dev/dwi_preprocessing/denoising.html)

<sup>5</sup> [https://sites.google.com/site/pierrickcoupe/softwares/denoising/dwi](https://sites.google.com/site/pierrickcoupe/softwares/denoising/dwi-denoising/dwi-denoising-software) [-denoising/dwi-denoising-software](https://sites.google.com/site/pierrickcoupe/softwares/denoising/dwi-denoising/dwi-denoising-software)

<sup>7</sup> [https://mrtrix.readthedocs.io/en/dev/reference/commands/mrdegibbs](https://mrtrix.readthedocs.io/en/dev/reference/commands/mrdegibbs.html) [.html](https://mrtrix.readthedocs.io/en/dev/reference/commands/mrdegibbs.html)

desc-ECMOCO dwi.nii. When multiple processing steps are involved, the labels are concatenated, as in sub01\_desc-ECMOCO-msPOAS\_dwi.nii. Model fitting appends three labels indicating the type of diffusion model, algorithm, and parametric map, such as sub01\_ desc-ECMOCO-msPOAS-DKI-OLS-FA\_dwi.nii. For BIDS-compliant input, ACID generates a bval and bvec file after each processing step. ACID stores all output in the derivatives folder, with separate subfolders for each module's output (e.g., derivatives/msPOAS-Run). ACID retains the same folder structure and naming convention even when non-BIDS input is provided.

#### 3. RESULTS

#### 3.1. Pipelines

ACID is fully integrated into the SPM12 batch system, allowing users to execute its functions individually or combined into linear pipelines with multiple steps. Each step can receive the output of any of the previous steps via flexible and easy-to-use dependencies. While pipelines are typically set up in the SPM batch system, they can also be converted into MATLAB code (SPM batch script) for automation and further customization. In addition to its own functions, ACID integrates seamlessly with a range of standard SPM features, including segmentation, coregistration (based on affine transformation), spatial normalization (including nonlinear registration), and voxel-based statistical analyses, as well as a growing number of SPM extensions.<sup>8</sup> For example, combining ACID with the hMRI toolbox enables multicontrast analysis of dMRI and other quantitative MRI data, such as relaxation rates [\(Tabelow et al., 2019\)](#page-23-9).

#### <span id="page-9-0"></span>3.2. Example applications

To demonstrate the application of ACID toolbox on different types of dMRI data, here we provide three example pipelines for in vivo brain, in vivo spinal cord, and ex vivo dMRI [\(Fig. 3\)](#page-10-0). Details of these three datasets are summarized in [Table 4](#page-11-1). The gradient schemes used for all datasets were based on the configurations proposed by [Caruyer et al. \(2013\),](#page-19-18) available online.<sup>9</sup> The design of the sampling schemes followed a uniform coverage on a sphere. Note that data with reverse phase-encoding direction were available for all three datasets, which refers to the acquisition of either a single b0 volume or all volumes with identical geometry and sequence parameters but opposite phase-encoding direction. All example pipelines consist of artifact correction (ECMOCO, msPOAS, RBC, HySCO) and model fitting steps. While Gibbs ringing removal is often part of dMRI processing pipelines ([Ades-Aron et al., 2018;](#page-19-6) [Kellner et al., 2016](#page-21-17); [Tournier](#page-24-2) 

9 <http://www.emmanuelcaruyer.com/q-space-sampling.php>

Fig. 3. Standard processing pipelines for typical (A) in vivo brain, (B) in vivo spinal cord, and (C) ex vivo dMRI datasets (refer to [Table 4](#page-11-1) for details on the datasets and [Table 5](#page-11-0) for details on the pipeline settings). Example batches for each type of dMRI data are stored in the Example Batches folder of the toolbox. The positions of the displayed slices of the dMRI data are indicated in purple on the corresponding structural images. For the ex vivo specimen (C), the brain region from which the sample was extracted is highlighted in an orange box. Although not explicitly shown here, noise estimation should be performed on the unprocessed data (see [Appendix C\)](#page-27-1), which serves as input for msPOAS, Rician bias correction, and diffusion tensor fitting (for fitting methods WLS and robust fitting). However, in case of substantial misalignments across volumes, and when using the *repeated measures* noise estimation method, it might be beneficial to perform this step after ECMOCO to prevent an overestimation of noise. For msPOAS, a zoomed-in visual comparison is shown between a diffusion-weighted (DW) image before (middle row) and after applying msPOAS (bottom row); the msPOAS-corrected image appears less noisy while preserving tissue edges. For HySCO, contour lines of the corresponding structural image (displayed as red lines) are overlaid on a zoomed-in DW image both before (middle row) and after applying HySCO (bottom row). HySCO improves the alignment between the DW and the structural image. For the in vivo brain dMRI dataset (A), an inferior slice is shown that presents high susceptibility-related distortions, making the effect of HySCO more visible. For the ex vivo dMRI dataset (C), the effect of HySCO is shown in a slice (illustrated in yellow) orthogonal to the original one (illustrated in purple) to better visualize susceptibility-related distortions and their correction. Note that HySCO is applied as the final preprocessing step, that is, after applying msPOAS; however, the HySCO field map used for "unwarping" the diffusion-weighted images is estimated on the ECMOCO-corrected datasets, that is, before applying msPOAS. Rician bias correction (not explicitly shown here) should be applied either before (recommended: between msPOAS and HySCO, using the RBC module) or during model fitting (using the Rician bias correction option in NLLS). Diffusion signal models are fitted on the processed dataset; here, we display the maps of fractional anisotropy (FA) and mean kurtosis tensor (MW) from diffusion kurtosis imaging (DKI). The output from DKI can be used to compute biophysical parameters of the white matter; shown here is the map of Watson concentration parameter (κ) from the WMTI-Watson biophysical model. Note that for the in vivo brain dMRI dataset, the inferior slice displayed contains relatively little white matter; hence, we refrained from using a white matter mask. The less smooth appearance of the κ map is due to the low values in the gray matter.

<sup>8</sup> <https://www.fil.ion.ucl.ac.uk/spm/ext/>

[et al., 2019](#page-24-2)) and is also available in ACID as an external tool, we refrained from including it in the example pipelines because the interaction between denoising and the interpolation associated with Gibbs ringing removal is not well characterized yet. We emphasize that these example pipelines might not be optimal for all cases; users might find that another combination of preprocessing steps,

which might also include Gibbs ringing removal, works even better for their data.

While the pipelines for in vivo brain, in vivo spinal cord, and ex vivo dMRI follow similar concepts, recommended settings for each region may differ [\(Table 5\)](#page-11-0). It is important to note that the settings listed in [Table 5](#page-11-0) serve as initial values for typical datasets. The optimal settings

<span id="page-10-0"></span>



<span id="page-11-1"></span>

<span id="page-11-0"></span>Table 5. Settings of selected modules for in vivo brain, in vivo spinal cord, and ex vivo dMRI datasets.



In the "degrees of freedom" settings (ECMOCO), x, y, and z represent the frequency-, phase-, and slice-encoding directions, respectively.

for a particular dataset depend on the sequence parameters, the subject, and the imaged region. Model fitting may be followed by spatial processing, such as coregistration to the structural image or spatial normalization to a template in a standard space (e.g., MNI152 space), and statistical analysis (e.g., ROI- or voxel-based analysis).

#### 4. DISCUSSION

We have developed the ACID toolbox, which extends the capabilities of the SPM framework by providing comprehensive preprocessing and model fitting techniques for in vivo brain, spinal cord, and ex vivo dMRI data. Besides commonly used diffusion signal models such as DTI and DKI, ACID also offers biophysical models that provide parameters of white matter tissue microstructure such as axonal water fraction and axon orientation dispersion. Being seamlessly integrated into the SPM batch system, ACID allows for user-friendly access to SPM's powerful spatial processing tools and statistical framework. In addition to offering recommended pipelines for in vivo brain, spinal cord, and ex vivo dMRI, ACID provides the flexibility for users to create customized pipelines tailored to their specific data. Adhering to the BIDS conventions facilitates data sharing, enhances data comprehension for investigators, and makes ACID compliant with software requiring BIDS input (<https://bids-apps.neuroimaging.io>).

## <span id="page-12-0"></span>4.1. Preprocessing dMRI data

ACID offers artifact correction steps typically applied to dMRI data, including image realignment (ECMOCO), adaptive denoising (msPOAS), Rician bias correction (RBC), and correction for susceptibility-induced geometric distortions (HySCO). Here, we discuss specific considerations regarding their use for various applications.

Correcting for displacements within the dMRI data through image realignment is one of the most important but also challenging tasks. ECMOCO provides users with the flexibility to choose the degrees of freedom for image realignment based on the anticipated type of displacement, but also offers a selection of predefined degrees of freedom that are optimized for brain, spinal cord, and ex vivo dMRI.

In brain dMRI, motion can be approximated as a rigid body displacement with 6 degrees of freedom (DOF). Eddy-current spatial displacements, to a first-order approximation, result in translation and scaling along the phase-encoding direction (typically, the y-axis), and inplane and through-plane shearing ([Mohammadi et al.,](#page-22-4) [2010](#page-22-4)). Since these displacements affect the entire brain, we recommend employing a 9-DOF volume-wise (volume to volume) registration with translation and rotation

along x, y, and z, scaling along y, and shearing in the x-y and y-z planes. First-order approximation of eddy-current displacements might not always be sufficient, as dMRI data can also be affected by higher-order eddy-current field inhomogeneities causing nonlinear distortions ([J. L.](#page-19-3)  [R. Andersson & Sotiropoulos, 2016](#page-19-3); [Rohde et al., 2004\)](#page-23-14). For example, in our observations, ECMOCO was not effective in removing pronounced eddy-current displacements present in the dMRI data of the Human Connectome Project ([Van Essen et al., 2012](#page-24-11)). In such cases, we recommend using FSL eddy, which incorporates higherorder eddy-current correction terms [\(J. L. R. Andersson &](#page-19-3)  [Sotiropoulos, 2016](#page-19-3)) and can be called directly from ACID as an external tool ([Section 2.6](#page-8-1)). In cases where ECMOCO is sufficient, an advantage of ECMOCO is that its performance is largely independent of the number of diffusion directions, whereas FSL eddy requires a minimum number of diffusion directions for good performance (see FSL website<sup>10</sup> for recommendations).

In spinal cord dMRI, volume-wise registration has been found to be less effective [\(Cohen-Adad et al., 2009](#page-20-13); [Mohammadi, Freund, et al., 2013](#page-22-6)) due to displacements that vary along the rostrocaudal axis of the spinal cord. These displacements appear mostly in the phaseencoding direction and are caused by physiological factors such as respiration and cardiac pulsation [\(Kharbanda](#page-21-18)  [et al., 2006;](#page-21-18) [Summers et al., 2006\)](#page-23-15). We recommend applying volume-wise registration for rough alignment and correction of through-slice displacements, followed by slice-wise (slice to slice) registration for correcting any remaining slice-dependent displacement. This combined approach has demonstrated effectiveness in realigning not only volumes but also individual slices [\(Appendix Fig.](#page-27-2)  [B2\)](#page-27-2), as well as improving the contrast-to-noise ratio between gray and white matter and reducing test–retest variability in DTI maps of the spinal cord [\(Mohammadi,](#page-22-6)  [Freund, et al., 2013](#page-22-6)). Eddy-current distortions are typically less severe in the spinal cord compared with the brain, because the in-plane field of view is smaller and located near the scanner isocenter. This makes the firstorder approximation of eddy-current displacements, as supported by ECMOCO, generally adequate. We recommend employing a 4-DOF volume-wise registration (translation along x, y, z; scaling along y) followed by a 3-DOF slice-wise registration (translation along x, y; scaling along y). In datasets with low SNR, slice-wise correction along x can be omitted, given the smaller range of movement which makes reliable estimation difficult. We advise against correcting for in-plane rotation and shearing, as their expected range is very small. Correction for these DOFs might introduce spurious displacements

<sup>10</sup> <https://fsl.fmrib.ox.ac.uk/fsl/fslwiki/eddy>

during realignment, a risk we consider greater than not applying correction at all.

Structures surrounding the spinal cord (bones, ligaments, etc.) may move independently from the spinal cord, potentially leading to inaccuracies in transformation parameters. Moreover, as these structures typically occupy a larger portion of the image, they can dominate the estimation of transformation parameters. To address this challenge, ECMOCO provides the option of specifying a spinal cord mask to restrict the estimation of transformation parameters to the spinal cord and its immediate surroundings ([Fig. 3](#page-10-0)). Any residual misalignments can be manually corrected using the *Slice-wise realignment* utility function ([Table 2](#page-4-0)).

In ex vivo dMRI, specimen motion is not anticipated if the specimen is appropriately fixed, for instance, by using a sample holder or embedding it in agarose. Thus, we recommend correcting only for the four first-order eddy-current displacements (y-translation, y-scaling, x-y shearing, y-z shearing). The first-order approximation is typically adequate for small specimens where eddycurrent displacements are not severe.

In general, the performance of msPOAS and HySCO is largely independent of the anatomical features present in the image; therefore, default parameters are expected to work well for in vivo brain, spinal cord, and ex vivo dMRI data. Nevertheless, the default regularization parameters for HySCO (alpha "diffusion" and beta "Jacobian" regulator), accessible through the script config/local/acid local defaults.m, are optimized for the brain and may require adjustment for the spinal cord if performance is inadequate.

Applying HySCO is particularly important for acquisitions with severe susceptibility-related distortions, such as multiband EPI without parallel imaging, and for multicontrast analyses where dMRI data or other quantitative maps are combined with structural reference images, for example, the dMRI-based axonal water fraction and magnetization transfer saturation maps in g-ratio mapping [\(Mohammadi & Callaghan, 2021\)](#page-22-13) or multicontrast MRI in the spinal cord ([David et al., 2019](#page-20-14)). In these cases, HySCO improves the overlap between the undistorted structural image and the dMRI data, improving the performance of subsequent coregistration and spatial normalization algorithms. HySCO has also been shown to improve the accuracy of g-ratio mapping [\(Clark et al., 2021;](#page-19-9) Mohammadi, [Tabelow, et al., 2015](#page-23-11)). While HySCO is far more efficient than FSL topup in terms of computation time ([Macdonald](#page-21-9)  [& Ruthotto, 2018](#page-21-9)), it does not integrate movement and susceptibility artifact correction into a single model. To mitigate the effects of subject movement, we propose acquiring images with reversed phase-encoding direction (the blip-up and blip-down images) in close succession.

The application of adaptive denoising (msPOAS) is important as it reduces the variance and, therefore, improves the precision of the tensor and kurtosis parameter estimates (see Supplementary Fig. S4 for an example illustrating the effect of msPOAS on DKI parameters, and refer to [Becker et al. \(2014\)](#page-19-4) for more examples and details). For high-SNR data, denoising might not be advantageous; instead, denoising methods could even introduce additional error (see analysis in [Appendix G\)](#page-30-0). For low-SNR data, Rician bias correction (RBC), either applied to the dMRI data or during model fitting, must be performed in addition to msPOAS to mitigate the Rician bias in parameter estimates (see [Appendix F](#page-30-1) for an example). An in-depth analysis of the impact of Rician bias correction on DKI and axisymmetric DKI can be found in [Oeschger et al. \(2023a\)](#page-22-5).

### 4.2. Model fitting on dMRI data

#### *4.2.1. Physical diffusion models*

At a given b-value, the SNR in spinal cord dMRI is typically lower than in brain dMRI due to (i) the smaller crosssectional area that requires higher in-plane resolution (see [Fig. 4A](#page-14-1) for a size comparison), (ii) the high signal attenuation for diffusion-gradient directions parallel to the highly aligned fibers in the head-feet direction [\(Fig. 4B](#page-14-1)), and (iii) the suboptimal coil configuration in the thoracic and lumbar regions, which are not covered by the head and neck coil. Lower SNR increases the variance of parameter estimates and makes spinal cord dMRI more susceptible to Rician bias. Consequently, SNR is often prohibitively low at higher b-values necessary for fitting the kurtosis tensor, making the application of DKI in the spinal cord very challenging.

The bias in parameters estimates induced by signal outliers from cardiac, respiratory, and other physiological artifacts [\(Mohammadi, Hutton, et al., 2013](#page-22-19)) can be mitigated by applying robust fitting as a tensor fitting method ([Appendix E.3\)](#page-29-1). Given the higher occurrence of signal outliers in the spinal cord, robust fitting holds particular relevance for spinal cord dMRI. In a previous study, we demonstrated that robust fitting leads to higher FA values within the white matter and lower FA values within the gray matter in spinal cord dMRI data, resulting in an approximately 8% enhancement in contrast-tonoise ratio ([Mohammadi, Freund, et al., 2013](#page-22-6)). While robust fitting demonstrated high resistance to contamination (presence of outliers) compared with OLS and NLLS estimations, it is important to note that robust fitting requires a sufficiently large number of artifact-free data points. Simulations suggested that robust tensor estimates begin to break down when the frequencies of



Fig. 4. (A) Illustration of differences in the cross-sectional area between the brain and spinal cord, displaying a single axial slice of the mean T2-weighted (b0) image (refer to [Table 4](#page-11-1) for details on the datasets). (B) Schematic visualization of the spinal cord, highlighting the "butterfly-shaped" gray matter, which is located in the middle of the spinal cord and contains neuronal cell bodies and loosely aligned fibers, and the surrounding white matter, which contains highly aligned fibers.

moderately intense cardiac pulsation artifacts exceed 27–30% ([Zwiers, 2010,](#page-24-12) [fig. 5\)](#page-17-0).

One potential limitation of linearized fitting methods is their operation on logarithmically transformed signals, where the assumption of Gaussian (or Rician) error distribution may not hold. The presence of logarithmically distorted Rician noise distribution not only restricts validity but can also impact the accuracy of the parameter estimates ([J. L. R. Andersson, 2008;](#page-19-19) [Chang et al., 2005;](#page-19-5) [Koay](#page-21-19) [et al., 2006](#page-21-19)), particularly in the low-SNR regime such as in spinal cord dMRI. The WLS and robust fitting algorithms incorporate the signal intensity into the weights of the estimator function (Appendices E.2 and E.3), which was shown to reduce the effect of log-Rician distortion [\(Salvador et al., 2005](#page-23-16)). Alternatively, the NLLS algorithm ([Appendix E.4](#page-30-2)) can be used, which circumvents the distortion of the Rician distribution by operating on the original (nonlogarithmic) signals, and is, therefore, expected to yield more accurate parameter estimates, provided that the numerical fitting problem is sufficiently well conditioned.

In summary, for data with relatively high SNR and a frequent occurrence of outliers, we recommend using robust fitting to mitigate the influence of outliers. NLLS, particularly when combined with Rician bias correction, may be more suitable for dMRI data with lower SNR, which is often encountered in acquisitions for DKI (refer to [Oeschger et al., 2023a,](#page-22-5) for recommended minimum SNR values and the *Rician bias simulation* utility function in [Table 2](#page-4-0) for simulating the Rician bias on dMRI data with a given SNR). Low-SNR data with a frequent occurrence of outliers pose challenges for model fitting, where

<span id="page-14-1"></span>a combination of msPOAS with RBC might reach their limits. In such cases, reliability masking can assist in identifying and excluding corrupted, thus unreliable, voxels from the parameter maps [\(David et al., 2017](#page-20-8)).

#### <span id="page-14-0"></span>*4.2.2. Biophysical diffusion models*

Of the biophysical models implemented in ACID, WMTI-Watson relies on DKI metrics (requiring at least two diffusion shells), while NODDI-DTI relies on DTI metrics (requiring a single diffusion shell only). This implies that the challenges associated with the estimation of DTI and DKI metrics, as discussed earlier, also apply to derived biophysical models. Accurate and precise estimation of DKI and DTI metrics is essential for the successful application of WMTI-Watson and NODDI-DTI, respectively.

In general, we recommend the DKI-based WMTI-Watson model over NODDI-DTI due to the fewer model assumptions, allowing it to better capture diffusion patterns in complex axonal configurations within the brain white matter. This aligns with the results from our example multishell brain dMRI dataset, where WMTI-Watson yielded more accurate estimates of κ and AWF compared with NODDI-DTI (Supplementary Fig. S5). For a more indepth comparison of biophysically derived values with histological values, refer to [Papazoglou et al. \(2024\)](#page-22-3).

On the other hand, complex models are more "datahungry" and more susceptible to noise due to the higher number of fitted parameters, which can lead to poorly conditioned optimization problems when the amount and/or the quality of input data are insufficient. Therefore, for low-SNR data, as is often the case in spinal cord dMRI, the less complex but better-conditioned NODDI-DTI model might be the preferred choice. The low b-values often used in spinal cord dMRI could lead to inadequate parameter estimation when using the WMTI-Watson model. Indeed, NODDI-DTI yielded a more accurate estimation of  $\kappa$  in the example spinal cord dMRI dataset, whereas WMTI-Watson highly overestimated it (Supplementary Fig. S5). A drawback of the NODDI-DTI model in the spinal cord is its assumption of fixed intra- and extracellular diffusivities, which were optimized for the brain and might not be valid for the spinal cord. Both low SNR [\(Veraart et al., 2011](#page-24-8)) and kurtosis bias ([Edwards et al., 2017\)](#page-20-7) can lead to an underestimation of MD (Supplementary Fig. S3), impacting the model parameter estimation when MD falls outside the range where the NODDI-DTI model provides a valid representation (refer to Equation (4) in [Edwards et al., 2017\)](#page-20-7). This was evident in the estimation of AWF, which proved unfeasible in the spinal cord dataset (see [Appendix Fig.](#page-29-0) [F1;](#page-29-0) Supplementary Fig. S5). We anticipate that future improvements in acquisition methods will enhance the SNR in spinal cord dMRI, enabling the acquisition of higher b-values, which would alleviate many of the above-mentioned drawbacks.

A compromise between these two models could be the white matter tract integrity (WMTI) model, which is included as an external tool in ACID ([Section 2.6](#page-8-1)). WMTI assumes highly aligned fibers, which holds true in white matter regions with high fiber alignment, such as the corpus callosum or the spinal cord white matter, but is less appropriate in regions with more complex axonal configurations, such as parts of the superior longitudinal fasciculus.

Ex vivo neuronal tissues exhibit different diffusivities compared with in vivo tissues due to various factors, including the effect of fixation, changes in chemical properties, and differences in temperature and composition of the embedding fluid. For example, white matter diffusivity was reported to reduce by approximately 85% from in vivo to ex vivo conditions, while the ratio between gray and white matter diffusivities remains similar, around 2–3 [\(Roebroeck et al., 2019](#page-23-17)). To accommodate the reduced diffusivities under ex vivo conditions, ACID offers the option to utilize compartmental diffusivities tailored for ex vivo datasets within the NODDI-DTI model. Such an adjustment is not necessary for WMTI and WMTI-Watson, as their compartmental diffusivities are fitted rather than fixed.

We emphasize that NODDI-DTI, WMTI, and WMTI-Watson have been developed to characterize diffusion in the white matter. Recently, several efforts have been made to extend biophysical models to the gray matter [\(Jelescu et al., 2020\)](#page-21-16). Notable examples include the SANDI ([Palombo et al., 2020\)](#page-22-20) and NEXI [\(Jelescu et al.,](#page-21-20) [2022](#page-21-20)) biophysical models. However, these models thus far, no study using these protocols on a clinical MRI system has been published.

# <span id="page-15-0"></span>4.3. Studies quantitatively evaluating the performance of ACID pipelines

Here, we briefly summarize and discuss the studies that quantitatively evaluated the performance of ACID tools individually or in comparison with other tools.

#### *4.3.1. Evaluating preprocessing pipelines*

In a previous study, we assessed the performance of ECMOCO as well as the combination of ECMOCO and msPOAS in simulated high- and low-SNR multishell brain dMRI datasets with added motion and eddy-current artifacts (i.e., perturbed data) (Mohammadi, [Tabelow, et al.,](#page-23-11) [2015](#page-23-11)). We found that the performance of ECMOCO in correcting the perturbed volumes was dependent on the SNR, with the number of incorrectly registered volumes increasing at lower SNR (SNR  $<$  16). However, the combined application of msPOAS and ECMOCO effectively reduced the number of incorrectly registered volumes even at low SNR (fig. 3 in [Mohammadi, Tabelow, et al.,](#page-22-9) [2015](#page-22-9)). Additionally, correcting the perturbed volumes with ECMOCO and msPOAS yielded FA maps closer to the "ground truth," that is, the FA map computed on the unperturbed data (fig. 5 in [Mohammadi, Tabelow, et al.,](#page-22-9) [2015](#page-22-9)). In another study utilizing clinical spinal cord dMRI data, we evaluated the impact of ECMOCO on the group differences observed in FA between patients with degenerative cervical myelopathy and healthy controls (fig. 7 in [David et al., 2017](#page-20-8)). Our analysis revealed that ECMOCO had only a minimal effect on the two-sample *t*-score computed between the FA values of the two groups.

We also tested the effects of different denoising methods (msPOAS, LPCA, and MP-PCA) on the accuracy of DKI metrics, with the details and results described in [Appendix G](#page-30-0). In short, we found that denoising (using any of the three methods) is beneficial only in the low-SNR domain (below an SNR of approximately 30). In high-SNR data, denoising did not lead to further improvements with MP-PCA and even introduced additional errors with msPOAS and LPCA. In terms of susceptibility artifacts, we previously found in a brain dMRI dataset that FSL topup was more efficient in correcting susceptibilityrelated distortions than HySCO, even when including a motion correction step between the reverse phaseencoded (blip-up and blip-down) images before running HySCO (fig. 3 in [Clark et al., 2021\)](#page-19-9). This is potentially because the HySCO pipeline involved multiple interpolation steps, introducing additional blurring effects, while

FSL topup incorporates motion and susceptibility distortion correction within the same model. The same study found that combining reverse phase-encoded images using the "weighted average" method (*HySCO: combine blip-up and blip-down images* module), as opposed to the "arithmetic average" method, reduces image blurring in the corrected brain dMRI data and achieves greater overlap between the dMRI data and the corresponding structural image. In fact, when using the "weighted average" method, HySCO performed comparably to FSL topup and even outperformed it in regions suffering from high levels of distortion (fig. 5 in [Clark et al., 2021](#page-19-9)). In spinal cord dMRI, a previous study found that HySCO is comparable with other distortion correction tools such as FSL topup ([Schilling et al., 2024\)](#page-23-18).

## *4.3.2. Evaluating diffusion signal models*

In brain dMRI datasets, we found that robust tensor fitting can reduce the effect of signal outliers due to motion, eddy-current artifacts, incorrectly registered volumes (fig. 5C, D in [Mohammadi, Tabelow, et al., 2015](#page-22-9)), or physiological noise (fig. 9 in [Mohammadi, Hutton, et al., 2013\)](#page-22-19). In spinal cord dMRI, we quantified the performance of robust fitting and showed that it can reduce the bias in FA, especially at tissue boundaries (fig. 7 in [Mohammadi,](#page-22-6)  [Freund, et al., 2013\)](#page-22-6). On the other hand, robust fitting had only a minor effect on group differences in FA between patients with degenerative cervical myelopathy and healthy controls, regardless of whether using the ACID implementation of robust fitting or using RESTORE (part of the CAMINO toolbox; [Chang et al., 2012\)](#page-19-20) (fig. 7 in [David et al., 2017](#page-20-8)). However, within the same study, we also found that supplementing the pipeline with reliability masking to exclude outlier voxels [\(Table 2](#page-4-0)) considerably increased the statistical differences between patients and controls (fig. 7 in [David et al., 2017](#page-20-8)).

#### 4.4. Applications

For all applications, it is highly recommended to assess the data quality before and after each processing step. In addition to the quality assessment utility functions *DWI series browser* and *DWI series movie* [\(Table 2\)](#page-4-0), multiple ACID modules generate diagnostic plots to identify the presence and type of artifacts in the dMRI data. Example diagnostic plots are provided in Supplementary Figures S1 and S2.

#### *4.4.1. Integration with SPM modules*

ACID can be readily combined with SPM tools for segmentation, spatial processing, and voxel-based analysis of parametric maps. Segmenting the brain or spinal cord is often necessary for coregistration, spatial normalization, or tissue-specific analyses. In the brain, tissue probability maps of white matter, gray matter, and cerebrospinal fluid can be created by unified segmentation, the default segmentation routine in SPM12 [\(Ashburner &](#page-19-15)  [Friston, 2005](#page-19-15)). These tissue probability maps can also be used to create a binary brain mask using the *Create brain mask* utility function [\(Table 2](#page-4-0)). To enable SPM's unified segmentation in the spinal cord, the brain tissue priors need to be substituted with the joint brain and spinal cord tissue priors from the probabilistic brain and spinal cord atlas ([Blaiotta et al., 2017\)](#page-19-21). However, this atlas only covers the upper cervical cord down to C3; for other spinal levels, the user is referred to automatic (e.g., deepseg [\(Perone et al., 2018](#page-22-21))) or semiautomatic (e.g., active surface method ([Horsfield et al., 2010\)](#page-21-21)) segmentation techniques.

Brain dMRI data can be coregistered to the corresponding structural image using *spm\_coreg*. For nonlinear spatial registration to the MNI space, we recommend SPM DAR-TEL [\(Ashburner, 2007\)](#page-19-22) or Geodesic Shooting ([Ashburner &](#page-19-23)  [Friston, 2011\)](#page-19-23). As SPM registration tools often rely on brain tissue priors, they cannot be applied directly on spinal cord dMRI. For the spinal cord, we recommend utilizing the PAM50 template (De Leener et al., 2018) and the corresponding normalization tools integrated into the Spinal Cord Toolbox [\(De Leener et al., 2017](#page-20-5)).

While brain and spinal cord images are typically analyzed separately, there are scenarios where combining them into a single image can be beneficial. For example, when registering the brain and spinal cord image to a joint brain–spinal cord template, such as the probabilistic atlas of the brain and spinal cord [\(Blaiotta et al., 2017\)](#page-19-21), the warping field is often obtained using a structural image with a large field of view (FOV) covering both regions [\(Fig. 5](#page-17-0)). To apply this warping field to the brain and spinal cord images, they need to be fused into a single image. ACID provides the *Fusion* utility function [\(Table 2\)](#page-4-0) which merges two distinct images, acquired with different FOV and geometric properties, into a unified large FOV image ([Fig. 5](#page-17-0)).

ACID benefits from SPM's rich statistical framework for voxel-based analysis. SPM's second-level analysis tool (SPM -> Specify 2nd-level) performs voxelbased statistical tests on the parametric maps using *t*-test, ANOVA, or general linear model. In the SPM -> Results module, the framework also offers (i) multiple comparison correction in the form of family-wise error rate and false discovery rate, (ii) thresholding the test statistics at cluster level and voxel level and providing a list of significant clusters/voxels, and (iii) various visualization tools for displaying and saving the significant clusters. Furthermore, ACID's *ROI analysis* utility function [\(Table 2\)](#page-4-0) can be used to extract mean metrics within subject-specific



Fig. 5. Merging of two fractional anisotropy (FA) maps, covering the brain and cervical cord, respectively, into a unified FA map using the *Fusion* utility function ([Table 2\)](#page-4-0). The two images should ideally share an overlapping region, but they may have different geometric properties such as resolution and number of slices. In the overlapping region, the voxel intensity values are computed as the average of the intensity values from the two images. The merging process requires a structural image as the registration target. The combined FA map is resampled onto the higher resolution structural image, resulting in a smoother appearance.

ROIs in the native space or perform atlas-based analysis in the template space. For atlas-based analysis in the spinal cord, the user is referred to the PAM50 white and gray matter atlas [\(De Leener et al., 2018](#page-20-15)).

Although ACID does not provide tractography or tractbased analysis tools, the output of its model fitting methods can be input into tractography tools such as FSL or the SPM12-based Fibertools toolbox (see Wiki<sup>11</sup> on the git repository for more details).

#### *4.4.2. Computation time*

To speed up the processing and analysis of dMRI data, parallel computing is implemented wherever applicable. This technique can substantially accelerate the most time-consuming ACID modules, including ECMOCO and DTI/DKI fit. Note that parallel computing requires the Parallel Computing Toolbox in MATLAB. [Table 6](#page-17-1) provides the computation times for selected ACID modules on a typical brain and spinal cord dMRI dataset.

#### *4.4.3. Research applications*

ACID has been used in a variety of clinical and neuroscience research, for example, in dMRI studies assessing cerebral changes in patients with multiple sclerosis (Deppe, Krä[mer, et al., 2016](#page-20-16); [Deppe, Tabelow, et al.,](#page-20-17)  [2016](#page-20-17); [Dossi et al., 2018;](#page-20-18) [Kugler & Deppe, 2018\)](#page-21-22) and <span id="page-17-1"></span><span id="page-17-0"></span>Table 6. Computation times of selected ACID modules on an example in vivo brain and in vivo spinal cord dMRI dataset (refer to [Table 4](#page-11-1) for details on the datasets), when run on a MacBook M1 laptop (4 cores, 16GB RAM).



Parkinson's disease [\(Szturm et al., 2021\)](#page-23-19), and to assess gliomas ([Paschoal et al., 2022](#page-22-22); [Raja et al., 2016\)](#page-23-20). We have also used ACID to investigate spinal cord white matter following spinal cord injury (Bü[eler et al., 2024](#page-19-24); [David](#page-20-14)  [et al., 2019](#page-20-14), [2021,](#page-20-19) [2022](#page-20-20); [Grabher et al., 2016;](#page-21-23) [Huber](#page-21-24)  [et al., 2018;](#page-21-24) [Seif et al., 2020](#page-23-21); [Vallotton et al., 2021\)](#page-24-13). A noncomprehensive list of studies using the ACID toolbox can be found on the project website.<sup>12</sup> Note that certain ACID functions can be applied to MRI data beyond dMRI as well; for instance, HySCO has been used to correct brain fMRI data for susceptibility artifacts (De Groote et al., [2020](#page-20-21)). It is important to note that ACID has not been approved for clinical applications by any health agency and it comes with no warranty. Therefore, it should not be used for diagnosis in clinical settings.

<sup>11</sup> [https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/wiki/Home) [/wiki/Home](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/wiki/Home) 12 <http://www.diffusiontools.org/sidebar/studies-using-acid.html>

## 4.5. Limitations and future directions

Comparing the tools within the ACID toolbox with alternative implementations in other software presents challenges because their performance depends on the specific dMRI data and the chosen parameter settings from a potentially large parameter space, which necessitates a systematic exploration of the parameter space. In addition, the evaluation of entire processing pipelines would drastically increase the number of parameters to test. While we have outlined the comparisons conducted so far in [Section 4.3,](#page-15-0) we assert that a thorough quantitative comparison between toolboxes warrants a dedicated future study. In general, we encourage users to undertake such comparisons on their own datasets.

The ACID toolbox is the result of a collaborative effort to extend the SPM ecosystem with state-of-the-art processing and modeling tools for dMRI data. Our aim is to make the toolbox widely accessible, leveraging SPM's large and vibrant community. Users can submit their questions, bug reports, and suggestions via the dedicated mailing list or by opening an issue on the git website. This paper offers an overview of the current state of the toolbox, with several ongoing developments not covered here. The modularity of the toolbox allows for integration of newly developed methods, even when used concurrently with old ones. Biophysical modeling is an emerging field, and we expect many methodological advancements to occur in the coming years. To align with this ongoing development, our goal is to consistently integrate state-of-the art biophysical models into ACID. We also plan to add the Rician maximum likelihood estimator [\(Sijbers et al., 1998\)](#page-23-4) as an alternative to the existing quasi-likelihood estimators ([Polzehl & Tabelow,](#page-23-12)  [2016](#page-23-12)).

## 5. CONCLUSION

ACID is an open-source extension to SPM12 that provides a comprehensive framework for processing and analyzing in vivo brain, spinal cord, and ex vivo dMRI data. The toolbox was developed to meet the increasing demand for studies involving spinal cord dMRI, research employing biophysical models, and validation studies utilizing ex vivo dMRI. ACID leverages the core SPM tools and other SPM extensions, which can be easily integrated into the ACID pipeline.

## DATA AND CODE AVAILABILITY

The source code of ACID is freely available at [https://](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/src/master/) [bitbucket.org/siawoosh/acid-artefact-correction-in](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/src/master/) [-diffusion-mri/src/master/.](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/src/master/) The authors will make the raw data used for the visualizations in this article available in an associate publication.

## AUTHOR CONTRIBUTIONS

Gergely David: Conceptualization, Data curation, Formal analysis, Investigation, Methodology, Resources, Software, Visualization, Writing—original draft, Writing—review & editing. Björn Fricke: Conceptualization, Data curation, Formal analysis, Investigation, Methodology, Software, Validation, Visualization, Writing—original draft, Writing review & editing. Jan Malte Oeschger: Formal analysis, Methodology, Software, Writing—original draft, Writing review & editing. Lars Ruthotto: Methodology, Software, Writing—review & editing. Francisco J. Fritz: Data curation, Resources. Ora Ohana: Data curation, Resources. Laurin Mordhorst: Software. Thomas Sauvigny: Data curation, Resources. Patrick Freund: Conceptualization, Project administration, Writing—review & editing. Karsten Tabelow: Conceptualization, Investigation, Methodology, Project administration, Software, Writing—review & editing. Siawoosh Mohammadi: Conceptualization, Formal analysis, Funding acquisition, Investigation, Methodology, Project administration, Resources, Software, Supervision, Writing—original draft, Writing—review & editing.

## DECLARATION OF COMPETING INTEREST

The authors declare no competing interests.

#### ETHICS STATEMENT

Three dMRI datasets from previous studies were reused in this paper. These studies complied with the principles of the Declaration of Helsinki and were approved by the local ethics committee (Ärztekammer Hamburg). The whole-brain dataset was measured in vivo (ethics approval number: PV5600). The dataset of the temporal lobe specimen was acquired ex vivo (PV5034). The spinal cord dataset was measured in vivo (PV5141).

#### ACKNOWLEDGMENTS

This work was supported by the German Research Foundation (DFG Priority Program 2041 "Computational Connectomics" (MO 2397/5-1, MO 2397/5-2)), the Emmy Noether Stipend (MO 2397/4-1 and 2397/4-2), the BMBF (01EW1711A and B) in the framework of ERA-NET NEURON, and the ERC (Acronym: MRStain, Grant agreement ID: 101089218, DOI: 10.3030/101089218). Views and opinions expressed are, however, those of the authors only and do not necessarily reflect those of the European Union or the European Research Council

Executive Agency. Neither the European Union nor the granting authority can be held responsible for them. Lars Ruthotto is supported in part by NSF awards (DMS 1751636 and DMS 2038118). Patrick Freund is funded by an SNF Eccellenza Professorial Fellowship grant (PCEFP3\_181362/1).

## SUPPLEMENTARY MATERIALS

Supplementary material for this article is available with the online version here: [https://doi.org/10.1162/imag\\_a](https://doi.org/10.1162/imag_a_00288) [\\_00288](https://doi.org/10.1162/imag_a_00288)

## **REFERENCES**

- <span id="page-19-6"></span>Ades-Aron, B., Veraart, J., Kochunov, P., McGuire, S., Sherman, P., Kellner, E., Novikov, D. S., & Fieremans, E. (2018). Evaluation of the accuracy and precision of the diffusion parameter EStImation with Gibbs and NoisE removal pipeline. *NeuroImage*, *183*, 532–543. [https://doi](https://doi.org/10.1016/j.neuroimage.2018.07.066) [.org/10.1016/j.neuroimage.2018.07.066](https://doi.org/10.1016/j.neuroimage.2018.07.066)
- <span id="page-19-11"></span>Aja-Fernández, S., Vegas-Sánchez-Ferrero, G., & Tristán-Vega, A. (2014). Noise estimation in parallel MRI: GRAPPA and SENSE. *Magnetic Resonance Imaging*, *32*(3), 281–290.<https://doi.org/10.1016/j.mri.2013.12.001>
- <span id="page-19-17"></span>Alexander, D. C., Dyrby, T. B., Nilsson, M., & Zhang, H. (2019). Imaging brain microstructure with diffusion MRI: Practicality and applications. *NMR in Biomedicine*, *32*(4), e3841. <https://doi.org/10.1002/nbm.3841>
- <span id="page-19-19"></span>Andersson, J. L. R. (2008). Maximum a posteriori estimation of diffusion tensor parameters using a Rician noise model: Why, how and but. *NeuroImage*, *42*(4), 1340–1356. [https://doi.org/10.1016/j.neuroimage.2008](https://doi.org/10.1016/j.neuroimage.2008.05.053) [.05.053](https://doi.org/10.1016/j.neuroimage.2008.05.053)
- <span id="page-19-3"></span>Andersson, J. L. R., & Sotiropoulos, S. N. (2016). An integrated approach to correction for off-resonance effects and subject movement in diffusion MR imaging. *NeuroImage*, *125*, 1063–1078. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2015.10.019) [.neuroimage.2015.10.019](https://doi.org/10.1016/j.neuroimage.2015.10.019)
- <span id="page-19-13"></span>Andersson, M., Pizzolato, M., Kjer, H. M., Skodborg, K. F., Lundell, H., & Dyrby, T. B. (2022). Does powder averaging remove dispersion bias in diffusion MRI diameter estimates within real 3D axonal architectures? *NeuroImage*, *248*, 118718. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2021.118718) [.neuroimage.2021.118718](https://doi.org/10.1016/j.neuroimage.2021.118718)
- <span id="page-19-14"></span>André, E. D., Grinberg, F., Farrher, E., Maximov, I. I., Shah, N. J., Meyer, C., Jaspar, M., Muto, V., Phillips, C., & Balteau, E. (2014). Influence of noise correction on intra- and inter-subject variability of quantitative metrics in diffusion kurtosis imaging. *PLoS One*, *9*(4), e94531. <https://doi.org/10.1371/journal.pone.0094531>
- <span id="page-19-22"></span>Ashburner, J. (2007). A fast diffeomorphic image registration algorithm. *NeuroImage*, *38*(1), 95–113. <https://doi.org/10.1016/j.neuroimage.2007.07.007>
- <span id="page-19-15"></span>Ashburner, J., & Friston, K. J. (2005). Unified segmentation. *NeuroImage*, *26*(3), 839–851. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2005.02.018) [.neuroimage.2005.02.018](https://doi.org/10.1016/j.neuroimage.2005.02.018)
- <span id="page-19-23"></span>Ashburner, J., & Friston, K. J. (2011). Diffeomorphic registration using geodesic shooting and Gauss-Newton optimisation. *NeuroImage*, *55*(3), 954–967. [https://doi.org](https://doi.org/10.1016/j.neuroimage.2010.12.049) [/10.1016/j.neuroimage.2010.12.049](https://doi.org/10.1016/j.neuroimage.2010.12.049)
- <span id="page-19-2"></span>Barazany, D., Basser, P. J., & Assaf, Y. (2009). In vivo measurement of axon diameter distribution in the corpus callosum of rat brain. *Brain*, *132*(5), 1210–1220. [https://](https://doi.org/10.1093/brain/awp042) [doi.org/10.1093/brain/awp042](https://doi.org/10.1093/brain/awp042)
- <span id="page-19-7"></span>Barker, G. J. (2001). Diffusion-weighted imaging of the spinal cord and optic nerve. *Journal of the Neurological Sciences*, *186*, 45–49. [https://doi.org/10.1016/S0022](https://doi.org/10.1016/S0022-510X(01)00490-7) [-510X\(01\)00490-7](https://doi.org/10.1016/S0022-510X(01)00490-7)
- <span id="page-19-16"></span>Basser, P. J., Mattiello, J., & LeBihan, D. (1994). Estimation of the effective self-diffusion tensor from the NMR spin echo. *Journal of Magnetic Resonance, Series B*, *103*(3), 247–254. <https://doi.org/10.1006/jmrb.1994.1037>
- <span id="page-19-12"></span>Basser, P. J., & Pajevic, S. (2000). Statistical artifacts in diffusion tensor MRI (DT-MRI) caused by background noise. *Magnetic Resonance in Medicine*, *44*(1), 41–50. [https://doi.org/10.1002/1522-2594\(200007\)44:1<41::AID](https://doi.org/10.1002/1522-2594(200007)44:1<41::AID-MRM8>3.0.CO;2-O) [-MRM8>3.0.CO;2-O](https://doi.org/10.1002/1522-2594(200007)44:1<41::AID-MRM8>3.0.CO;2-O)
- <span id="page-19-4"></span>Becker, S. M. A., Tabelow, K., Mohammadi, S., Weiskopf, N., & Polzehl, J. (2014). Adaptive smoothing of multishell diffusion weighted magnetic resonance data by msPOAS. *NeuroImage*, *95*, 90–105. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2014.03.053) [.1016/j.neuroimage.2014.03.053](https://doi.org/10.1016/j.neuroimage.2014.03.053)
- <span id="page-19-10"></span>Becker, S. M. A., Tabelow, K., Voss, H. U., Anwander, A., Heidemann, R. M., & Polzehl, J. (2012). Positionorientation adaptive smoothing of diffusion weighted magnetic resonance data (POAS). *Medical Image Analysis*, *16*(6), 1142–1155. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.media.2012.05.007) [.media.2012.05.007](https://doi.org/10.1016/j.media.2012.05.007)
- <span id="page-19-21"></span>Blaiotta, C., Freund, P., Cardoso, M. J., & Ashburner, J. (2017). Generative diffeomorphic atlas construction from brain and spinal cord MRI data. *ArXiv*. [http://arxiv.org](http://arxiv.org/abs/1707.01342) [/abs/1707.01342](http://arxiv.org/abs/1707.01342)
- <span id="page-19-24"></span>Büeler, S., Freund, P., Kessler, T. M., Liechti, M. D., & David, G. (2024). Improved inter-subject alignment of the lumbosacral cord for group-level in vivo gray and white matter assessments: A scan-rescan MRI study at 3T. *PLoS One*, *19*(4), e0301449. [https://doi.org/10.1371](https://doi.org/10.1371/JOURNAL.PONE.0301449) [/JOURNAL.PONE.0301449](https://doi.org/10.1371/JOURNAL.PONE.0301449)
- <span id="page-19-0"></span>Callaghan, P. T., Eccles, C. D., & Xia, Y. (1988). NMR microscopy of dynamic displacements: K-space and q-space imaging. *Journal of Physics E: Scientific Instruments*, *21*(8), 820–822. [https://doi.org/10.1088](https://doi.org/10.1088/0022-3735/21/8/017) [/0022-3735/21/8/017](https://doi.org/10.1088/0022-3735/21/8/017)
- <span id="page-19-18"></span>Caruyer, E., Lenglet, C., Sapiro, G., & Deriche, R. (2013). Design of multishell sampling schemes with uniform coverage in diffusion MRI. *Magnetic Resonance in Medicine*, *69*(6), 1534–1540. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.24736) [.24736](https://doi.org/10.1002/mrm.24736)
- <span id="page-19-5"></span>Chang, L. C., Jones, D. K., & Pierpaoli, C. (2005). RESTORE: Robust estimation of tensors by outlier rejection. *Magnetic Resonance in Medicine*, *53*(5), 1088–1095. <https://doi.org/10.1002/mrm.20426>
- <span id="page-19-20"></span>Chang, L. C., Walker, L., & Pierpaoli, C. (2012). Informed RESTORE: A method for robust estimation of diffusion tensor from low redundancy datasets in the presence of physiological noise artifacts. *Magnetic Resonance in Medicine*, *68*(5), 1654–1663. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.24173) [.24173](https://doi.org/10.1002/mrm.24173)
- <span id="page-19-1"></span>Chun, S. Y., Li, K. C., Xuan, Y., Xun, M. J., & Qin, W. (2005). Diffusion tensor tractography in patients with cerebral tumors: A helpful technique for neurosurgical planning and postoperative assessment. *European Journal of Radiology*, *56*(2), 197–204. [https://doi.org/10.1016/j.ejrad](https://doi.org/10.1016/j.ejrad.2005.04.010) [.2005.04.010](https://doi.org/10.1016/j.ejrad.2005.04.010)
- <span id="page-19-9"></span>Clark, I. A., Callaghan, M. F., Weiskopf, N., Maguire, E. A., & Mohammadi, S. (2021). Reducing susceptibility distortion related image blurring in diffusion MRI EPI data. *Frontiers in Neuroscience*, *15*, 955. [https://doi.org/10.3389/fnins](https://doi.org/10.3389/fnins.2021.706473) [.2021.706473](https://doi.org/10.3389/fnins.2021.706473)
- <span id="page-19-8"></span>Coelho, S., Baete, S. H., Lemberskiy, G., Ades-Aron, B., Barrol, G., Veraart, J., Novikov, D. S., & Fieremans, E. (2022). Reproducibility of the Standard Model of diffusion

in white matter on clinical MRI systems. *NeuroImage*, *257*, 119290. [https://doi.org/10.1016/j.neuroimage.2022](https://doi.org/10.1016/j.neuroimage.2022.119290) [.119290](https://doi.org/10.1016/j.neuroimage.2022.119290)

- <span id="page-20-13"></span>Cohen-Adad, J., Rossignol, S., & Hoge, R. (2009). Slice-byslice motion correction in spinal cord fMRI: SliceCorr. In *Proceedings of the 17th Scientific Meeting, International Society for Magnetic Resonance in Medicine, Honolulu, USA* (abstract #3181). [https://archive.ismrm.org/2009](https://archive.ismrm.org/2009/3181.html) [/3181.html](https://archive.ismrm.org/2009/3181.html)
- <span id="page-20-3"></span>Cohen, Y., Anaby, D., & Morozov, D. (2017). Diffusion MRI of the spinal cord: From structural studies to pathology. *NMR in Biomedicine*, *30*(3), e3592. [https://doi.org/10](https://doi.org/10.1002/nbm.3592) [.1002/nbm.3592](https://doi.org/10.1002/nbm.3592)
- <span id="page-20-10"></span>Constantinides, C. D., Atalar, E., & McVeigh, E. (1997). Signal-to-noise measurements in magnitude images from NMR phased arrays. *Proceedings of the Annual International Conference of the IEEE Engineering in Medicine and Biology*, *1*, 456–459. [https://doi.org/10](https://doi.org/10.1109/iembs.1997.754578) [.1109/iembs.1997.754578](https://doi.org/10.1109/iembs.1997.754578)
- <span id="page-20-8"></span>David, G., Freund, P., & Mohammadi, S. (2017). The efficiency of retrospective artifact correction methods in improving the statistical power of between-group differences in spinal cord DTI. *NeuroImage*, *158*, 296– 307.<https://doi.org/10.1016/j.neuroimage.2017.06.051>
- <span id="page-20-22"></span>David, G., Fricke, B., Oeschger, Jan, M., Ruthotto, L., Fritz, Francisco, J., Ohana, O., Sauvigny, T., Freund, P., Tabelow, K., & Mohammadi, S. (2024). *ACID: A Comprehensive Toolbox for Image Processing and Modeling of Brain, Spinal Cord, and Ex Vivo Diffusion MRI Data—Software*.<https://doi.org/10.20347/ACIDTBX>
- <span id="page-20-19"></span>David, G., Pfyffer, D., Vallotton, K., Pfender, N., Thompson, A., Weiskopf, N., Mohammadi, S., Curt, A., & Freund, P. (2021). Longitudinal changes of spinal cord grey and white matter following spinal cord injury. *Journal of Neurology, Neurosurgery and Psychiatry*, *92*, 1222–1230. <https://doi.org/10.1136/jnnp-2021-326337>
- <span id="page-20-14"></span>David, G., Seif, M., Huber, E., Hupp, M., Rosner, J., Dietz, V., Weiskopf, N., Mohammadi, S., & Freund, P. (2019). In vivo evidence of remote neural degeneration in the lumbar enlargement after cervical injury. *Neurology*, *92*(12), E1367–E1377. [https://doi.org/10.1212/WNL](https://doi.org/10.1212/WNL.0000000000007137) [.0000000000007137](https://doi.org/10.1212/WNL.0000000000007137)
- <span id="page-20-20"></span>David, G., Vallotton, K., Hupp, M., Curt, A., Freund, P., & Seif, M. (2022). Extent of cord pathology in the lumbosacral enlargement in non-traumatic versus traumatic spinal cord injury. *Journal of Neurotrauma*, *39*(9–10), 639–650. [https://doi.org/10.1089/neu.2021](https://doi.org/10.1089/neu.2021.0389) [.0389](https://doi.org/10.1089/neu.2021.0389)
- <span id="page-20-21"></span>De Groote, S., Goudman, L., Peeters, R., Linderoth, B., Vanschuerbeek, P., Sunaert, S., De Jaeger, M., De Smedt, A., & Moens, M. (2020). Magnetic resonance imaging exploration of the human brain during 10 kHz spinal cord stimulation for failed back surgery syndrome: A resting state functional magnetic resonance imaging study. *Neuromodulation*, *23*(1), 46–55. [https://doi.org/10](https://doi.org/10.1111/ner.12954) [.1111/ner.12954](https://doi.org/10.1111/ner.12954)
- <span id="page-20-15"></span>De Leener, B., Fonov, V. S., Collins, D. L., Callot, V., Stikov, N., & Cohen-Adad, J. (2018). PAM50: Unbiased multimodal template of the brainstem and spinal cord aligned with the ICBM152 space. *NeuroImage*, *165*, 170–179. [https://doi.org/10.1016/j.neuroimage.2017.10](https://doi.org/10.1016/j.neuroimage.2017.10.041) [.041](https://doi.org/10.1016/j.neuroimage.2017.10.041)
- <span id="page-20-5"></span>De Leener, B., Lévy, S., Dupont, S. M., Fonov, V. S. Stikov, N., Collins, D. L., Callot, V., & Cohen-Adad, J. (2017). SCT: Spinal Cord Toolbox, an open-source software for processing spinal cord MRI data. *NeuroImage*, *145*, 24–43. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2016.10.009) [.neuroimage.2016.10.009](https://doi.org/10.1016/j.neuroimage.2016.10.009)
- <span id="page-20-16"></span>Deppe, M., Krämer, J., Tenberge, J. G., Marinell, J., Schwindt, W., Deppe, K., Groppa, S., Wiendl, H., & Meuth, S. G. (2016). Early silent microstructural degeneration and atrophy of the thalamocortical network in multiple sclerosis. *Human Brain Mapping*, *37*(5), 1866–1879. <https://doi.org/10.1002/hbm.23144>
- <span id="page-20-17"></span>Deppe, M., Tabelow, K., Krämer, J., Tenberge, J. G., Schiffler, P., Bittner, S., Schwindt, W., Zipp, F., Wiendl, H., & Meuth, S. G. (2016). Evidence for early, non-lesional cerebellar damage in patients with multiple sclerosis: DTI measures correlate with disability, atrophy, and disease duration. *Multiple Sclerosis*, *22*(1), 73–84. [https://doi.org](https://doi.org/10.1177/1352458515579439) [/10.1177/1352458515579439](https://doi.org/10.1177/1352458515579439)
- <span id="page-20-11"></span>Dietrich, O., Raya, J. G., Reeder, S. B., Reiser, M. F., & Schoenberg, S. O. (2007). Measurement of signal-tonoise ratios in MR images: Influence of multichannel coils, parallel imaging, and reconstruction filters. *Journal of Magnetic Resonance Imaging*, *26*(2), 375–385. [https://](https://doi.org/10.1002/jmri.20969) [doi.org/10.1002/jmri.20969](https://doi.org/10.1002/jmri.20969)
- <span id="page-20-18"></span>Dossi, D. E., Chaves, H., Heck, E. S., Murúa, S. R., Ventrice, F., Bakshi, R., Quintana, F. J., Correale, J., & Farez, M. F. (2018). Effects of systolic blood pressure on brain integrity in multiple sclerosis. *Frontiers in Neurology*, *9*, 487. [https://doi.org/10.3389/fneur.2018](https://doi.org/10.3389/fneur.2018.00487) [.00487](https://doi.org/10.3389/fneur.2018.00487)
- <span id="page-20-1"></span>Draganski, B., Ashburner, J., Hutton, C., Kherif, F., Frackowiak, R. S. J., Helms, G., & Weiskopf, N. (2011). Regional specificity of MRI contrast parameter changes in normal ageing revealed by voxel-based quantification (VBQ). *NeuroImage*, *55*(4), 1423–1434. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2011.01.052) [.1016/j.neuroimage.2011.01.052](https://doi.org/10.1016/j.neuroimage.2011.01.052)
- <span id="page-20-0"></span>Dubois, J., Dehaene-Lambertz, G., Kulikova, S., Poupon, C., Hüppi, P. S., & Hertz-Pannier, L. (2014). The early development of brain white matter: A review of imaging studies in fetuses, newborns and infants. *Neuroscience*, *276*, 48–71. [https://doi.org/10.1016/j.neuroscience.2013](https://doi.org/10.1016/j.neuroscience.2013.12.044) [.12.044](https://doi.org/10.1016/j.neuroscience.2013.12.044)
- <span id="page-20-7"></span>Edwards, L. J., Pine, K. J., Ellerbrock, I., Weiskopf, N., & Mohammadi, S. (2017). NODDI-DTI: Estimating neurite orientation and dispersion parameters from a diffusion tensor in healthy white matter. *Frontiers in Neuroscience*, *11*, 720. [https://doi.org/10.3389/fnins](https://doi.org/10.3389/fnins.2017.00720) [.2017.00720](https://doi.org/10.3389/fnins.2017.00720)
- <span id="page-20-9"></span>Fan, Q., Nummenmaa, A., Witzel, T., Ohringer, N., Tian, Q., Setsompop, K., Klawiter, E. C., Rosen, B. R., Wald, L. L., & Huang, S. Y. (2020). Axon diameter index estimation independent of fiber orientation distribution using high-gradient diffusion MRI. *NeuroImage*, *222*, 117197. <https://doi.org/10.1016/j.neuroimage.2020.117197>
- <span id="page-20-2"></span>Farbota, K. D., Bendlin, B. B., Alexander, A. L., Rowley, H. A., Dempsey, R. J., & Johnson, S. C. (2012). Longitudinal diffusion tensor imaging and neuropsychological correlates in traumatic brain injury patients. *Frontiers in Human Neuroscience*, *6*, 1–15. <https://doi.org/10.3389/fnhum.2012.00160>
- <span id="page-20-12"></span>Fieremans, E., Jensen, J. H., & Helpern, J. A. (2011). White matter characterization with diffusional kurtosis imaging. *NeuroImage*, *58*(1), 177–188. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2011.06.006) [.neuroimage.2011.06.006](https://doi.org/10.1016/j.neuroimage.2011.06.006)
- <span id="page-20-6"></span>Friston, K. J., & Ashburner, J. (1997). Multimodal image coregistration and partitioning—A unified framework. *NeuroImage*, *6*(3), 209–217. [https://doi.org/10.1006/nimg](https://doi.org/10.1006/nimg.1997.0290) [.1997.0290](https://doi.org/10.1006/nimg.1997.0290)
- <span id="page-20-4"></span>Garyfallidis, E., Brett, M., Amirbekian, B., Rokem, A., van der Walt, S., Descoteaux, M., & Nimmo-Smith, I. (2014). Dipy, a library for the analysis of diffusion MRI data. *Frontiers in Neuroinformatics*, *8*, 8. [https://doi.org/10](https://doi.org/10.3389/fninf.2014.00008) [.3389/fninf.2014.00008](https://doi.org/10.3389/fninf.2014.00008)
- <span id="page-21-2"></span>Gerstner, E. R., & Sorensen, A. G. (2011). Diffusion and diffusion tensor imaging in brain cancer. *Seminars in Radiation Oncology*, *21*(2), 141–146. [https://doi.org/10](https://doi.org/10.1016/j.semradonc.2010.10.005) [.1016/j.semradonc.2010.10.005](https://doi.org/10.1016/j.semradonc.2010.10.005)
- <span id="page-21-6"></span>Gorgolewski, K. J., Auer, T., Calhoun, V. D., Craddock, R. C., Das, S., Duff, E. P., Flandin, G., Ghosh, S. S., Glatard, T., Halchenko, Y. O., Handwerker, D. A., Hanke, M., Keator, D., Li, X., Michael, Z., Maumet, C., Nichols, B. N., Nichols, T. E., Pellman, J., … Poldrack, R. A. (2016). The brain imaging data structure, a format for organizing and describing outputs of neuroimaging experiments. *Scientific Data*, *3*(1), 1–9. [https://doi.org/10](https://doi.org/10.1038/sdata.2016.44) [.1038/sdata.2016.44](https://doi.org/10.1038/sdata.2016.44)
- <span id="page-21-23"></span>Grabher, P., Mohammadi, S., Trachsler, A., Friedl, S., David, G., Sutter, R., Weiskopf, N., Thompson, A. J., Curt, A., & Freund, P. (2016). Voxel-based analysis of grey and white matter degeneration in cervical spondylotic myelopathy. *Scientific Reports*, *6*(1), 1–10. [https://doi.org/10.1038](https://doi.org/10.1038/srep24636) [/srep24636](https://doi.org/10.1038/srep24636)
- <span id="page-21-4"></span>Gu, X., & Eklund, A. (2019). Evaluation of six phase encoding based susceptibility distortion correction methods for diffusion MRI. *Frontiers in Neuroinformatics*, *13*, 76.<https://doi.org/10.3389/fninf.2019.00076>
- <span id="page-21-11"></span>Gudbjartsson, H., & Patz, S. (1995). The rician distribution of noisy MRI data. *Magnetic Resonance in Medicine*, *34*(6), 910–914. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.1910340618) [.1910340618](https://doi.org/10.1002/mrm.1910340618)
- <span id="page-21-25"></span>Hampel, F. R. (1974). The influence curve and its role in robust estimation. *Journal of the American Statistical Association*, *69*(346), 383. [https://doi.org/10.2307](https://doi.org/10.2307/2285666) [/2285666](https://doi.org/10.2307/2285666)
- <span id="page-21-14"></span>Hansen, B., Shemesh, N., & Jespersen, S. N. (2016). Fast imaging of mean, axial and radial diffusion kurtosis. *NeuroImage*, *142*, 381–393. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2016.08.022) [.neuroimage.2016.08.022](https://doi.org/10.1016/j.neuroimage.2016.08.022)
- <span id="page-21-1"></span>Horsfield, M. A., Lai, M., Webb, S. L., Barker, G. J., Tofts, P. S., Turner, R., Rudge, P., & Miller, D. H. (1996). Apparent diffusion coefficients in benign and secondary progressive multiple sclerosis by nuclear magnetic resonance. *Magnetic Resonance in Medicine*, *36*(3), 393–400. <https://doi.org/10.1002/mrm.1910360310>
- <span id="page-21-21"></span>Horsfield, M. A., Sala, S., Neema, M., Absinta, M., Bakshi, A., Sormani, M. P., Rocca, M. A., Bakshi, R., & Filippi, M. (2010). Rapid semi-automatic segmentation of the spinal cord from magnetic resonance images: Application in multiple sclerosis. *NeuroImage*, *50*(2), 446–455. [https://](https://doi.org/10.1016/j.neuroimage.2009.12.121) [doi.org/10.1016/j.neuroimage.2009.12.121](https://doi.org/10.1016/j.neuroimage.2009.12.121)
- <span id="page-21-13"></span>Howard, A. F., Cottaar, M., Drakesmith, M., Fan, Q., Huang, S. Y., Jones, D. K., Lange, F. J., Mollink, J., Rudrapatna, S. U., Tian, Q., Miller, K. L., & Jbabdi, S. (2022). Estimating axial diffusivity in the NODDI model. *NeuroImage*, *262*, 119535. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.neuroimage.2022.119535) [.neuroimage.2022.119535](https://doi.org/10.1016/j.neuroimage.2022.119535)
- <span id="page-21-24"></span>Huber, E., David, G., Thompson, A. J., Weiskopf, N., Mohammadi, S., & Freund, P. (2018). Dorsal and ventral horn atrophy is associated with clinical outcome after spinal cord injury. *Neurology*, *90*(17), E1510–E1522. <https://doi.org/10.1212/WNL.0000000000005361>
- <span id="page-21-20"></span>Jelescu, I. O., de Skowronski, A., Geffroy, F., Palombo, M., & Novikov, D. S. (2022). Neurite Exchange Imaging ((NEXI): A minimal model of diffusion in gray matter with inter-compartment water exchange. *NeuroImage*, *256*. [https://doi.org/10.1016/j.neuroimage](https://doi.org/10.1016/j.neuroimage.2022.119277) [.2022.119277](https://doi.org/10.1016/j.neuroimage.2022.119277)
- <span id="page-21-16"></span>Jelescu, I. O., Palombo, M., Bagnato, F., & Schilling, K. G. (2020). Challenges for biophysical modeling of microstructure. *Journal of Neuroscience Methods*, *344*, 108861.<https://doi.org/10.1016/j.jneumeth.2020.108861>
- <span id="page-21-15"></span>Jensen, J. H., Helpern, J. A., Ramani, A., Lu, H., & Kaczynski, K. (2005). Diffusional kurtosis imaging: The quantification of non-Gaussian water diffusion by means of magnetic resonance imaging. *Magnetic Resonance in Medicine*, *53*(6), 1432–1440. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.20508) [.20508](https://doi.org/10.1002/mrm.20508)
- <span id="page-21-10"></span>Jespersen, S. N., Olesen, J. L., Hansen, B., & Shemesh, N. (2018). Diffusion time dependence of microstructural parameters in fixed spinal cord. *NeuroImage*, *182*, 329– 342.<https://doi.org/10.1016/j.neuroimage.2017.08.039>
- <span id="page-21-8"></span>Jezzard, P., Barnett, A. S., & Pierpaoli, C. (1998). Characterization of and correction for eddy current artifacts in echo planar diffusion imaging. *Magnetic Resonance in Medicine*, *39*(5), 801–812. [https://doi.org](https://doi.org/10.1002/mrm.1910390518) [/10.1002/mrm.1910390518](https://doi.org/10.1002/mrm.1910390518)
- <span id="page-21-12"></span>Jones, D. K., & Basser, P. J. (2004). "Squashing peanuts and smashing pumpkins": How noise distorts diffusionweighted MR data. *Magnetic Resonance in Medicine*, *52*(5), 979–993.<https://doi.org/10.1002/mrm.20283>
- <span id="page-21-17"></span>Kellner, E., Dhital, B., Kiselev, V. G., & Reisert, M. (2016). Gibbs-ringing artifact removal based on local subvoxelshifts. *Magnetic Resonance in Medicine*, *76*(5), 1574– 1581.<https://doi.org/10.1002/mrm.26054>
- <span id="page-21-3"></span>Kelm, N. D., West, K. L., Carson, R. P., Gochberg, D. F., Ess, K. C., & Does, M. D. (2016). Evaluation of diffusion kurtosis imaging in ex vivo hypomyelinated mouse brains. *NeuroImage*, *124*, 612–626. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2015.09.028) [.1016/j.neuroimage.2015.09.028](https://doi.org/10.1016/j.neuroimage.2015.09.028)
- <span id="page-21-18"></span>Kharbanda, H. S., Alsop, D. C., Anderson, A. W., Filardo, G., & Hackney, D. B. (2006). Effects of cord motion on diffusion imaging of the spinal cord. *Magnetic Resonance in Medicine*, *56*(2), 334–339. [https://doi.org](https://doi.org/10.1002/mrm.20959) [/10.1002/mrm.20959](https://doi.org/10.1002/mrm.20959)
- <span id="page-21-19"></span>Koay, C. G., Chang, L. C., Carew, J. D., Pierpaoli, C., & Basser, P. J. (2006). A unifying theoretical and algorithmic framework for least squares methods of estimation in diffusion tensor imaging. *Journal of Magnetic Resonance*, *182*(1), 115–125. [https://doi.org/10.1016/j](https://doi.org/10.1016/j.jmr.2006.06.020) [.jmr.2006.06.020](https://doi.org/10.1016/j.jmr.2006.06.020)
- <span id="page-21-22"></span>Kugler, A. V., & Deppe, M. (2018). Non-lesional cerebellar damage in patients with clinically isolated syndrome: DTI measures predict early conversion into clinically definite multiple sclerosis. *NeuroImage: Clinical*, *19*, 633–639. <https://doi.org/10.1016/j.nicl.2018.04.028>
- <span id="page-21-0"></span>Le Bihan, D., Breton, E., Lallemand, D., Aubin, M. L., Vignaud, J., & Laval-Jeantet, M. (1988). Separation of diffusion and perfusion in intravoxel incoherent motion MR imaging. *Radiology*, *168*(2), 497–505. [https://doi.org](https://doi.org/10.1148/radiology.168.2.3393671) [/10.1148/radiology.168.2.3393671](https://doi.org/10.1148/radiology.168.2.3393671)
- <span id="page-21-5"></span>Leemans, A., Jeurissen, B., Sijbers, J., & Jones, D. K. (2009). ExploreDTI: A graphical toolbox for processing, analyzing, and visualizing diffusion MR data. In *Proceedings of the 17th Scientific Meeting, International Society for Magnetic Resonance in Medicine*, Honolulu, USA (abstract #3537). [https://archive.ismrm.org/2009](https://archive.ismrm.org/2009/3537.html) [/3537.html](https://archive.ismrm.org/2009/3537.html)
- <span id="page-21-7"></span>Littlejohns, T. J., Holliday, J., Gibson, L. M., Garratt, S., Oesingmann, N., Alfaro-Almagro, F., Bell, J. D., Boultwood, C., Collins, R., Conroy, M. C., Crabtree, N., Doherty, N., Frangi, A. F., Harvey, N. C., Leeson, P., Miller, K. L., Neubauer, S., Petersen, S. E., Sellors, J., … Allen, N. E. (2020). The UK Biobank imaging enhancement of 100,000 participants: Rationale, data collection, management and future directions. *Nature Communications*, *11*(1), 1–12. [https://doi.org/10.1038](https://doi.org/10.1038/s41467-020-15948-9) [/s41467-020-15948-9](https://doi.org/10.1038/s41467-020-15948-9)
- <span id="page-21-9"></span>Macdonald, J., & Ruthotto, L. (2018). Improved susceptibility artifact correction of echo-planar MRI using

the alternating direction method of multipliers. *Journal of Mathematical Imaging and Vision*, *60*(2), 268–282. <https://doi.org/10.1007/s10851-017-0757-x>

- <span id="page-22-23"></span>Mangin, J. F., Poupon, C., Clark, C., Le Bihan, D., & Bloch, I. (2002). Distortion correction and robust tensor estimation for MR diffusion imaging. *Medical Image Analysis*, *6*(3), 191–198. [https://doi.org/10.1016/S1361](https://doi.org/10.1016/S1361-8415(02)00079-8) [-8415\(02\)00079-8](https://doi.org/10.1016/S1361-8415(02)00079-8)
- <span id="page-22-18"></span>Manjón, J. V., Coupé, P., Concha, L., Buades, A., Collins, D. L., & Robles, M. (2013). Diffusion weighted image denoising using overcomplete local PCA. *PLoS One*, *8*(9), e73021. [https://doi.org/10.1371/JOURNAL](https://doi.org/10.1371/JOURNAL.PONE.0073021) [.PONE.0073021](https://doi.org/10.1371/JOURNAL.PONE.0073021)
- <span id="page-22-2"></span>Martin, A. R., Aleksanderek, I., Cohen-Adad, J., Tarmohamed, Z., Tetreault, L., Smith, N., Cadotte, D. W., Crawley, A., Ginsberg, H., Mikulis, D. J., & Fehlings, M. G. (2016). Translating state-of-the-art spinal cord MRI techniques to clinical use: A systematic review of clinical studies utilizing DTI, MT, MWF, MRS, and fMRI. *NeuroImage: Clinical*, *10*, 192–238. [https://doi.org/10](https://doi.org/10.1016/j.nicl.2015.11.019) [.1016/j.nicl.2015.11.019](https://doi.org/10.1016/j.nicl.2015.11.019)
- <span id="page-22-1"></span>Meinzer, M., Mohammadi, S., Kugel, H., Schiffbauer, H., Flöel, A., Albers, J., Kramer, K., Menke, R., Baumgärtner, A., Knecht, S., Breitenstein, C., & Deppe, M. (2010). Integrity of the hippocampus and surrounding white matter is correlated with language training success in aphasia. *NeuroImage*, *53*(1), 283–290. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2010.06.004) [.1016/j.neuroimage.2010.06.004](https://doi.org/10.1016/j.neuroimage.2010.06.004)
- <span id="page-22-11"></span>Miller, A. J., & Joseph, P. M. (1993). The use of power images to perform quantitative analysis on low SNR MR images. *Magnetic Resonance Imaging*, *11*(7), 1051–1056. [https://doi.org/10.1016/0730-725X\(93\)90225-3](https://doi.org/10.1016/0730-725X(93)90225-3)
- <span id="page-22-0"></span>Miller, S. P., Vigneron, D. B., Henry, R. G., Bohland, M. A., Ceppi-Cozzio, C., Hoffman, C., Newton, N., Partridge, J. C., Ferriero, D. M., & Barkovich, A. J. (2002). Serial quantitative diffusion tensor MRI of the premature brain: Development in newborns with and without injury. *Journal of Magnetic Resonance Imaging*, *16*(6), 621–632. <https://doi.org/10.1002/jmri.10205>
- <span id="page-22-12"></span>Modersitzki, J. (2009). *FAIR—Flexible Algorithms for Image Registration*. Society for Industrial and Applied Mathematics (SIAM). [https://epubs.siam.org/doi/book](https://epubs.siam.org/doi/book/10.1137/1.9780898718843) [/10.1137/1.9780898718843](https://epubs.siam.org/doi/book/10.1137/1.9780898718843)
- <span id="page-22-13"></span>Mohammadi, S., & Callaghan, M. F. (2021). Towards in vivo g-ratio mapping using MRI: Unifying myelin and diffusion imaging. *Journal of Neuroscience Methods*, *348*, 108990. <https://doi.org/10.1016/j.jneumeth.2020.108990>
- <span id="page-22-8"></span>Mohammadi, S., Carey, D., Dick, F., Diedrichsen, J., Sereno, M. I., Reisert, M., Callaghan, M. F., & Weiskopf, N. (2015). Whole-brain in-vivo measurements of the axonal G-ratio in a group of 37 healthy volunteers. *Frontiers in Neuroscience*, *9*, 1–13. [https://doi.org/10.3389/fnins](https://doi.org/10.3389/fnins.2015.00441) [.2015.00441](https://doi.org/10.3389/fnins.2015.00441)
- <span id="page-22-6"></span>Mohammadi, S., Freund, P., Feiweier, T., Curt, A., & Weiskopf, N. (2013). The impact of post-processing on spinal cord diffusion tensor imaging. *NeuroImage*, *70*, 377–385. [https://doi.org/10.1016/j.neuroimage.2012.12](https://doi.org/10.1016/j.neuroimage.2012.12.058) [.058](https://doi.org/10.1016/j.neuroimage.2012.12.058)
- <span id="page-22-19"></span>Mohammadi, S., Hutton, C., Nagy, Z., Josephs, O., & Weiskopf, N. (2013). Retrospective correction of physiological noise in DTI using an extended tensor model and peripheral measurements. *Magnetic Resonance in Medicine*, *70*(2), 358–369. [https://doi.org](https://doi.org/10.1002/mrm.24467) [/10.1002/mrm.24467](https://doi.org/10.1002/mrm.24467)
- <span id="page-22-4"></span>Mohammadi, S., Möller, H. E., Kugel, H., Müller, D. K., & Deppe, M. (2010). Correcting eddy current and motion effects by affine whole-brain registrations: Evaluation of three-dimensional distortions and comparison with

slicewise correction. *Magnetic Resonance in Medicine*, *64*(4), 1047–1056.<https://doi.org/10.1002/mrm.22501>

- <span id="page-22-9"></span>Mohammadi, S., Tabelow, K., Ruthotto, L., Feiweier, T., Polzehl, J., & Weiskopf, N. (2015). High-resolution diffusion kurtosis imaging at 3T enabled by advanced post-processing. *Frontiers in Neuroscience*, *9*, 427. <https://doi.org/10.3389/fnins.2014.00427>
- <span id="page-22-16"></span>Mollink, J., Kleinnijenhuis, M., van Cappellen van Walsum, A.-M., Sotiropoulos, S. N., Cottaar, M., Mirfin, C., Heinrich, M. P., Jenkinson, M., Pallebage-Gamarallage, M., Ansorge, O., Jbabdi, S., & Miller, K. L. (2017). Evaluating fibre orientation dispersion in white matter: Comparison of diffusion MRI, histology and polarized light imaging. *NeuroImage*, *157*, 561–574. [https://doi.org](https://doi.org/10.1016/j.neuroimage.2017.06.001) [/10.1016/j.neuroimage.2017.06.001](https://doi.org/10.1016/j.neuroimage.2017.06.001)
- <span id="page-22-14"></span>Novikov, D. S. (2021). The present and the future of microstructure MRI: From a paradigm shift to normal science. *Journal of Neuroscience Methods*, *351*, 108947. <https://doi.org/10.1016/j.jneumeth.2020.108947>
- <span id="page-22-15"></span>Novikov, D. S., Fieremans, E., Jespersen, S. N., & Kiselev, V. G. (2019). Quantifying brain microstructure with diffusion MRI: Theory and parameter estimation. *NMR in Biomedicine*, *32*(4), e3998. [https://doi.org/10.1002/nbm](https://doi.org/10.1002/nbm.3998) [.3998](https://doi.org/10.1002/nbm.3998)
- <span id="page-22-17"></span>Novikov, D. S., Veraart, J., Jelescu, I. O., & Fieremans, E. (2018). Rotationally-invariant mapping of scalar and orientational metrics of neuronal microstructure with diffusion MRI. *NeuroImage*, *174*, 518–538. [https://doi.org](https://doi.org/10.1016/j.neuroimage.2018.03.006) [/10.1016/j.neuroimage.2018.03.006](https://doi.org/10.1016/j.neuroimage.2018.03.006)
- <span id="page-22-5"></span>Oeschger, J. M., Tabelow, K., & Mohammadi, S. (2023a). Axisymmetric diffusion kurtosis imaging with Rician bias correction: A simulation study. *Magnetic Resonance in Medicine*, *89*(2), 787–799. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.29474) [.29474](https://doi.org/10.1002/mrm.29474)
- <span id="page-22-10"></span>Oeschger, J. M., Tabelow, K., & Mohammadi, S. (2023b). Investigating apparent differences between standard DKI and axisymmetric DKI and its consequences for biophysical parameter estimates. *BioRxiv*, 2023.06.21.545891. [https://doi.org/10.1101/2023.06.21](https://doi.org/10.1101/2023.06.21.545891) [.545891](https://doi.org/10.1101/2023.06.21.545891)
- <span id="page-22-20"></span>Palombo, M., Ianus, A., Guerreri, M., Nunes, D., Alexander, D. C., Shemesh, N., & Zhang, H. (2020). SANDI: A compartment-based model for non-invasive apparent soma and neurite imaging by diffusion MRI. *NeuroImage*, *215*, 116835. [https://doi.org/10.1016/j.neuroimage.2020](https://doi.org/10.1016/j.neuroimage.2020.116835) [.116835](https://doi.org/10.1016/j.neuroimage.2020.116835)
- <span id="page-22-3"></span>Papazoglou, S., Ashtarayeh, M., Oeschger, J. M., Callaghan, M. F., Does, M. D., & Mohammadi, S. (2024). Insights and improvements in correspondence between axonal volume fraction measured with diffusion-weighted MRI and electron microscopy. *NMR in Biomedicine*, *37*(3), e5070. <https://doi.org/10.1002/nbm.5070>
- <span id="page-22-22"></span>Paschoal, A. M., Zotin, M. C. Z., da Costa, L. M., dos Santos, A. C., & Leoni, R. F. (2022). Feasibility of intravoxel incoherent motion in the assessment of tumor microvasculature and blood–brain barrier integrity: A case-based evaluation of gliomas. *Magnetic Resonance Materials in Physics, Biology and Medicine*, *35*(1), 17–27. <https://doi.org/10.1007/s10334-021-00987-0>
- <span id="page-22-21"></span>Perone, C. S., Calabrese, E., & Cohen-Adad, J. (2018). Spinal cord gray matter segmentation using deep dilated convolutions. *Scientific Reports*, *8*(1), 1–13. [https://doi](https://doi.org/10.1038/s41598-018-24304-3) [.org/10.1038/s41598-018-24304-3](https://doi.org/10.1038/s41598-018-24304-3)
- <span id="page-22-7"></span>Pierpaoli, C., Walker, L., Irfanoglu, M. O., Barnett, A., Basser, P., Chang, L.-C., Koay, C., Pajevic, S., Rohde, G., Sarlls, J., & Wu, M. (2010). TORTOISE: An integrated software package for processing of diffusion MRI data. In *Proceedings of the 18th Scientific Meeting, International*

*Society for Magnetic Resonance in Medicine*, Stockholm, Sweden (abstract #1597). [https://archive.ismrm.org/2010](https://archive.ismrm.org/2010/1597.html) [/1597.html](https://archive.ismrm.org/2010/1597.html)

- <span id="page-23-12"></span>Polzehl, J., & Tabelow, K. (2016). Low SNR in diffusion MRI models. *Journal of the American Statistical Association*, *111*(516), 1480–1490. [https://doi.org/10.1080/01621459](https://doi.org/10.1080/01621459.2016.1222284) [.2016.1222284](https://doi.org/10.1080/01621459.2016.1222284)
- <span id="page-23-20"></span>Raja, R., Sinha, N., Saini, J., Mahadevan, A., Rao, K. N., & Swaminathan, A. (2016). Assessment of tissue heterogeneity using diffusion tensor and diffusion kurtosis imaging for grading gliomas. *Neuroradiology*, *58*(12), 1217–1231. [https://doi.org/10.1007/s00234-016](https://doi.org/10.1007/s00234-016-1758-y) [-1758-y](https://doi.org/10.1007/s00234-016-1758-y)
- <span id="page-23-17"></span>Roebroeck, A., Miller, K. L., & Aggarwal, M. (2019). Ex vivo diffusion MRI of the human brain: Technical challenges and recent advances. *NMR in Biomedicine*, *32*(4), e3941. <https://doi.org/10.1002/nbm.3941>
- <span id="page-23-14"></span>Rohde, G. K., Barnett, A. S., Basser, P. J., Marenco, S., & Pierpaoli, C. (2004). Comprehensive approach for correction of motion and distortion in diffusion-weighted MRI. *Magnetic Resonance in Medicine*, *51*(1), 103–114. <https://doi.org/10.1002/mrm.10677>
- <span id="page-23-23"></span>Rousseeuw, P. J., & Croux, C. (1993). Alternatives to the median absolute deviation. *Journal of the American Statistical Association*, *88*(424), 1273–1283. [https://doi](https://doi.org/10.1080/01621459.1993.10476408) [.org/10.1080/01621459.1993.10476408](https://doi.org/10.1080/01621459.1993.10476408)
- <span id="page-23-3"></span>Ruthotto, L., Kugel, H., Olesch, J., Fischer, B., Modersitzki, J., Burger, M., & Wolters, C. H. (2012). Diffeomorphic susceptibility artifact correction of diffusion-weighted magnetic resonance images. *Physics in Medicine and Biology*, *57*(18), 5715–5731. [https://doi.org/10.1088/0031](https://doi.org/10.1088/0031-9155/57/18/5715) [-9155/57/18/5715](https://doi.org/10.1088/0031-9155/57/18/5715)
- <span id="page-23-10"></span>Ruthotto, L., Mohammadi, S., Heck, C., Modersitzki, J., & Weiskopf, N. (2013). Hyperelastic susceptibility artifact correction of DTI in SPM. In *Proceedings of the German Workshop on Medical Image Computing (Informatik Aktuell)*, Heidelberg, Germany (pp. 344–349). [https://link](https://link.springer.com/chapter/10.1007/978-3-642-36480-8_60) [.springer.com/chapter/10.1007/978-3-642-36480-8\\_60](https://link.springer.com/chapter/10.1007/978-3-642-36480-8_60)
- <span id="page-23-16"></span>Salvador, R., Peña, A., Menon, D. K., Carpenter, T. A., Pickard, J. D., & Bullmore, E. T. (2005). Formal characterization and extension of the linearized diffusion tensor model. *Human Brain Mapping*, *24*(2), 144–155. <https://doi.org/10.1002/hbm.20076>
- <span id="page-23-18"></span>Schilling, K. G., Combes, A. J. E., Ramadass, K., Rheault, F., Sweeney, G., Prock, L., Sriram, S., Cohen-Adad, J., Gore, J. C., Landman, B. A., Smith, S. A., & O'Grady, K. P. (2024). Influence of preprocessing, distortion correction and cardiac triggering on the quality of diffusion MR images of spinal cord. *Magnetic Resonance Imaging*, *108*, 11–21.<https://doi.org/10.1016/j.mri.2024.01.008>
- <span id="page-23-2"></span>Scholz, J., Klein, M. C., Behrens, T. E. J., & Johansen-Berg, H. (2009). Training induces changes in white-matter architecture. *Nature Neuroscience*, *12*(11), 1370–1371. <https://doi.org/10.1038/nn.2412>
- <span id="page-23-8"></span>Sébille, S. B., Rolland, A. S., Welter, M. L., Bardinet, E., & Santin, M. D. (2019). Post mortem high resolution diffusion MRI for large specimen imaging at 11.7 T with 3D segmented echo-planar imaging. *Journal of Neuroscience Methods*, *311*, 222–234. [https://doi.org/10](https://doi.org/10.1016/j.jneumeth.2018.10.010) [.1016/j.jneumeth.2018.10.010](https://doi.org/10.1016/j.jneumeth.2018.10.010)
- <span id="page-23-21"></span>Seif, M., David, G., Huber, E., Vallotton, K., Curt, A., & Freund, P. (2020). Cervical cord neurodegeneration in traumatic and non-traumatic spinal cord injury. *Journal of Neurotrauma*, *37*(6), 860–867. [https://doi.org/10.1089](https://doi.org/10.1089/neu.2019.6694) [/neu.2019.6694](https://doi.org/10.1089/neu.2019.6694)
- <span id="page-23-4"></span>Sijbers, J., den Dekker, A. J., Scheunders, P., & Van Dyck, D. (1998). Maximum-likelihood estimation of rician distribution parameters. *IEEE Transactions on Medical*

*Imaging*, *17*(3), 357–361. [https://doi.org/10.1109/42](https://doi.org/10.1109/42.712125) [.712125](https://doi.org/10.1109/42.712125)

- <span id="page-23-5"></span>Smith, S. M., Jenkinson, M., Woolrich, M. W., Beckmann, C. F., Behrens, T. E. J., Johansen-Berg, H., Bannister, P. R., De Luca, M., Drobnjak, I., Flitney, D. E., Niazy, R. K., Saunders, J., Vickers, J., Zhang, Y., De Stefano, N., Brady, J. M., & Matthews, P. M. (2004). Advances in functional and structural MR image analysis and implementation as FSL. *NeuroImage*, *23*(Suppl. 1), S208–S219. [https://doi.org/10.1016/j.neuroimage.2004](https://doi.org/10.1016/j.neuroimage.2004.07.051) [.07.051](https://doi.org/10.1016/j.neuroimage.2004.07.051)
- <span id="page-23-22"></span>Sotiropoulos, S. N., Moeller, S., Jbabdi, S., Xu, J., Andersson, J. L., Auerbach, E. J., Yacoub, E., Feinberg, D., Setsompop, K., Wald, L. L., Behrens, T. E. J., Ugurbil, K., & Lenglet, C. (2013). Effects of image reconstruction on fiber orientation mapping from multichannel diffusion MRI: Reducing the noise floor using SENSE. *Magnetic Resonance in Medicine*, *70*(6), 1682–1689. [https://doi.org](https://doi.org/10.1002/mrm.24623) [/10.1002/mrm.24623](https://doi.org/10.1002/mrm.24623)
- <span id="page-23-0"></span>Stejskal, E. O., & Tanner, J. E. (1965). Spin diffusion measurements: Spin echoes in the presence of a timedependent field gradient. *The Journal of Chemical Physics*, *42*(1), 288–292.<https://doi.org/10.1063/1.1695690>
- <span id="page-23-7"></span>Stroman, P. W., Wheeler-Kingshott, C., Bacon, M., Schwab, J. M., Bosma, R., Brooks, J., Cadotte, D., Carlstedt, T., Ciccarelli, O., Cohen-Adad, J., Curt, A., Evangelou, N., Fehlings, M. G., Filippi, M., Kelley, B. J., Kollias, S., Mackay, A., Porro, C. A., Smith, S., … Tracey, I. (2014). The current state-of-the-art of spinal cord imaging: Methods. *NeuroImage*, *84*, 1070–1081. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2013.04.124) [.1016/j.neuroimage.2013.04.124](https://doi.org/10.1016/j.neuroimage.2013.04.124)
- <span id="page-23-1"></span>Sullivan, E. V., Rohlfing, T., & Pfefferbaum, A. (2010). Quantitative fiber tracking of lateral and interhemispheric white matter systems in normal aging: Relations to timed performance. *Neurobiology of Aging*, *31*(3), 464–481. [https://doi.org/10.1016/j.neurobiolaging](https://doi.org/10.1016/j.neurobiolaging.2008.04.007) [.2008.04.007](https://doi.org/10.1016/j.neurobiolaging.2008.04.007)
- <span id="page-23-15"></span>Summers, P., Staempfli, P., Jaermann, T., Kwiecinski, S., & Kollias, S. S. (2006). A preliminary study of the effects of trigger timing on diffusion tensor imaging of the human spinal cord. *American Journal of Neuroradiology*, *27*(9), 1952–1961. [https://www.ncbi.nlm.nih.gov/pmc/articles](https://www.ncbi.nlm.nih.gov/pmc/articles/PMC7977904/) [/PMC7977904/](https://www.ncbi.nlm.nih.gov/pmc/articles/PMC7977904/)
- <span id="page-23-19"></span>Szturm, T., Kolesar, T. A., Mahana, B., Goertzen, A. L., Hobson, D. E., Marotta, J. J., Strafella, A. P., & Ko, J. H. (2021). Changes in metabolic activity and gait function by dual-task cognitive game-based treadmill system in Parkinson's disease: Protocol of a randomized controlled trial. *Frontiers in Aging Neuroscience*, *13*, 283. [https://doi](https://doi.org/10.3389/fnagi.2021.680270) [.org/10.3389/fnagi.2021.680270](https://doi.org/10.3389/fnagi.2021.680270)
- <span id="page-23-9"></span>Tabelow, K., Balteau, E., Ashburner, J., Callaghan, M. F., Draganski, B., Helms, G., Kherif, F., Leutritz, T., Lutti, A., Phillips, C., Reimer, E., Ruthotto, L., Seif, M., Weiskopf, N., Ziegler, G., & Mohammadi, S. (2019). hMRI—A toolbox for quantitative MRI in neuroscience and clinical research. *NeuroImage*, *194*, 191–210. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2019.01.029) [.1016/j.neuroimage.2019.01.029](https://doi.org/10.1016/j.neuroimage.2019.01.029)
- <span id="page-23-11"></span>Tabelow, K., Mohammadi, S., Weiskopf, N., & Polzehl, J. (2015). POAS4SPM: A toolbox for SPM to denoise diffusion MRI data. *Neuroinformatics*, *13*(1), 19–29. <https://doi.org/10.1007/s12021-014-9228-3>
- <span id="page-23-13"></span>Tabesh, A., Jensen, J. H., Ardekani, B. A., & Helpern, J. A. (2011). Estimation of tensors and tensor-derived measures in diffusional kurtosis imaging. *Magnetic Resonance in Medicine*, *65*(3), 823–836. [https://doi.org](https://doi.org/10.1002/mrm.22655) [/10.1002/mrm.22655](https://doi.org/10.1002/mrm.22655)
- <span id="page-23-6"></span>Taylor, P. A., & Saad, Z. S. (2013). FATCAT: (An Efficient) functional and tractographic connectivity analysis

toolbox. *Brain Connectivity*, *3*(5), 523–535. [https://doi.org](https://doi.org/10.1089/brain.2013.0154) [/10.1089/brain.2013.0154](https://doi.org/10.1089/brain.2013.0154)

- <span id="page-24-2"></span>Tournier, J. D., Smith, R., Raffelt, D., Tabbara, R., Dhollander, T., Pietsch, M., Christiaens, D., Jeurissen, B., Yeh, C. H., & Connelly, A. (2019). MRtrix3: A fast, flexible and open software framework for medical image processing and visualisation. *NeuroImage*, *202*, 116137. <https://doi.org/10.1016/j.neuroimage.2019.116137>
- <span id="page-24-0"></span>Urbach, H., Flacke, S., Keller, E., Textor, J., Berlis, A., Hartmann, A., Reul, J., Solymosi, L., & Schild, H. H. (2000). Detectability and detection rate of acute cerebral hemisphere infarcts on CT and diffusion-weighted MRI. *Neuroradiology*, *42*(10), 722–727. [https://doi.org/10.1007](https://doi.org/10.1007/s002340000401) [/s002340000401](https://doi.org/10.1007/s002340000401)
- <span id="page-24-13"></span>Vallotton, K., David, G., Hupp, M., Pfender, N., Cohen-Adad, J., Fehlings, M. G., Samson, R. S., Gandini Wheeler-Kingshott, C. A. M., Curt, A., Freund, P., & Seif, M. (2021). Tracking white and gray matter degeneration along the spinal cord axis in degenerative cervical myelopathy. *Journal of Neurotrauma*, *38*(21), 2978–2987. <https://doi.org/10.1089/neu.2021.0148>
- <span id="page-24-4"></span>Van Essen, D. C., Smith, S. M., Barch, D. M., Behrens, T. E. J., Yacoub, E., & Ugurbil, K. (2013). The WU-Minn Human Connectome Project: An overview. *NeuroImage*, *80*, 62–79. <https://doi.org/10.1016/j.neuroimage.2013.05.041>
- <span id="page-24-11"></span>Van Essen, D. C., Ugurbil, K., Auerbach, E., Barch, D., Behrens, T. E. J., Bucholz, R., Chang, A., Chen, L., Corbetta, M., Curtiss, S. W., Della Penna, S., Feinberg, D., Glasser, M. F., Harel, N., Heath, A. C., Larson-Prior, L., Marcus, D., Michalareas, G., Moeller, S., … Yacoub, E. (2012). The Human Connectome Project: A data acquisition perspective. *NeuroImage*, *62*, 2222–2231. <https://doi.org/10.1016/j.neuroimage.2012.02.018>
- <span id="page-24-1"></span>Veraart, J., Novikov, D. S., Christiaens, D., Ades-aron, B., Sijbers, J., & Fieremans, E. (2016). Denoising of diffusion MRI using random matrix theory. *NeuroImage*, *142*, 394–406. [https://doi.org/10.1016/j.neuroimage.2016](https://doi.org/10.1016/j.neuroimage.2016.08.016) [.08.016](https://doi.org/10.1016/j.neuroimage.2016.08.016)
- <span id="page-24-9"></span>Veraart, J., Rajan, J., Peeters, R. R., Leemans, A., Sunaert, S., & Sijbers, J. (2013). Comprehensive framework for

## <span id="page-24-6"></span>APPENDIX A. IMPLEMENTATION AND **ORGANIZATION**

# APPENDIX A.1. INSTALLATION AND TOOLBOX **DOCUMENTATION**

The ACID toolbox is an extension of SPM12 that requires existing MATLAB and SPM12 installations. To run the toolbox without a Matlab license, ACID is also available as a compiled standalone version which only requires MAT-LAB Runtime [\(David et al., 2024\)](#page-20-22). The toolbox has been developed and tested with MATLAB versions R2017b to R2024a, and SPM12 from versions r6906 onward. It is recommended to use the latest SPM release, which can be downloaded from the SPM website,<sup>13</sup> as developments in ACID are synchronized with those in SPM.

accurate diffusion MRI parameter estimation. *Magnetic Resonance in Medicine*, *70*(4), 972–984. [https://doi.org](https://doi.org/10.1002/mrm.24529) [/10.1002/mrm.24529](https://doi.org/10.1002/mrm.24529)

- <span id="page-24-14"></span>Veraart, J., Sijbers, J., Sunaert, S., Leemans, A., & Jeurissen, B. (2013). Weighted linear least squares estimation of diffusion MRI parameters: Strengths, limitations, and pitfalls. *NeuroImage*, *81*, 335–346. <https://doi.org/10.1016/j.neuroimage.2013.05.028>
- <span id="page-24-8"></span>Veraart, J., Van Hecke, W., & Sijbers, J. (2011). Constrained maximum likelihood estimation of the diffusion kurtosis tensor using a Rician noise model. *Magnetic Resonance in Medicine*, *66*(3), 678–686. [https://doi.org/10.1002/mrm](https://doi.org/10.1002/mrm.22835) [.22835](https://doi.org/10.1002/mrm.22835)
- <span id="page-24-10"></span>Weiskopf, N., Edwards, L. J., Helms, G., Mohammadi, S., & Kirilina, E. (2021). Quantitative magnetic resonance imaging of brain anatomy and in vivo histology. *Nature Reviews Physics*, *3*, 570–588. [https://doi.org/10.1038](https://doi.org/10.1038/s42254-021-00326-1) [/s42254-021-00326-1](https://doi.org/10.1038/s42254-021-00326-1)
- <span id="page-24-5"></span>Woletz, M., Chalupa-Gantner, F., Hager, B., Ricke, A., Mohammadi, S., Binder, S., Baudis, S., Ovsianikov, A., Windischberger, C., & Nagy, Z. (2024). Toward printing the brain: A microstructural ground truth phantom for MRI. *Advanced Materials Technologies*, *9*(3), 2300176. <https://doi.org/10.1002/admt.202300176>
- <span id="page-24-7"></span>Yiannakas, M. C., Kearney, H., Samson, R. S., Chard, D. T., Ciccarelli, O., Miller, D. H., & Wheeler-Kingshott, C. A. M. (2012). Feasibility of grey matter and white matter segmentation of the upper cervical cord in vivo: A pilot study with application to magnetisation transfer measurements. *NeuroImage*, *63*(3), 1054–1059. [https://](https://doi.org/10.1016/j.neuroimage.2012.07.048) [doi.org/10.1016/j.neuroimage.2012.07.048](https://doi.org/10.1016/j.neuroimage.2012.07.048)
- <span id="page-24-3"></span>Zhang, H., Schneider, T., Wheeler-Kingshott, C. A., & Alexander, D. C. (2012). NODDI: Practical in vivo neurite orientation dispersion and density imaging of the human brain. *NeuroImage*, *61*(4), 1000–1016. [https://doi.org/10](https://doi.org/10.1016/j.neuroimage.2012.03.072) [.1016/j.neuroimage.2012.03.072](https://doi.org/10.1016/j.neuroimage.2012.03.072)
- <span id="page-24-12"></span>Zwiers, M. P. (2010). Patching cardiac and head motion artefacts in diffusion-weighted images. *NeuroImage*, *53*(2), 565–575. [https://doi.org/10.1016/j.neuroimage](https://doi.org/10.1016/j.neuroimage.2010.06.014) [.2010.06.014](https://doi.org/10.1016/j.neuroimage.2010.06.014)

Information about the toolbox can be found on the main project website.<sup>14</sup> The source code is available on Bitbucket,<sup>15</sup> where the latest version as well as all previous versions of the toolbox can be downloaded. There are four ways to install the toolbox: (i) by cloning the repository (recommended for staying up-to-date with the latest release), (ii) by downloading the toolbox as a zip file and placing the unzipped directory into the spm12/toolbox directory, (iii) by downloading the toolbox as a zip file and using a redirection script that enables switching between different local versions of ACID, or (iv) by downloading the compiled standalone version. The full documentation of the toolbox is available as a Wiki on the git repository, $16$  which provides

<sup>14</sup> <http://www.diffusiontools.com/>

<sup>15</sup> <https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri>

<sup>16</sup> [https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/wiki/Home) [/wiki/Home](https://bitbucket.org/siawoosh/acid-artefact-correction-in-diffusion-mri/wiki/Home)

<sup>13</sup> <http://www.fil.ion.ucl.ac.uk/spm/software/spm12/>



<span id="page-25-1"></span>Appendix Fig. A1. The left panel shows the location of the ACID toolbox in the SPM Batch Editor after successful installation (SPM -> Tools). The toolbox is organized into six modules, each of which may be further divided into submodules. The right panel provides an example of a submodule (*Diffusion Tensor Imaging* within the *Diffusion tensor/ kurtosis imaging* module). Each (sub-) module requires at least one mandatory input, indicated by "X," as well as several optional inputs and parameter settings, which can be adjusted for customization. Recommended settings for typical in vivo brain, in vivo spinal cord, and ex vivo dMRI datasets are presented in [Table 5.](#page-11-0)

detailed installation instructions, module descriptions, and step-by-step instructions for typical analysis pipelines.

ACID is free but copyrighted software, distributed under the terms of the GNU General Public License as published by the Free Software Foundation (either version 2 of the License or, at your option, any later version). Further details on "copyleft" can be found at the GNU website.17 It should be noted that ACID is supplied as is and no formal support or maintenance is provided. The toolbox was developed for academic research purposes only and comes with no warranty, nor is it intended for clinical and diagnostics use.

#### Appendix A.2. Organization of the toolbox

The ACID modules can be found in the SPM12 Batch Editor by navigating to  $SPM \rightarrow \text{Tools} \rightarrow \text{ACID Tool}$ box. The toolbox is divided into six modules, as shown in [Appendix Figure A1:](#page-25-1) *Startup*, *Pre-processing*, *Diffusion tensor/kurtosis imaging*, *Biophysical models*, *Utilities*, and *External tools*.

## Appendix A.3. Startup

The ACID modules rely on a set of default settings, which were selected to yield reasonable results for typical dMRI data. However, adjustments may be necessary depending on the specific dataset (see [Section 3.2](#page-9-0) for recommendations). For convenience, the module's graphical

user interface (GUI) only presents the settings that are likely to be modified. Advanced users can access and modify all settings through the script config/local/ acid local defaults.m. To use modified settings, the *Startup* module must be executed with the customized file provided as input; these settings will remain in effect even after restarting SPM or MATLAB until new settings are specified.

ACID requires all input images to be in NIfTI format (either NIfTI-1 or NIfTI-2), with dMRI data required to be in 4D NIfTI format. ACID also supports compressed NIfTI images with the extension .nii.gz and outputs compressed images for compressed input and uncompressed images for uncompressed input. Users can convert from DICOM to NIfTI format using SPM's DICOM Import function, which can also export metadata into JSON files if the "Export metadata" option is enabled. To bring dMRI data into the required format, the *Startup* module can be utilized to (i) convert a set of 3D NIfTI files into a single 4D NIfTI file, (ii) generate corresponding bval/bvec files from the JSON files (if not already available), (iii) create an additional metadata file containing the most commonly reported subject and acquisition parameters (such as TE and TR) to provide a concise overview of the dataset, and (iv) set an output directory alternative to the default one. The output from *Startup* can be automatically passed to subsequent processing steps through dependencies.

## <span id="page-25-0"></span>APPENDIX B. DETAILS ON ECMOCO

ECMOCO consists of four steps [\(Appendix Fig. B1](#page-26-0)):

<sup>17</sup> <http://www.gnu.org/copyleft/>



<span id="page-26-0"></span>Appendix Fig. B1. Registration scheme for an example dMRI dataset, which consists of two sets of nondiffusionweighted (b0) volumes (*n* volumes each) and two sets of diffusion-weighted (DW) volumes (*N* volumes each) interspersed with each other. The b0 and DW volumes form separate registration groups and are registered to their corresponding target volumes. First, the b0 volumes are registered using the rigid-body components of the specified degrees of freedom (DOF), followed by the registration of the DW volumes using all specified DOF. The parameter iteration for a given b0 or DW can be initialized using previously obtained transformation parameters (*initialized registration*).

- 1 The type of registration (*slice-wise* or *volume-wise*) and the degrees of freedom (DOF) for the affine transformation are specified by the user.
- 2 Shell-specific target volumes are generated, and transformation parameters are obtained between all nondiffusion-weighted (b0) volumes and their corresponding target. The parameter iteration for a given b0 volume can be initialized by the transformation parameters of the preceding b0 volume (*initialized registration*, see details below). Only the DOF associated with rigid-body transformation are estimated for b0 volumes, as eddy currents are expected to be negligible in b0 volumes due to the absence of diffusion-sensitizing gradients.
- 3 Transformation parameters are obtained between all diffusion-weighted (DW) volumes and their corresponding target. The parameter iteration for a given DW volume can be initialized by the interpolated transformation parameters from the b0 volumes (*initialized registration*, see details below).
- 4 The obtained transformation parameters are applied to reslice all volumes.

In addition to *slice-wise* registration, introduced in [Section 2.2.1](#page-2-1) and demonstrated in [Appendix Figure B2](#page-27-2), ACID incorporates two additional recent features: *initialized*  *registration* and *exclusion mode*. *Initialized registration* is based on the observation that transformation parameters obtained from high-SNR b0 volumes tend to be more accurate than those obtained from low-SNR DW volumes. With *initialized registration*, the parameter iteration for each b0 volume starts with the transformation parameters obtained from the preceding b0 volume. Once all the b0 volumes have been registered, their rigid-body transformation parameters are interpolated to the positions of the DW volumes situated between the b0 volumes. Subsequently, the parameter iteration for each DW starts with these interpolated values. If interpolation is not feasible (e.g., the DW volume is situated before the first or after the last b0 volume), the parameter iteration starts with the parameters obtained from the nearest b0 volume. This approach is particularly useful for correcting slow spatial drifts across volumes.

The *exclusion mode* is designed to address volumes with very low SNRs, which can make obtaining reliable transformation parameters difficult. Volumes that are considered not feasible for registration can be identified through visual inspection, for example, using the *DWI series browser* utility function, and can be input into ECMOCO. For these volumes, the rigid-body transformation parameters from the preceding nonexcluded volume are applied instead.



<span id="page-27-2"></span>Appendix Fig. B2. Qualitative comparison of different motion correction techniques including no correction, volumewise ECMOCO, and the combination of volume- and slice-wise ECMOCO. The plots show the concatenation of 1D cross-sections along the phase-encoding (PE) direction (anterior-posterior), extracted at fixed x- and z-coordinates from each of the 120 diffusion-weighted (DW) volumes in an in vivo spinal cord dMRI dataset. Additionally, zoomed-in views of a subset of DW volumes are provided to facilitate the assessment of improvements by ECMOCO. Substantial motion along the y-direction was initially observed, which was notably reduced after applying ECMOCO. Importantly, volume-wise ECMOCO did not entirely correct for spatial misalignments in all volumes (an example of failed correction is indicated by the red arrow). Conversely, the combination of volume- and slice-wise ECMOCO effectively corrected spatial misalignments in all DW volumes.

## <span id="page-27-1"></span>APPENDIX C. REGIONS FOR NOISE ESTIMATION

For optimal denoising (msPOAS, [Section 2.2.2](#page-3-0)) and Rician bias correction ([Section 2.2.3](#page-3-1)), it is crucial to accurately estimate the image noise within the appropriate region of interest. Noise measurements taken from regions outside the body are often suboptimal due to the lower parallelization factor (g-factor) at the edge compared with the center of the field of view. Instead, we recommend estimating the noise by considering two distinct scenarios, employing the *repeated measures* method in each case (see *Noise estimation* in [Table 2\)](#page-4-0). In datasets affected by (temporally varying) physiological artifacts, such as in in vivo brain and spinal cord datasets, we recommend estimating the noise across images with high b-values and within regions where the signal reaches the noise plateau (i.e., within cerebrospinal fluid compartments). For automatic ventricle segmentation within the brain, ACID provides an example segmentation batch located at ACID TPM/acid-ventricles-batch.m, which utilizes the *spm\_segment* function. In datasets unaffected by physiological artifacts, such as in ex vivo dMRI, we recommend estimating the noise across nondiffusionweighted (b0) images within either the entire specimen or a specific part. The latter recommendation, however, requires repeated measurements of b0 images. Example noise regions are shown in [Appendix Figure C1.](#page-27-3)

# <span id="page-27-0"></span>APPENDIX D. RECOMMENDATIONS FOR ADAPTIVE DENOISING (MSPOAS)

If the overall noise reduction is insufficient, *kstar* can be increased at the cost of longer computation time



<span id="page-27-3"></span>Appendix Fig. C1. Definition of noise regions of interest (ROI) for the *repeated measures* noise estimation method (see *Noise estimation* in [Table 2\)](#page-4-0). Binary noise ROIs are outlined in red. For in vivo brain and spinal cord dMRI, we recommend creating a noise ROI within the cerebrospinal fluid (CSF), such as the lateral ventricles in the brain and the subarachnoid space in the spinal cord, on the b0 images. Subsequently, we recommend estimating the noise on the images with the highest b-value (ideally above 1500 s/mm<sup>2</sup>) within the CSF mask. For ex vivo dMRI, the noise ROI is recommended to encompass the specimen itself, but noise estimation should be applied only on the b0 images. Since ex vivo dMRI is not affected by physiological artifacts, signal variations across the b0 images are considered noise.



<span id="page-28-1"></span>Appendix Fig. E1. Schematic illustration of how robust fitting down-weights outliers in the model fit. The scatter plot shows the logarithm of diffusion-weighted voxel intensities against the squared cosine of the angle ψ between the diffusion gradient direction (bvec) and the direction of the first eigenvector in a corpus callosum voxel (see blue crosshairs for location). Blue crosses in the scatter plot indicate data points not affected by artifacts ("No outliers"), while cyan crosses indicate data points affected by strong artifacts ("Outliers"). Outliers were generated by removing the center of the k-space of the original image to illustrate the effect of strong motion artifacts. Two example images corresponding to a nonartifactual ("No outlier," top image) and an artifactual data point ("Outlier," bottom image) are shown on the right. During the model fit, a linear curve is fitted to the logarithmic voxel intensities. The presence of outlier data points leads to a biased model fit (red line) and consequently biased tensor estimates when using ordinary least squares (OLS) model fitting. In contrast, robust fitting down-weights the influence of outliers, leading to a more accurate model fit (orange line) which is closer to the ground truth (green line) obtained by an OLS fit to the nonartifactual data points (blue crosses) only.

([Tabelow et al., 2015](#page-23-11)). It is important to note that msPOAS assumes a single global value of *sigma*, which may not always hold. If *sigma* is correctly estimated, the default *lambda* value will ensure optimal adaptation. Incorrect estimation of *sigma* can be compensated by the choice of *lambda*, which makes msPOAS robust against misspecification of *sigma* ([Becker et al., 2014\)](#page-19-4). We recommend determining *kappa* automatically based on the number of diffusion directions [\(Tabelow et al., 2015\)](#page-23-11). However, manual adjustment of *kappa* may be necessary in cases where the SNR is low (e.g., for spinal cord dMRI) or if the dataset has more images with high b-values than with low b-values. The effective number of coils (*ncoils)* is 1 when using SENSE1 reconstructions ([Polzehl](#page-23-12) [& Tabelow, 2016;](#page-23-12) [Sotiropoulos et al., 2013\)](#page-23-22), but the correct value is more difficult to determine when using multiple receiver channels (Aja-Ferná[ndez et al., 2014](#page-19-11)). It is important to use the same *ncoils* for the estimation of *sigma* and in msPOAS to ensure the same number of degrees of freedom.

# <span id="page-28-0"></span>APPENDIX E. MODEL FITTING METHODS IMPLEMENTED IN ACID

#### Appendix E.1. Ordinary least squares

Tensor fitting involves solving the linear regression problem  $y = Bα + ε$ , where y contains the logarithmic signals, *B* (b-matrix) contains the gradient directions and strengths,  $\alpha$  contains the elements of the diffusion tensor, and ε contains the model-fit errors (the difference between the actual and fitted signal). The ordinary least squares (OLS) approach employs the estimator function  $\rho(\varepsilon_i) = \varepsilon_i^2$ , where  $\varepsilon_i$  represents the model-fit error of acquisition *i*. The solution is obtained by minimizing  $\Sigma_i \varepsilon_i^2$ ,  $y$ ielding  $\alpha_{ols} = (B^T B)^{-1} B^T y$ .

## Appendix E.2. Weighted least squares

The weighted least squares (WLS) approach addresses the heteroscedasticity of the logarithmic data by assigning individual weights to each image in the form of  $\omega_i = \hat{S}_i/\sigma_i$ ,



<span id="page-29-0"></span>Appendix Fig. F1. The impact of Rician bias correction (RBC) on maps of biophysical parameter estimates, derived from the NODDI-DTI and WMTI-Watson models, including Watson concentration parameter (κ) and axonal water fraction (AWF), in an in vivo brain and spinal cord dataset (refer to [Table 4](#page-11-1) for details on the datasets). Being derived from white matter biophysical models, the parameter maps were masked for the white matter in the brain dataset. For the spinal cord, we refrained from masking due to the difficulty of obtaining an accurate white matter mask. These maps were computed both without (left column) and with (middle column) RBC; their voxel-wise difference, referred to as the Rician bias, is shown in the right column. RBC slightly decreased the mean of the kurtosis tensor in both the brain and spinal cord, which resulted in an increase in κ. The estimation of AWF using the NODDI-DTI model was not feasible in the spinal cord, as the mean diffusivity (MD) values derived from DTI fell below the range where the NODDI-DTI model provides a valid representation (refer to Equation (4) in [Edwards et al., 2017\)](#page-20-7). This discrepancy could be attributed to either the underestimation of MD due to kurtosis bias (Supplementary Fig. S3) or the invalidity of fixed compartmental diffusivities in the NODDI-DTI model.

where *S*ˆ *<sup>i</sup>* represents the unknown true signal (without noise) and σ*<sup>i</sup>* is the background noise for acquisition *i*. The estimator function now becomes  $\rho(\varepsilon_i) = (\omega_i \varepsilon_i)^2$ , yielding the solution  $\alpha_{\mathsf{w/s}} = \left(\boldsymbol{W}^{\boldsymbol{\tau}} \boldsymbol{B}^{\boldsymbol{\tau}} \boldsymbol{W} \boldsymbol{B}\right)^{-1} \boldsymbol{W}^{\boldsymbol{\tau}} \boldsymbol{B}^{\boldsymbol{\tau}} \boldsymbol{W} \boldsymbol{y}$ , with  $\boldsymbol{W}$  being the diagonal matrix of ω*<sup>i</sup>* . Note that OLS is a special case of WLS, where  $\omega_i = 1$  for all *i*. A practical consideration in obtaining α*wls* is related to estimating *S*<sup>ˆ</sup> *i* . One approach is to use the measured noisy signal  $\mathcal{S}_i$  as an estimate of  $\hat{\mathcal{S}}_i$ . Another approach is to start with the OLS solution and use the fitted signal as an estimate of *S*ˆ *i* , which was shown to be more accurate [\(Veraart, Sijbers, et al., 2013\)](#page-24-14).

#### <span id="page-29-1"></span>Appendix E.3. Robust fitting

The concept behind robust fitting is to assign lower weights to data points with higher model-fit errors during the fitting process ([Mangin et al., 2002\)](#page-22-23). The robust fitting method implemented in ACID is based on the "Patching ArTefacts from Cardiac and Head motion" (PATCH) technique introduced by [Zwiers \(2010\)](#page-24-12). While the form of the estimator function is similar to that of WLS, PATCH factorizes the weighting function ω*<sup>i</sup>* into three components as  $\omega_i = \omega_{i1} \omega_{i2} \omega_{i3}$ , where each component is designed to address different types of artifacts:  $\omega_{i1}$  and  $\omega_{i2}$  account for regional and slice-wise artifacts, respectively, while ω<sub>i3</sub> is identical to the weight term in WLS.  $\omega_{i1}$  and  $\omega_{i2}$  are expo- $-2)$ 

nentially decaying functions of 
$$
\varepsilon_i
$$
:  $\omega_{i1} = \exp\left(-\left[\frac{A_1 \varepsilon_i}{C_1}\right]^2\right)$ ,  
\n $\omega_{i2} = \exp\left(-\left[\frac{A_2 \varepsilon_{i,sl}}{C_2}\right]^2\right)$ , where  $\varepsilon_{i,sl} = \sum_{k=1}^n \frac{\varepsilon_{ik}}{\sqrt{n}}$  is the

slice-average model-fit error, with *n* being the number of voxels within the slice.  $A_1$  and  $A_2$  are model parameters, by default set to 0.3 and 0.1, respectively, with higher values resulting in a faster exponential decay.  $C_1$  and  $C_2$  are estimates of the standard deviation of ε*i* and ε*i*,*sl* , respectively, in the absence of outliers, and are computed



Appendix Fig. G1. Qualitative illustration of the effect of denoising on maps derived from diffusion kurtosis imaging (DKI). Shown are maps of axial diffusivity (AD), radial diffusivity (RD), mean kurtosis tensor (MW), axial kurtosis tensor (AW), and radial kurtosis tensor (RW). The maps were obtained by fitting the kurtosis model to simulated noisy dMRI data (signal + noise) with a signal-to-noise ratio (SNR) of 5, both before (no denoising) and after employing different denoising methods (msPOAS, LPCA, MP-PCA). The DKI metric maps obtained from the simulated noisefree dMRI data (signal only) are also shown for comparison (ground truth). The white matter mask used for calculating the normalized root-mean-square error (NRMSE) between the obtained DKI metrics and the ground truth is overlaid as a red segmentation line on the ground truth maps.

<span id="page-30-3"></span>as  $C_1 = 1.4826 \cdot \text{median}(|\epsilon_i|)$  and  $C_2 = 1.4826 \cdot \text{median}(|\epsilon_{i,sl}|)$ [\(Hampel, 1974;](#page-21-25) [Rousseeuw & Croux, 1993](#page-23-23)). Note that accurate estimation of  $C_1$  and  $C_2$  is crucial for effectively down-weighting outliers. This holds true as long as outliers are sparsely distributed and the median of the model-fit errors remains unaffected. However, a frequent occurrence of outliers can increase *C*, leading to a less effective down-weighting of outliers.

While OLS and WLS independently fit the tensor in each voxel, PATCH makes use of the observation that physiological noise represents a structured, spatially correlated noise. To accommodate the anticipated smoothness of *C*1, the median operator is spatially smoothed using a 2D Gaussian kernel before computing *C*1 ([Zwiers, 2010\)](#page-24-12).

As a modification to PATCH, the robust fitting method incorporates Tikhonov regularization to handle ill-conditioned weighting matrices resulting from a high

occurrence of outliers. This leads to the solution  $\boldsymbol{\alpha}_{\boldsymbol{\lambda}} = \left[ \boldsymbol{W}^{\boldsymbol{\tau}} \boldsymbol{B}^{\boldsymbol{\tau}} \boldsymbol{W} \boldsymbol{B} + \lambda \boldsymbol{B}^{\boldsymbol{\tau}} \boldsymbol{B} \right]$ −1 *W<sup>T</sup> BTWy*, where *W* represents the diagonal matrix of factorized weights, and λ is the Tikhonov regularization factor. Notably, in the two extreme cases, the Tikhonov solution either becomes  $\alpha_{\text{wls}}$  (albeit with a different **W**) ( $\lambda$  = 0) or converges to  $\alpha_{\text{ols}}$  $(\lambda \rightarrow \infty)$ . The above equation cannot be solved readily, as *W* is a function of ε, which is only available after obtaining the solution. This is addressed by using an iteratively reweighted least squares (IRLS) algorithm. In the first iteration, ω*<sup>i</sup>* is set to 1 for all *i* to obtain the OLS solution α*ols* and the initial ε. In the second iteration, an updated *W* is computed based on the initial ε, which is then used to compute  $\alpha_{\lambda}$ . In each further iteration,  $\varepsilon$  from the preceding iteration is used to update *W*, which is in turn used to compute the updated  $\alpha_{\lambda}$ . This iterative process is repeated until convergence or until the predefined number of iterations is exceeded.

## <span id="page-30-2"></span>Appendix E.4. Nonlinear least squares

The nonlinear least squares (NLLS) method solves the optimization problem  $\underline{\alpha}_{\textit{nlls}} = \underset{\alpha}{\text{argmin}} \sum_{i} (S_{b,\bar{g}} - m(\alpha))^2$ , where *m* represents the signal model (DTI or DKI), α the model parameters (elements of the diffusion and/or kurtosis tensors), and  $\mathsf{S}_{b,\vec{g}}$  the measured signal intensities for a specific diffusion weighting *b* and diffusion gradient direction  $\vec{g}$ . The NLLS optimization problem is solved using a Gauss–Newton algorithm.

# <span id="page-30-1"></span>APPENDIX F. EFFECT OF RICIAN BIAS CORRECTION ON BIOPHYSICAL PARAMETER ESTIMATES

Here, we demonstrate the influence of Rician bias correction on the estimation of Watson concentration parameter (κ) and axonal water fraction (AWF) ([Appendix Fig. F1\)](#page-29-0). These biophysical parameters were estimated on the fully processed dataset using either the NODDI-DTI model applied on a single (lower b-value) shell or the WMTI-Watson model applied on two shells. For an in-depth analysis of the impact of Rician bias correction on DKI and axisymmetric DKI, refer to [Oeschger et al. \(2023a\).](#page-22-5)

# <span id="page-30-0"></span>APPENDIX G. EVALUATING DENOISING **METHODS**

Several denoising methods have been developed, including the Multi-shell Position-Orientation Adaptive Smoothing (msPOAS; [Section 2.2.2](#page-3-0)) ([Becker et al.,](#page-19-4)  [2014](#page-19-4)), as well as methods based on local principal component analysis (LPCA) (Manjó[n et al., 2013\)](#page-22-18) and



<span id="page-31-0"></span>Appendix Fig. G2. Quantitative illustration of the effect of denoising on maps derived from diffusion kurtosis imaging (DKI) (one noise realization). The plots show the normalized root-mean-square error (NRMSE) between (i) DKI metrics obtained from simulated noisy dMRI data (signal + noise) with varying signal-to-noise ratios (SNR), both before (no denoising) and after employing different denoising methods (msPOAS, LPCA, MP-PCA), and (ii) DKI metrics obtained from noise-free dMRI data (signal only). NRMSE was computed across white matter voxels (see Appendix Fig. G1 for the white matter mask) for the following DKI metrics: axial diffusivity (AD), radial diffusivity (RD), mean kurtosis tensor (MW), axial kurtosis tensor (AW), and radial kurtosis tensor (RW). Denoising methods reduced NRMSE from the ground truth compared with the "no denoising" scenario only in the low-SNR domain, although not consistently for all DKI metrics. At high SNRs (above 30–40), denoising increased NRMSE for all DKI metrics, except for the MP-PCA method, which yielded results comparable with the "no denoising" scenario.



<span id="page-32-0"></span>Appendix Fig. G3. Quantitative illustration of the effect of denoising on maps derived from diffusion kurtosis imaging (DKI). The plots show the relative difference in DKI metrics obtained from simulated noisy dMRI data (signal + noise) with varying signal-to-noise ratios (SNR) after employing different denoising methods (msPOAS, LPCA, MP-PCA) to those obtained without denoising (one noise realization). The relative difference was computed across white matter voxels (see Appendix Fig. G1 for the white matter mask) for the following DKI metrics: axial diffusivity (AD), radial diffusivity (RD), mean kurtosis tensor (MW), axial kurtosis tensor (AW), and radial kurtosis tensor (RW). Denoising introduced substantial improvements in the investigated DKI metrics only in the low-SNR domain, although not consistently across all DKI metrics. When using msPOAS and LPCA, the relative differences were greater compared with using MP-PCA, with msPOAS introducing the highest bias. At high SNRs (above 30–40), the relative difference to the "no denoising" scenario was negligible for MP-PCA.

Marchenko-Pastur principal component analysis (MP-PCA) ([Veraart et al., 2016\)](#page-24-1). Here, we evaluated these three denoising methods using a simulated dMRI dataset of the human brain. Specifically, we fitted the kurtosis model to an in vivo brain dMRI dataset (refer to [Table 4](#page-11-1) for details on the dataset) and considered the fitted dMRI signal as the "noise-free" ground truth. Then, we added varying amounts of noise to the ground truth, drawn from a circularly symmetric complex normal distribution *CN*(0,  $\sigma^2$ ) with  $\sigma = \frac{S_0}{SNR}$ , using the same set of SNR values (SNR = 5, 15, 30, 39, 52, 100) as in our previous study [\(Oeschger et al., 2023b](#page-22-10)). The code for the simulation is available online.<sup>18</sup> For each SNR, the kurtosis model was fitted to the noisy magnitude dMRI data, both before (no denoising) and after denoising (msPOAS, LPCA, MP-PCA), using the nonlinear least squares (NLLS) algorithm implemented in ACID. Slices of axial diffusivity (AD), radial diffusivity (RD), mean kurtosis tensor (MW), axial kurtosis tensor (AW), and radial kurtosis tensor (RW) maps obtained from the dMRI data with the lowest SNR (SNR = 5) are shown in [Appendix Figure G1](#page-30-3). Deviations from the ground truth were quantified by computing the normalized root-mean-square error (NRMSE) between the obtained DKI metrics and the ground truth across

white matter voxels for one noise realization [\(Appendix](#page-31-0)  [Fig. G2](#page-31-0)). The white matter mask applied is overlaid on the ground truth DKI metric maps in [Appendix Figure G1](#page-30-3).

In general, denoising methods proved beneficial in reducing NRMSE from the ground truth compared with the "no denoising" scenario in the low-SNR domain, although not consistently across all DKI metrics. Specifically, denoising reduced NRMSE for RD and RW below an SNR of 15, and for AW below an SNR of 30. However, it did not reduce NRMSE for AD, and the trend was not clear for MW. At higher SNRs (above 30–40), denoising increased NRMSE for all DKI metrics compared with the nondenoised data, except for the MP-PCA denoising method, which yielded results comparable with the nondenoised scenario. The relative difference between the maps generated using denoising and those generated without denoising is shown in [Appen](#page-32-0)[dix Figure G3](#page-32-0). These results suggest that denoising (using any of the three methods) is beneficial for increasing the similarity to ground truth DKI metrics only in the low-SNR domain. In the high-SNR domain, denoising either does not lead to further improvements (MP-PCA) or even introduces additional errors (msPOAS and LPCA).

<sup>18</sup> <https://github.com/quantitative-mri-and-in-vivo-histology/esmrmb2024>