1	Supporting Information for
2	Thermodynamically inconsistent extreme precipitation
3	sensitivities across continents driven by cloud-radiative
4	effects
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20	This PDF file includes:
21 22 23	Figures from S1 to S16



Figure S1: same as figure 1 but with GPCP rainfall data.





35 Figure S2: Global distribution of cloud radiative effects (defined as the difference between 36 the "clear-sky" and "all-sky" radiative fluxes) for absorbed shortwave (A) and 37 downwelling longwave (C) radiation. Box plots for shortwave CRE (B) and downwelling 38 longwave CRE (D) separated into different zones. The tropical regions are classified as 39 grids between 23S and 23N, mid-latitudes as grids from 23S-55S and 23N-55N and high-40 latitudes as grids beyond 55S and 55N. The classification into humid and arid regions is 41 derived from the Budyko Aridity index, which is calculated as the ratio of mean annual 42 potential evapotranspiration to mean annual precipitation. The region is classified as humid 43 when aridity index is less than 1 and arid when it is greater than 1.



Figure S3: Variation of cloud radiative effects with precipitation for absorbed shortwave (blue) and Downwelling longwave (red) radiation.

- 52







57 Figure S4: (A) Comparison of daily estimated surface temperatures using the 58 thermodynamically constrained surface energy balance model against observations from 59 the NASA-CERES dataset. (B) Global map of root mean squared error (RMSE) between 60 the estimated surface temperatures and NASA-CERES observations, computed for the daily timeseries at each grid point. (C, D) same as (A, B) but for the comparison between 61 62 ERA-5 reanalysis data and NASA-CERES observations. Note: The surface temperature 63 was diagnosed from the upwelling longwave radiation from NASA-CERES dataset using 64 the Stefan-Boltzmann law.





Figure S5: (A) Comparison of the first-order sensitivity of daily surface temperatures to 70 changes in cloud cover, estimated by the thermodynamically constrained energy balance 71 72 model, with those derived from NASA-CERES observations. Each black dot represents the sensitivity at each grid point over land. (B) Same as (A) but for the comparison of cloud-73 cover sensitivities of ERA-5 surface temperatures with those derived from CERES 74 75 observations.



Figure S6: Variation of estimated temperature difference between "clear-sky" and "allsky" conditions (K) as a function of precipitation. Note: positive temperature difference
indicates cooling.





87 88 89 90 91 Figure S7: Global map of temperature difference between "clear-sky" and "all-sky" conditions.





95 96 Figure S8: same as figure 3 but with GPCP rainfall data.



Figure S9: Global map of extreme precipitation – temperature (EP-T) sensitivities for 99th
percentile rainfall (A, C) and 99.9th percentile rainfall (B, D) with observed temperatures
(A, B) and with corrected temperatures for cloud-effects (C, D). Note the rainfall and
temperature data is from CPC.





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Figure S10: Global map of extreme precipitation (P95) – temperature (EP-T) sensitivities estimated from ERA-5 data using temperatures (A) with cloud-cooling and (B) after correcting for cloud-cooling, (C) zonal variation of estimated EP-T sensitivities with and

114 without the cloud effects as red and blue respectively.







Figure S11: Maps of EP-T sensitivities for observations (C), Net cloud radiative effect on 119 120 extreme rainfall (P95) days (D) and EP-T sensitivities after correcting for cloud-effects (E) isolated over Southeast Asia region. Black solid and black dotted boxes further separate 121 122 these regions into two parts. (A, E) shows the scaling curves of extreme precipitation with 123 observed temperatures (red line) and temperatures corrected for cloud-effects (blue-line) 124 for grids within black solid box and black dotted box respectively. (B, F) shows the variation of net cloud radiative effect with rainfall for grids within black solid box and 125 126 black dotted box respectively.





Figure S12: (A) Comparison of estimated daily sea surface temperatures with the energy balance model with temperatures derived from (NASA-CERES). Root mean squared error (RMSE) between daily estimated and observed temperatures from CERES across all the oceanic grids. Global map of extreme precipitation-temperature sensitivities over oceanic grids with (C) observed temperatures and (D) temperatures corrected for cloud-effects.





Figure S13: Grids exhibiting super CC scaling (EP-T sensitivity $> 7\%/^{\circ}$ C) in observations 142 (A, B) and ERA-5 reanalysis (C, D) with cloud-effects (A, C) and after correcting for

- 142 (A, B) and ERA-5 re143 cloud-effects (B, D).



148

Figure S14: Deviation in EP-T sensitivities (P95) from CC rate (7%/°C) after correcting for cloud-effects as a function of (A) standardized anomalies in vertical pressure velocity at 650 hpa on extreme rainfall (P95) days and (B) standardized anomalies in the temperature difference between cloud-base and cloud-top on extreme rainfall days (P95).
(C, D) same as (A, B) but for grids between 30S and 30N.



159 Figure S15: (Top row) Global map of extreme precipitation-temperature sensitivities estimated using quantile regression with (A) observed temperatures, (B) 1-day time lagged 160 temperatures and (C) temperatures corrected for cloud-radiative effects. (Bottom row-D) 161 Comparison of EP-T scaling rates estimated using observed temperatures (red), time-162 163 lagged temperatures (orange) and with temperatures corrected for the cloud-cooling effect 164 (blue) for tropics, mid-latitudes and high-latitudes. (E) same as (D) but for the residuals 165 between observations and fitted quantile regression 166







171 Figure S16: Variation along the Budyko aridity index (defined as the ratio between mean

172 net radiation and the energy equivalent to mean annual precipitation, where higher values

173 (> 1) indicate more arid conditions) of (A) Net Cloud radiative effects (W/m^2) and (B)

174 Extreme precipitation-temperature scaling after removing the effect of clouds.