



# T- and p-Measurement

Wolfgang Ranke  
Dep. Inorganic Chemistry  
Group Surface Analysis  
Fritz-Haber-Institut der MPG

For script:  
see homepage

or

mail to: [ranke@fhi-berlin.mpg.de](mailto:ranke@fhi-berlin.mpg.de)

## Content:

### T

Resistance T-detectors  
Thermocouple  
Pyrometer  
Comparison

### P

Direct: Mechanical force  
Indirect: Heat conductivity  
Indirect: Gas ionization  
gauge combinations  
QMS

### **Literature - T-measurement:**

F.X. Eder, Arbeitsmethoden der Thermodynamik, Bd. I, Springer, Berlin 1981.

L. Weichert et al., Temperaturmessung in der Technik, Lexika-Verlag, Grafenau, 1976.

F. Henning, Temperaturmessung, H. Moser ed., Springer, Berlin 1977.

G. Heyne, Einführung in die elektronische Messtechnik, 1997.

M. v. Ardenne, G. Musiol, S. Reball, Effekte der Physik und ihre Anwendungen, Deutsch, Thun, 1997.

Catalogs from Heraeus Sensor GmbH, Hanau:

Temperaturmessung mit Thermoelementen, Ausgleichsleitungen..., Mantel-Thermoelemente,  
Temperaturmessung mit Widerstandsthermometern, Messwiderstände

Pyrometerhandbuch, IMPAC Infrared GmbH, Frankfurt 2004.

<http://www.ir-impac.com/deutsch/Pyrometerhandbuch.pdf>

Wikipedia English: <http://en.wikipedia.org>

German: <http://de.wikipedia.org>

### **Literature - p-measurement:**

W. Pupp, H.K. Hartmann, Vakuumtechnik, Grundlagen und Anwendungen, Carl Hanser, München (1991).

M. Wutz, H. Adam, W. Walcher, Theorie und Praxis der Vakuumtechnik, Vieweg, Braunschweig (1982). (*New edition available*).

Leybold-Heraeus GmbH, Grundlagen der Vakuumtechnik, Berechnungen und Tabellen.

A. Roth, Vacuum Technology, North Holland, Amsterdam (1976).

J.F. O'Hanlon, A User's Guide to Vacuum Technology, 2<sup>nd</sup> ed. Wiley, New York (1989).

N.S. Harris, Modern Vacuum Practice, McGraw-Hill, Maidenhead (1989).

**T**

**emperature**

# Temperature measurement

## Simplest definition of temperature:

$$p V = n R T.$$

(ideal gas law, „zeroth law“ of thermodynamics)

For a given amount of gas (n moles), T is simply given by p and V

→ gas thermometer.

## Practical T-measurement uses:

Thermal expansion of

gases  
liquids  
solids

gas thermometer  
„normal“ thermometers  
bimetal thermometers

T-dependent electrical resistance

metals  
semicond.

resistance T-detectors  
diodes, thermistors

T-dependence of work function  
(Seebeck-effect)

metals

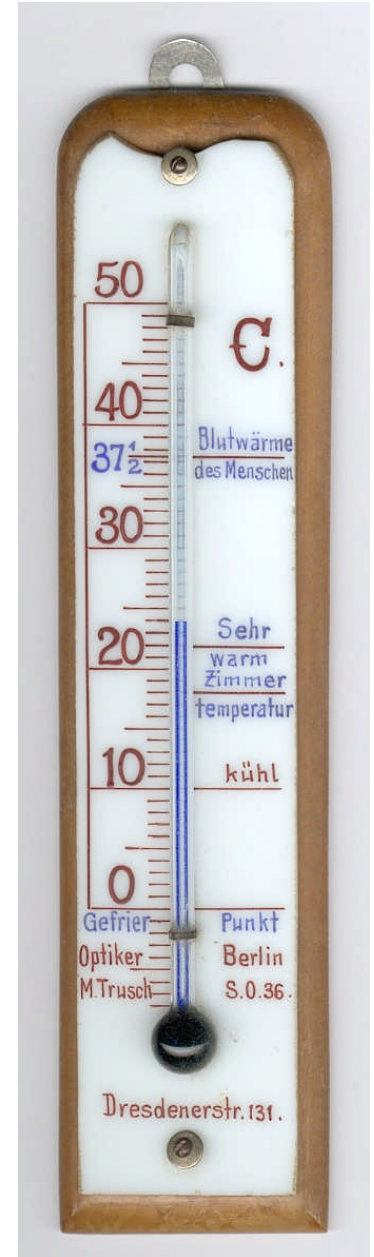
thermocouple

Radiation detectors

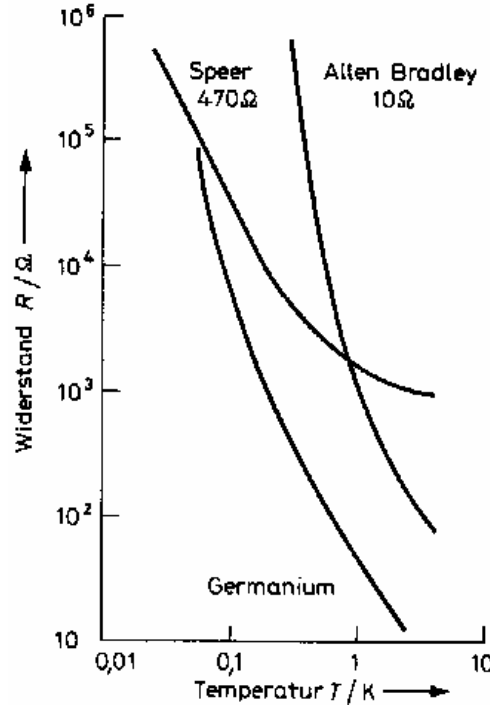
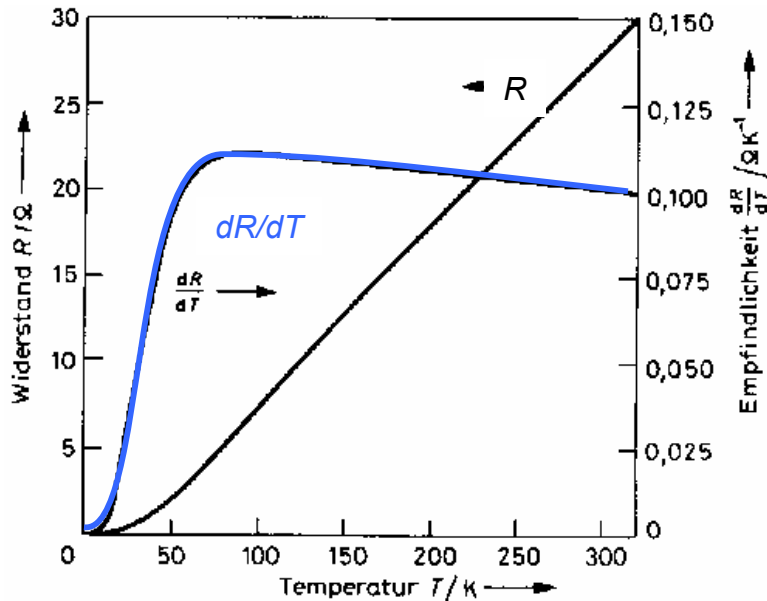
via heat  
direct

bolometer, thermopile  
pyrometer

More information: => separate sheet



# T-measurement - Resistance T-detectors



**Metals (Pt):** R almost linear with T

Empirically  
for standard Pt resistors,  $R_{0^\circ C} = 100\Omega$ ):

$0 < t < 850^\circ C$ :

$$R_t = 100 (1 + 3.90802 \times 10^{-3} t - 0.5802 \times 10^{-6} t^2)$$

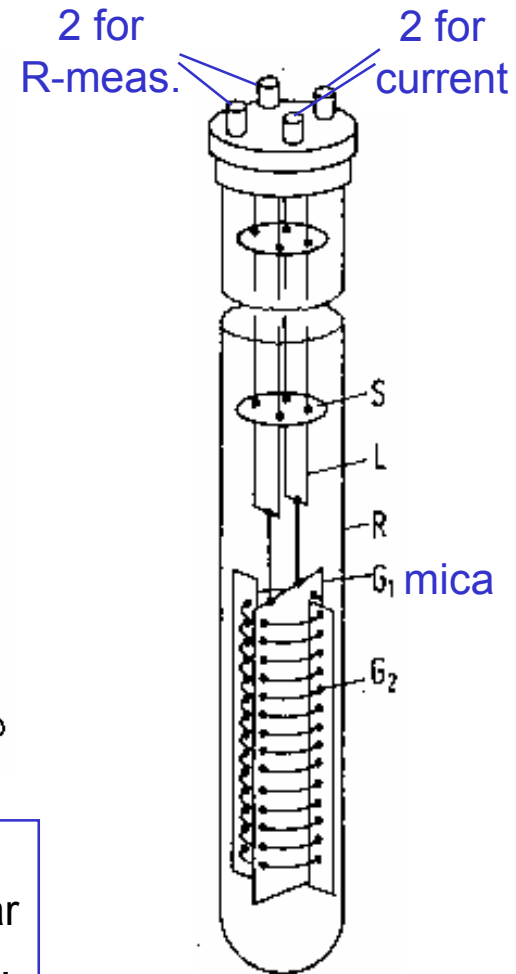
$-200 < t < 0^\circ C$

$$R_t = 100 (1 + 3.90802 \times 10^{-3} t - 0.5802 \times 10^{-6} t^2 + 0.42735 \times 10^{-9} t^3 - 4.2735 \times 10^{-12} t^4)$$

Max deviation:  
+-(0.3+0.005 |t|) (class B)

**Semiconductors:**  
Strong but nonlinear  
T-dependence of R,  
used at low T.

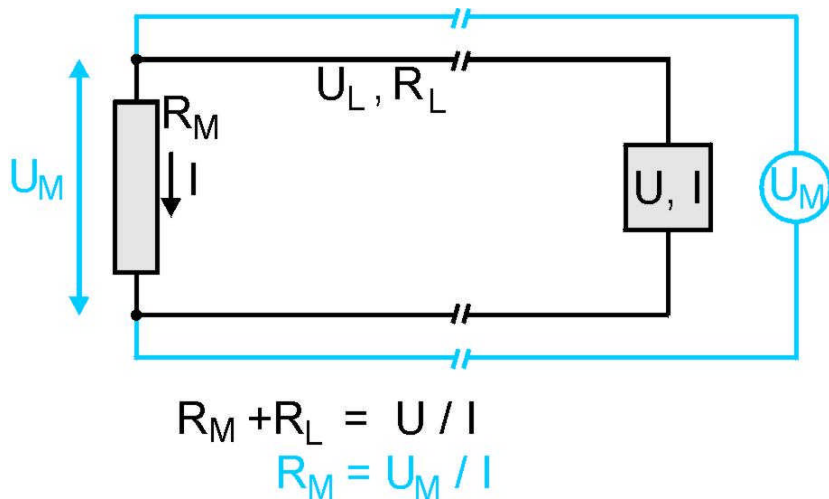
Thermistor:  
T-dependence of  
transistor properties



*Pt-Resistance thermometer for calibration (NBS) secondary standard*

## T-measurement - Resistance T-detectors

How to measure R precisely? – Don't forget the resistance of the wiring!



In order to measure a resistance  $R_M$ , always a current has to be passed through it. Then, according to Ohm's law,

$$R_{\text{tot}} = U / I.$$

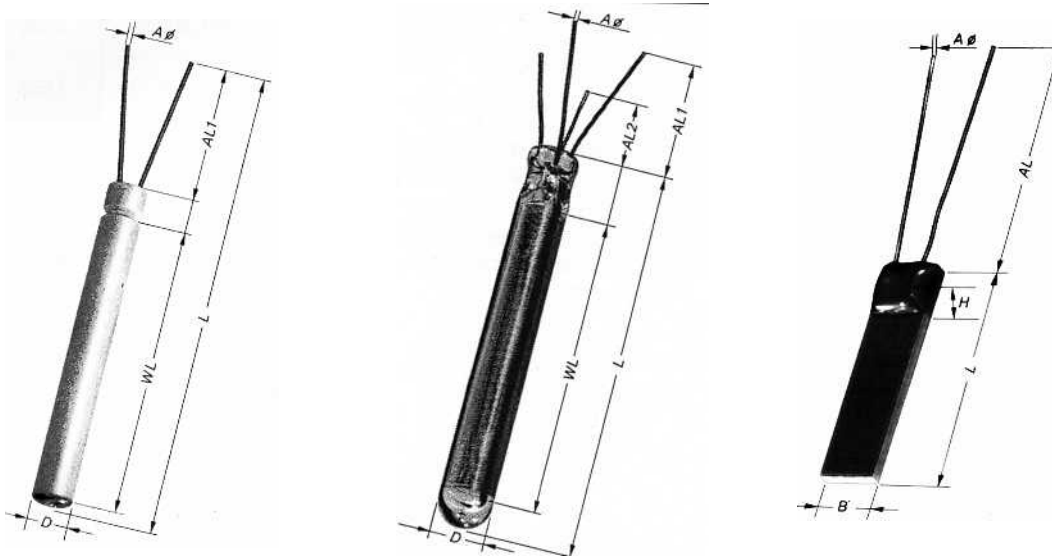
Part of the voltage drops along the wires with their resistance  $R_L$  (which usually is not precisely known).

Therefore,  $U_M$  has to be measured separately (blue wires):

**Four-wire-technique**

# T-measurement - Resistance T-detectors

Examples of resistance sensors (Heraeus)



Ex.1:  
 Pt in ceramics  
 -200°C to +850°C  
 WL                    20mm  
 D                      1.5mm  
 t1/2 (water)    0.2s  
                   (air 1 m/s) 5s

Ex.2:  
 Pt in glass, 2 filaments  
 0°C to +600°C  
 WL                    30mm  
 D                      5mm  
 t1/2 (water)    0.8s  
                   (air 1 m/s) 13s

Ex.2:  
 Pt film on ceramics  
 -70°C to +500°C  
 L                      min. 3.9mm  
 B                      min. 1.9mm  
 t1/2 (water)    0.1s  
                   (air 1 m/s) 5s

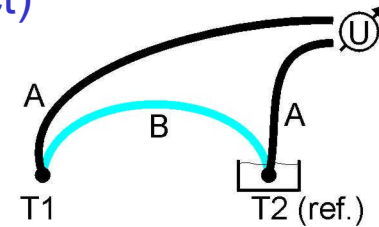
*Complete  
 resistance  
 thermometers  
 (resistors  
 in housing)*

two galvanically separated filaments:  
 one for T-display  
 one for process control

## T-measurement - Thermocouple (Seebeck-effect)

Advantages: small, fast, simple, electrical signal

Disadvantages: reference T needed



standard:  
 $T_{ref} = 0^{\circ}\text{C}$

Ty pe	Material	Symbol	Temp. range ( $^{\circ}\text{C}$ )
<b>K</b>	nickel-chromium / nickel „chromel-alumel“	NiCr-Ni	-200...900 (1300)
<b>J</b>	iron / copper-nickel „iron-konstantan“	Fe-CuNi	-200...700 (1200)
<b>N</b>	nickel-chromium-silicon / nickel- silicon, „nicrosil-nisil“	NiCrSi-NiSi	-200...1200
<b>E</b>	nickel-chromium / copper-nickel „chromel-konstantan“	NiCr-CuNi	-200...900 (1000)
<b>T</b>	copper / copper-nickel „copper-konstantan“	Cu-CuNi	-200...400
<b>S</b>	platinum-10rhodium./platinum	Pt10%Rh-Pt	0...1300 (1700)
<b>R</b>	platinum-13rhodium./platinum	Pt13%Rh-Pt	0...1300 (1600)
<b>B</b>	platinum-30rhodium./platinum- 6rhodium	Pt30%Rh- Pt6%Rh	0...1800

More  
information  
=>  
separate  
sheet

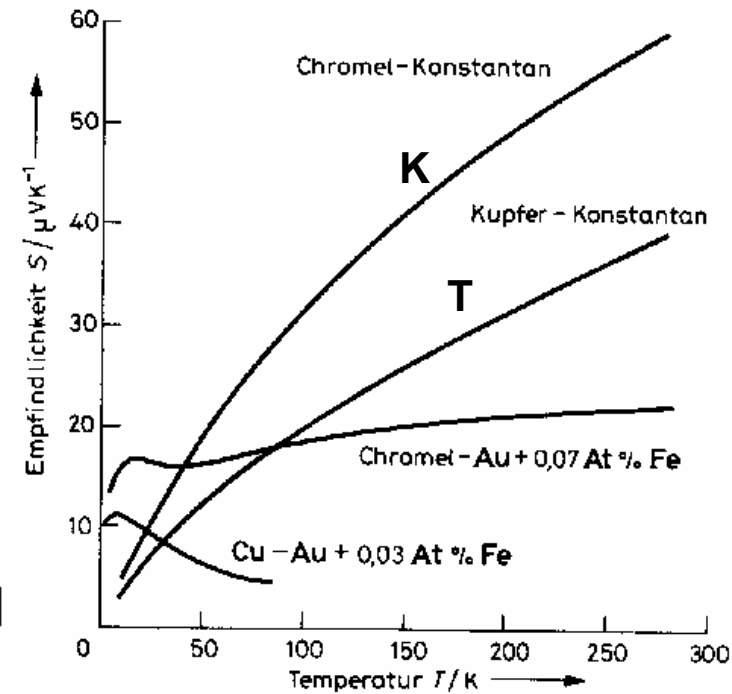
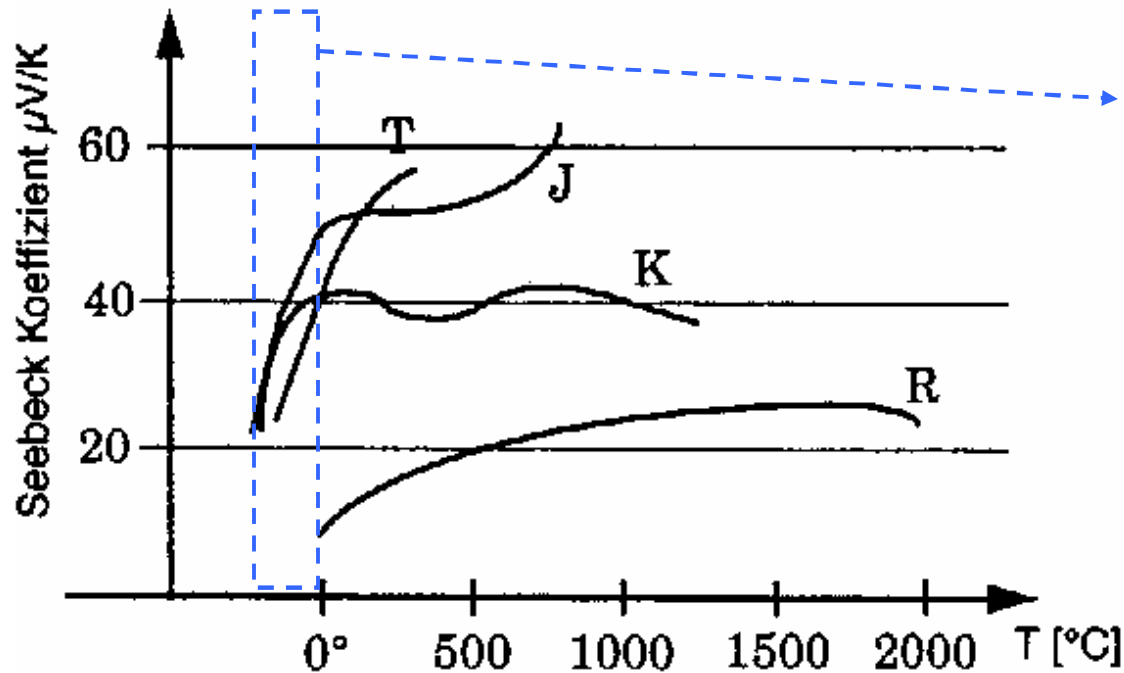
values in ( ): not for permanent use, not in reactive atmosphere



## T-measurement - Thermocouple

Thermovoltage generally not linear in T

Low T: generally more problematic.



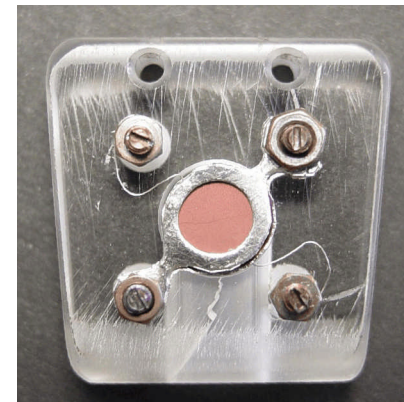
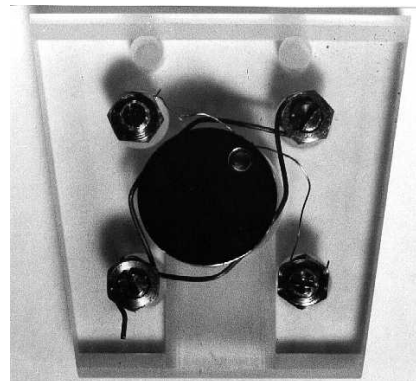
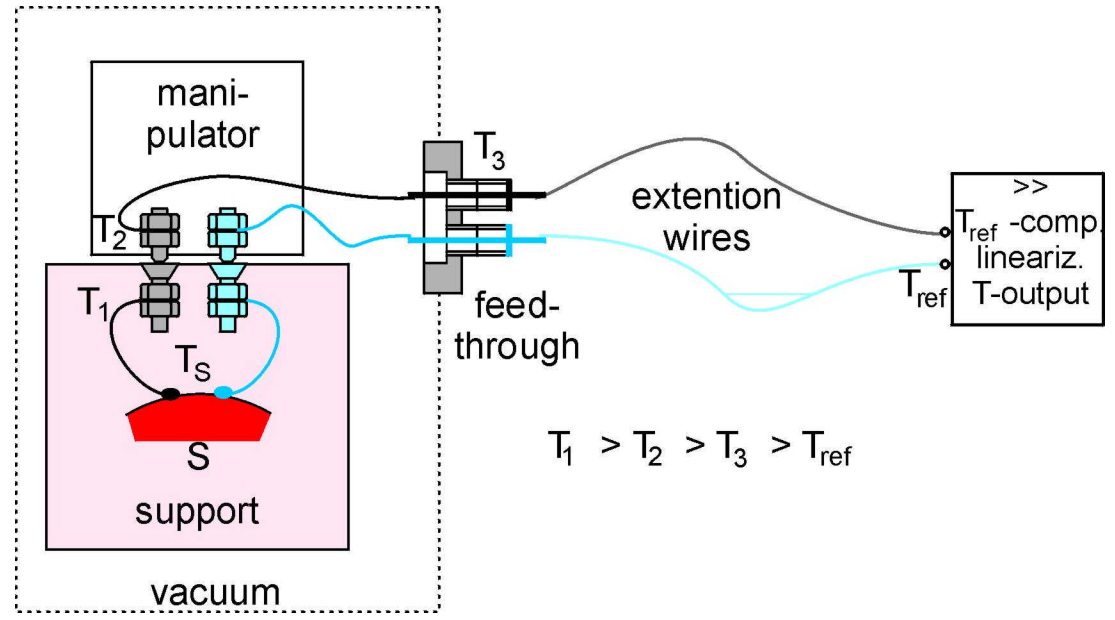
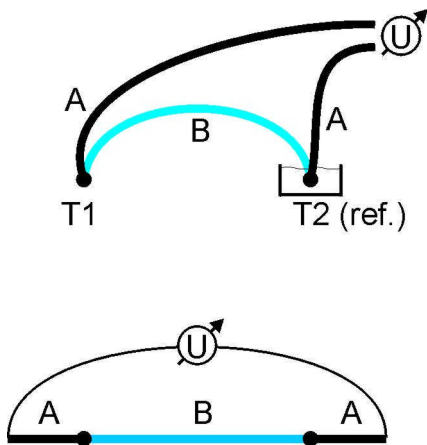
Seebeck coefficient:

$$\Delta U_{\text{th}}/\Delta T \quad \mu\text{V/K}$$

change of thermovoltage per degree

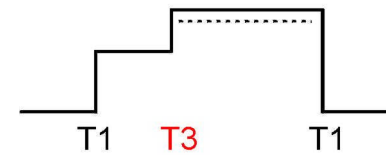
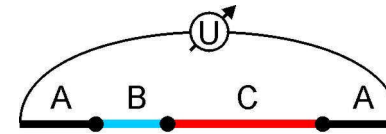
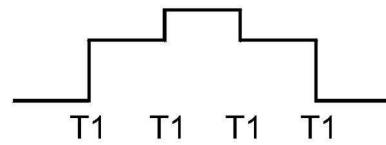
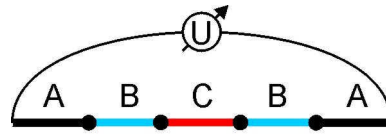
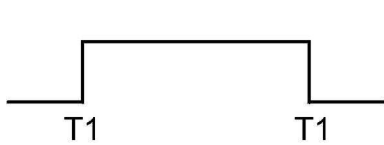
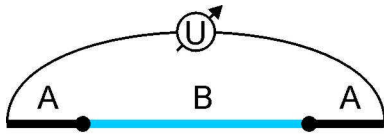
# T-measurement - Thermocouple

Wiring and unintended thermovoltages

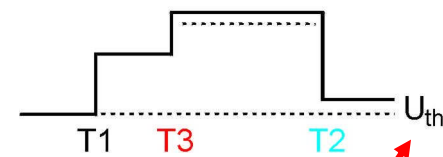
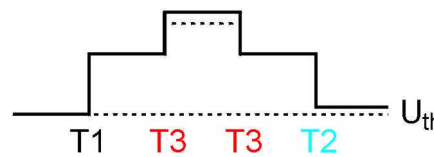
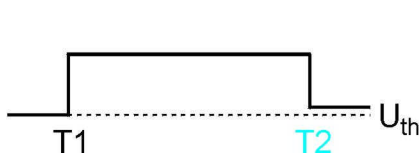
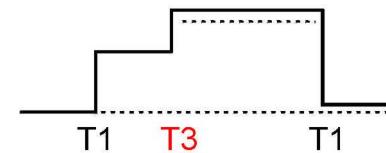
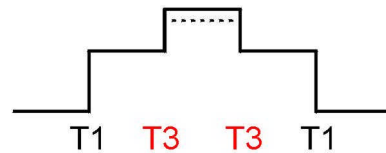


# T-measurement - Thermocouple

Wiring and unintended thermovoltages



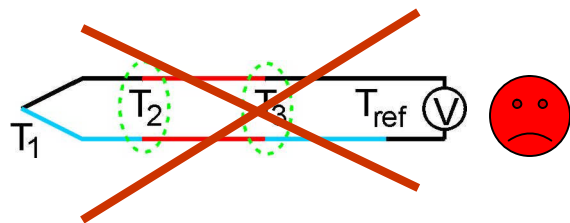
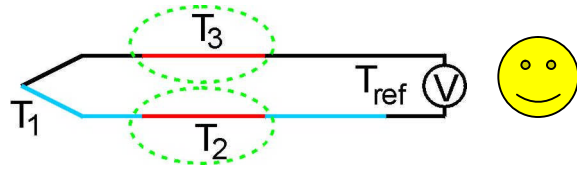
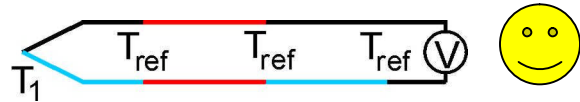
or: ?



**different!?**

Thermovoltages additive (like electrochem. potentials) ?

# T-measurement - Thermocouple



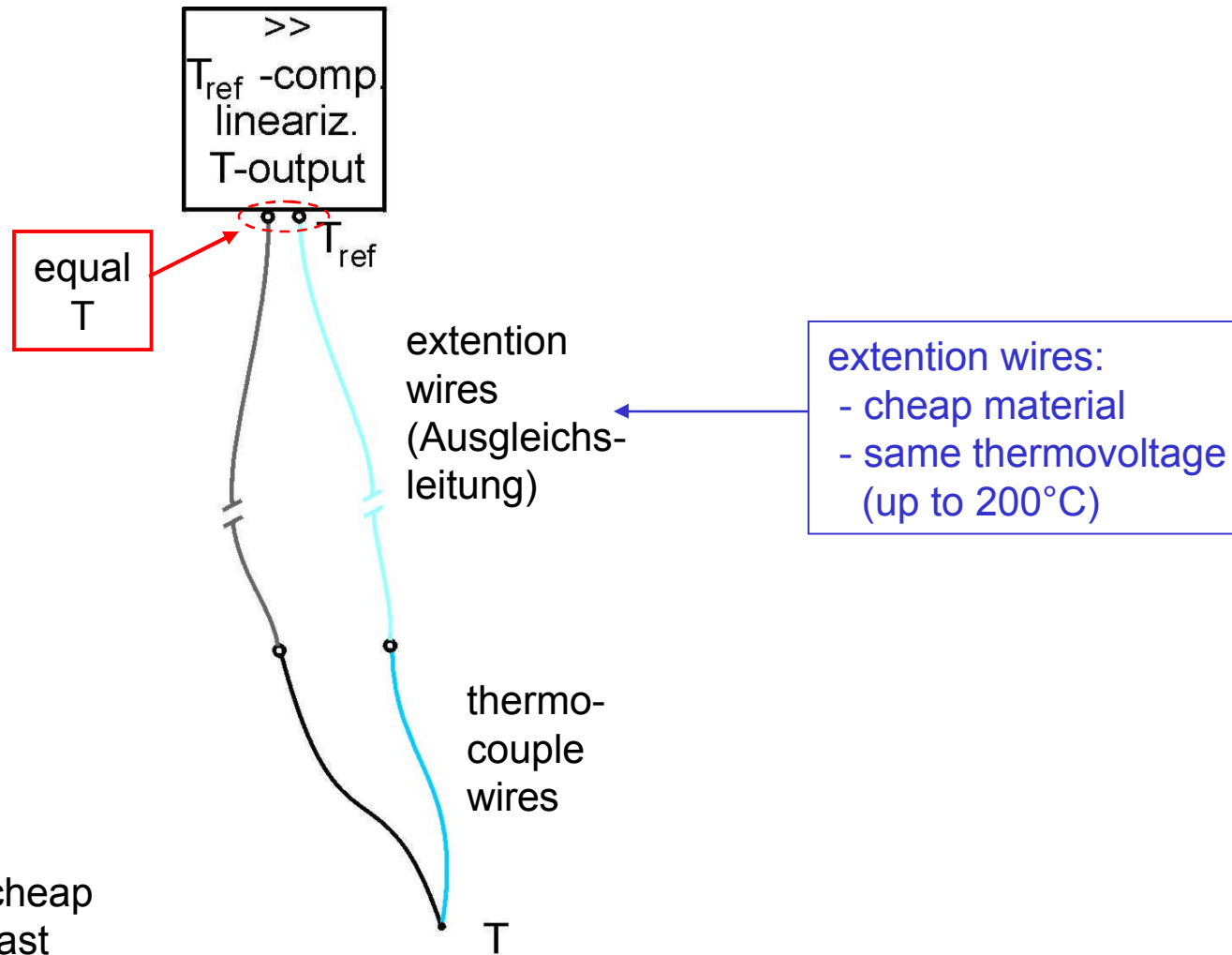
Thermovoltages not simply additive!

When T-gradients exist:

all materials in each branch  
must be made from the  
same (thermocouple) material  
(or extension wire material)

# T-measurement - Thermocouple

# Self-made thermocouples



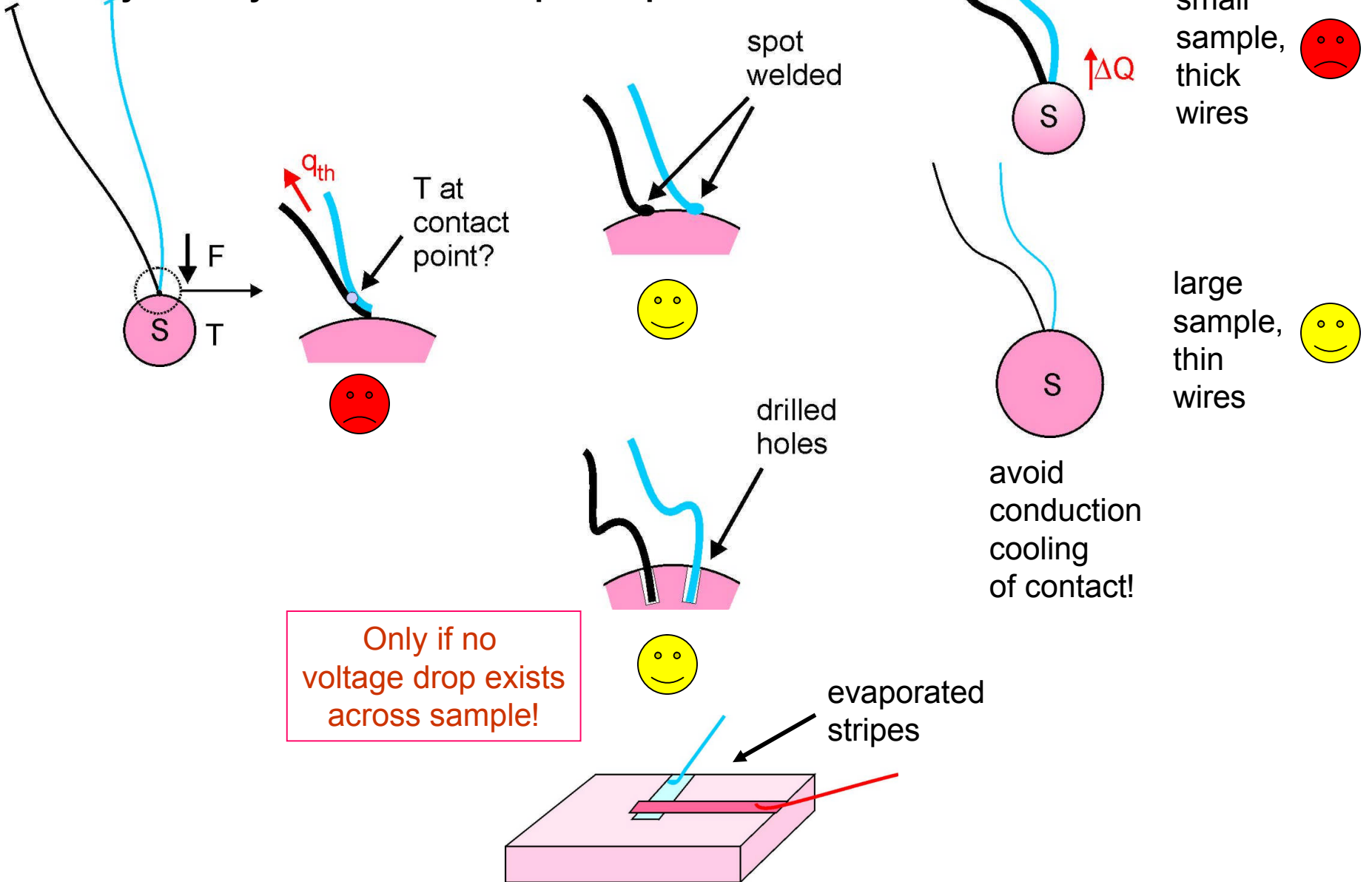
😊 cheap fast

☹ no galvanic separation

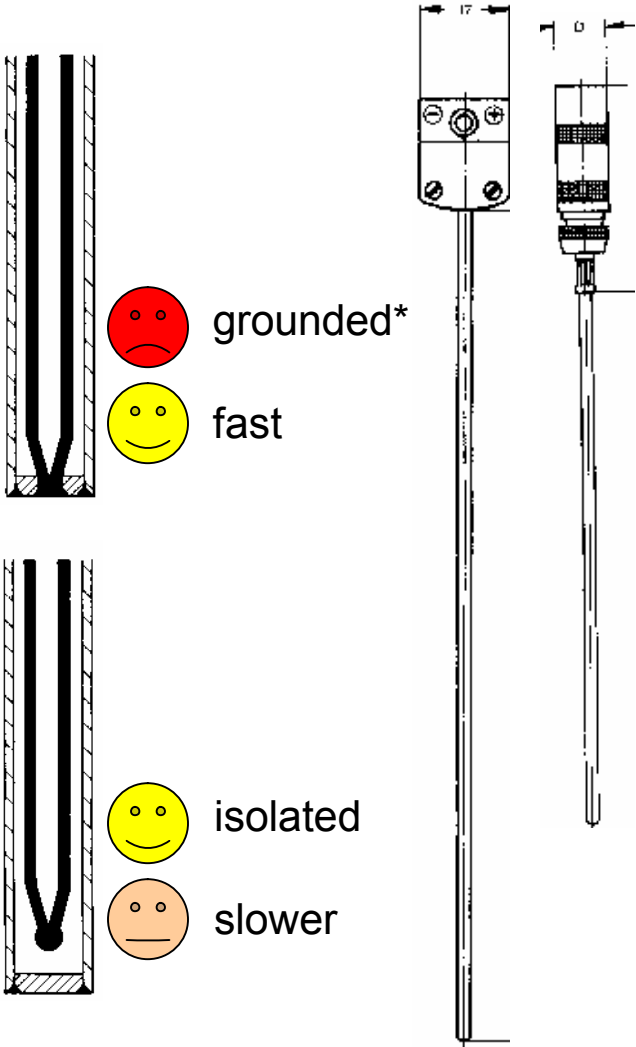
simple wires, "self-made"

# T-measurement - Thermocouple

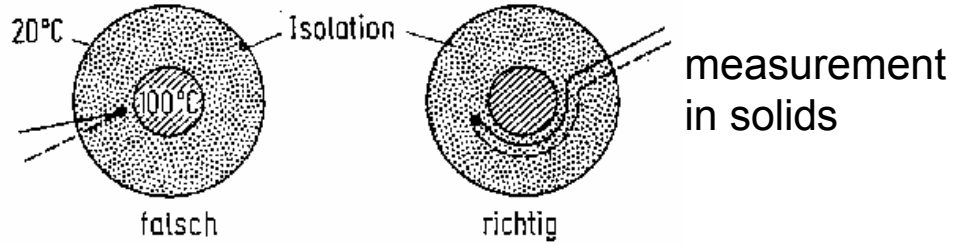
Do you really measure the sample temperature?



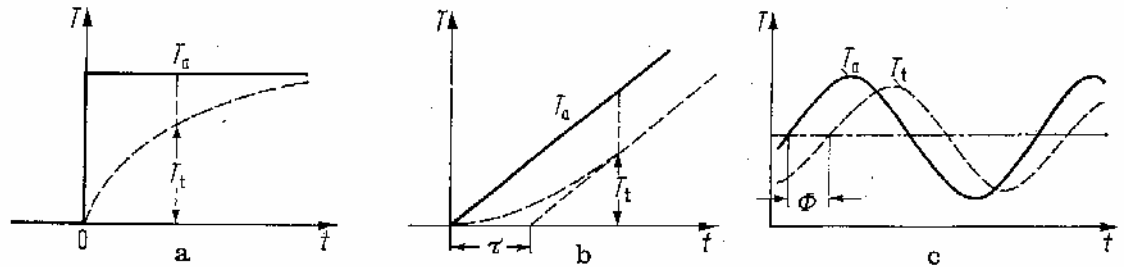
# T-measurement - Thermocouple Escapsulated thermocouples (Mantelthermoelemente)



	stainless steel	Iconel
d (mm)	0.5 – 3	0.25 – 6
l (m)	200 – 1000	
isol.-R	>1000 M $\Omega$	
bending-r	2 x d	



## Time response



T-jump

continuous T-change

periodic T-change

\* not shielded, bias, noise, inductive voltages, ground loops

# T-measurement - Thermocouple

## Accuracy

Voltage measurement (floating ground? noise? ground loops?)  
see manual, ask electronics workshop

Reproducibility of thermomaterials and thermovoltages  
Ex.: K-type, allowed  $\pm 2.5^\circ$  or  $0.0075 |t|$  ( $\pm 7.5^\circ$  at  $1000^\circ\text{C}$ )

Linearization of thermovoltage  
see manual, ask electronics workshop

Thermal contact  
**your responsibility!**

Thermal loss by heat conductivity  
**your responsibility!**

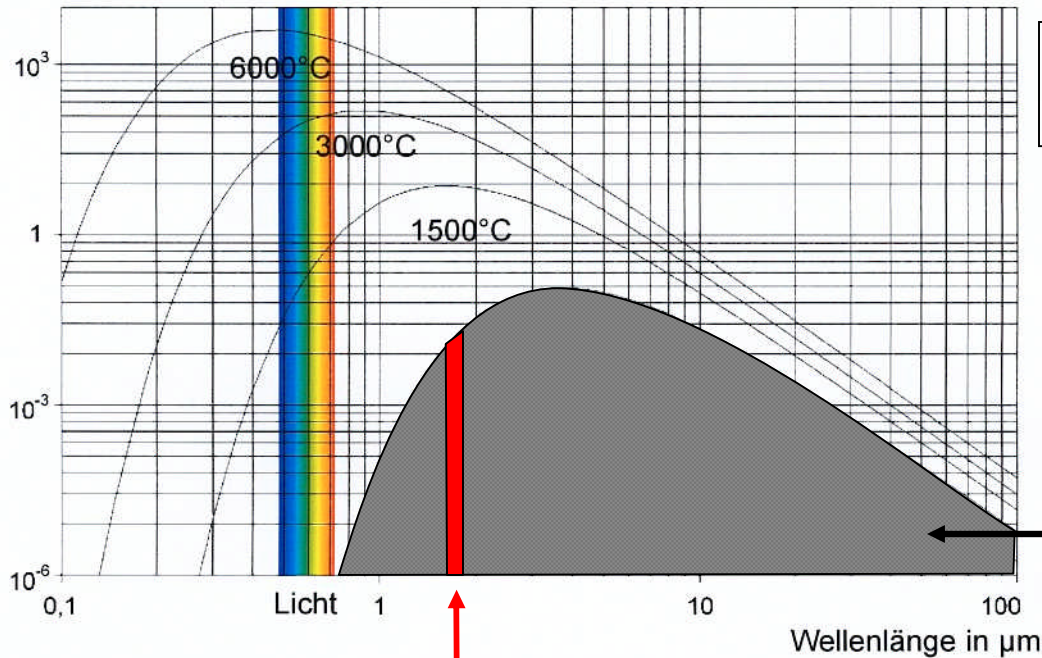
## Reproducibility

Usually high



# T-measurement - Pyrometer, Thermal radiation measurement

non-contact measurement



Spectral distribution of light emission, black-body radiation

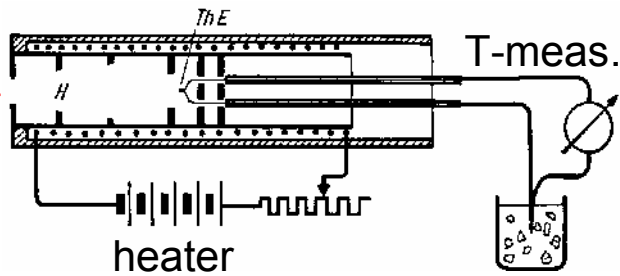
$I_{\text{tot}} \sim T^4$  (Stefan Boltzmann),  
total-radiation pyrometer,  
thermal sensors  
(bolometer, thermopile)

$I_{\text{part}}$ , weaker (but still strong) T-dependence  
band- or partial radiation pyrometer,  
photon sensors: photo diodes

# T-measurement - Pyrometer

Cavity radiator (black-body)

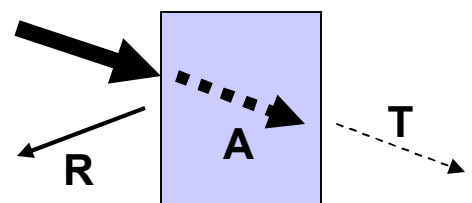
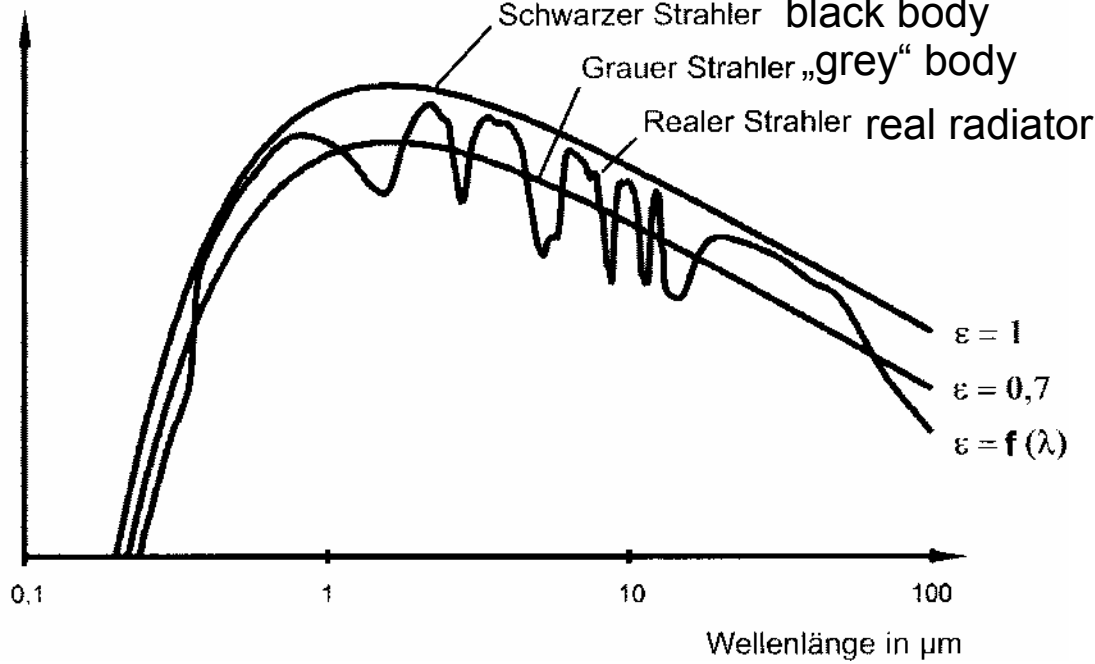
black-body radiation



Kirchhoff:  
 emissivity = absorptivity  
 $\epsilon(\lambda) = \alpha(\lambda)$   
 black body:  
 $\epsilon = \text{const} = 1$   
 „grey body“  
 $\epsilon = \text{const} < 1$   
 „real“ or „colored“ radiator  
 $\epsilon = f(\lambda)$

attention with transparent materials!

Spektrale Intensität (relativ)



$$\alpha + r (+ t + \text{lum}) = 1$$

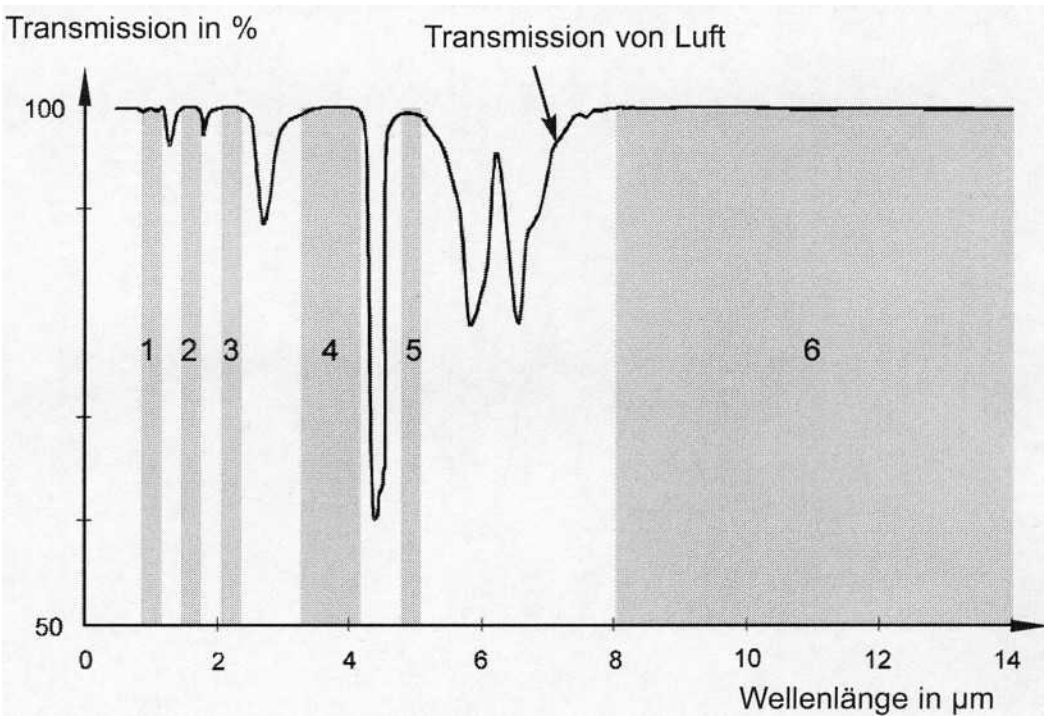
If r is small:  $\alpha (= \epsilon)$  is high  
 high: low

**$P = \epsilon P_s$**   
**emission power = emissivity x emission power**  
**black-body**

# T-measurement - Pyrometer

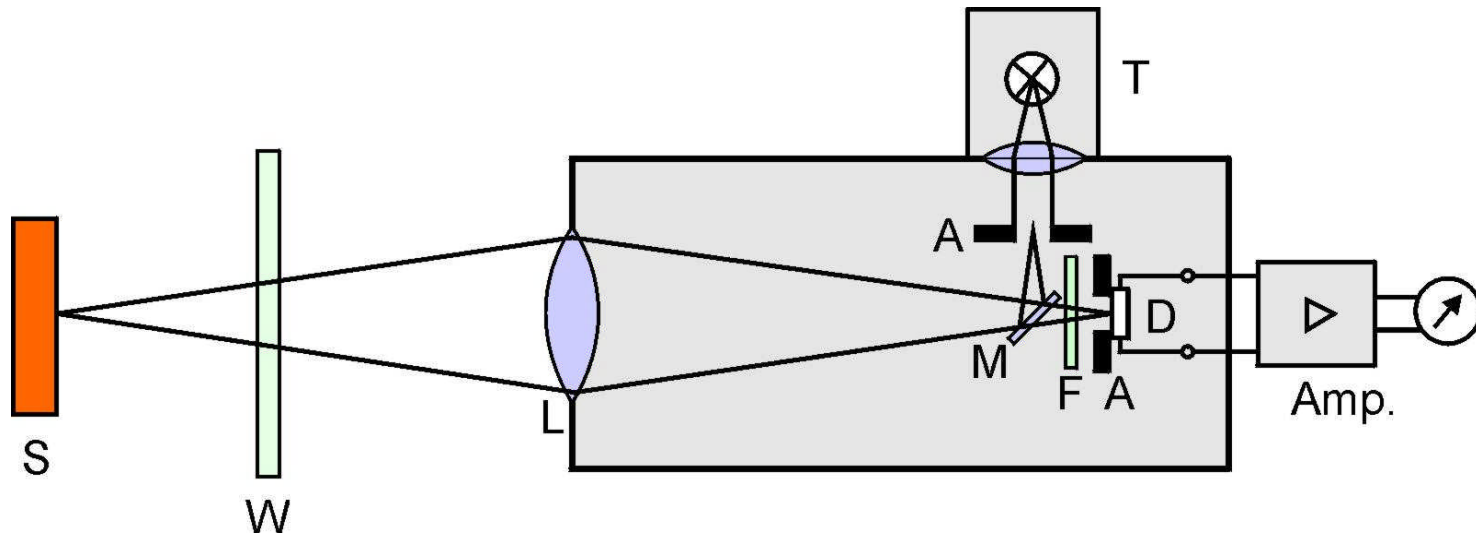
„Atmospheric windows“

In order to avoid absorption effects of the air in the light path, partial radiation pyrometers use regions without absorption.



Win- dow	Used detector type
1	Si diode
2	Ge-diode
3	PbS-diode
4	PbSe-diode, bolometer (resistance change) thermopile (ser. of thermocouples)
5, 6	bolometer (resistance change) thermopile (ser. of thermocouples)

# T-measurement - Pyrometer



must be transparent for the used wavelength!

- S sample
- W window
- L lens
- M semitransparent or removable mirror
- F filter, attenuator
- A apertures
- D radiation detector
- T lamp for sighting

## T-measurement - comparison

	Resistance thermometer	Thermocouple	Pyrometer
Advantages	exact almost linear wide T-range	very small very fast very wide T-range easy to make self	non-contact very high T quite fast
Disadvantages	not very small not very fast $\tau \sim 1$ s	not linear esp. at low T	only for $T > \sim 400^\circ\text{C}$ line of sight necessary emissivity-problem => low precision
Price	medium	lowest	high

**p**

**ressure**

## Pressure measurement

This lecture does not deal with:

- how to make vacuum (pumps)
- how to make a vacuum device (materials)
- gas flow and flow ranges

(see class 2002/2003, ask for manuscript)

Pressure, definition:

$$p = F/A = \text{force / area (N m}^{-2}\text{)}$$

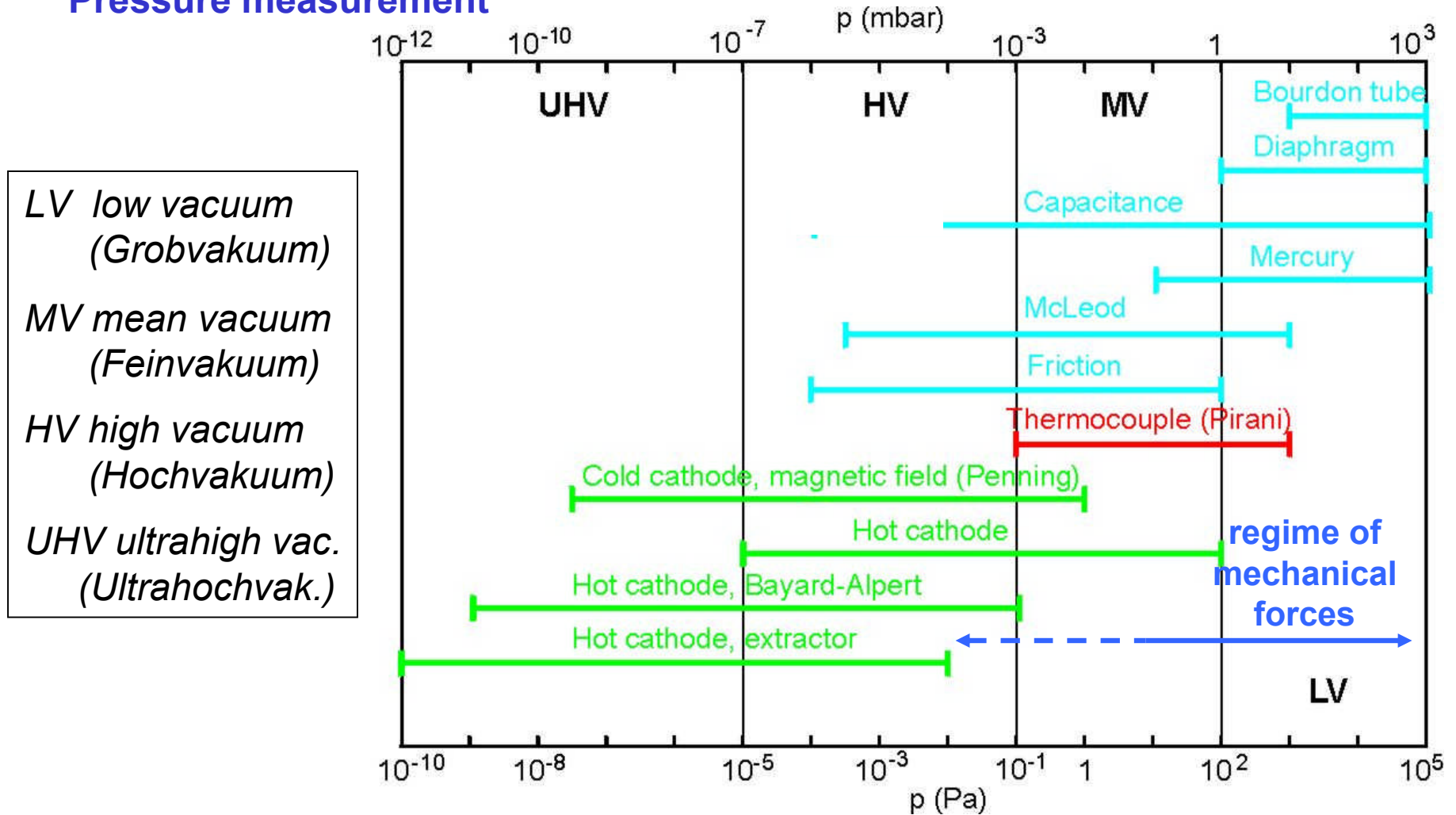
$$1 \text{ N m}^{-2} = 1 \text{ Pa};$$

$$10^5 \text{ Pa} = 1 \text{ bar}$$

$$100 \text{ Pa} = 1 \text{ mbar}$$

$$1 \text{ Torr} = 1 \text{ mm Hg} = 1.333 \text{ mbar}$$

## Pressure measurement



Pressure ranges for different vacuum gauges.

*Blue: Direct measurement of force.*

*Red: Indirect, p-dependence of thermal conductivity.*

*Green: Indirect, p-dependence of ion current in electrical discharge.*

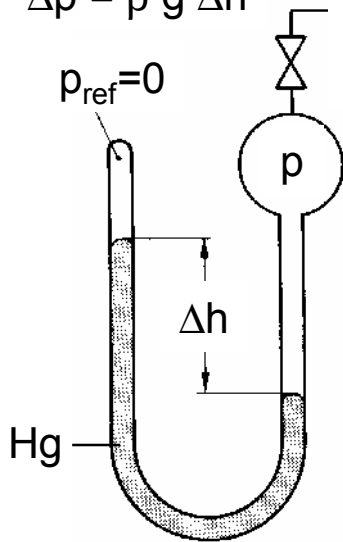


# p-measurement - Direct measurement of mechanical force

## Hg U-tube

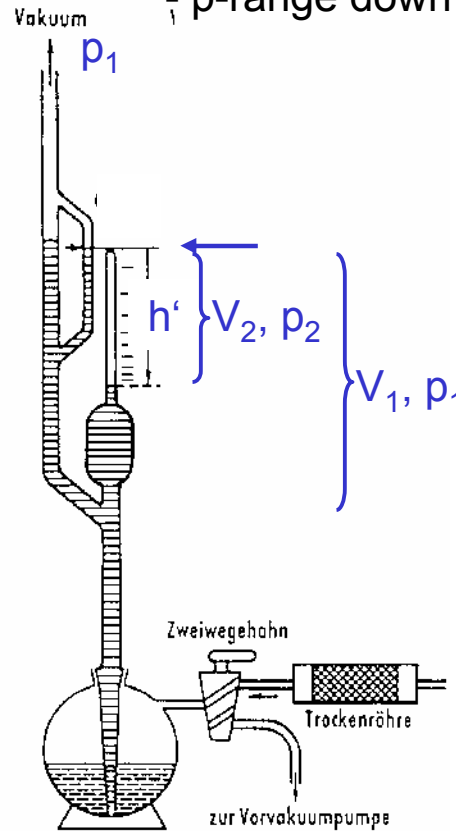
- absolute p
- no gas dependence
- limited precision for  $p < 10$  mbar

$$\Delta p = \rho g \Delta h$$



## Hg-compression gauge (McLeod)

- absolute
- no gas dependence (gas condensation!?)
- p-range down to  $\sim 10^{-5}$  mbar



How to measure:

1. All Hg in reservoir  $p_1$  in volume  $V_1$
2. Pump up Hg until arrow  $V_1$  gets compressed to  $V_2$ ,  $p_1$  rises to  $p_2$

According to

$$p V = n R T = \text{const.}$$

$$p_1 V_1 = p_2 V_2$$

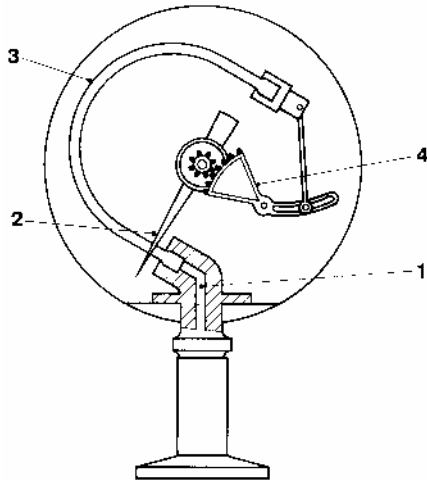
$$p_2 = p_1 V_1 / V_2 \gg p_1$$

Primary standard for p-calibration!

# p-measurement - Direct measurement of mechanical force

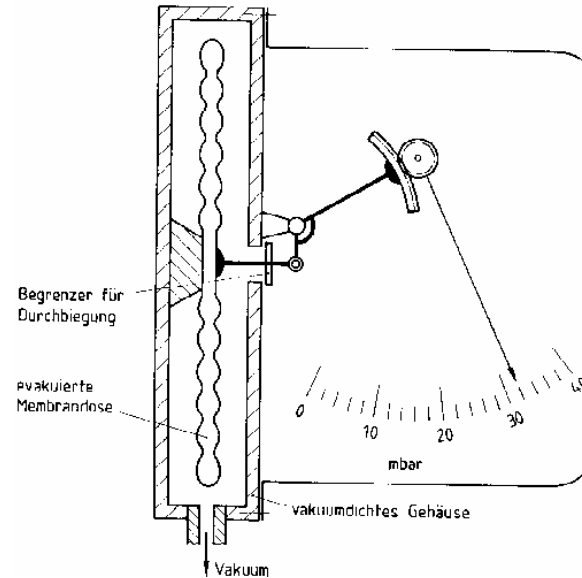
mechanical pressure indication

## Bourdon tube



$p > 10 \text{ mbar}$

## Diaphragm



Mechanical barometer

$p > 1 \text{ mbar}$

**So far:**  
not well suited for  
process control.

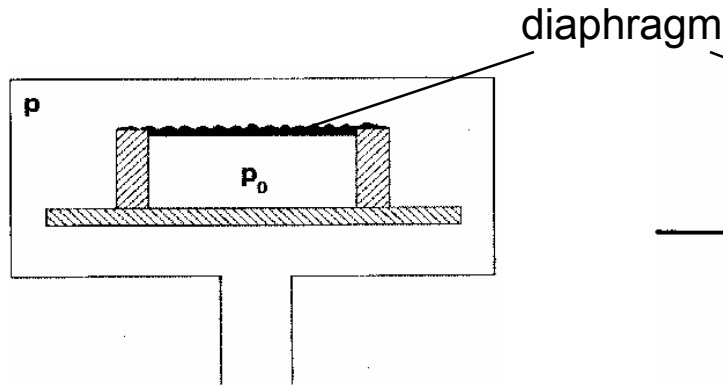
**Wanted:**  
Electrical output signals

# p-measurement - Direct measurement of mechanical force

## Piezoresistive diaphragm:

Diaphragm: Semicond.

*Si diaphragm,  
with deformation  
dependent  
R-bridge*



### Advantage:

- simple, robust
- insensitive to high p
- gas-independent
- also for higher p available

### Problems:

- limited precision

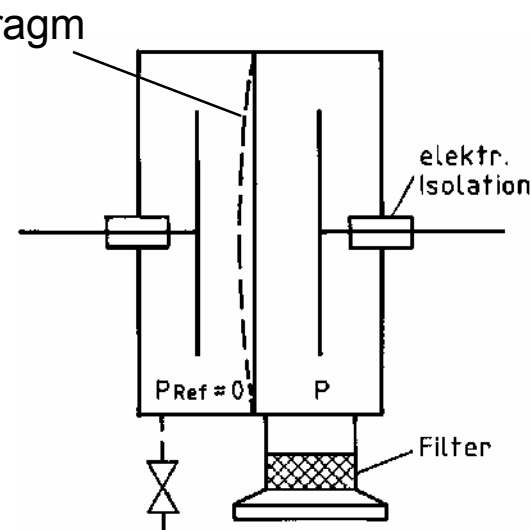
Range: 0.1 – 55 000 mbar

Precision:

+/- 10 mbar

## Capacitance diaphragm:

Diaphragm: ceramics or stainless steel



*Dp deforms  
diaphragm  
and changes  
the capacitance,  
electricval  
measurement*

### Advantage:

- simple, robust
- insensitive to high p
- high precision

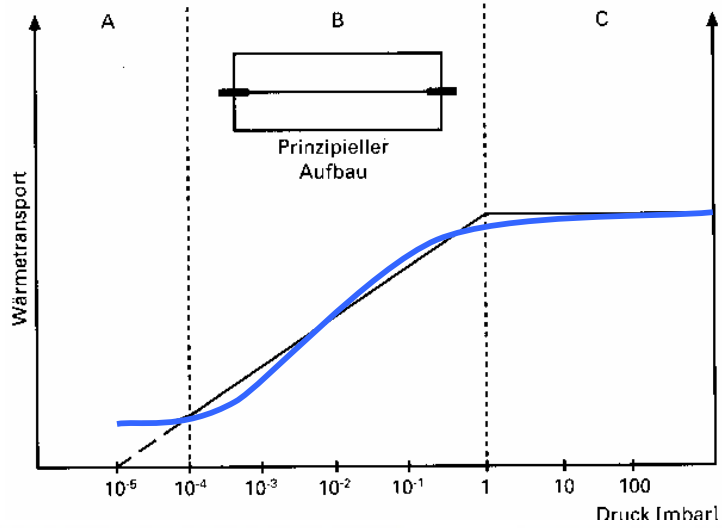
Problems: no

Range:  $10^{-4}$  – 1000 mbar

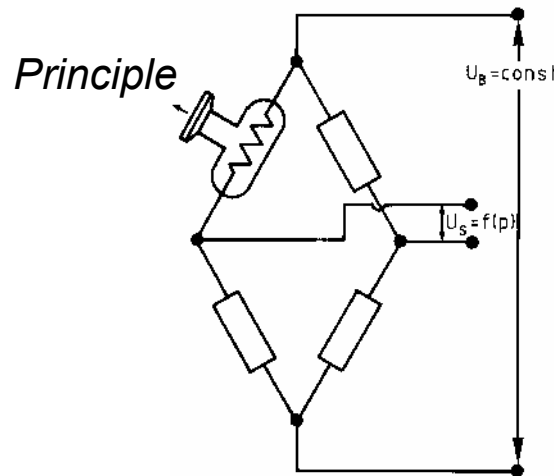
Precision:

0.15% typically

# p-measurement - Indirect measurement, heat conductivity



## Pirani



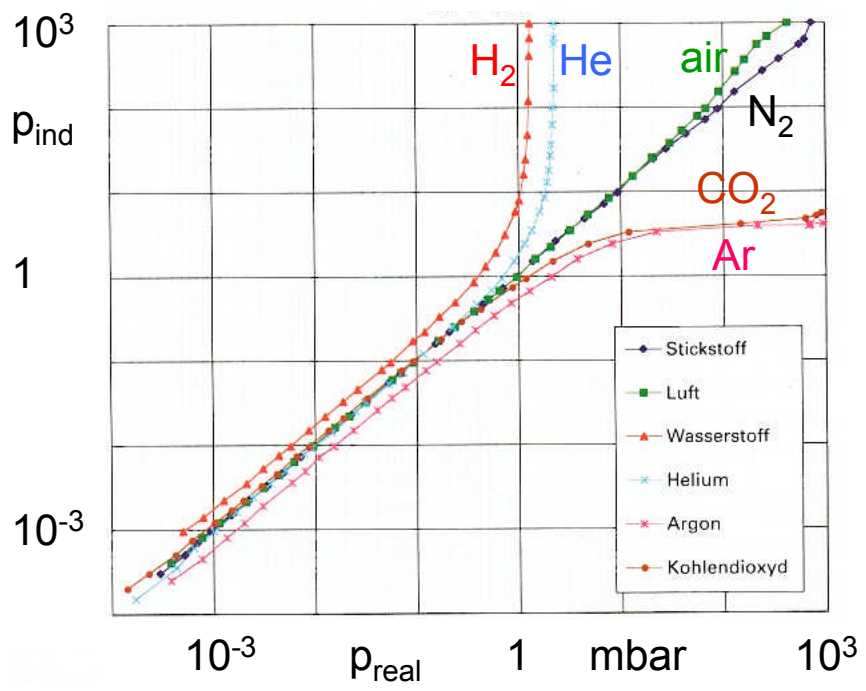
- Advantage:**
- simple, robust
  - insensitive to high p

- Problems:**
- gas dependent
  - highly non-linear p-characteristics
  - low precision for  $p < 10^{-3}$  mbar and  $p > 10^{-1}$  mbar

**Range:**  $10^{-3} - 10$  (100)  
**Precision:**  
 5% at  $10^{-3}$  mbar  
 (+ gas dependence!)

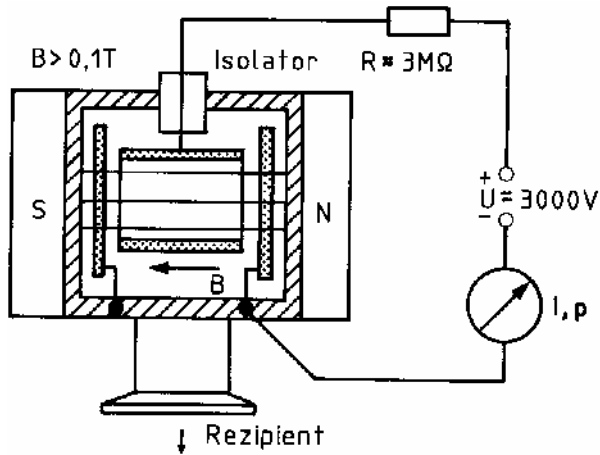
A wire is heated and at the same time its R is measured. The T and hence the R depends on cooling by heat conduction through the gas.

*gas dependent pressure indication*

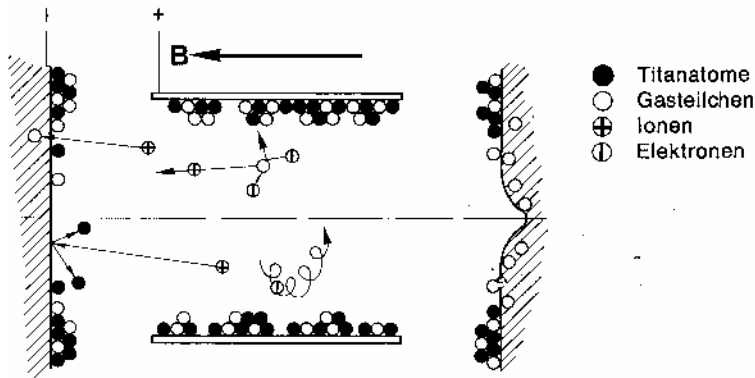


# p-measurement - Indirect measurement, gas ionization

Cold cathode, inverse magnetron, **Penning**



Incidentally produced ions move to anode, electrons to cathode. Electrons are forced on long spiral paths by B-field in order to increase the probability to produce further ions by impact. The ion/electron current is proportional to the gas density and thus p.



working principle:  
like in ion getter pump (diode type):  
each Penning pumps!

Advantage:

- simple, robust
- insensitive to high p

Problems:

- gas dependent
- ignition
- maintain discharge at low p
- leak currents (contamination)

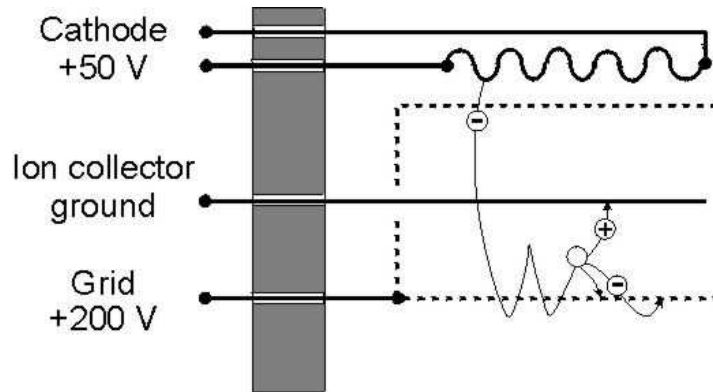
Range:  $(10^{-10}) 10^{-8} - 10^{-2}$

Precision:

low +/- 30% at  
(+ gas dependence!)

## p-measurement - Indirect measurement, gas ionization

Hot cathode, **Bayard-Alpert**-type



The hot cathode emits electrons which pass the grid several times before they hit it. They ionize particles. Ions are collected by a thin wire (collector).

X-ray limit:

$e^-$  generate X-rays when hitting the grid which generate a photoionization current from the collector.

Its size determines the low-p limit.

Advantage:

- linear for  $p < 10^{-4}$  mbar
- wide range  $10^{-3} - 10^{-11}$  mbar

Problems:

- gas dependent
- cathode burns at  $p > 10^{-2}$  mbar (safety circuit necessary)

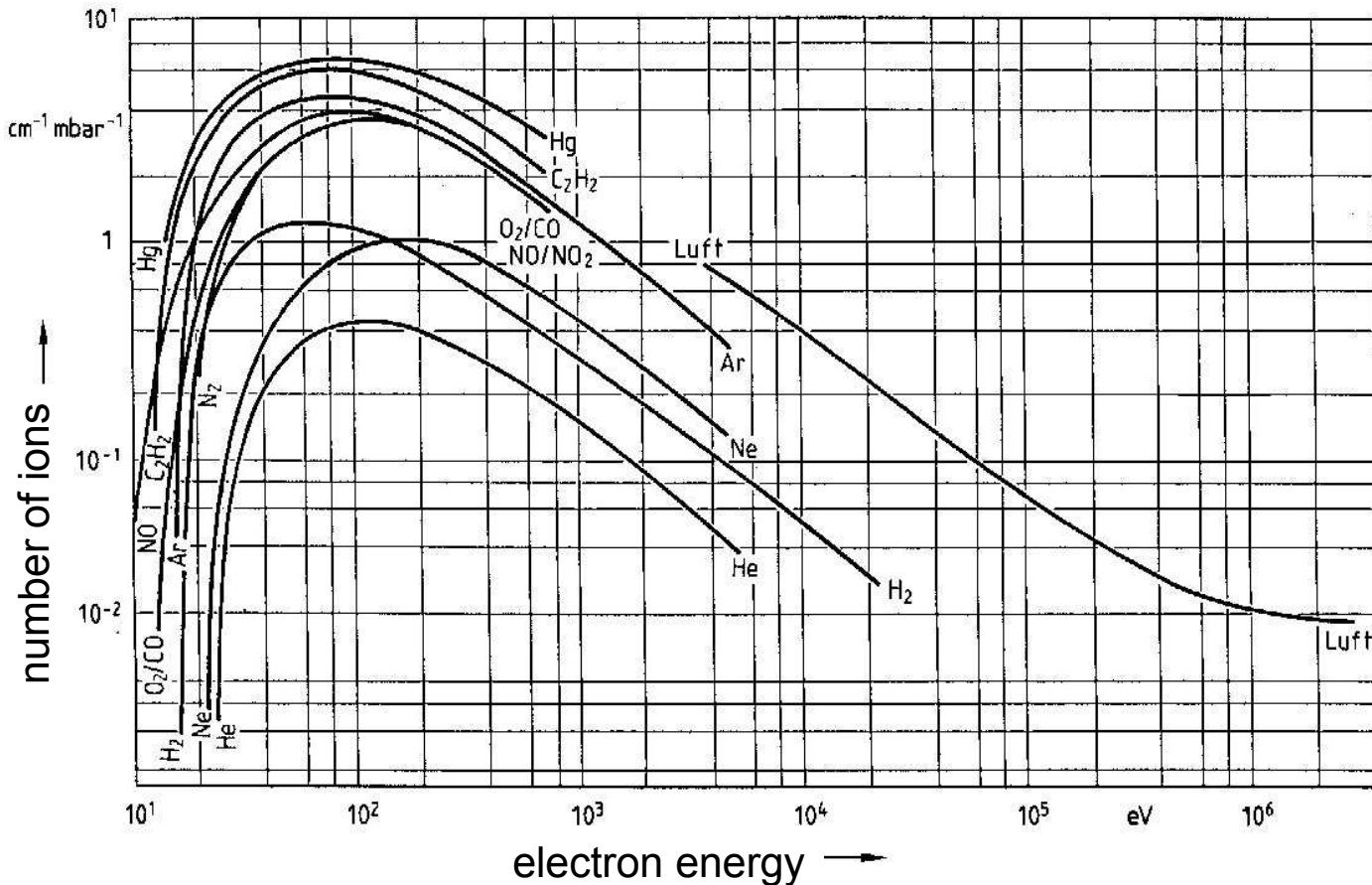
Range:  $3 \times 10^{-11} - 10^{-3}$

Precision:

rel. high,  $\pm 10\%$  at  $10^{-7}$  mbar  
(+ gas dependence!)

More information  
=> separate sheet

## p-measurement - Indirect measurement, gas ionization



Molecule ion gauge sens. S

<b>He</b>	<b>0.19</b>
H <sub>2</sub>	0.44
<b>N<sub>2</sub></b>	<b>1</b>
CO	1.02
H <sub>2</sub> O	1.25
Ar	1.37
CH <sub>4</sub>	1.49
C <sub>2</sub> H <sub>6</sub>	2.53
<b>C<sub>6</sub>H<sub>6</sub></b>	<b>5.18</b>

F. Nakao, Vacuum 25 (1975) 431

Consequence for p-measurement:

- need to know gas composition
  - divide p-indication by sens. factor
- $$p = p_{\text{indic}}/S$$

The energy needed for ionization depends on the kind of the gas (ionization potential) and determines the onset of the curves.

The maximum ionizability occurs for all gases at around 100 eV

## p-measurement - gauge combinations

For wide p-ranges and process control:

- combination of two principles as one unit („Full Range“ or „Wide Range“ gauges)
- automatic switching between gauges
- digital indication

### Examples:

Piezo + Pirani  
(diaphragm) (heat cond.)  
1200 mbar –  $10^{-3}$  mbar

Pirani + Penning  
(heat cond.) (cold cathode)  
100 mbar –  $10^{-8}$  mbar

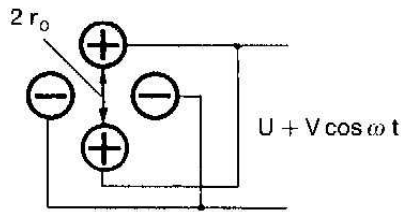
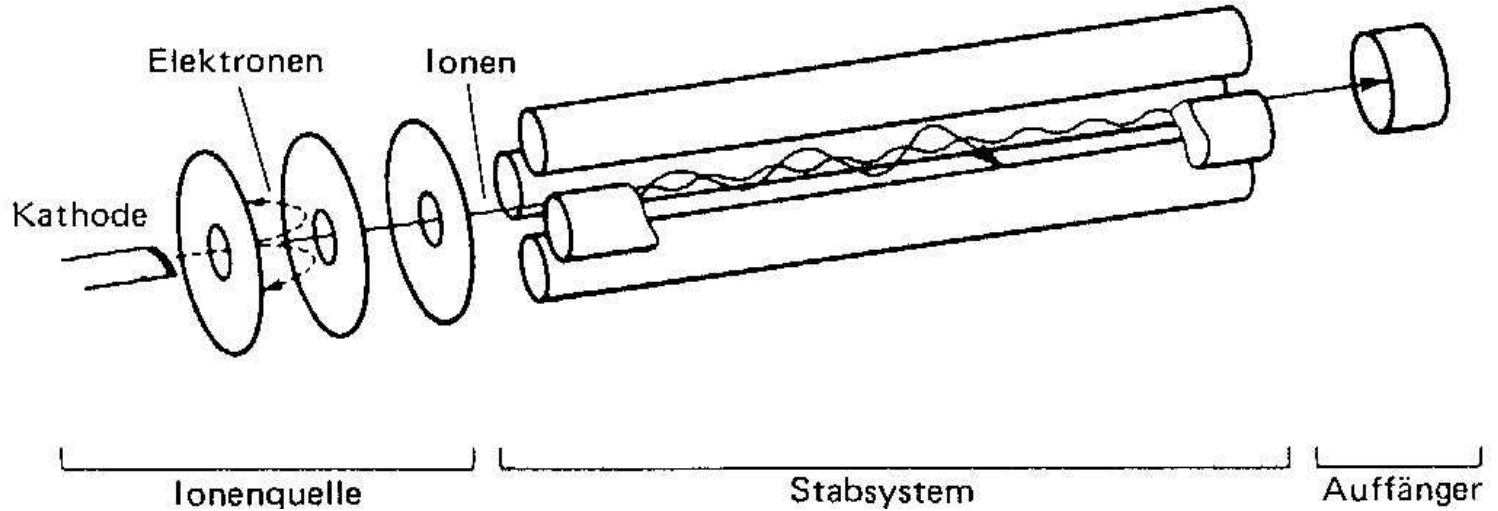
Pirani + Bayard-Alpert  
(heat cond.) (hot cathode)  
100 mbar –  $10^{-11}$  mbar

**Be careful:  
digital indication  
makes you believe  
in high precision!**

**The actual pressure  
may be up to +/-30%  
wrong due to  
the measuring principle  
and in addition  
depends mostly  
on the kind of gas!**



## p-measurement - quadrupole mass spectrometer (QMS)



*Quadrupole rod system,  
applied DC voltage  $U$   
and AC voltage  $V \cos \omega t$*

*QMS consisting of ionizer, mass separator (rod system)  
and collector (Faraday cup or multiplier).*

*Particles are excited to vibrations in the separator.*

*For given values of  $U$  and  $V$ , the amplitude for a particle  
with certain  $m/e$  remains limited and the particle  
is transmitted.*

*All others are in resonance, hit a rod and are neutralized.*



## T and p:

Don't simply believe what your instruments indicate!

- T:        Sensor - type?  
              T-range?  
              linearity?  
              mounting?
- p:        Sensor - type?  
              cleanliness?  
              mounting -  
              degassing of surrounding?