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Electron attachment to POCl_3 . III. Measurement and kinetic modeling of branching fractions

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Electron attachment to POCl_3 was studied in the bath gas He over the pressure range 0.4–3.1 Torr and the temperature range 300–1210 K. Branching fractions of POCl_3^- , POCl_2^- , Cl^- , and Cl_2^- were measured. The results are analyzed by kinetic modeling, using electron attachment theory for the characterization of the nonthermal energy distribution of the excited POCl_3^{*-} anions formed and chemical activation-type unimolecular rate theory for the subsequent competition between collisional stabilization of POCl_3^{*-} and its dissociation to various dissociation products. Primary and secondary dissociations and/or thermal dissociations of the anions are identified. The measured branching fractions are found to be consistent with the modeling results based on molecular parameters obtained from quantum-chemical calculations. © 2011 American Institute of Physics. [doi:10.1063/1.3549139]

I. INTRODUCTION

Electron attachment to phosphoryl chloride (POCl_3) is characterized by product branching fractions which depend on the temperature and the pressure of the bath gas.^{1–3} This observation is taken as evidence for the intermediate formation of metastable, relatively long-lived, vibrationally highly excited POCl_3^{*-} anions. The analysis of the properties of the branching fractions then may make use of the approach generally applied to unimolecular reactions with chemical activation, see e.g., Ref. 4. Essential elements of this treatment are the characterization of the primary electron attachment step, the dissociation of the excited anion, and inelastic collisional energy transfer of the excited anion. Previous investigations of the system have already followed this concept, but only rather simplified versions of modeling were employed.

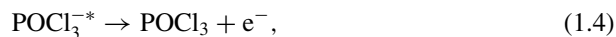
In the present series of articles, we are providing a more detailed treatment than was given before. In part I,³ new measurements of product branching fractions as functions of bath gas pressure and temperature were presented and the results were fitted by a step-ladder model for the competition between fragmentation and collisional stabilization of the intermediate excited anion POCl_3^{*-} . At the same time, the dependence of the attachment rate on buffer gas and electron temperature was investigated. At the simplified level of the analysis, however, the attachment process was assumed to result in thermal energy distributions of the excited intermediate before dissociation and collisional stabilization set in. Analyzing the attachment rate more carefully, such as was done in part II of our series,⁵ allows one to characterize more correctly the starting distribution of the dissociation/collisional stabilization sequence. On this basis, the present part III provides

an improved kinetic modeling of the system. Our measurements of the branching fractions are extended and a more detailed model for the chemical activation system is elaborated. Our treatment unavoidably is not parameter-free. However, we try to keep the number of fit parameters to a minimum and to employ expressions which have been tested previously for other systems. In this way, we provide a route to extrapolate the results beyond the range of conditions studied.

Electron attachment to POCl_3 is known^{1–3} to lead to the anionic products POCl_3^- , POCl_2^- , POCl^- , Cl_2^- , and Cl^- . The mechanism forming POCl_3^- and POCl_2^- is assumed to be



Heretofore, it has not been clear whether the other products directly arise from POCl_3^{*-} in its electronic ground state, from electronically excited POCl_3^{*-} , or from secondary dissociation of POCl_2^- , either through residual excitation from reaction (1.2) or thermal reactivation of POCl_2^- . We extend the measurements of branching fractions from part I to broader ranges of temperature in order to answer some of these questions. We also inspect the possibilities for electron autodetachment from POCl_3^{*-} via



as well as the extent of thermal dissociation of POCl_3^- initiated by thermal reactivation of POCl_3^- ,

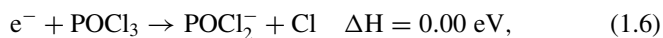


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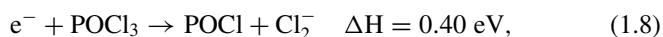
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These questions require extensive kinetic modeling analogous to our previous work on the electron attachment to SF₆.^{6–9} A comparison of the two reaction systems appears attractive for a number of reasons, last but not least because SF₆ has no permanent dipole moment while POCl₃ is markedly polar. This has consequences for the starting distribution of the dissociation/collisional stabilization sequence.

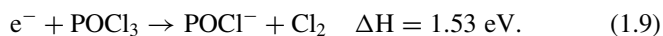
While the dissociative component of reactions (1.1)–(1.3), i.e., the dissociative attachment reaction



is almost thermoneutral, the products Cl[−], Cl₂[−], and POCl[−] are formed in endothermic processes



and



The given enthalpies of reactions (1.6)–(1.9) at 298 K are from Ref. 10 using the Gaussian G3 model chemistry and are estimated to be accurate within about ±0.1 eV, see the Appendix. In the present work, we investigate whether channels (1.7) and (1.8) like channel (1.6) proceed through vibrationally highly excited electronic ground state POCl₃^{−*} or whether there is evidence for the participation of other pathways.

II. EXPERIMENTAL TECHNIQUE AND RESULTS

The two flowing-afterglow Langmuir-probe (FALP) apparatuses used in the present work were described in part II of this series⁵ and in greater detail in earlier literature.^{11–13} One apparatus was a conventional FALP apparatus normally used in the 300–550 K temperature range.^{11,12} The second apparatus was a high-temperature FALP (HT-FALP, 300–1200 K). In both, we first measure the ambipolar diffusion rate, with no POCl₃ present, and then observe the decay of the electron density along the flow tube axis due to the coupled effects of diffusion and electron attachment to POCl₃, from which the electron attachment rate coefficient k_{at} is determined. Technical differences between the FALP and HT-FALP and problems related to high-temperature measurements were discussed in part II.⁵ For the present work, we shall focus on matters relevant to the product branching fraction measurements. Axial apertures at the downstream ends of the flow tubes are used to pass a sample of the ion swarm into a high vacuum region for mass analysis with an rf quadrupole mass spectrometer and detection with an electron multiplier. Only relative ion intensities are needed for product branching fractions. For accurate data, account must be taken of mass discrimination effects. Possible mass discrimination sources include differential diffusion of ions in the flow tube, collisions in the lens region following the extraction aperture, differential transmission of ions by the mass spectrometer, and differential detection in the electron multiplier. In the

FALP, we have determined overall mass discrimination factors using two methods that were described in Ref. 14, (a) via ion–molecule reactions, e.g., Cl[−] + SO₂ → SO₂Cl[−], in which the product ion intensity should equal the precursor ion intensity if no mass discrimination occurs; and (b) introducing a concentration of an electron-attaching gas (e.g., SF₆) that causes the electron density to drop by half at a fixed point beyond the reactant inlet port, and recording the resulting anion intensities for various electron-attaching gases which yield anions of different masses. With these methods, we mapped out the discrimination as a function of ion mass, and used this distribution to correct the raw ion intensities in the present POCl₃ experiments. Light, monatomic ions tended to be discriminated against relative to heavier polyatomic ions over the mass range of these experiments. The mass discrimination factors were found to be stable to within 10% during the course of this work as long as no significant adjustments were made to the ion lenses, mass spectrometer, or electron multiplier. Rather than repeating these experiments for the HT-FALP, we measured the branching fractions at 1.67 Torr and 500 K in both apparatuses and determined the mass discrimination factors in the HT-FALP so that the results were identical. In the HT-FALP, heavier ions are slightly discriminated against.

For rate constant measurements, the nominal buffer gas pressure in the FALP flow tube was set to $T/300$ Torr, which maintains a constant gas number density over the FALP temperature range. In order to measure the effect of buffer gas pressure on the branching fractions at 300–500 K, the FALP flow tube pump was throttled to drive the pressure as high as 8 Torr. Higher pressure appeared to begin to overload the diffusion pump on the ion lensing section of the ion sampling system. Throttling the flow tube pump caused the gas and plasma flow velocities to be proportionately reduced, so that the electron attachment reaction occurred over a shorter distance, and the ion drift time to the sampling aperture was longer. Anions do not diffuse to the flow tube walls as long as electrons are still present to handle the task, but once all electrons have attached or diffused away, anions may diffuse to the walls, possibly at different rates. Calculated and experimental ion diffusion rates in He gas roughly fit a power law ($M^{-0.51}$) dependence on ion mass M and imply that there is a difference of a factor of ~2 in the diffusion rates for our lightest and heaviest anions (Cl[−] and POCl₃[−]).¹⁵ These differences in diffusion rates (along with other discrimination factors) are taken into account empirically by the mass discrimination measurements described above, and should not change with pressure in the 1–8 Torr range. However, no mass discrimination calibrations were made specifically under the high-pressure conditions. During the pressure tests, the electric potential between the sampling aperture and the first lens element was kept low (<1 V), to minimize differential scattering in the lens region. We assign a ±10% uncertainty to the product branching fractions reported here.

Our modeling of branching fractions given below is based on three sets of experimental data: (i) branching fractions of POCl₃[−] and POCl₂[−] obtained in part I (Ref. 3) in the bath gas He in the pressure range 0.4–7 Torr and at the temperatures 297, 372, 457, and 552 K; (ii) branching

TABLE I. Measured branching fractions Y of reaction products in the electron attachment to POCl₃.

T/K	$Y(\text{POCl}_3^-)$	$Y(\text{POCl}_2^-)$	$Y(\text{Cl}^-)$	$Y(\text{Cl}_2^-)$
(a) $[\text{He}] = 3.2 \times 10^{16} \text{ cm}^{-3}$; reaction time 4.4 ms.				
300	0.25	0.74	0.012	...
400	0.10	0.89	0.02	...
500	0.035	0.93	0.03	0.002
550	0.02	0.94	0.04	0.005
(b) $[\text{He}] = 1.9 \times 10^{16} \text{ cm}^{-3}$ ($2.5 \times 10^{16} \text{ cm}^{-3}$ at 300 K); reaction time 2.3 ms.				
300	0.24	0.74	0.012	...
507	0.023	0.946	0.031	...
603	0.009	0.955	0.034	0.005
698	0.003	0.933	0.048	0.016
805	0.001	0.896	0.064	0.038
853	...	0.855	0.105	0.04
905	...	0.704	0.235	0.062
957	...	0.453	0.46	0.088
1031	...	0.063	0.845	0.092
1110	...	0.008	0.929	0.064
1210	...	0.002	0.94	0.056
(c) $T = 300 \text{ K}$, $M = \text{He}$				
P/Torr				
0.75	0.24	0.74	0.01	...
1.0	0.25	0.74	0.01	...
2.02	0.33	0.66	0.01	...
3.05	0.37	0.62	0.01	...
(d) $T = 500 \text{ K}$, $M = \text{He}$				
P/Torr				
0.4	0.02	0.95	0.02	0.002
0.81	0.03	0.94	0.03	0.002
1.01	0.03	0.93	0.03	0.002
2.07	0.05	0.92	0.03	0.002
3.07	0.06	0.91	0.03	0.002

fractions of POCl₃⁻ and POCl₂⁻ from Ref. 2 in the bath gas N₂ in the pressure range 1–760 Torr and at the temperatures 300, 373, and 423 K; (iii) branching fractions of POCl₃⁻, POCl₂⁻, Cl⁻, and Cl₂⁻ from the present work in the bath gas He in the pressure range 0.4–3.1 Torr and at temperatures from 300 to 1210 K. For the data (i) and (ii), see Refs. 2 and 3. Our new results are summarized in Table I. They were taken at reaction times between 2 and 12 ms; the higher numbers refer to higher pressure. The data are discussed along with the kinetic modeling results in Section III. Confirming the results of part II,⁵ we did not observe a pressure dependence of the overall rate of the attachment forming POCl₃⁻, POCl₂⁻, Cl⁻, and Cl₂⁻ between 0.7 and 4 Torr. We measured this by adding small amounts of both POCl₃ and SF₆ and measuring the relative branching between the sum of the POCl₃ derived ions to SF₆⁻. Since the SF₆ rate coefficient was already shown not to have a pressure dependence, this implies that neither does that for POCl₃⁻.^{6–9}

III. THEORETICAL ANALYSIS

A. Electron attachment

Attachment rate coefficients k_{at} as functions of buffer gas temperature T_{gas} and electron temperature T_{el} have been

analyzed in part II (Ref. 5) in terms of electron capture theory^{16–18} and “electron-phonon coupling” or “intramolecular vibrational relaxation” factors P^{IVR} . The latter were empirically fitted to the experimental data. The attachment leads to broad distributions $g(E, J)$ of the internal energy E and the total angular momentum (quantum number J) of the formed excited anions. These distributions allow one to analyze the various potential processes the anions undergo. Once the attachment rate has been analyzed such as described in part II,⁵ one may quantitatively determine the $g(E, J)$. Obviously the $g(E, J)$ depend on the gas temperature T_{gas} and the electron temperature T_{el} in thermal environments. We show, however, that, even when $T_{\text{el}} = T_{\text{gas}}$, the $g(E, J)$ do not correspond to thermal distributions at the gas temperature T_{gas} . This is the issue of the present section.

The energies E_i of the vibrational states i of the neutral target and the energy E_{el} of the attaching electrons both contribute to the internal energy E of the formed anion, i.e., $E = E_i + E_{\text{el}}$. We assume that both, E_i and E_{el} , are thermally distributed. This does not mean that the energies E of POCl₃^{-*} are also thermal and in the following we investigate to what extent they differ from thermal distributions at the temperature of the E_i and E_{el} .

We consider the distribution $g(E, J, T_{\text{gas}}, T_{\text{el}})$ of vibrational energies and total angular momenta of POCl₃^{-*}, formed by attachment of electrons (at temperature T_{el}) to POCl₃ (at temperature T_{gas}). As only very few partial waves of the electron contribute to the attachment,⁵ J is essentially determined by the angular momentum of POCl₃. In the following we neglect the J -dependence and omit J . The distribution $g(E, T_{\text{gas}}, T_{\text{el}})$ is proportional to the rate coefficient $k_{\text{at}}(E, T_{\text{gas}}, T_{\text{el}})$ of attachment resulting in POCl₃^{-*} at an energy E and hence to the average of the product $\sigma_{\text{at}}\nu$ of the attachment cross section $\sigma_{\text{at}}(E, T_{\text{gas}}, T_{\text{el}})$ and the relative velocity $\nu(E_{\text{el}})$ of POCl₃ and the electrons, i.e.,

$$g(E, T_{\text{gas}}, T_{\text{el}}) \propto \langle \sigma_{\text{at}}(E, T_{\text{gas}}, T_{\text{el}}) \nu(E_{\text{el}}) \rangle, \quad (3.1)$$

where E_{el} denotes the kinetic energy of the attaching electron, the energy E of POCl₃^{-*} is given by $E = E_{\text{el}} + E_i$ with the vibrational energy E_i of POCl₃, and the averaging extends over thermal distributions of E_{el} and E_i . With $\sigma_{\text{at}}(E_{\text{el}}) \propto P(E_{\text{el}})$ and $\nu(E_{\text{el}}) \propto E_{\text{el}}^{1/2}$, see Ref. 6, one then has

$$g(E, T_{\text{gas}}, T_{\text{el}}) \propto \sum_{E_i=0}^E P(E - E_i)(E - E_i)^{-1/2} \times \exp(-E_i/kT_{\text{gas}}) \exp[-(E - E_i)/kT_{\text{el}}], \quad (3.2)$$

where $g(E, T_{\text{gas}}, T_{\text{el}})$ is a distribution per energy interval and $P(E_{\text{el}}) = P(E - E_i)$ is the attachment probability, including a Vogt–Wannier capture factor and an IVR factor, such as determined in Ref. 5. Comparing $g(E, T_{\text{gas}} = T_{\text{el}})$ from Eq. (3.2) with the corresponding thermal distribution [given by Eq. (3.2) with the preexponential factor $P(E - E_i)(E - E_i)^{-1/2}$ omitted], the two distributions look similar but are not identical. However, the quantum structure of the two curves makes it difficult to illustrate the differences. Replacing Eq. (3.2) by a smoothed expression with a continuous

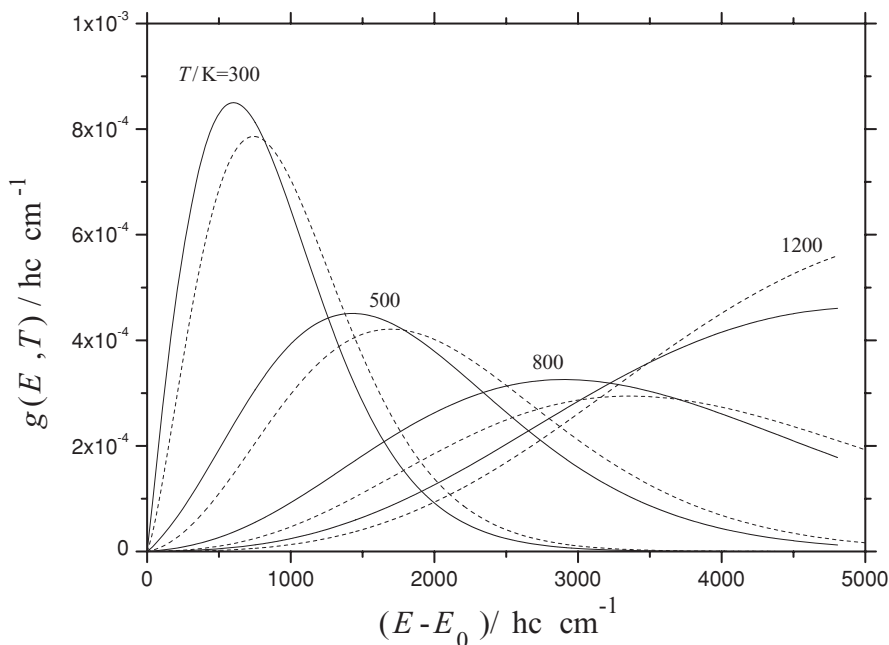


FIG. 1. Energy distributions $g(E, T)$ of POCl_3^- generated by electron attachment (full lines) in comparison to thermal distributions (dashed lines) at $T = T_{\text{el}} = T_{\text{gas}}$, see text.

vibrational density of states of POCl_3 , $\rho_{\text{vib}}(E_i)$, facilitates the representation. For this purpose, Eq. (3.2) is replaced by

$$g(E, T_{\text{gas}}, T_{\text{el}}) \propto \int_0^E P(E - E_i)(E - E_i)^{-1/2} \times \exp(-E_i/kT_{\text{gas}}) \exp[-(E - E_i)/kT_{\text{el}}] \times \rho_{\text{vib}}(E_i) dE_i. \quad (3.3)$$

The vibrational density of states $\rho_{\text{vib}}(E_i)$ is calculated in Whitten–Rabinovitch approximation,^{4,19} with the vibrational frequencies of POCl_3 (from DFT calculations for consistency with POCl_3^- frequencies, see the Appendix). Figure 1 illustrates $g(E, T_{\text{gas}} = T_{\text{el}})$ from Eq. (3.3) in comparison to the corresponding thermal distributions [from Eq. (3.3) with the preexponential factor $P(E - E_i)(E - E_i)^{-1/2}$ omitted]. By using Eq. (3.3), the differences between thermal and “kinetically generated” distributions of POCl_3^- are becoming more clearly visible than by using Eq. (3.2). The figure shows that the distributions generated by attachment are quasithermal; however, they correspond to slightly lower temperatures than the gas temperatures. Systematically evaluating results like those shown in Fig. 1 with respect to the positions T_{eff} of the maxima of $g(E, T)$ leads to differences between T_{eff} and $T_{\text{gas}} (= T_{\text{el}}) = T$ given approximately by

$$T_{\text{eff}} \approx 0.9 T_{\text{gas}}. \quad (3.4)$$

One notices some narrowing of the distribution compared to a thermal distribution at T_{eff} . It should be emphasized that these results are system specific. The differences, according to Eq. (3.3), will be more pronounced for smaller and less pronounced for larger target molecules. Nevertheless, the simplification of assuming thermal distributions made in Ref. 3 in

practice does not appear too serious, provided that Eq. (3.4) is obeyed. We later illustrate the quantitative consequences of reducing $T_{\text{eff}} = T_{\text{gas}}$ to $T_{\text{eff}} = 0.9 T_{\text{gas}}$.

B. Anion dissociation (1.2) and collisional stabilization (1.3)

Having characterized the energy distribution $g(E, T)$ of POCl_3^- generated by the electron attachment process (1.1), we proceed to the analysis of the measured branching fractions for POCl_3^- and POCl_2^- . We modify the analysis elaborated in part I of this series³ in several ways. For each energy E , we express the stabilization fraction $S/(S + D)$ by

$$\left[\frac{S}{S + D} \right]_E \approx \frac{k_{\text{stab}}(E)[M]}{k_{\text{stab}}(E)[M] + k_{\text{diss}}(E)}, \quad (3.5)$$

where $k_{\text{diss}}(E)$ is the specific rate constant for the dissociation process (1.2) and $k_{\text{stab}}(E)$ denotes the effective rate coefficient for the collisional stabilization process (1.3). Like in Ref. 3, we employ a statistical adiabatic channel model/classical trajectory (SACM/CT) approach^{20–25} for the characterization of $k_{\text{diss}}(E)$. We express $k_{\text{diss}}(E)$ by

$$k_{\text{diss}}(E) = f_{\text{rigid}}^{\text{tot}}(E) k(E)^{\text{PST}}, \quad (3.6)$$

where $k(E)^{\text{PST}}$ is obtained from phase space theory (PST) and the total rigidity factor $f_{\text{rigid}}^{\text{tot}}(E)$, being smaller than unity, accounts for the anisotropy of the potential. The determination of $k(E)^{\text{PST}}$ follows the method outlined in Ref. 26 and is not repeated here. However, compared to part I (Ref. 3) we employ a different method for the representation of the rigidity factor $f_{\text{rigid}}^{\text{tot}}(E)$. The functional form of $f_{\text{rigid}}^{\text{tot}}(E)$ is not obvious. Since publishing part I, in an analysis of halobenzene cation dissociations²⁴ we have gained more experience with simplified one-fit parameter expressions to determine

$f_{\text{rigid}}^{\text{tot}}(E)$ via a partial rigidity factor $f_{\text{rigid}}^{\text{trans}}(E)$ of only the transitional modes. Following this work, in contrast to part I we now express $f_{\text{rigid}}^{\text{trans}}(E)$ in the form

$$f_{\text{rigid}}^{\text{trans}}(E) = (1 - f_{\infty}) \exp[-(E - E_0)/c_{\text{loose}}] + f_{\infty}, \quad (3.7)$$

i.e., in a procedure which we term²⁴ SSACM (simplified SACM). As the present dissociation also produces a neutral atom and an ion like in halobenzene cation dissociations, we expect a similarly good performance of Eq. (3.7) as in Ref. 24. Once the parameter c_{loose} is fitted at one energy, it is applicable for all other conditions. E_0 is the dissociation energy at 0 K. The high-energy limiting value f_{∞} is estimated as $f_{\infty} = B_{\infty}(E - E_0 + E_z^*)/(s - 1)h\nu_1 h\nu_2$ where B_{∞} is the geometrical mean of the rotational constants (in energy units) of POCl_2^- , $h\nu_1$ and $h\nu_2$ are the two transitional mode quanta of POCl_3^- turning into free rotations of POCl_2^- (see the Appendix), s is the number of oscillators of POCl_3^- , and E_z^* is the zero-point energy of rigid activated complex POCl_3^- dissociating to $\text{POCl}_2^- + \text{Cl}$. This expression for f_{∞} , for the case of an atom loss, mimics the transition from PST to rigid activated complex RRKM (Rice—Ramsperger—Kassel—Marcus) theory when the parameter c_{loose} approaches zero. (For the case of the loss of a diatomic fragment, the analogous expression is constructed following Ref. 26).

Employing the molecular parameters of POCl_3^- and POCl_2^- given in the Appendix, $k_{\text{diss}}(E)$ is calculated for a variety of values of the fit parameter c_{loose} and the results are shown in Fig. 2. $k(E)^{\text{PST}}$ from phase space theory, which corresponds to $c_{\text{loose}} \rightarrow \infty$, determines the upper limit for $k_{\text{diss}}(E)$. The special form of $f_{\text{rigid}}^{\text{trans}}(E)$, such as given by Eq. (3.7) and termed SSACM, is responsible for the observation that $k_{\text{diss}}(E)$ approaches $k(E)^{\text{PST}}$ near $E = E_0$ and with increasing energy decreases toward values corresponding to RRKM theory.

The competition between dissociation (1.2) and collisional deactivation proceeds as a multistep process and can be described by a master equation. However, the finer details of the collisional deactivation and the dissociation are not known. Therefore, we simplify the approach by replacing the master equation by a step-ladder model as we did previously in part I.³ It was shown in Ref. 27 that the two approaches are nearly equivalent when the step size is chosen as the average total energy $\langle \Delta E \rangle$ transferred per collision (up- and down-transitions included). For a starting energy E , then the branching fraction $Y = S/(S + D)$ for stabilization S (competing with dissociation D) is given by

$$Y(E) = \left(\frac{S}{S + D} \right)_E = \prod_{i=1}^{T(E)} \frac{Z[M]}{Z[M] + k(E - (i - 1)|\langle \Delta E \rangle|)}, \quad (3.8)$$

where $T(E) = \text{Integer}[(E - E_0)/|\langle \Delta E \rangle|] + 1$ denotes the number of steps between E and energies below E_0 required for stabilization. $Y(E)$ finally has to be averaged over the starting energy distribution derived in Sec. III A. Z is the appropriate total collision frequency for energy transfer, here being given by the Langevin collision frequency between POCl_3^- and the bath gas M (see the Appendix). It was shown that,

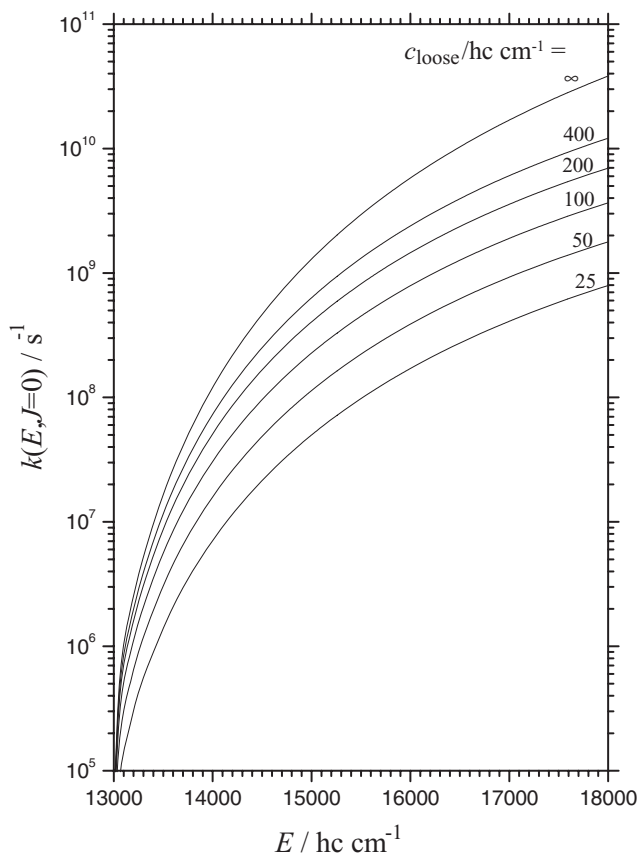


FIG. 2. Specific rate constants $k(E, J = 0)$ for the dissociation of $\text{POCl}_3^- \rightarrow \text{POCl}_2^- + \text{Cl}$. Modeling by simplified statistical adiabatic channel model [SSACM, see Eq. (3.7)] with various rigidity fit parameters c_{loose} [$c_{\text{loose}} \rightarrow \infty$ corresponds to phase space theory (PST)].

in the high pressure limit with substantial collisional stabilization, Eq. (3.8) approaches a linear Stern–Volmer-type dependence of $1/Y(E)$ on $[M]$ while a nonlinear dependence is typical for small stabilization yields at very low pressures. Averaging $Y(E)$ over broad starting distributions $g(E)$ of energies like illustrated in Sec. III A results in more pronounced nonlinearities over the complete pressure range. In Sec. III C we represent our modeling results of the averaged stabilization fraction

$$\langle Y \rangle = \int_0^{\infty} g(E, T) Y(E) dE, \quad (3.9)$$

by plotting $\langle Y \rangle^{-1}$ as a function of $[M]$ in a Stern–Volmer-type representation. Besides the parameter c_{loose} of $k(E)$, we then have a second parameter $\langle \Delta E \rangle$. We keep the two parameters constant for all conditions and test whether the experimental results are reproduced over wide ranges of conditions without further parameter changes. It turns out that the parameters cannot be fitted independently. Instead, different pairs of parameters fit the experiments equally well, see below.

C. Modeled stabilization fractions

Combining the present experimental stabilization fractions $\langle S/(S+D) \rangle$ with those of Refs. 2 (for $M = \text{N}_2$) and 3 (for $M = \text{He}$), we first fit measurements of pressure de-

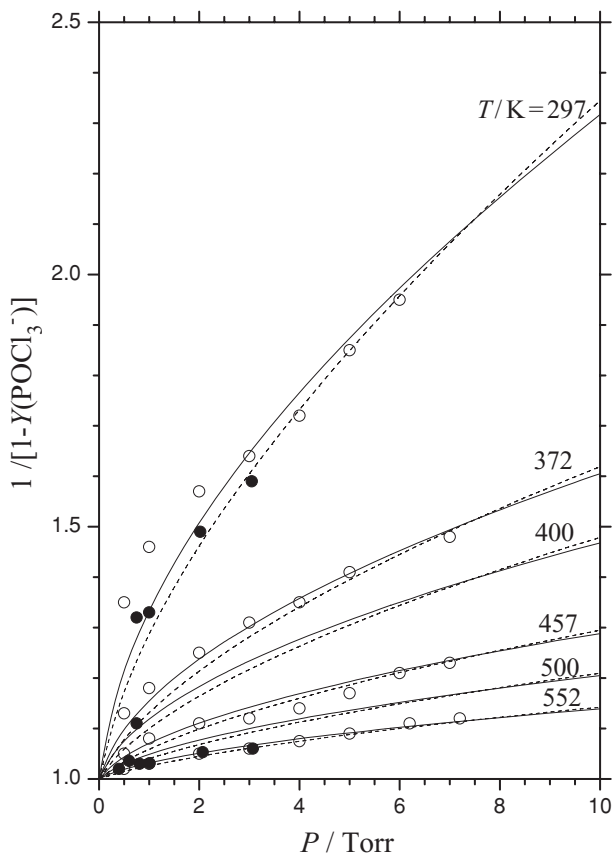


FIG. 3. Measured and modeled branching parameters $1/[1 - Y(\text{POCl}_3^-)]$ in the electron attachment to POCl_3 in the bath gas He [full circles: present work, open circles: Ref. 3, dashed lines: phase space theory (PST) with energy transfer step size $-\langle\Delta E\rangle/hc = 150 \text{ cm}^{-1}$, full lines: rigidity fit parameter $c_{\text{loose}}/hc = 25 \text{ cm}^{-1}$ and $-\langle\Delta E\rangle/hc = 10 \text{ cm}^{-1}$; see text].

pendences of branching fractions at fixed temperatures under conditions where Cl^- and Cl_2^- formations are almost negligible. This first part of the analysis covers the temperature range 300–550 K. Higher temperatures are considered later in Sec. III D.

We employ the Stern–Volmer-type representation $1/[1 - Y(\text{POCl}_3^-)]$ as a function of the pressure P where $Y(\text{POCl}_3^-)$ corresponds to $\langle S/(S+D) \rangle$, see Eqs. (3.8) and (3.9). Figure 3 compares the combined experimental results of the present work and of part I,³ for the bath gas He, with the present modeling. One indeed notices the marked curvature of the plots which is the consequence of the broad energy distribution of POCl_3^{*-} generated by the attachment process. Additional small curvatures for $Y(\text{POCl}_2^-) \rightarrow 1$ occur at very low pressures. Those are due to the multistep character of the process which can be neglected over our range of conditions.²⁷ There are only small differences between our present results (full circles in Fig. 3) and our previous measurements³ (open circles in Fig. 3). As mentioned above, one notices that different pairs of fit parameters $(c_{\text{loose}}, \langle\Delta E\rangle)$ fit the Stern–Volmer-type plots equally well. Figure 3 compares $(c_{\text{loose}} \rightarrow \infty, -\langle\Delta E\rangle/hc = 150 \text{ cm}^{-1})$, corresponding to phase space theory in $k(E)$ (dashed lines), with $(c_{\text{loose}}/hc = 25 \text{ cm}^{-1}, -\langle\Delta E\rangle/hc = 10 \text{ cm}^{-1})$ (full lines). The modeling with $(c_{\text{loose}}/hc = 100 \text{ cm}^{-1}, -\langle\Delta E\rangle/hc$

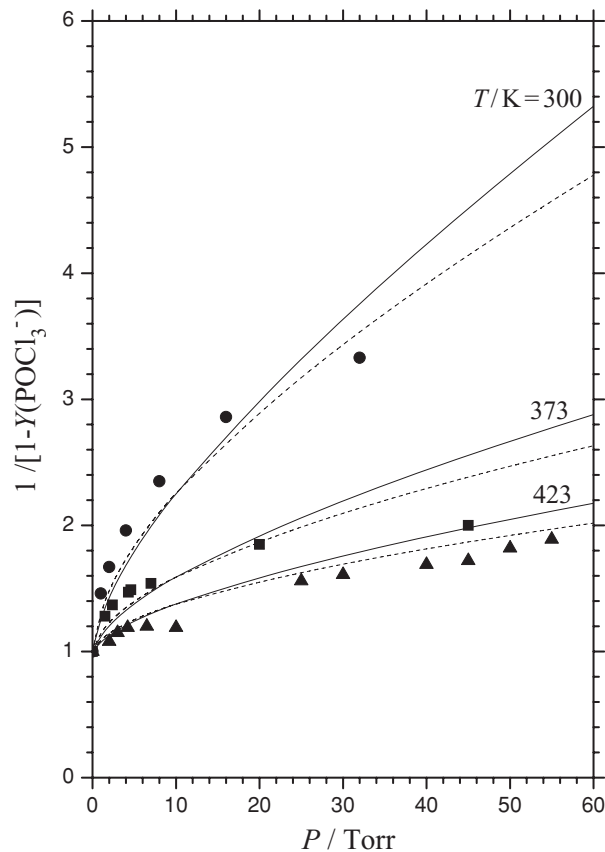


FIG. 4. As Fig. 3, but for the bath gas N_2 [experimental points from Ref. 2, dashed lines: PST with $-\langle\Delta E\rangle/hc = 120 \text{ cm}^{-1}$, full lines: $(c_{\text{loose}}/hc, -\langle\Delta E\rangle/hc) = (25 \text{ cm}^{-1}, 8 \text{ cm}^{-1})$].

$= 42 \text{ cm}^{-1}$) is between these cases and is not shown. The order of magnitude of $-\langle\Delta E\rangle/hc$, with its maximum of 150 cm^{-1} for PST in $k(E)$, is consistent with the conclusion that collisional energy transfer of excited ions is far from being “strong.” It is rather of similar character to the “weak” collisional energy transfer observed for excited neutral molecules.^{28–32}

The results of Ref. 2 with the bath gas N_2 , extending over the temperature range 300–423 K and employing pressures up to 1 bar, have been evaluated previously in part I.³ We reevaluated them in the present work using our improved modeling scheme. As the $1/Y(\text{POCl}_2^-)$ versus pressure plot exaggerates experimental scatter at high pressures, we limited our Stern–Volmer-type representation of the data to pressures below 60 Torr. Figure 4 illustrates our new modeling results for two pairs of the parameters $(c_{\text{loose}}, \langle\Delta E\rangle)$. Slightly surprisingly we find that essentially the same parameter pairs with the same $\langle\Delta E\rangle$ represent the results within the experimental scatter. For example, Fig. 4 shows results for $(c_{\text{loose}}/hc, -\langle\Delta E\rangle/hc) = (\infty, 120 \text{ cm}^{-1})$; (dashed lines) and $(25 \text{ cm}^{-1}, 8 \text{ cm}^{-1})$; (full lines). Similar values of $\langle\Delta E\rangle$ in $M = \text{He}$ and N_2 in some cases have also been observed with excited neutral molecules, see e.g., Ref. 28, although He in most cases was found to be less efficient than N_2 (see e.g., Refs. 29 and 30 and references cited therein). The temperature dependences of Figs. 3 and 4 also illustrate the consequences of reducing $T_{\text{eff}} = T_{\text{gas}}$ to $T_{\text{eff}} = 0.9 T_{\text{gas}}$ such as given by Eq. (3.4). A reduction of T_{eff} by

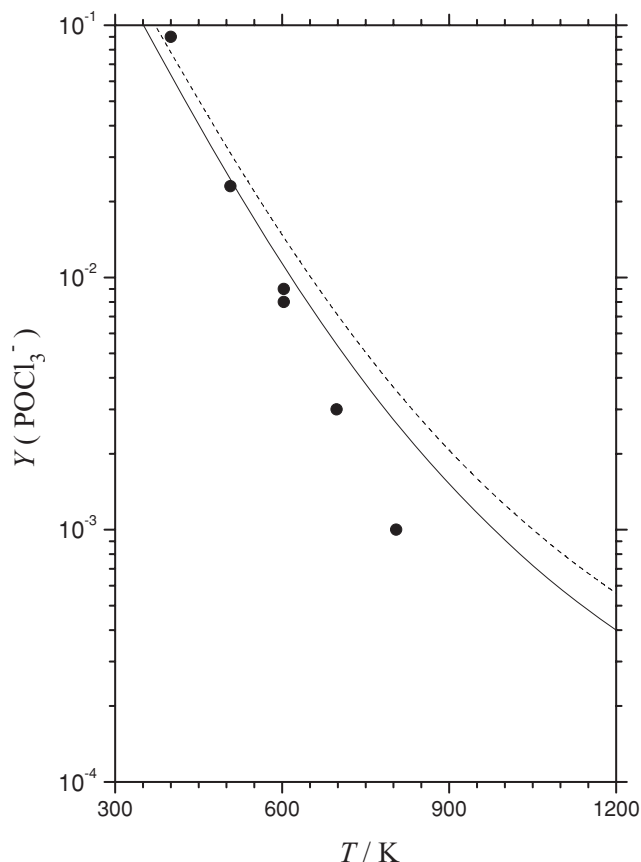


FIG. 5. As Fig. 3, with experiments and modeling from the present work for $[\text{He}] = 1.9 \times 10^{16} \text{ cm}^{-3}$ [dashed line: PST with $-(\Delta E)/hc = 150 \text{ cm}^{-1}$, full line: $(c_{\text{loose}}/hc, -(\Delta E)/hc) = (25 \text{ cm}^{-1}, 10 \text{ cm}^{-1})$].

10%, e.g., in Fig. 3 would be quite visible. It would have to be compensated by increasing the fitted $\langle \Delta E \rangle$ by about 50% when agreement with the experiments is intended.

D. High temperature results

At temperatures above about 600 K, additional pathways become important and influence the measured branching fractions. We first analyze the yield of POCl_3^- , before we proceed to the reaction products POCl_2^- , Cl^- , and Cl_2^- .

Figure 3 illustrates very good agreement between measured and modeled yields of POCl_3^- and POCl_2^- over the range 297–552 K. An extension of the modeling to the range 600–1200 K studied in the present work shows increasing differences between measured and modeled branching fractions of POCl_3^- . Above 800 K, no POCl_3^- is observed above the experimental threshold of $Y(\text{POCl}_3^-) = 10^{-3}$. Figure 5 illustrates this observation. With decreasing stabilization yields the step-ladder model in principle may become inaccurate. However, from what follows later a different explanation appears more probable. At temperatures above about 600 K, collisionally stabilized POCl_3^- may be reactivated in collisions with the buffer, see Eq. (1.5) which leads to thermal dissociation under the conditions of the present experiments. As there are only few results, we have not modeled the falloff curve for this reaction. However, a crude esti-

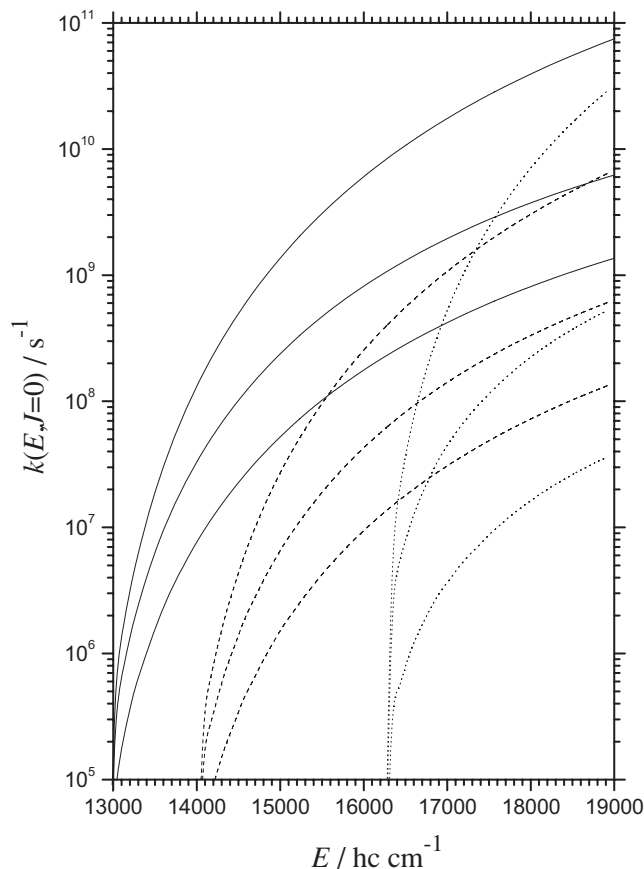


FIG. 6. SSACM modeling of specific rate constants $k(E, J=0)$ for dissociations of POCl_3^- [full lines: $\text{POCl}_3^- \rightarrow \text{POCl}_2^- + \text{Cl}$, Eq. (1.6); dashed lines: $\text{POCl}_3^- \rightarrow \text{POCl}_2 + \text{Cl}^-$, Eq. (1.7), dotted lines: $\text{POCl}_3^- \rightarrow \text{POCl} + \text{Cl}_2^-$, Eq. (1.8); within each group of three lines, the rigidity fit parameter in Eq. (3.7) is varied from $c_{\text{loose}}/hc = \infty$ (top, PST), 100 cm^{-1} (middle), to 25 cm^{-1} (bottom); see text].

mate of a high pressure thermal dissociation rate constant of $10^{16} \exp(-1.6 \text{ eV}/RT) \text{ s}^{-1}$ indicates that thermal dissociation should be fast at temperatures above 600 K. There is the second possibility that the effective $k(E)$ in the step-ladder equation (3.8), at the higher energies reached at higher temperatures, increases because of the onset of reactions (1.7) and (1.8). In order to analyze this possibility more quantitatively, specific rate constants $k(E)$ for the formation of Cl^- and Cl_2^- are modeled in the following.

Using the molecular parameters given in the Appendix, SSACM calculations of $k(E)$ for the reactions of Eqs. (1.6)–(1.8) have been made and illustrated in Fig. 6. Again there is the uncertainty of the SSACM rigidity fit parameter c_{loose} . However, a comparison of the PST curves ($c_{\text{loose}} \rightarrow \infty$) of the three channels provides already some hints. Only if c_{loose} for reaction (1.6) would be very much smaller than c_{loose} for the reactions (1.7) and (1.8), then this could explain the points in Fig. 5 at T larger than 600 K. However, this is ruled out below.

With the modeled $k(E)$ for reactions (1.7) and (1.8) one may now analyze the branching fractions for Cl^- and Cl_2^- formation. A first step in this direction is the comparison of measured branching fractions (obtained essentially in the absence of collisional stabilization of POCl_3^-) with modeling results for $Y_i = k_i(E)/\sum k_i(E)$ using $k_i(E)$ obtained by phase

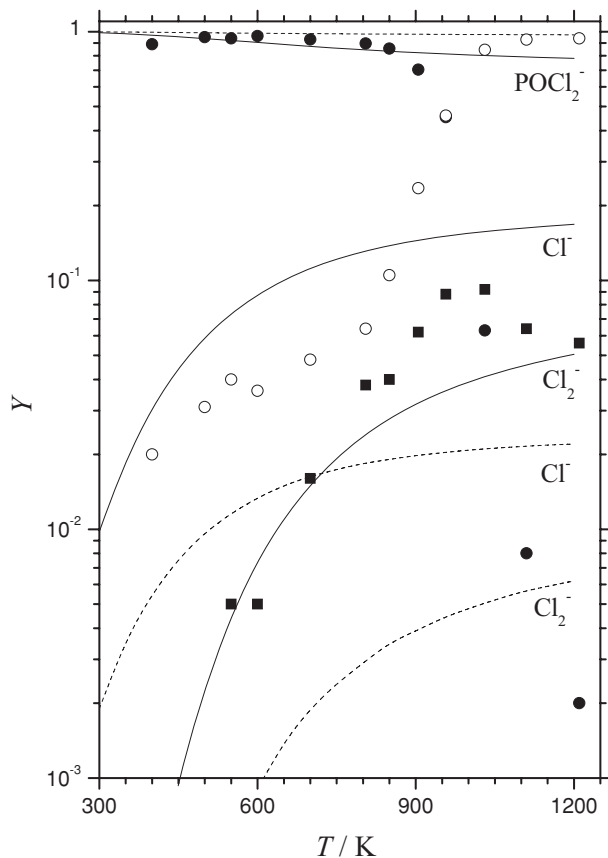


FIG. 7. Branching fractions Y of POCl_2^- , Cl^- , and Cl_2^- from electron attachment to POCl_3^- at low bath gas pressures [essentially no collisional stabilization]; experimental points from this work for POCl_2^- (●), Cl^- (○), and Cl_2^- (■); modeling results with $k(E, J=0)$ from phase space theory (dashed lines); modeling results with $c_{\text{loose}}/hc = 100 \text{ cm}^{-1}$ for POCl_2^- formation and PST for Cl^- and Cl_2^- formation (full lines); see text].

space theory, see the dashed lines in Fig. 7. The most striking difference is the marked decrease of $Y(\text{POCl}_2^-)$ and increase of $Y(\text{Cl}^-)$ at temperatures above about 700 K. This observation cannot be attributed to failures of the $k(E)$ calculations. Instead a secondary fragmentation of POCl_2^- must take place via



which destroys POCl_2^- nearly completely at 1200 K. There are two possibilities for this fragmentation, either thermal dissociation analogous to the thermal dissociation of POCl_3^- such as illustrated in Fig. 5 or dissociation by secondary chemical activation, using residual vibrational excitation from the energy partitioning between the products of the primary dissociation of POCl_3^- . As the dissociation energy of POCl_2^- (1.70 eV) is only slightly higher than that of POCl_3^- (1.60 eV), thermal dissociation is the more probable pathway. The next step is to modify the $k_i(E)$ from the PST values. When c_{loose}/hc for POCl_2^- formation is lowered to 100 cm^{-1} and $k_i(E)$ for Cl^- and Cl_2^- formation are left unchanged at PST values, the full lines in Fig. 7 are obtained. Apart from the high temperature effects associated with POCl_2^- dissociation, the agreement with Cl^- and Cl_2^- yields now is much better [one may attribute again the decrease of $Y(\text{Cl}_2^-)$ at tem-

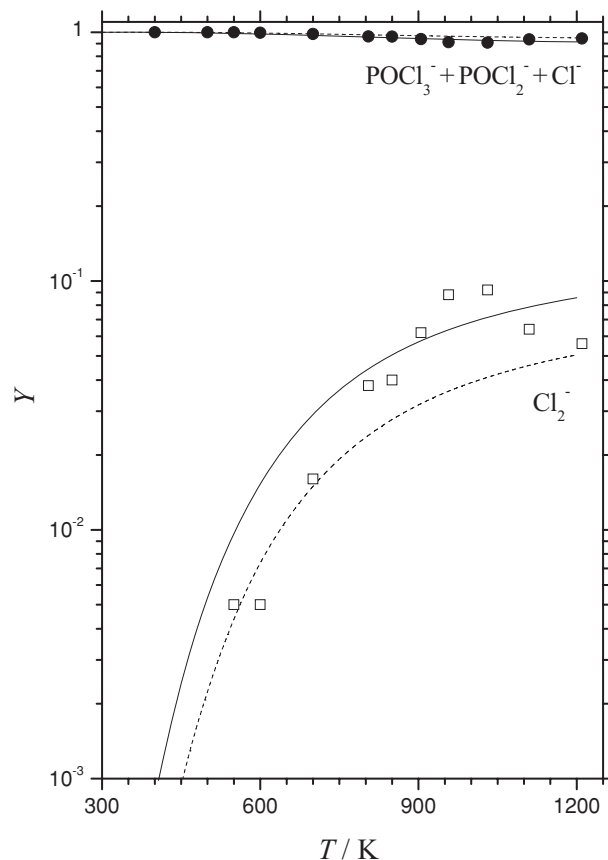


FIG. 8. Branching fractions Y for $(\text{POCl}_3^- + \text{POCl}_2^- + \text{Cl}^-)$ and Cl_2^- , as Fig. 7 [full lines for $E_0(\text{POCl}_3^- \rightarrow \text{POCl} + \text{Cl}_2^-) = 1.98 \text{ eV}$, dashed lines for $E_0(\text{POCl}_3^- \rightarrow \text{POCl} + \text{Cl}_2^-) = 2.01 \text{ eV}$].

peratures above 1000 K to thermal dissociation: the dissociation energy of Cl_2^- , 1.29 eV, is smaller than that of POCl_3^- or POCl_2^- , but the dissociation here would be in the low pressure limiting range such that higher temperatures are required for dissociation]. For a fine-tuning, in Fig. 8 we compare the combined branching fraction [$Y(\text{POCl}_3^-) + Y(\text{POCl}_2^-) + Y(\text{Cl}^-)$], accounting for reactions (1.6), (1.7), and (3.10), and $Y(\text{Cl}_2^-)$ with modeling results. For reaction (1.6) we employ $c_{\text{loose}}/hc = 100 \text{ cm}^{-1}$, while for reactions (1.7) and (1.8) we use PST (values). The modeling sensitively depends on the dissociation energies of POCl_3^- . If the G3 value of 2.01 eV for Cl_2^- formation by reaction (1.8) (dashed lines in Fig. 8) is lowered to 1.98 eV, the full lines in Fig. 8 are obtained. In view of the 0.1 eV uncertainty of the G3 calculations, the agreement with the experiments appears quite acceptable.

One may ask why PST modeling for the reactions $\text{POCl}_3^- \rightarrow \text{POCl}_2 + \text{Cl}^-$ and $\text{POCl}_3^- \rightarrow \text{POCl} + \text{Cl}_2^-$ is acceptable while SSACM with considerable rigidity ($c_{\text{loose}}/hc = 100 \text{ cm}^{-1}$) is employed for $\text{POCl}_3^- \rightarrow \text{POCl}_2^- + \text{Cl}$. The difference can be attributed to the polarizability of the neutral fragments, which for Cl ($\alpha = 2.18 \times 10^{-24} \text{ cm}^3$) is markedly smaller than for POCl ($\alpha = 6.10 \times 10^{-24} \text{ cm}^3$) and POCl_2 ($\alpha = 8.5 \times 10^{-24} \text{ cm}^3$) such that stronger isotropic long-range potentials in reactions (1.7) and (1.8) may produce a smaller anisotropy of the overall potential which results in larger values of the rigidity fit parameter c_{loose} to be used in the SSACM calculations.

IV. CONCLUSIONS

The present work illustrates the necessity to perform a detailed kinetic modeling of the electron attachment processes when metastable anions are formed as intermediates. Even when the anions are not stabilized by collisions (or radiation), the fragments may undergo secondary dissociations employing residual energy from the primary dissociation. In the presence of collisions, thermal dissociations may also take place and gain importance with increasing temperature. The present analysis of electron attachment to POCl₃ has illustrated the variety of possible pathways and its modeling by unimolecular rate theory. This modeling is not parameter-free. However, the present approach has limited the number of fit parameters to a minimum. Once the parameters are fixed, extrapolations of experimental data over wide ranges of conditions can be made.

Analyzing the dynamics of the metastable anions generated in electron attachment by chemical activation-type unimolecular rate theory requires knowledge of their energy distributions. The present work has demonstrated that this distribution is nearly thermal, but that its effective temperature is lower than the electron and gas temperature. In order to determine the distribution, the electron attachment rate coefficients have to be known over a wide range and have to be analyzed. In part II of this series, this was done in the framework of electron capture theory leading to empirical electron-phonon coupling factors (IVR factors) which then are used for the determination of the energy distribution of the excited anions formed by attachment.

The present series of three articles (Refs. 3, 5, and the present work) on electron attachment to the polar target POCl₃ nicely complements our earlier series (Refs. 6–8) on electron attachment to the nonpolar target SF₆. The polarity influences the attachment rate but the kinetic modeling of the processes of the anions formed is largely independent of this quantity. We showed that the complexity of the two attachment systems can be unraveled when the kinetic modeling is done on a very detailed level. In this way, the two systems present useful prototypes for the analysis of electron attachment dynamics with intermediate stabilizable anion formation.

ACKNOWLEDGMENTS

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APPENDIX: MOLECULAR PARAMETERS USED IN MODELING

Frequencies (in cm⁻¹). POCl₃: 1304.4, 561.1 (2), 456.4, 322.1 (2), 256.0, 181.1 (2); POCl₃⁻: 1232.1, 401.1, 383.2,

268.7, 208.2, 172.9, 133.7, 80.8, 39.6; POCl₂: 1216.4, 509.7, 454.0, 312.8, 264.9, 182.7; POCl₂⁻: 1201.3, 392.3, 329.6, 250.8, 199.0, 127.2; POCl: 1273.3, 477.4, 296.7; Cl₂⁻: 201.0 [all from B3LYP/6–311+G (3df) calculations with scaling factor 0.989].

Rotational constants (in cm⁻¹). POCl₂⁻: 0.1481, 0.0776, 0.0550; POCl₂: 0.1708, 0.0890, 0.0610; POCl: 1.108, 0.1477, 0.1303; Cl₂⁻: 0.1316 ($\sigma = 2$).

Dissociation energies (at 0 K, in eV). Cl-POCl₂⁻: 1.60; POCl₂-Cl⁻: 1.73; POCl-Cl₂⁻: 2.01; POCl-Cl⁻: 1.70; Cl₂⁻ → Cl⁻ + Cl: 1.29, from GAUSSIAN 03 calculations, see also Ref. 10.

PST calculations with $W(E, J = 0) \approx E/B_1$ for transitional modes leading to an atom and a spherical top (B₁) and $W(E, J = 0) \approx (E^2/2B_1^{3/2}B_2^{1/2}) \arcsin[B_1/(B_1 + B_2)]^{1/2}$ for transitional modes leading to a linear molecule (B₂) and a spherical top (B₁); B₁ = geometrical mean of rotational constants: B₁(POCl₂⁻) = 0.0858, B₁(POCl₂) = 0.0975, B₁(POCl) = 0.277 cm⁻¹; see Ref. 26. Frequencies of transitional modes becoming free rotors: 80.8 and 133.7 cm⁻¹ for POCl₃⁻ → POCl₂⁻ + Cl.

Langevin rate constants for POCl₃^{-*} + M: 5.37 × 10⁻¹⁰ cm³ s⁻¹ (M = He) and 6.37 × 10⁻¹⁰ cm³ s⁻¹ (M = N₂).

Polarizabilities (in 10⁻²⁴ cm³). POCl₂: 8.51, POCl: 6.10, from B3LYP/6–311 +G(3df) calculations; Cl: 2.18 from Ref. 33. Dipole moment of POCl₃: 2.54(±0.5)D from Ref. 34.

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