Large-scale flow dynamics and radiation in pulsar $\gamma$-ray binaries

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ABSTRACT

Several gamma-ray binaries show extended X-ray emission that may be associated to interactions of an outflow with the medium. Some of these systems are, or may be, high-mass binaries harboring young nonaccreting pulsars, in which the stellar and the pulsar winds collide, generating a powerful outflow that should terminate at some point in the ambient medium.

Aims. This work studies the evolution and termination, as well as the related radiation, of the shocked-wind flow generated in high-mass binaries harboring powerful pulsars.

Methods. A characterization, based on previous numerical work, is given for the stellar/pulsar wind interaction. Then, an analytical study of the further evolution of the shocked flow and its dynamical impact on the surrounding medium is carried out. Finally, the expected nonthermal emission from the flow termination shock, likely the dominant emitting region, is calculated.

Results. The shocked wind structure, initially strongly asymmetric, becomes a quasi-spherical, supersonically expanding bubble, with its energy coming from the pulsar and mass from the stellar wind. This bubble eventually interacts with the environment on $\sim$ pc scales, producing a reverse and, sometimes, a forward shock. Nonthermal leptonic radiation may be efficient in the reverse shock. Radio emission is expected to be faint, whereas X-rays can easily reach detectable fluxes. Under very low magnetic fields and large nonthermal luminosities, gamma rays may also be significant.

Conclusions. The complexity of the stellar/pulsar wind interaction is likely to be smoothed out outside the binary system, where the wind-mixed flow accelerates and eventually terminates in a strong reverse shock. This shock may be behind the extended X-rays observed in some binary systems. For very powerful pulsars, part of the unshocked pulsar wind may directly interact with the large-scale environment.

Key words. X-rays: binaries–ISM: jets and outflows–Radiation mechanisms: nonthermal

1. Introduction

Gamma-ray binaries are compact sources that present nonthermal emission in the GeV and/or TeV bands and, typically, they are also moderate-to-strong emitters in radio and X-rays. The radiation in gamma-ray binaries is related to transient or persistent outflows, which can interact either with themselves in the form of internal shocks or with the environment on different scales. The number of members of the class of gamma-ray binaries is growing, being at present around ten, including unconfirmed candidates (e.g. Albert et al. 2006, 2007; Aharonian et al. 2005a, 2005b; Abdo et al. 2009a, 2009b, 2009c, 2010a, 2010b, 2011; Tavani et al. 2009a, 2009b; Sabatini et al. 2010; Williams et al. 2010; Tam et al. 2010; Hill et al. 2011; Falcone et al. 2011; Corbet et al. 2011).

Several gamma-ray binaries present hints or clear evidence of interactions between an outflow and their medium on large scales: Cygnus X-3, LS I +61 303, LS 5039, PSR B1259–63, and the gamma-ray emitter candidate Cygnus X-1 (Heindl et al. 2003; Sánchez-Sutil et al. 2008; Paredes et al. 2007; Pavlov et al. 2011a; Durant et al. 2011; Marti et al. 1996; Gallo et al. 2005; Russell et al. 2007).
Sarty et al. [2011] Rea et al. [2010, 2011] McSwain et al. [2011] Ribó [2011] see also Bosch-Ramon & Khangulyan [2009]. In the past, several works have considered LS 5039 and LS 1 +61 303 good microquasar candidates because of their radio morphology and emission properties (e.g. Taylor et al. [1992]; Paredes et al. [2000]; Massi et al. [2001, 2004]; Paredes et al. [2002] Romero et al. [2005]; Paredes et al. [2006] Bosch-Ramon et al. [2006] Massi & Kaufman Bernadó [2009]. However, it has also been proposed that the phenomenology of these sources and, in particular, their milliarcsecond (mas) scale radio morphology may be more compatible with a nonaccreting pulsar scenario (e.g. Maraschi & Treves [1981]; Martocchia et al. [2013]; Dubus [2006] Chernyakova et al. [2006]; Sierpowska-Bartosik & Torres [2008]; Sierpowska-Bartosik & Torres [2009]; see however Romero et al. [2007]). Both binaries are high-mass systems, with LS 5039 harboring an O6.5 V star (Clark et al. [2001]), and LS 1 +61 303, an early Be star (Hutchings & Crampton [1981]).

Extended X-rays have been found in LS 5039, with angular size $\theta \sim 1'\!-\!2'\!-\!3' (\sim 2\!-\!4\!\times\!10^{15} \text{ cm at 2.5 kpc};$ Casares et al. [2005a]), X-ray flux $\approx 9\times 10^{-15} \text{ erg s}^{-1} \text{ cm}^{-2}$ and photon index $\sim 1.9\!-\!3.1$ (Durant et al. [2011]), and possibly also in LS 1 +61 303, with $\theta \sim 10'' (\sim 3\!\times\!10^{15} \text{ cm at 2 kpc};$ Frail & Hjellming [1991]), and X-ray flux $\approx 2\times 10^{-14} \text{ erg s}^{-1} \text{ cm}^{-2}$ (Paredes et al. [2001]). It is noteworthy that the gamma-ray binaries HESS J0632+057 (Aharonian et al. [2007]; Hinton et al. [2009]; Skilton et al. [2010]; Falcone et al. [2010, 2011]; Moldon et al. [2011]) and 1FGL J1018.6–5856 (Corbet et al. [2011]; Pavlov et al. [2011]; de Ona Wilhelmi et al. [2010]) may host a nonaccreting pulsar as well, although a microquasar scenario cannot be discarded.

Summarizing, among the several gamma-ray binaries presenting hints or evidence of interactions with the medium, three of them may (one for sure) host a nonaccreting pulsar. In addition, extended X-ray emission may be eventually discovered as well in HESS J0632+057 and 1FGL J1018.6–5856, another two pulsar binary candidates. At present, the dynamics and radiation of an outflow from a pulsar gamma-ray binary has not been studied far from the binary system. Given the recent findings of extended emission, it seems necessary to analyze the flow evolution beyond the stellar/pulsar wind region and its interaction with the ISM. This is the goal of this work, which is distributed as follows. In Sect. 2.1 the main properties of the binary generated flow are described. In Sect. 2.2 the general properties of the interaction between the flow and the external medium, the progenitor supernova remnant (SNR; young sources), or the interstellar medium (ISM; older sources) are characterized analytically, and in Sect. 3 the expected nonthermal emission from radio to gamma rays is computed. Finally, in Sect. 4 the results are discussed in the context of PSR B1259–63, LS 1 +61 303 and LS 5039 (assuming that the last two host a powerful pulsar), and some final remarks are made in Sect. 6. All through the paper, egs units are used.

1 Rea et al. [2010] did not find evidence of extended X-rays in LS 1 +61 303 in longer observations than those studied in Paredes et al. [2007]. However, in their observations the X-ray counts were integrated along one spatial dimension in the CCDs, which only allows finding an extension signal in specific directions.

2. Physical scenario

2.1. The stellar-pulsar wind shock

In Figure 1 the pulsar high-mass binary scenario is sketched. For a general description of the scenario on the binary scales, see for instance Tavani & Arons [1997]. As seen in the figure, the stellar and the pulsar winds collide to form two bow-shaped standing shocks. An important parameter that characterizes the wind interaction region is the pulsar to stellar wind momentum flux ratio (e.g. Bogovalov et al. [2003]):

$$\eta = \frac{L_{\text{sd,12}}}{M_{w,12} c} \approx 0.06 \frac{L_{\text{sd,37}} M_{\text{w,12}}^{-1} v_{w,8.5}^{-1}}{v_{\text{orb,12}}},$$

where $M_{w,12} = (M_{w}/3 \times 10^{-7} M_{\odot}) \text{ yr}^{-1}$ is the stellar mass-loss rate, $v_{w,8.5} = (v_{w}/3 \times 10^{8} \text{ cm s}^{-1})$ is the stellar wind velocity, and $L_{\text{sd,37}} = (L_{\text{sd}}/10^{37} \text{ erg s}^{-1})$ is the pulsar spin-down luminosity, taken here as equal to the kinetic luminosity of the pulsar wind. The stellar wind is assumed isotropic. The pulsar orbital velocity, of a few hundred km s$^{-1}$, is much lower than $v_{w}$, typically $\sim 2 \times 10^{5} \text{ cm s}^{-1}$ for massive stars (e.g. Puls et al. [2009]), so it has been neglected in this section. However, the orbital velocity may play a relevant role in determining $\eta$ in some cases, e.g. in the presence of a stellar decretion disk, as discussed in Sect. 2.2.3. It is also noteworthy that the pulsar wind is simplified here as isotropic, although a more refined treatment should account for anisotropy (see e.g., Bogovalov & Khangoulia [2002]; Bogovalov et al. [2011]).

For reasonable $\eta$-values < 1 (a scenario with $\eta > 1$ is briefly discussed in Sect. 2.2.2), the shocked wind structure is dominated by the stellar wind ram pressure, and points away from the star on the binary scales. The size of the wind colliding region can be characterized by the distance between the two shocks contact discontinuity (CD) and the pulsar,

$$R_{p} = \frac{\sqrt{\eta} R_{\text{orb}}}{1 + \sqrt{\eta}},$$

which is $\approx 7 \times 10^{11} \text{ cm}$ for $\eta = 0.1$ and a distance between the star and the pulsar of $R_{\text{orb}} = 3 \times 10^{12} \text{ cm}$. The distance between the CD and the star is then $\approx 2.5 \times 10^{12} \text{ cm}$. The CD, which separates the shocked stellar and pulsar winds, has an asymptotic half-opening angle (see Bogovalov et al. [2003] and references therein):

$$\alpha \approx 28.6° (4 - \eta^{2/3})^{1/3}.$$

Whereas the main contribution of momentum an mass generally comes from the stellar wind, the energy is mostly provided by the pulsar wind, as seen from the pulsar to stellar wind luminosity ratio:

$$\frac{L_{\text{sd,12}}}{L_{w,12}} = \frac{2 L_{\text{sd,12}}}{M_{w,12} c^{2}} \approx 12 \frac{L_{\text{sd,37}} M_{\text{w,12}}^{-1} v_{w,8.5}^{-2}}{v_{\text{orb,12}}^{2}}.$$

We notice that the wind of the pulsar prevents the latter to accrete from the stellar wind for a wide range of $\eta$-values. As a conservative estimate, we can derive the $\eta$-value for which $R_{p}$ is equal to the gravitational capture radius (Bondi & Hoyle [1944]):

$$\eta \approx \left(\frac{2GM}{R_{\text{orb}} c^{2}}\right)^{2} \approx 2 \times 10^{-6} R_{\text{orb,12}}^{2} v_{w,8.5}^{4},$$

where $M$ is the pulsar mass, and $R_{\text{orb,12}} = (R_{\text{orb}}/3) \times 10^{12} \text{ cm}$.
2.2. Shocked flow evolution

After being shocked, the pulsar wind facing the star moves at a speed $c/3$, but suffers a strong reacceleration along the CD produced by a strong pressure gradient, related to the anisotropy and inhomogeneity of the stellar wind at the pulsar location (Bogovalov et al. 2008). Because of the very low density in the downstream region, the pulsar wind shock is adiabatic (Bogovalov et al. 2008; Khangulyan et al. 2008). The stellar wind shock could be either adiabatic or radiative, but in either case the stellar wind velocity will be $\ll c$. Therefore, the two shocked winds have a relative velocity $\sim c/3 - c$, depending on how much the shocked pulsar wind has reaccelerated. Such a large velocity difference is likely to lead to the development of Kelvin-Helmholtz (KH) instabilities in the CD. This will produce entrainment of shocked stellar wind into the lighter and faster shocked pulsar wind. If the stellar wind shock is radiative, then the matter downstream collapses into a dense and cool thin layer, diminishing even farther the stability of the whole shocked structure (e.g. Stevens et al. 1992; Pittard 2009). Perturbations generated in the interface will initially move with the stellar shocked wind, growing on a timescale $t_{KH} \sim 1/c_{sw}$, where $l$ is the size of the perturbation, and $c_{sw}$ the sound speed of the shocked stellar wind. Taking $c_{sw} \approx v_{sw} \sim 10^8$ cm s$^{-1}$ and $l \sim R_p = 10^{12}$ cm, one obtains $t_{KH} \sim 10^4$ s, approximately the lapse needed by the perturbations to enter in the nonlinear regime. This implies that instabilities, turbulence, and mixing will develop on spatial scales that are similar though slightly larger than those of the binary system.

We now discuss the impact of the orbital motion on the shocked winds. To do this, we focus on three cases: the possibly more common $\eta < 1$, (e.g. $M_w > 2.5 \times 10^{-8} M_\odot$ yr$^{-1}$ for $v_w \sim 2 \times 10^8$ cm s$^{-1}$ and $L_{sd} \sim 10^{37}$ erg s$^{-1}$); more briefly, the extreme case $\eta > 1$; and under the presence of a stellar decretion disk.

2.2.1. Stellar wind momentum flux dominance

We analyze the dynamics of the gas flow in the coordinate system that corotates with the binary system at an angular velocity $\Omega = 2\pi/T$, where $T$ is the orbital period. The X-axis coincides with the line connecting the centers of the stars, the Y-axis lies in the orbital plane, and the Z-axis is normal to the orbital plane. In such a coordinate system, the Coriolis acceleration is $a_c = -2\Omega \times v$. The stellar wind moves along the X-axis with speed $\sim v_w$, acquiring a velocity $v_\perp = 2\Omega v_w t$ in the Y-direction. In the frame of the shocked-wind flow, $t = x/v_w$, and $x$ is the distance, along the X-axis, between the pulsar and a point farther away from the star. The dynamical pressure of the stellar wind in the Y-direction can be estimated as $P_\perp \approx \rho_w v_w^2 \approx (2\Omega)^2 \rho_w v_w^2 \approx (2\Omega)^2 P_w$ ($P_w = \rho_w v_w^2$). From this, the location where the pulsar wind total pressure is balanced by the stellar wind can be derived with

$$\frac{L_{sd}}{4\pi c_T^2} = P_\perp \approx \rho_w \left(\frac{4\pi}{T}\right)^2 x^2,$$

where $\rho_w = \rho_{w0}/(1 + x/R_{orb})^2$, with $\rho_{w0} = \dot{M}_w/4\pi R_{orb}^2 v_w$ the stellar wind density at the pulsar location. For $x \ll R_{orb}$, Eq. (6) can be simplified to

$$x = \left(\frac{L_{sd} v_w T^2 R_{orb}^2}{(4\pi)^2 c_T M_w}\right)^{1/4};$$

and for $x \gg R_{orb}$,

$$x = \left(\frac{L_{sd} v_w T^2}{(4\pi)^2 c_T M_w}\right)^{1/2}.$$

For typical parameters, the solution is closer to the one given by Eq. (6), therefore the bending distance can be written as

$$x_0 \approx 7 \times 10^{12} L_{sd 37} v_{w8.5}^{1/2} T_6^{1/2} \dot{M}_w^{-1/2} M_8^{-1/2} 6.5 \text{ cm},$$

where $L_{sd}$ is the luminosity of the pulsar in units of $10^{37}$ erg s$^{-1}$, $v_w$ is the pulsar wind speed in units of $10^8$ cm s$^{-1}$, $T_6$ is the age of the SNR in units of $10^6$ yr, and $\dot{M}_w$ is the wind mass-loss rate in units of $10^{-7} M_\odot$ yr$^{-1}$. The bending distance $x_0$ can vary from $10^{13}$ cm (corresponding to $\eta < 1$) to $10^{16}$ cm (corresponding to $\eta > 1$).
where $T_0 = (T/10^6 \text{ s})$. This distance is much less than in the purely ballistic case, for which $x_0 \sim cT = 3 \times 10^{16} T_0 \text{ cm}$.

It is noteworthy that the pulsar wind is shocked even in the direction opposite to the star, within a distance $\sim x_0$. Therefore, a significant fraction of the pulsar wind luminosity is reprocessed outside the binary system. Interestingly, this region may dominate the very high-energy output in pulsar gamma-ray binaries with high photon-photon absorption (see the discussion in Bosch-Ramon et al. [2008]).

If KH instabilities by themselves have not already mixed the shocked winds, isotropizing their particle, momentum, and energy fluxes, together with the Coriolis force they very likely will. Eventually, the shocked-wind flow will probably end up as a trans- or subsonic turbulent bubble, loaded with stellar wind mass and pulsar wind energy. The bubble is not confined because there is still a strong pressure gradient radially outwards. Therefore, and assuming that the whole process is adiabatic, any thermal, turbulent, or magnetic energy will eventually end up in the form of radial bulk motion. The role of the magnetic field should not change this picture much, unless the initial stellar and pulsar winds had a dynamically dominant magnetic field. (For the role of the magnetic field on binary scales; see Bogovalov et al. [2011]). The maximum velocity expansion of the bubble will be roughly its initial sound speed, which for a maximum entropy initial state (i.e. right after isotropization) is

$$v_{\text{exp}} \sim \sqrt{\frac{2 L_{\text{sd}}}{M_w}} \approx 10^9 L_{\text{sd}}^{1/2} \dot{M}_{w}^{-1/2} \text{ cm s}^{-1}. \quad (10)$$

Typically, the mas radio emission in pulsar massive binaries will come from scales larger than $x_0$, and thus this radiation should be strongly affected by the Coriolis force, as well as by shocked-wind mixing. The situation described in this section is pictured in Fig. 1 (left).

### 2.2.2. Pulsar wind momentum flux dominance

For a dominant pulsar wind, the shocked structure closes toward the star. In this case, the Coriolis force exerted by the light pulsar wind is too low and the shocked structure moves ballistically, with a bending typical distance $\sim v_w T$. Along the orbit, however, the natural bending of the shocked structure directly exposes it to the pulsar wind ram pressure, which pushes and opens the spiral to some degree. As for $\eta < 1$, for $\eta > 1$ the instabilities in the CD will also take place, and the formation of a mixing layer is expected to occupy part of the region of the free pulsar wind. However, in the direction perpendicular to the orbital plane, the pulsar wind will likely propagate freely. The energetics of this free wind may be significant, eventually terminating as a jet-like structure interacting with the surrounding medium (see, e.g., Bordas et al. [2009]). A sketch of the two cases discussed, with $\eta > 1$ and $\eta < 1$, is shown in Fig. 2.

### 2.2.3. The equatorial flow case

The situation discussed so far is that of two spherical winds interacting with each other. However, some of the systems considered in this work host Be stars, which present decretion disks around the equator. These disks are thought to be much denser than the radiatively driven stellar wind.

The disk flow is quasi-Keplerian, and moves subsonically in the radial direction with velocities around $\sim 1 \text{ km s}^{-1}$ (e.g. Porter & Rivinius 2003). Given the slow flow velocity, the flow speed determining the flux momentum ratio, in the pulsar reference frame, is near the orbital velocity of the pulsar. Outside the equatorial disk, the radiatively driven wind in Be stars is most likely polar. Such a configuration of the two stellar flows probably makes the geometry of the colliding wind region quite complex, enhancing the development of instabilities in the shocked-flow contact discontinuity (for simulations of this scenario on binary system scales, see Romero et al. [2007] and Okazaki et al. [2011]). The shocked disk material has a much larger density than the light polar wind. This implies that development of instabilities may be slower, although the sound speed of the shocked disk will be similar to the pulsar’s orbital velocity, the dynamical speed in this case. The high density of the shocked equatorial flow implies that it will likely be radiative, thereby potentiating instabilities and fragmentation. Finally, the mass-loss rate of the disk is similar or even smaller than that of the polar wind, and thus once accelerated by the pulsar wind, the flow evolution on the largest scales should not be very different from the isotropic wind case. The dense and fragmented shocked disk material will likely introduce inhomogeneities into the larger scale shocked flow, although eventually the isotropization of the particle, momentum, and energy fluxes of the larger scale structure seems a reasonable guess. However, hydrodynamical simulations on larger scales than the binary are mandatory for validating the assumption.

### 2.3. Bubble large-scale evolution

The pulsar started its life after a supernova explosion. For an explosion energy $E_{\text{SNR}} \sim 10^{51} \text{ erg}$ and ISM density $\rho_{\text{ISM}} = 1.7 \times 10^{-23} \text{ g cm}^{-3}$ ($r_{\text{ISM}} = 10 \text{ cm}^{-3}$), the SNR becomes radiative (Blinnikov et al. 1982) af-

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Fig. 2. Sketch of the two possibilities for the outcome of the interaction between the pulsar and the star winds, in the context of a binary system. To the right, the case for a very powerful pulsar, with $\eta > 1$, is presented. To the left, the case with $\eta < 1$. 
ter $t_c \approx 2 \times 10^4$ yr when achieving the radius $R_c \approx 11 (E_{\text{SNR51}}/n_{\text{ism1}})^{1/3}$ pc, where $E_{\text{SNR51}} = (E_{\text{SNR}}/10^{51}$ erg) and $n_{\text{ism1}} = (n_{\text{ism}}/10$ cm$^{-3}$). In this context, the binary system will leave the SNR after a time

$$t_{sp} \approx \left( \frac{2.8 E_{\text{SNR}} R_c^2}{\rho_{\text{ism}}} \right)^{1/5} v_p^{-7/5}, \quad (11)$$

i.e., $t_{sp} \approx 8 \times 10^4$ yr for $v_p \approx 2 \times 10^7$ cm s$^{-1}$.

Inside the SNR, given the high sound speed of the ambient medium, the binary driven bubble cannot generate a forward shock. Once in the ISM, the bubble forms a slow forward shock. In both situations, the supersonic expanding bubble suffers a strong reverse shock to balance the external pressure, either from the hot SNR ejecta or the shocked ISM. This reverse shock is expected to have a speed $\sim v_{exp}$ in the bubble reference frame. If the pulsar is powerful enough, the reverse shock can power a moderately bright nonthermal emitter, with a potential nonthermal luminosity $L_{\text{nt}}$ as high as $L_{\text{sd}}$. This estimate is done by neglecting the radiation losses on the binary system scales, but as long as adiabatic losses are likely to dominate in the colliding wind region (e.g., Khangulyan et al. 2008), this approximation should suffice at this stage. Thermal emission from the reverse shock can be discarded, given the low densities. Some extended thermal emission will be generated in the shocked ISM, but with its peak in the ultraviolet it may be hard to detect. Figure 1 (right) sketches the bubble termination region.

3. Dynamics of the bubble interacting with the medium

The interaction between the bubble and its environment takes place in three steps. At early times, the bubble is still surrounded by the SNR in its adiabatic or Sedov phase (Sedov 1959). Later on, the SNR forward shock in the ISM becomes radiative, entering into the so-called snow-plow phase (Cox 1972; Blinnikov et al. 1982). Finally, after the binary leaves the SNR or the latter dissipates, the bubble interacts directly with the ISM.

In the adiabatic regime, the SNR properties can be characterized through the SNR/ISM forward shock radius (Sedov 1959)

$$R_{\text{SNR}} \approx 1.15 (E_{\text{SNR}}/\rho_{\text{ism}})^{1/5} t_p^{2/5}, \quad (12)$$

where $t_p$ is the pulsar age, velocity

$$v_{\text{SNR}} \approx (2/5) R_{\text{SNR}}/t_p, \quad (13)$$

and the inner pressure is

$$P_{\text{SNR}} \approx \frac{E_{\text{SNR}}}{2 \pi R_{\text{SNR}}^2}, \quad (14)$$

assumed here to be constant. Equilibrium between bubble and SNR pressures determines the location of the boundary between these two regions: $R_{\text{ads}} \approx (3 L_{\text{sd}} t_p/10 \pi \rho_{\text{ism}} v_p^2)^{1/3}$, and the equilibrium between bubble preshock and postshock total pressures determines the location of the bubble reverse shock:

$$R_{\text{bbrs}} \approx \sqrt{\frac{L_{\text{sd}}}{2 \pi P_{\text{SNR}} v_{\text{exp}}}}. \quad (15)$$

Since the hot ejecta region has a high sound velocity, the bubble forward shock inside the SNR quickly becomes a sound wave, and the bubble shape becomes spherical.

For $t > t_c$, the SNR enters into the radiative phase, so the snow-plow solution has to be used (Blinnikov et al. 1982). The SNR/ISM forward shock has now a radius of

$$R_{\text{SNR}} \approx \left( \frac{2.8 E_{\text{SNR}} R_c^2}{\rho_{\text{ism}}} \right)^{1/7}, \quad (16)$$

a velocity of

$$v_{\text{SNR}} = (2/7) R_{\text{SNR}}/t_p, \quad (17)$$

and an inner pressure of

$$P_{\text{SNR}} \approx \frac{1}{2 \pi} \frac{\epsilon E_{\text{SNR}} R_c^2}{R_{\text{SNR}}^2}, \quad (18)$$

where $\epsilon = 0.24$. As before, the bubble reverse shock radius can be estimated using Eq. 15.

The bubble/ISM direct interaction has a strong resemblance to the interaction between a supersonic stellar wind and the ISM. Therefore, for this case the solution for a supersonic wind with continuous injection has been adopted (Castor et al. 1975). This renders the ISM forward shock location at

$$R_b \approx 0.76 \left( \frac{L_{\text{sd}}}{\rho_{\text{ism}}^2} \right)^{1/5} t_p^{2/5}, \quad (19)$$

moving with velocity

$$v_b \approx (3/5) R_b/t_p. \quad (20)$$

The inner pressure is now

$$P_b \sim \rho_{\text{ism}} v_b^2, \quad (21)$$

and again the preshock and postshock total pressure balance gives the location of the bubble reverse shock: $R_{\text{bbrs}} \approx \sqrt{L_{\text{sd}}/2 \pi P_b v_{\text{exp}}}$. Since the bubble external medium has a low sound speed, the precise shape of the bubble is less clear now, although it has been assumed to be spherical, as discussed in Sect. 2.2.

For old enough sources, say $t_p > 10^5$ yr, the proper motion of the system can affect the ISM shock, leading to the formation of a bow-shaped ISM shock. In this case, the reverse shock is located approximately at the point where the bubble and ISM ram pressures become equal:

$$R_{\text{brs}} \sim \sqrt{\frac{L_{\text{sd}}}{2 \pi P_{\text{SNR}} v_{\text{exp}}^2}} \approx 0.3 \text{ pc}. \quad (22)$$

Using the model just described, the relevant distances, velocities, and pressures can be computed for different system ages. Parameter values similar to those of LS 5039 and LS 1 +61 303 have been adopted, and their values are presented in Table 1. The dynamical, as well as the radiative (see next section), results may also apply to PSR B1259–63, although the comparison is less straightforward, as discussed in Sect. 5. It is noteworthy that, as long as $x_\phi$ is much smaller than the largest scales of interaction with the medium, the size difference between PSR B1259–63 and the other two sources should not introduce strong differences in the bubble propagation and termination. The results are shown in Figs. 5 and 4. The breaks in reverse shock and CD distances, and pressures,
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Table 1. Adopted parameter values

<table>
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<tr>
<th>Parameter</th>
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<tr>
<td>Star mass-loss rate [M_☉ yr⁻¹]</td>
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<td>Stellar wind velocity [cm s⁻¹]</td>
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<td>Reverse shock velocity [cm s⁻¹]</td>
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<td>Source distance [kpc]</td>
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Fig. 3. a) Evolution with time of the radii of the SNR/ISM forward shock (black solid line), SNR/bubble contact discontinuity (red dashed line), and bubble reverse shock (blue dotted line). The CD radius becomes larger than the SNR shock radius, which indicates that the model adopted here does not apply after a few ×10⁴ yr. b) Evolution with time of the radii of the bubble/ISM forward (black solid line) and reverse shocks (blue dotted line).

4. Nonthermal radiation estimates

The reverse shock is a good candidate for nonthermal emission, since it is fast and strong, and basically all the bubble energy goes through it. The forward shock in the ambient medium, on the other hand, is either much slower and also less energetic (bubble/ISM case), or just a sound wave (SNR case).

4.1. Emitter characterization

To compute the particle acceleration rate in the reverse shock, we adopted the expression for a non-relativistic hydrodynamical shock in the test particle and Bohm diffusion approximations: \( \dot{\rho} = (1/2\pi)(\nu_{\text{exp}}/c)^2 q B c \) (e.g., Drury 1983), where \( B \) is the magnetic field and \( q \) the particle charge. The same \( B \) and diffusion coefficient values were assumed in both sides of the shock. The resulting energy distribution of the particles injected in the emitter depends on energy as \( \propto E^{-2} \). The \( B \)-energy density was taken equal to \( \xi_B \rho_{\text{SNR,b}} \), with \( \xi_B = 0.1 \) and 0.01. Smaller values seem less plausible, because some magnetic field is expected to be transported from the binary scales, but cannot be discarded. The maximum energies are the minimum value between the synchrotron-limited case, \( E_{\text{max}} \approx \sqrt{q c/a_2} B \), with \( a_2 = 1.6 \times 10^{-3} \), and the diffusive-escape one, \( E_{\text{max}} \approx \sqrt{3/4\pi} (\nu_b/c) q B R_{\text{sh}} \). Although the stellar photon energy density, the dominant radiation field, is higher than the \( B \)-energy density at \( R_{\text{sh}} \), the Klein-Nishina (KN) effect makes IC losses less important than synchrotron (or escape) ones at \( E_{\text{max}} \). For a wide source age range, in the case of electrons \( E_{\text{max}} \approx 100 \text{ TeV} \), but determined by synchrotron cooling for \( \xi_B = 0.1 \), and by diffusive escape for \( \xi_B = 0.01 \). For protons, the maximum energies are \( \sim 300 \text{ TeV} \) for \( \xi_B = 0.1 \) and 100 TeV for \( \xi_B = 0.01 \), both limited by diffusive escape. The differences between the maximum energies in the SNR and the bubble/ISM case are small; in particular, under diffusive escape, they are equal. Synchrotron-limited maximum energies are \( \propto B^{-1/2} \), but diffusive-escape ones are constant, because \( B \times R_{\text{sh}} \) is also constant.
via synchrotron and inverse Compton (IC) scattering. The most energetic protons may diffuse away from the reverse shock to reach the shocked ISM, but to be efficient, this mechanism requires target densities to be much higher than those considered here. To compute the synchrotron and IC emission (e.g. Blumenthal & Gould [1970]), we modeled the emitter as only one zone, taking homogeneous $B$- and radiation fields. This approach is valid for the synchrotron calculations as long as the flow is subsonic, and $\xi n$ is the same everywhere, which is admittedly a rough approximation in an ideal MHD flow. The role of diffusion in electron transport is negligible in the present context unless diffusion coefficients are much higher than Bohm. Owing to fast cooling, synchrotron X-rays are radiated close to the reverse shock region, whereas the synchrotron radio emission comes from a more distant location due to advection. The particle flux conservation means that the advection speed downstream of the reverse shock is roughly $1/R^2$, where $R$ is the distance to the reverse shock. This makes particles accumulate at

$$R \sim R_{brs} \left( 1 + 3 \frac{v_{exp}}{v_{cool}}/4 R_{brs} \right)^{1/3} \sim 10 R_{brs} ,$$

with $v_{cool}$ the relevant cooling time. Most of the IC radiation comes also from a distance $\sim R$ to the star. This is not true for very high-energy IC photons, but for the adopted $B$-values and due to the KN effect, their fluxes are minor so were neglected here (see however Sect. 4). Given the quasispherical shape of the emitter, the target photon field for IC has been taken as isotropic and monoenergetic, given its narrow band. The stellar luminosity and photon energy have been fixed to $10^{39}$ erg s$^{-1}$ and 10 eV. The luminosity injected in the form of nonthermal electrons at the bubble reverse shock was taken as 1% of the pulsar wind luminosity: $L_{nt} = 0.01 L_{wd}$. Although $L_{nt}$ is hard to determine, changes in this parameter only affect the nonthermal fluxes linearly. Adiabatic cooling has been included in the calculations, with the cooling timescale taken as $R_{SNR}^{2}/\xi v_{SNR}^{2}$. 

4.2. Spectral energy distributions and lightcurves

After characterizing the emitter as a region with roughly homogeneous properties, the maximum particle energies, and the dominant cooling processes (adiabatic and radiative), it is easy to calculate the electron evolution. For that, a constant particle injection is assumed, and electrons are evolved up to the source age of interest. Once the particle energy distribution is known, the synchrotron and IC spectral energy distributions, as well as the specific and integrated fluxes, are calculated by convolving the synchrotron and IC specific power per electron by the particle energy distribution.

The results of the radiation calculations are shown in Figs. 5 and 6. Figure 5 shows the computed synchrotron and IC spectral energy distributions for a source age of $10^4$ yr (SNR) and $3 \times 10^4$ yr (bubble/ISM), with the remaining parameter values given in Table 1. Figure 6 presents the time evolution of the surface brightness at 5 GHz, and the 1-10 keV and 0.1-10 GeV bolometric fluxes. The radio surface brightness was computed by just dividing the specific flux by the source solid angle in 1" units at 3 kpc, taking $R$ as the source size. We point out that our aim is just to provide with a crude estimate of the expected radiation. More detailed calculations of the nonthermal emission will be presented elsewhere.

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Fig. 4. a) Evolution with time of the SNR/ (black solid line) and bubble/ISM forward shock velocities (red dashed line). b) Evolution with time of the SNR/ (black solid line) and bubble/ISM pressures (red dashed line). c) Evolution with time of the SNR/ (black solid blue dashed line) and bubble/ISM magnetic fields (red dotted green dot-dashed line).
As seen in the figures, the break of the adiabatic-to-radiative phase transition appears in all the SNR lightcurves, although it is more apparent for the radio surface brightness and IC fluxes, which are strongly affected by the jump in $R$. The general evolution of $R$ produces the long-term strong decay of the SNR radio and GeV lightcurves, and a smoother decay of the bubble/ISM radio lightcurve, whereas the bubble/ISM GeV lightcurve remains more or less constant. The differences are partially caused by the evolution of the relative importance of the different radiation channels and the adiabatic one, which is not the same in the SNR and the bubble/ISM cases. The synchrotron and IC emissivities have also different time dependencies, the former depending on $\xi_B$ as well. For $\xi_B = 0.1$, X-ray emitting electrons radiate all their energy through synchrotron, rendering a flat X-ray lightcurve and photon indexes $\sim 2$. For $\xi_B = 0.01$, with the electron maximum energies limited by diffusive-escape, the maximum energy of synchrotron photons ($\propto B E^2$) decreases with time, and it quenches the X-ray flux for $t_p \gtrsim 10^5$ yr. This also explains the steepening of the synchrotron X-ray spectrum for the bubble/ISM case seen in Fig. 5. The SNR X-ray spectrum does not show this feature because it has been computed for $t = 10^4$ yr $< t_p$.

![Fig. 5. Spectral energy distributions of the synchrotron (thick lines) and IC (thin lines) emission computed for the SNR ($10^4$ yr) and the bubble/ISM ($3 \times 10^4$ yr) cases, and $\xi_B = 0.01, 0.1$.](image)

5. Discussion

The sizes of the bubble reverse shock and its downstream region give an idea of the source angular size at different wavelengths. At 3 kpc, the hard X-ray emitter would have $\theta \approx 10^\circ$ when still inside the SNR ($t \lesssim 10^4$ yr), and $\sim 20^\circ - 1^\circ$ in the bubble/ISM case ($t \approx 10^4 - 10^5$ yr). These $\theta$ values were calculated for the $\rho_{\text{rms}}$, $E_{\text{SNR}}$, and $L_{\text{sd}}$ values given in Table 1, although we need to recall their weak inter-dependence: $\theta \propto (E_{\text{SNR}} |L_{\text{sd}}/\rho_{\text{rms}}|)^{1/3}$. Extended X-ray fluxes could be detectable by an instrument like Chandra up to $t_p \sim 10^5$ yr. It is worth noting that, if synchrotron X-ray energies are detected from the reverse shock, the diffusion coefficient should be close to Bohm.

![Fig. 6. a) Lightcurve of the radio (5 GHz) surface brightness. b) Lightcurve of X-ray flux in the range 1–10 keV. c) Lightcurve of the IC flux in the range 0.1–10 GeV. Both the SNR and the bubble/ISM cases are shown in the age range $t_p = 3 \times (10^3 - 10^5)$ yr and for $\xi_B = 0.01, 0.1$.](image)
Radio emission is possibly detectable for the SNR case with $\xi_B = 0.1$, it may be hard to be found for the case $\xi_B = 0.01$, and its detection seems discarded for the bubble/ISM case for any $\xi_B$-value.

The GeV fluxes seem too low to be detectable by any current instrument, and the chances are even lower in TeV due to the Klein-Nishina effect and dominant synchrotron cooling. However, it may still be possible to get higher IC GeV and TeV fluxes increasing ten times $L_{\text{int}}$ and reducing strongly $\xi_B$ not to overcome the radio/X-ray constraints. This would lead to GeV-TeV fluxes that could be detectable by present (GeV: Fermi, AGILE; TeV: HESS, MAGIC, VERITAS) and/or forthcoming instruments (e.g. TeV: CTA). Given the spectral break at $\sim 10$ GeV introduced by adiabatic losses, the bubble reverse shock would be a good target for a $\sim 10$ GeV-threshold Cherenkov instrument.

We now briefly discuss whether the evidence or hints of extended X-rays from LS 5039, LS I +61 303, and PSR B1259–63 can be understood in the scenario posed here.

5.1. LS 5039

LS 5039 is likely a young source with an age range $(4 - 10) \times 10^5$ yr, and it has already abandoned its SNR (e.g. Ribó et al. 2002, Moldón et al. 2011). The angular size at 2.5 kpc for the bubble/ISM case is consistent with the observed angular size of the emitter, $\theta \sim 1' - 2'$, and the fluxes can be explained in the framework given here. The photon index at distances $\sim 1'$ is $\sim 1.9 \pm 0.7$, consistent with the SED shown in Fig. 5 and then softens farther out reaching $\sim 3.1 \pm 0.5$ at $\sim 2''$ (Durant et al. 2011). This can be explained by the cooling of the highest energy electrons close to the reverse shock, thereby depleting the highest energy part of photons and softening the spectrum farther from the shock. The adopted $n_{\text{ism}} = 10^{-3}$ cm$^{-3}$ is similar to the values derived for the surroundings of the LS 5039 SNR candidate (Ribó et al. 2002), and the pulsar $L_{\text{rad}}$ is probably $\sim 10^{37}$ erg s$^{-1}$, which is required to explain the GeV luminosity of the source (see Sect. 4 in Zabalza et al. 2011a). The morphology of the extended radio emission found by Durant et al. (2011) is not completely spherical, which may be explained by the only partial isotropization of the momentum flux in the inner regions of the bubble (see Sect. 2.2). A scenario with $\eta > 1$ could be also behind the anisotropy (see Sect. 2.2.2), but it seems less likely.

5.2. LS I +61 303

Assuming that the hints of extended X-rays in LS I +61 303 are real, we see that the angular size, $\theta \sim 10''$, is compatible with the bubble/ISM scenario for $t_p \lesssim 10^4$ yr, but with a low nonthermal efficiency or a very low magnetic field, given the weak X-ray flux (Paredes et al. 2007) and the radio nondetection on those scales (Martí et al. 1998).

The SNR progenitor of LS I +61 303 has not yet been found. However, extended 5 GHz emission has been detected centered on the location of LS I +61 303, with a typical size of 6-8 arcminutes and fluxes of tens of mJy (Martí et al. 1998, Muñoz-Arjona et al. 2009). It has been argued that the lack of extended X-rays on the same scales, and the low surface radio brightness (in a nonthermal scenario), may go against an SNR interpretation (Martí et al. 1998, Muñoz-Arjona et al. 2009). However, the radio emission surrounding LS I +61 303 may be mostly thermal (Muñoz-Arjona et al. 2009), coming from an SNR/ISM shock close to its radiative phase. If the $n_{\text{ism}}$ values in the region of LS I +61 303 are a bit higher than those adopted here, an SNR remnant with energy $E_{\text{SNR}} = 10^{51}$ erg would enter its radiative phase after $\sim 10^5$ yr, with a radius $\sim 10^{19}$ cm, a few arcminutes at 2 kpc. Thermal X-rays would not be expected in that case, since the shocked ISM material would be too cold. The slow proper motion of the source (Dhawan et al. 2009) is compatible with LS I +61 303 being at the center of the SNR (see however Martí et al. 1998 for image deformation). As in LS 5039, the $L_{\text{rad}}$-value in LS I +61 303 is expected to be $\sim 10^{37}$ erg s$^{-1}$ because of the high GeV luminosity of the source (see Sect. 5 in Zabalza et al. 2011b).

5.3. PSR B1259–63

PSR B1259–63 has an age of $t_p \approx 3 \times 10^5$ yr (Wex et al. 1998), and is likely now interacting directly with the ISM. With this age, and the pulsar spin-down luminosity $L_{\text{sd}} \approx 8 \times 10^{45}$ erg s$^{-1}$ (Manchester et al. 1995, Eq. 19) yields $R_{\text{res}} \sim 2 \times 10^{18}$ cm ($\sim 1$), assuming $n_{\text{ism}} = 10$ cm$^{-3}$. This is about one arcminute at 2.3 kpc and much larger than the observed $\theta \sim 4'' - 15''$ (Pavlov et al. 2011a). Nevertheless, in PSR B1259–63 it seems likely that the proper motion has already bow-shaped the ISM shock. In that case, for $n_{\text{ism}} = 10^{-3}$ cm$^{-3}$ and $v_{\text{p}} \sim 10^7$ cm s$^{-1}$, the reverse shock would be located at a distance of $\sim 3 \times 10^{17}$ cm from the system, or $\sim 10''$ neglecting projection effects. Unfortunately, the large errors of the proper motion measurements (Zacharias et al. 2005) and the low statistics of the X-ray data make it difficult to compare the X-ray extension and proper motion directions.

There is another possibility behind the extended X-rays found in PSR B1259–63. The most significant detection comes from $\sim 4''$, or $\sim 10^{17}$ cm in linear (projected) size, which is $\sim v_{\text{exp}} T$. Although the flow bending distance, $x_0$, should be less than that, the X-ray emission may be related to the asymmetric shock produced by the Coriolis force, and/or to spiral-arm merging. This radiation could not be resolved in the case of LS I +61 303 and LS 5039, which are much more compact than PSR B1259–63.

6. Final remarks

Gamma-ray binaries hosting powerful pulsars can produce supersonic flows that originate in the interaction of a pulsar wind with the wind of the companion, which may present strong anisotropies and inhomogeneities. The likely mixing of these flows on larger scales than the binary will render an expanding, rather isotropic, supersonic bubble, which will eventually terminate in the surrounding medium. The interaction of the supersonic bubble with the surrounding medium can take place in different ways depending on the age of the pulsar. For young sources, the environment will be the hot SNR ejecta, whereas it will be the shocked ISM for older objects. Although this interaction is expected to be rather symmetric, for old enough sources, possibly like PSR B1259–63, the proper motion can bow-shape the interaction structure with the ISM.
The radiation from the shocked bubble interacting with the environment may explain the observed extended X-ray emission from LS 5039, and possibly also from LS I +61 303 (if real). For PSR B1259−63, the found extended X-rays could come from inner regions of the bubble, triggered perhaps by Coriolis force shocks or some other type of dissipation mechanism. Extended X-ray emission may also eventually be detected in HESS J0632+057 and 1FGL J1018.6−5856, which could also originate in shocked wind outflows. The shape of the interaction region might allow the distinction of the driving flow, i.e. a jet or a pulsar wind, but as shown in Sect. 2.2.1 it may be not straightforward.

The complexity of the flow evolution on the different relevant scales makes a proper analytical characterization difficult, and thus makes magnetohydrodynamical simulations important. The geometry, level of anisotropy, velocity and density of the stellar flow requires careful study, in particular for binaries hosting stars with an equatorial disk, like PSR B1259−63 and LS I +61 303. Anisotropy in the pulsar wind has been also neglected here, but may play some role, at least up to intermediate scales.

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References
Albert, J. et al. 2006, Science, 312, 1771
Blinnikov, S. I., Ishchenko, V. S., Utrobin, V. P. 1982, SvAL, 8, 361
Corbet, R. H. D., Cheung, C. C., Kerr, M., 2011, ATel, 3221, 1
de Ona Wilhelmi, E. 2010, 38th COSPAR Scientific Assembly, Bremen, Germany, p.6
Dhawan, V., Miodeszniewski, A., Rupen, M. 2006, Proceedings of the VI Microquasar Workshop: Microquasars and Beyond, Como, Italy, 52.1
Drury, L. O'C., 1983, Reports on Progress in Physics, 46, 973
Hutchings, J. B., Crampton, D. 1981, PASP, 93, 486
Koldoba, A. V., Ustyugova, G. V. 2008, IJMPD, 17, 2009