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"Illusions of a Parallel Motion Algorithm"

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Please note: These are preliminary notes intended for internal distribution only.

## **Illusions of a Parallel Motion Algorithm**

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## **Overview**

### **■ A Parallel Motion Algorithm**

- **based on voting for consistent motion**
- **and winner-take-all**
- **implemented on the Connection Machine**

### **■ Psychophysics**

- **Barber Pole Illusion**
- **Non-rigidity Illusion**
- **Motion Capture Illusion**
- **Aperture Illusion**

### **■ Physiology**

- **Plaid Motion**

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## Motion Detection Theory

### Minimal Requirements

- two inputs
- non-linearity
- asymmetry

### Many EMD Algorithms

- Correlation Model (Reichardt)
- Energy Model (Adelson-Bergen)
- Veto Model (Barlow-Levick)
- Shunting Inhibition (Torre-Poggio)

### New Parallel Algorithm

- based on biology
- edge-based Alg. motivated by Veto-Scheme
- intensity-based Alg. motivated by Correlation Model

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## Voting for Motion

Our new parallel algorithm for computing the optical flow is based on the simple assumption, that the optical flow is locally uniform .

Physical constraints on motion limit the spatial variation of the optical flow field.

### Constraints

- uniqueness, each image point has a unique velocity
- continuity, surface are locally smooth

This results in a partial solution to the aperture problem

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## **The Aperture Problem**

**is an instance of the correspondence problem.**

**Without features, corresponding points can not be matched, eg. straight lines with constant intensity.**

**This is the aperture problem of the first kind.**

**For curved contours or lines with intensity variations the aperture problem can be solved.**

**This is the aperture problem of the second kind.**

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## **Voting for Motion**

**Our Parallel Motion Algorithm can solve the aperture problem of the second kind.**

- **all points in a neighborhood of a feature (edge or intensity) identify the correct motion**
- **lines with constant intensity are not disambiguated, since there are no features to match**
- **heuristic can select the motion of smallest magnitude in case of ambiguity**

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## Edge-based VMA

- 1. find and label edges
- 2. match edges by shift and compare
- 3. find local support by counting the matches in a neighborhood of a pixel
- 4. vote by choosing the displacement which has maximum local support

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## Connection Machine Implementation

- maps easily into CM-architecture
- retinotopic mapping into CM-memory
- one processor per pixel
- parallel shift and match operation
- each processor keeps record of correct matches
- vote for maximum consistency in area

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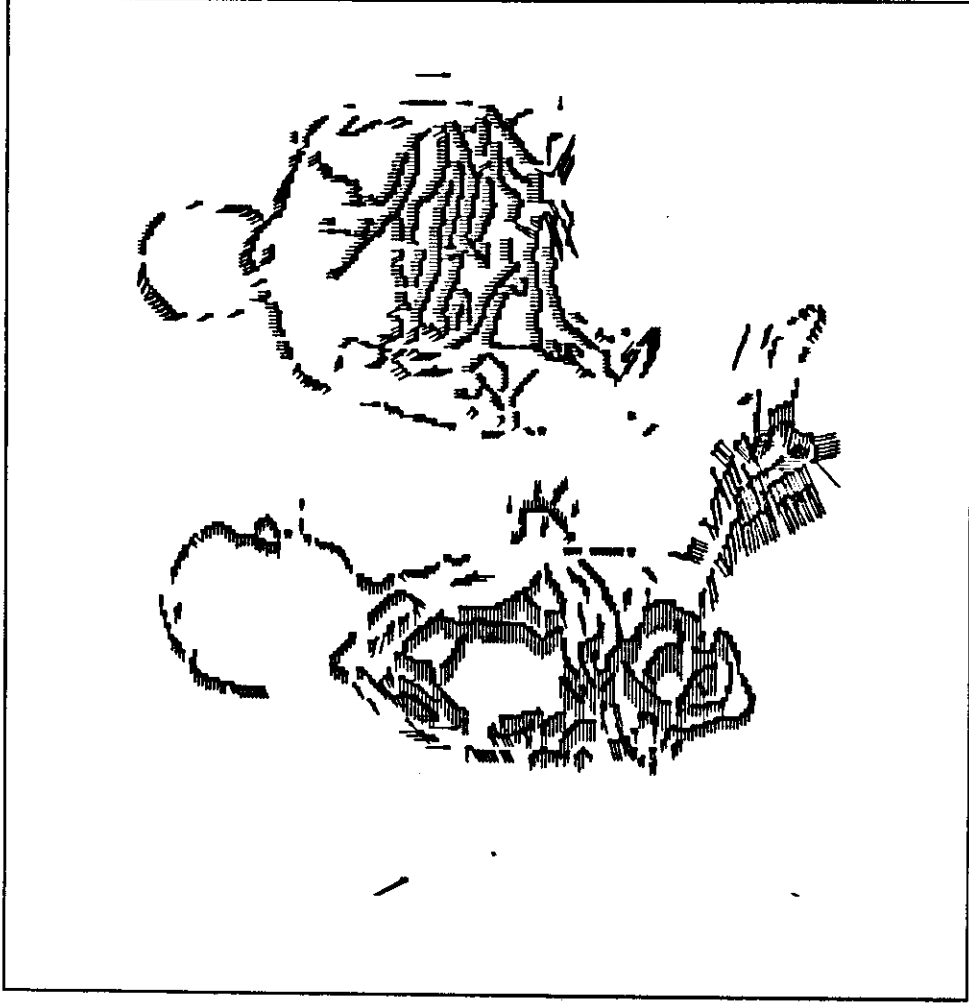
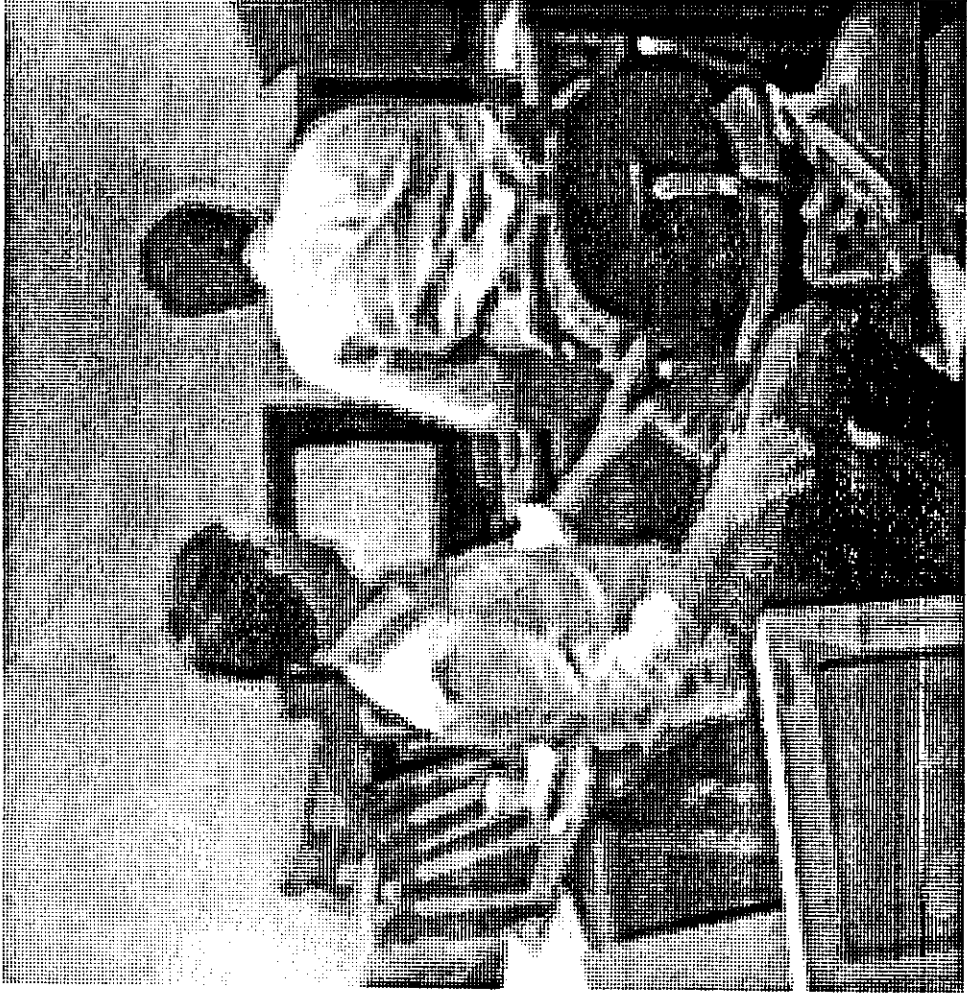


Fig. 2

## Advantages of VMA

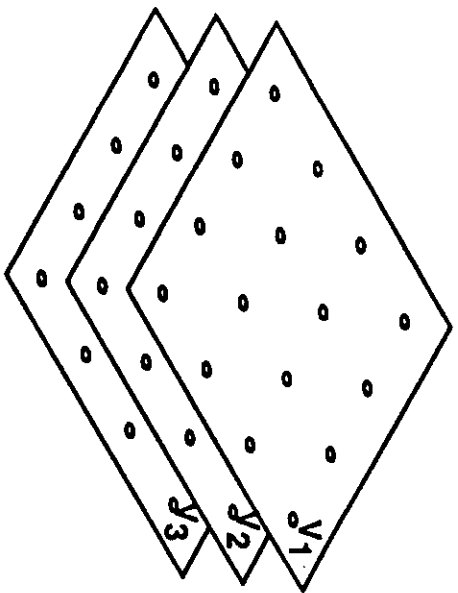
- facilitates image segmentation
- segmentation not based on output
- segmentation internal to the computational mechanism
- non-iterative  $\Rightarrow$  faster
- not noise-sensitive due to patch integ.
- dense output for intensity-based VMA
- biological plausible (based on Veto- or Correlation Model)
- psychophysical plausible (shows Barber Pole, Motion Capture and other illusions)

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## Neurophysiological Implementation ???

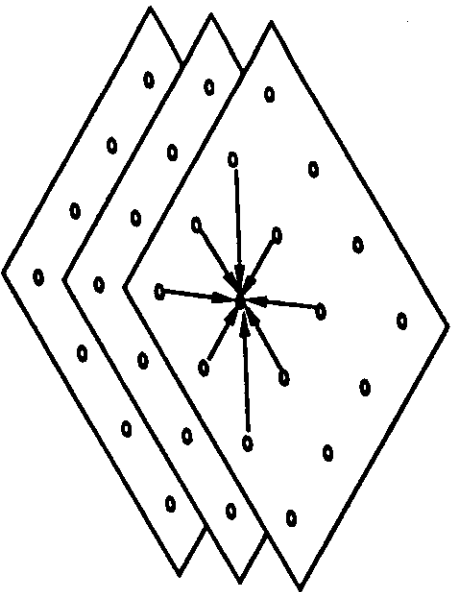
- based on a layered structure
- matching stage in V1 ?
- in different layers with progressively larger sampling basis
- summation stage (excitation)
- in mapping from V1 to MT ?
- larger receptive fields in MT summate output from V1
- consistent with psychophysical data (Adelson and Bergen, 1982)
- consistent with physiological data (Movshon et al., 1985)

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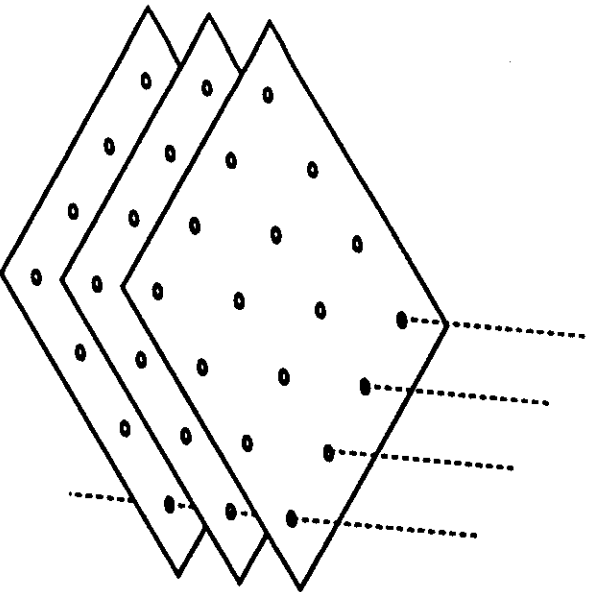
$$\tilde{E}_1(x) \circ \tilde{E}_2(x + \underline{v}\Delta t)$$

matching



$$\int_{\text{patch}} \tilde{E}_1 \circ \tilde{E}_2$$

voting



$$\max_{\text{patch}} \int \tilde{E}_1 \circ \tilde{E}_2$$

winner-take-all

Fig. 1



## Plaid Motion

- **superimposed sine-waves moving in different direction lead to perception of a coherent moving pattern (depending on relative contrast and frequency)**
- **V1 cells "see" component motion**
- **MT cells (about 20%) "see" pattern motion**
- **Algorithm "sees" pattern motion**

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## Barber Pole Illusion

- **true motion field for rotating Barber Pole is horizontal**
- **Perception is vertical**
- **but, horizontal motion field is also a possible physical interpretation of the flow field (curvature matching)**
- **therefore it is not surprising, that also many other motion algorithm show the socalled Barber Pole Illusion**
- **which is not really an illusion**

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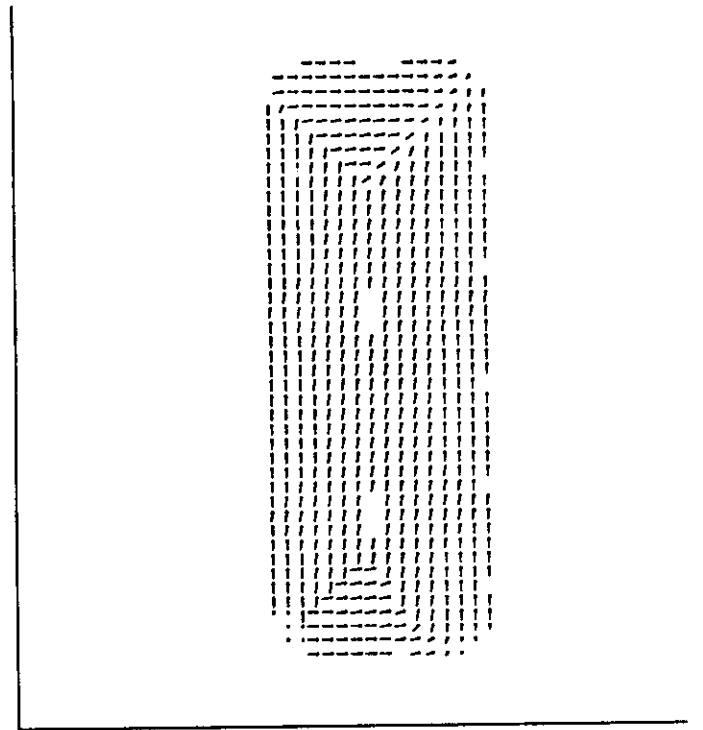
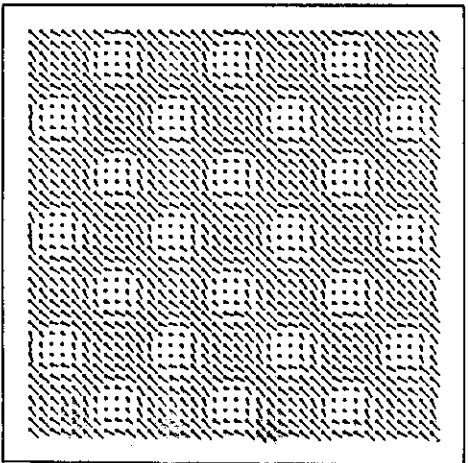
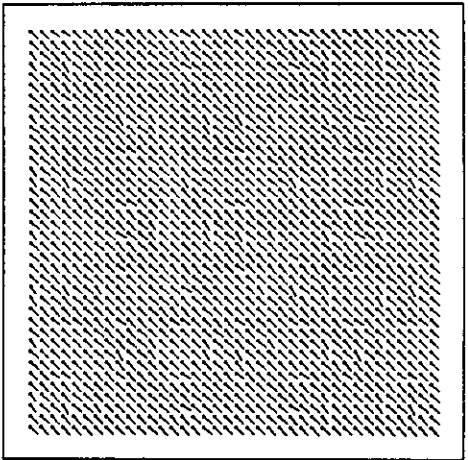
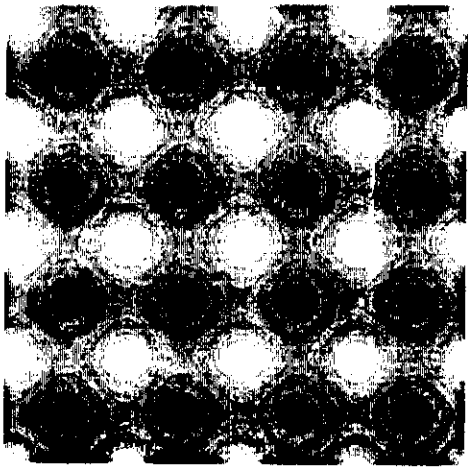


Fig 3d

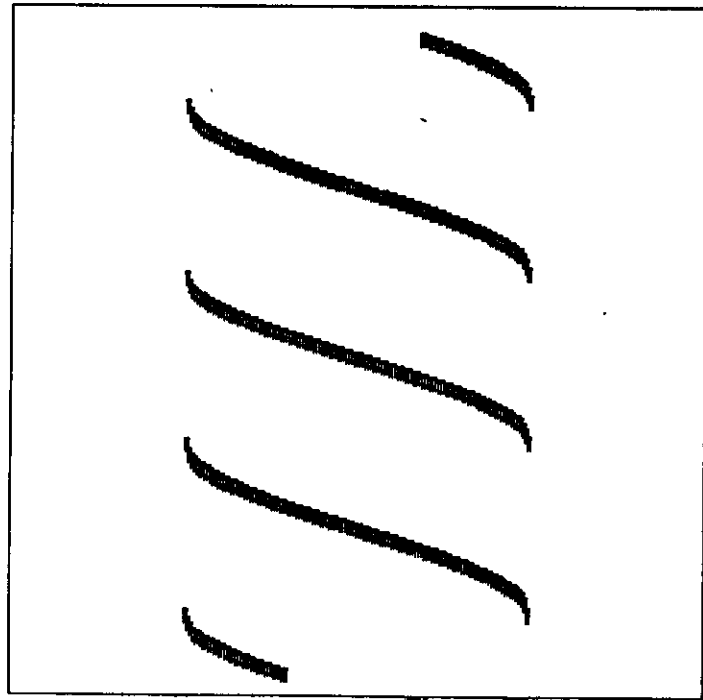
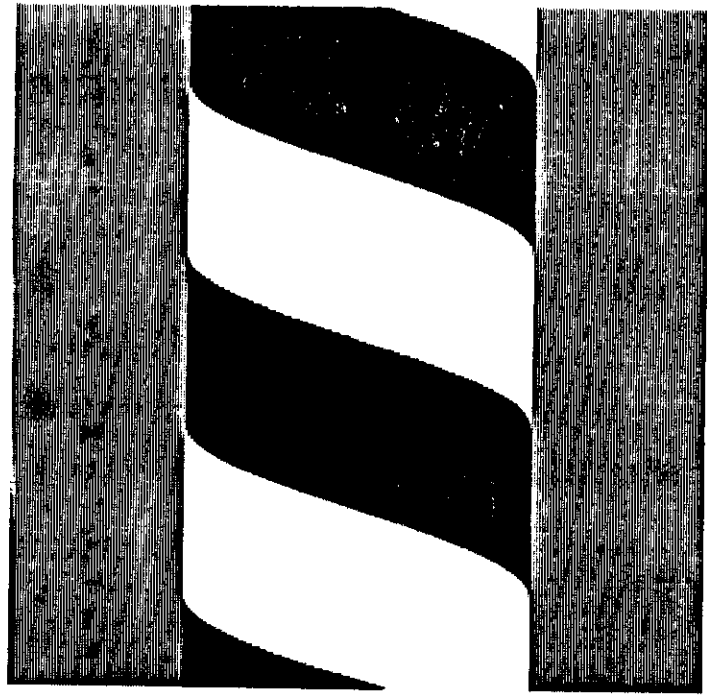
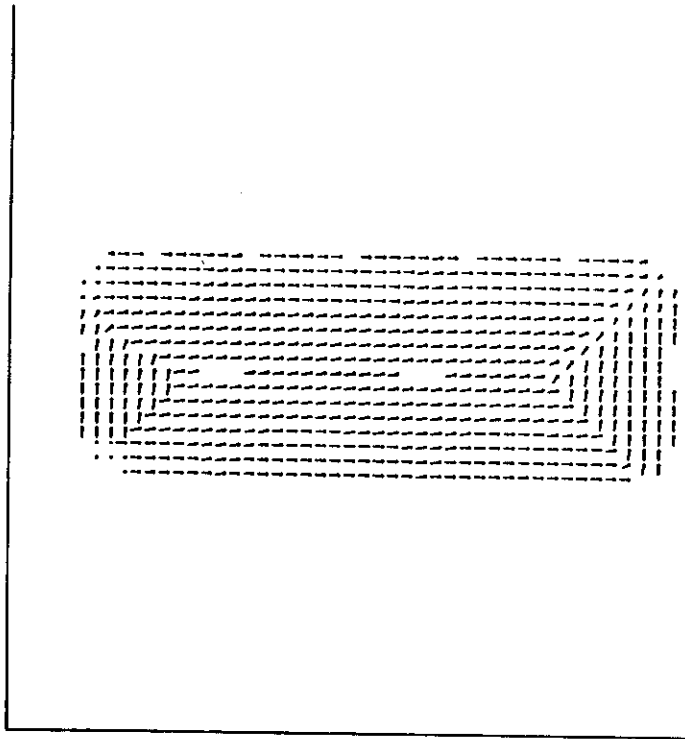


Fig. 3a

## Motion Capture Illusion

- described by Ramachandran & Inada  
Vis. Res. 1986
- **Experiment:** superimpose moving sinewave on uncorrelated random dot patterns
- **Percept:** dots move coherently with sinewave
- **Explanation:** Votes for displacement vectors are biased by intensity (local summation)
- **Note:** works only with intensity-based algorithm
- **Ramachandran Tricks:** not necessary

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## Non-rigid Motion Illusion

- described by Nakayama & Silverman  
Vis. Res. 1988
- translating curved lines look non-rigid if curvature is small enough
- hard to simulate, because our algorithm is very sensitive to curvature matching
- we had to reduce the resolution of the summation stage
- observation: end-points are very critical

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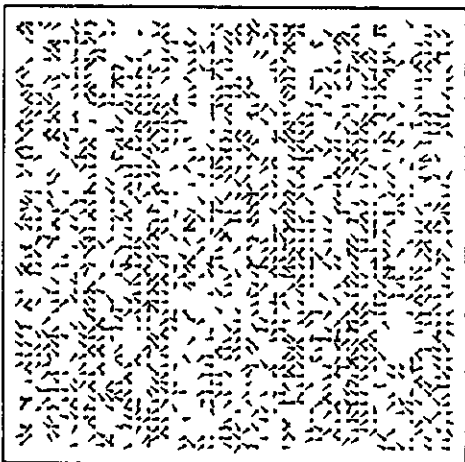
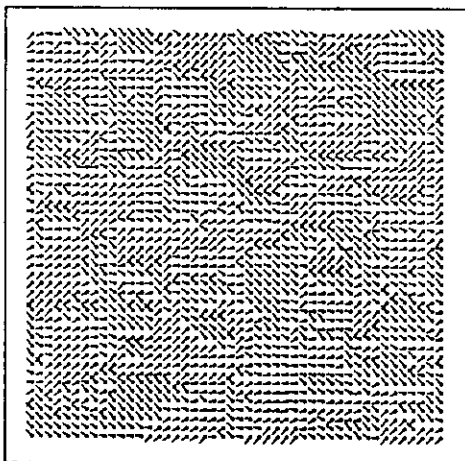
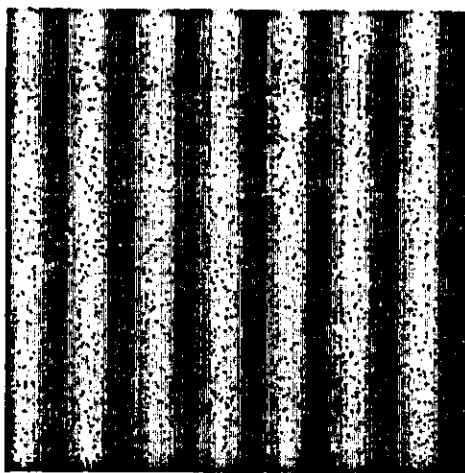


Fig. 3c

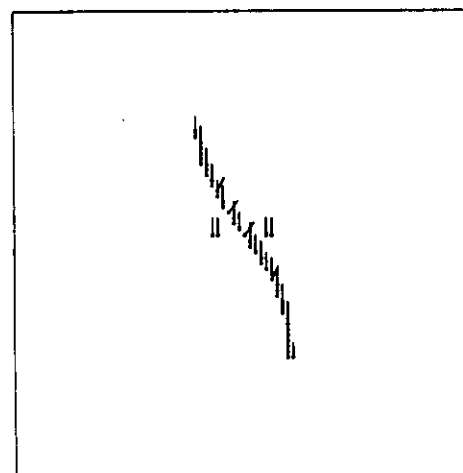
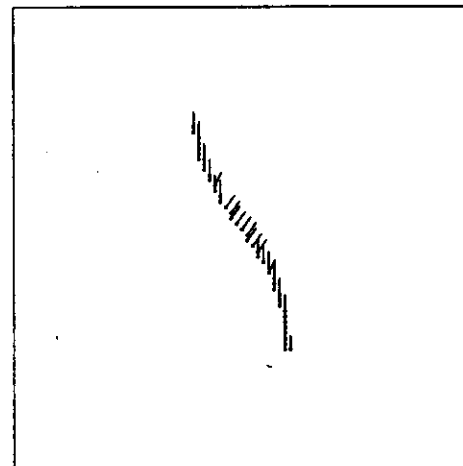
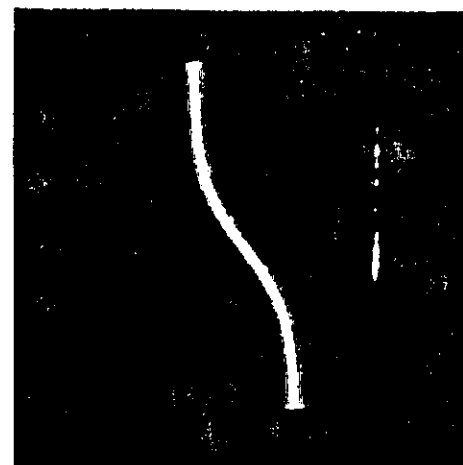


Fig 3b

