Antiproton–to–electron mass ratio determined by two-photon laser spectroscopy of antiprotonic helium atoms

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Abstract. The ASACUSA collaboration of CERN has recently carried out two-photon laser spectroscopy of antiprotonic helium atoms. Three transition frequencies were determined with fractional precisions of 2.3–5 parts in 10\textsuperscript{9}. By comparing the results with three-body QED calculations, the antiproton-to-electron mass ratio was determined as 1836.1526736(23).

1 Introduction

Antiprotonic helium ($\bar{p}$He\textsuperscript{+}) is a three-body atom [1–4] consisting of a helium nucleus, an electron in the 1s state, and an antiproton occupying a Rydberg state with high principal and angular momentum quantum numbers $n \sim \ell + 1 \sim 38$. The transition frequencies of $\bar{p}$He\textsuperscript{+} have been calculated by QED calculations to fractional precisions of $1 \times 10^{-9}$ [5]. The calculations included relativistic and radiative recoil corrections up to order $m_e c^2 \alpha^6 / h$, and nuclear size effects. By comparing the measured and calculated transition frequencies, the antiproton-to-electron mass ratio was determined [4] as 1836.1526736(23).

We have previously measured some $\bar{p}$He\textsuperscript{+} transition frequencies with a fractional precision of $10^{-7} - 10^{-8}$, by single-photon laser spectroscopy [6–9]. The precision was limited by the Doppler broadening of the resonance lines which arose from the thermal motions of the $\bar{p}$He\textsuperscript{+}. Recently [4], two-photon transitions of the type $(n, \ell) = (n - 2, \ell - 2)$ [Fig. 1(a)] were excited using two counterpropagating laser beams, such that the Doppler broadening was partially canceled [10].

2 Experiment and results

The two-photon transitions were induced between $\bar{p}$He\textsuperscript{+} states with microsecond and nanosecond-scale lifetimes against Auger emission of the electron. After Auger decay, the remaining two-body
The $\overline{p}^4$He$^+$ ion [11] was destroyed by Stark collisions with other helium atoms in the experimental target. The charged pions emerging from the resulting antiproton annihilations were detected by Cherenkov detectors [12] placed around the target. The two-photon resonance condition between the laser and $\overline{p}^4$He$^+$ was revealed as a sharp spike in the rate of antiproton annihilations [Fig. 1 (b)].

Two sets of Ti:Sapphire lasers [13] of pulse length 30-100 ns with a spectral linewidth of $\sim 6$ MHz and a pulse energy of 50–100 mJ were used to excite the antiprotonic transitions. The system included continuous-wave ( cw) lasers whose frequencies were measured to a precision of $< 1 \times 10^{-10}$ against a femtosecond optical frequency comb [14].

The experiments were carried out at the Antiproton Decelerator (AD) facility of CERN as part of its atomic physics [15] program. The AD provided 200-ns-long pulsed beams, which contained $\sim 10^7$ antiprotons of kinetic energy 5.3 MeV. The antiprotons were decelerated to $\sim 70$ keV using a radiofrequency quadrupole decelerator [7]. Secondary electron emission detectors measured the spatial profiles of the beam [16]. The $\overline{p}^4$He$^+$ atoms were produced by stopping the antiprotons in a target filled with $^4$He or $^3$He gas at temperature $T \sim 15$ K and pressure $p = 0.8 - 3$ mbar. Two horizontally-polarized laser beams of energy density $\sim 1$ mJ/cm$^2$ fired through the target excited the two-photon transitions.

The Cherenkov signal corresponding to some $10^7\overline{p}^4$He$^+$ atoms is shown in Fig. 1(b), as a function of time elapsed since the arrival of antiproton pulses at the experimental target. Lasers of wavelengths $c/\nu_1 = 417$ and $c/\nu_2 = 372$ nm were tuned to the two-photon transition $(n, \ell) = (36, 34) \rightarrow (34, 32)$, so that the virtual intermediate state lay $\Delta\nu_d \sim 6$ GHz away from the real state (35, 33). This arrangement strongly enhanced the transition probability. The annihilation spike which corresponds to the two-photon transition can be seen at $t = 2.4\mu$s. The intensity of the spike reflects the number of antiprotons populating state $(36, 34)$ [17, 18]. When the 417-nm laser was tuned some $\sim 0.5$ GHz off the two-photon resonance condition, the signal disappeared as indicated in the same figure.

Fig. 2(b) shows the resonance profile measured by detuning the $\nu_1$ laser to $\Delta\nu_d = -6$ GHz, whereas the $\nu_2$ laser was scanned between -1 and 1 GHz around the two-photon resonance defined by $\nu_1 + \nu_2$. 

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**Figure 1.** Energy level diagram of $\overline{p}^4$He$^+$ involved in the two-photon transition $(n, \ell) = (36, 34) \rightarrow (34, 32)$ (a). Cherenkov detector signals for two-photon transition (b). Experimental layout (c). From Ref. [4].
Figure 2. Single-photon resonance $^{(36,34)} \rightarrow ^{(35,33)}$ of $\bar{p}^4\text{He}^+$ (a). Sub-Doppler two-photon profiles of $(36,34) \rightarrow (34,32)$ (b) and $(33,32) \rightarrow (31,30)$ (c) of $\bar{p}^4\text{He}^+$, and $(35,33) \rightarrow (33,31)$ of $\bar{p}^3\text{He}^+$ (d). Solid lines indicate best fit of theoretical line profiles (see text) and partly overlapping arrows the positions of the hyperfine lines. From Ref. [4].

Figure 3. Fractional deviation between theoretical (squares) and experimental (circles) transition frequencies of $\bar{p}\text{He}^+$ isotopes measured by two-photon laser spectroscopy. From Ref. [4].

The linewidth (~200 MHz) of this two-photon resonance is more than an order of magnitude smaller than the Doppler- and power-broadened profile of the single-photon resonance $(36,34) \rightarrow (35,33)$ [Fig. 2(a)]. The two-peak fine structure arises due to the interaction between the electron spin and the orbital angular momentum of the antiproton. We also detected the $(33,32) \rightarrow (31,30)$ and $(35,33) \rightarrow (33,31)$ resonances of $\bar{p}^4\text{He}^+$ and $\bar{p}^3\text{He}^+$, respectively [Fig. 2(c)–(d)]. The latter resonance profile contains eight partially-overlapping hyperfine lines, which arose from the spin-spin interactions of the three constituent particles. The spin-independent transition frequencies $\nu_{\text{exp}}$ were obtained by fitting these measured profiles with a theoretical lineshape (solid lines in Fig. 2) which was determined by numerically solving the rate equations of the two-photon process [10]. The positions of the hyperfine lines were fixed to the theoretical values [19], which have a precision of < 0.5 MHz.

The experimental transition frequencies $\nu_{\text{exp}}$ (filled circles with error bars in Fig. 3) agree with the theoretical frequencies $\nu_{\text{th}}$ (squares) within a fractional precision of $(2.3 - 5) \times 10^{-9}$. The calculation
uses the fundamental constants compiled in CODATA2002 [20], such as the $^3$He- and $^4$He-to-electron mass ratios, the Bohr radius, and Rydberg constant. The charge radii of the $^3$He and $^4$He nuclei give relatively small corrections to $\nu_{th}$ of 4 – 7 MHz [5]. The correction from the antiproton radius is less than 1 MHz. The theoretical precision of $\nu_{th}$ is now mainly limited by the uncalculated radiative corrections of order $m_e c^2 \alpha^8 / h$ [5]. When the antiproton-to-electron mass ratio $M_P/m_e$ in these calculations was increased by a relative amount of $10^{-9}$, the $\nu_{th}$-value changed by 2.3–2.8 MHz. By minimizing the difference between $\nu_{th}$ and $\nu_{exp}$ and considering the systematic errors, we obtained the above antiproton-to-electron mass ratio which yielded the best agreement between theoretical and experimental frequencies. The uncertainty includes the statistical and systematic experimental, and theoretical contributions of $18 \times 10^{-7}$, $12 \times 10^{-7}$, and $10 \times 10^{-7}$. This is in good agreement with previous measurements[21–24] of the proton-to-electron mass ratio (Fig. 4). Under the assumption that CPT invariance is valid (i.e, $M_P = M_P = 1.00727646677(10)$ u), we derived a value for the electron mass, $m_e = 0.0005485799091(7)$ u [4].

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References