

# Antiproton–to–electron mass ratio determined by two-photon laser spectroscopy of antiprotonic helium atoms

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**Abstract.** The ASACUSA collaboration of CERN has recently carried out two-photon laser spectroscopy of antiprotonic helium atoms. Three transition frequencies were determined with fractional precisions of 2.3–5 parts in  $10^9$ . By comparing the results with three-body QED calculations, the antiproton-to-electron mass ratio was determined as 1836.1526736(23).

## 1 Introduction

Antiprotonic helium ( $\bar{p}\text{He}^+$ ) is a three-body atom [1–4] consisting of a helium nucleus, an electron in the 1s state, and an antiproton occupying a Rydberg state with high principal and angular momentum quantum numbers  $n \sim \ell + 1 \sim 38$ . The transition frequencies of  $\bar{p}\text{He}^+$  have been calculated by QED calculations to fractional precisions of  $1 \times 10^{-9}$  [5]. The calculations included relativistic and radiative recoil corrections up to order  $m_e c^2 \alpha^6 / h$ , and nuclear size effects. By comparing the measured and calculated transition frequencies, the antiproton-to-electron mass ratio was determined [4] as 1836.1526736(23).

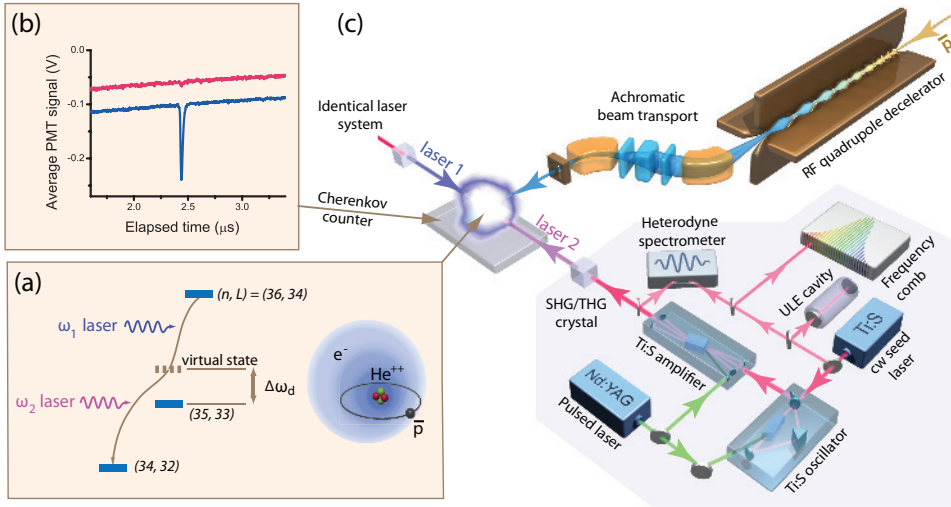
We have previously measured some  $\bar{p}\text{He}^+$  transition frequencies with a fractional precision of  $10^{-7} - 10^{-8}$ , by single-photon laser spectroscopy [6–9]. The precision was limited by the Doppler broadening of the resonance lines which arose from the thermal motions of the  $\bar{p}\text{He}^+$ . Recently [4], two-photon transitions of the type  $(n, \ell) = (n - 2, \ell - 2)$  [Fig. 1(a)] were excited using two counterpropagating laser beams, such that the Doppler broadening was partially canceled [10].

## 2 Experiment and results

The two-photon transitions were induced between  $\bar{p}\text{He}^+$  states with microsecond and nanosecond-scale lifetimes against Auger emission of the electron. After Auger decay, the remaining two-body

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**Figure 1.** Energy level diagram of  $\bar{p}^4\text{He}^+$  involved in the two-photon transition  $(n, \ell) = (36, 34) \rightarrow (34, 32)$ . Cherenkov detector signals for two-photon transition (b). Experimental layout (c). From Ref. [4].

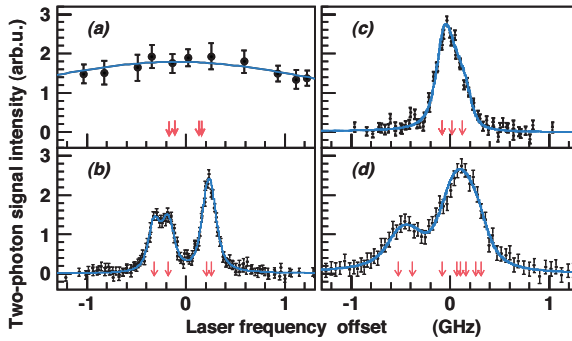
$\bar{p}\text{He}^{2+}$  ion [11] was destroyed by Stark collisions with other helium atoms in the experimental target. The charged pions emerging from the resulting antiproton annihilations were detected by Cherenkov detectors [12] placed around the target. The two-photon resonance condition between the laser and  $\bar{p}\text{He}^+$  was revealed as a sharp spike in the rate of antiproton annihilations [Fig. 1 (b)].

Two sets of Ti:Sapphire lasers [13] of pulse length 30–100 ns with a spectral linewidth of  $\sim 6$  MHz and a pulse energy of 50–100 mJ were used to excite the antiprotonic transitions. The system included continuous-wave (cw) lasers whose frequencies were measured to a precision of  $< 1 \times 10^{-10}$  against a femtosecond optical frequency comb [14].

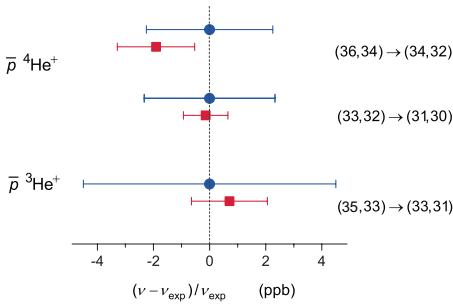
The experiments were carried out at the Antiproton Decelerator (AD) facility of CERN as part of its atomic physics [15] program. The AD provided 200-ns-long pulsed beams, which contained  $\sim 10^7$  antiprotons of kinetic energy 5.3 MeV. The antiprotons were decelerated to  $\sim 70$  keV using a radiofrequency quadrupole decelerator [7]. Secondary electron emission detectors measured the spatial profiles of the beam [16]. The  $\bar{p}\text{He}^+$  atoms were produced by stopping the antiprotons in a target filled with  $^4\text{He}$  or  $^3\text{He}$  gas at temperature  $T \sim 15$  K and pressure  $p = 0.8 - 3$  mbar. Two horizontally-polarized laser beams of energy density  $\sim 1$  mJ/cm $^2$  fired through the target excited the two-photon transitions.

The Cherenkov signal corresponding to some  $10^7$   $\bar{p}\text{He}^+$  atoms is shown in Fig. 1(b), as a function of time elapsed since the arrival of antiproton pulses at the experimental target. Lasers of wavelengths  $c/\nu_1 = 417$  and  $c/\nu_2 = 372$  nm were tuned to the two-photon transition  $(n, \ell) = (36, 34) \rightarrow (34, 32)$ , so that the virtual intermediate state lay  $\Delta\nu_d \sim 6$  GHz away from the real state (35, 33). This arrangement strongly enhanced the transition probability. The annihilation spike which corresponds to the two-photon transition can be seen at  $t = 2.4\mu\text{s}$ . The intensity of the spike reflects the number of antiprotons populating state (36, 34) [17, 18]. When the 417-nm laser was tuned some  $\sim 0.5$  GHz off the two-photon resonance condition, the signal disappeared as indicated in the same figure.

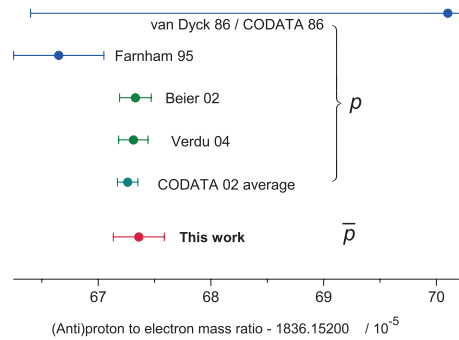
Fig. 2(b) shows the resonance profile measured by detuning the  $\nu_1$  laser to  $\Delta\nu_d = -6$  GHz, whereas the  $\nu_2$  laser was scanned between -1 and 1 GHz around the two-photon resonance defined by  $\nu_1 + \nu_2$ .



**Figure 2.** Single-photon resonance  $(36, 34) \rightarrow (35, 33)$  of  $\bar{p}^4\text{He}^+$  (a). Sub-Doppler two-photon profiles of  $(36, 34) \rightarrow (34, 32)$  (b) and  $(33, 32) \rightarrow (31, 30)$  (c) of  $\bar{p}^4\text{He}^+$ , and  $(35, 33) \rightarrow (33, 31)$  of  $\bar{p}^3\text{He}^+$  (d). Solid lines indicate best fit of theoretical line profiles (see text) and partly overlapping arrows the positions of the hyperfine lines. From Ref. [4].



**Figure 3.** Fractional deviation between theoretical (squares) and experimental (circles) transition frequencies of  $\bar{p}\text{He}^+$  isotopes measured by two-photon laser spectroscopy. From Ref. [4].



**Figure 4.** Mass ratio  $M_{\bar{p}}/m_e$  determined in this work, compared with  $M_p/m_e$  measured previously [21–24] and the CODATA 2002 value obtained by averaging them. From Ref. [4].

The linewidth ( $\sim 200$  MHz) of this two-photon resonance is more than an order of magnitude smaller than the Doppler- and power-broadened profile of the single-photon resonance  $(36, 34) \rightarrow (35, 33)$  [Fig. 2(a)]. The two-peak fine structure arises due to the interaction between the electron spin and the orbital angular momentum of the antiproton. We also detected the  $(33, 32) \rightarrow (31, 30)$  and  $(35, 33) \rightarrow (33, 31)$  resonances of  $\bar{p}^4\text{He}^+$  and  $\bar{p}^3\text{He}^+$ , respectively [Fig. 2(c)–(d)]. The latter resonance profile contains eight partially-overlapping hyperfine lines, which arose from the spin-spin interactions of the three constituent particles. The spin-independent transition frequencies  $\nu_{\text{exp}}$  were obtained by fitting these measured profiles with a theoretical lineshape (solid lines in Fig. 2) which was determined by numerically solving the rate equations of the two-photon process [10]. The positions of the hyperfine lines were fixed to the theoretical values [19], which have a precision of  $< 0.5$  MHz.

The experimental transition frequencies  $\nu_{\text{exp}}$  (filled circles with error bars in Fig. 3) agree with the theoretical frequencies  $\nu_{\text{th}}$  (squares) within a fractional precision of  $(2.3 - 5) \times 10^{-9}$ . The calculation

uses the fundamental constants compiled in CODATA2002 [20], such as the  $^3\text{He}$ - and  $^4\text{He}$ -to-electron mass ratios, the Bohr radius, and Rydberg constant. The charge radii of the  $^3\text{He}$  and  $^4\text{He}$  nuclei give relatively small corrections to  $\nu_{\text{th}}$  of 4 – 7 MHz [5]. The correction from the antiproton radius is less than 1 MHz. The theoretical precision of  $\nu_{\text{th}}$  is now mainly limited by the uncalculated radiative corrections of order  $m_e c^2 \alpha^8 / h$  [5]. When the antiproton-to-electron mass ratio  $M_{\bar{p}}/m_e$  in these calculations was increased by a relative amount of  $10^{-9}$ , the  $\nu_{\text{th}}$ -value changed by 2.3–2.8 MHz. By minimizing the difference between  $\nu_{\text{th}}$  and  $\nu_{\text{exp}}$  and considering the systematic errors, we obtained the above antiproton-to-electron mass ratio which yielded the best agreement between theoretical and experimental frequencies. The uncertainty includes the statistical and systematic experimental, and theoretical contributions of  $18 \times 10^{-7}$ ,  $12 \times 10^{-7}$ , and  $10 \times 10^{-7}$ . This is in good agreement with previous measurements [21–24] of the proton-to-electron mass ratio (Fig. 4). Under the assumption that CPT invariance is valid (i.e.,  $M_{\bar{p}} = M_p = 1.00727646677(10) \text{ u}$ ), we derived a value for the electron mass,  $m_e = 0.0005485799091(7) \text{ u}$  [4].

## Acknowledgements

This work was supported by the European Research Council (ERC-StG), European Science Foundation (EURYI), Monbukagakusho (grant no 20002003), Hungarian Research Foundation (K72172), and the Austrian Federal Ministry of Science and Research.

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