

Electric-field sensing using single diamond spins

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The ability to sensitively detect individual charges under ambient conditions would benefit a wide range of applications across disciplines. However, most current techniques are limited to low-temperature methods such as single-electron transistors^{1,2}, single-electron electrostatic force microscopy³ and scanning tunnelling microscopy⁴. Here we introduce a quantum-metrology technique demonstrating precision three-dimensional electric-field measurement using a single nitrogen-vacancy defect centre spin in diamond. An a.c. electric-field sensitivity reaching $202 \pm 6 \text{ V cm}^{-1} \text{ Hz}^{-1/2}$ has been achieved. This corresponds to the electric field produced by a single elementary charge located at a distance of $\sim 150 \text{ nm}$ from our spin sensor with averaging for one second. The analysis of the electronic structure of the defect centre reveals how an applied magnetic field influences the electric-field-sensing properties. We also demonstrate that diamond-defect-centre spins can be switched between electric- and magnetic-field sensing modes and identify suitable parameter ranges for both detector schemes. By combining magnetic- and electric-field sensitivity, nanoscale detection and ambient operation, our study should open up new frontiers in imaging and sensing applications ranging from materials science to bioimaging.

Sensitive imaging or detection of charges is an outstanding task in a variety of applications. The development, for example, of single-electron transistors (SET; ref. 5) has pushed charge sensing to an unprecedented sensitivity of 10^{-6} electron charge, and is being used in low-temperature detection and scanning applications², and in sensors in quantum devices⁶. Inspired by the development of tunnelling microscopy a variety of scanning probes have been devised to measure surface electrical properties, such as scanning capacitance microscopy (SCM; ref. 7), scanning Kelvin probe (ref. 8) and electric field-sensitive atomic force microscopy (EFM; ref. 9). Indeed, the last method has shown the remarkable ability to detect the presence of individual charges³.

We report on a fundamentally new method that uses the spin of single defect centres in diamond to sense electric-field-dependent shifts in energy levels. Sensitive electric-field detection is based on the remarkable properties of the NV centre¹⁰. The most notable of these are: the detection of fluorescence from single defects to provide an atom-sized local probe¹¹, outstandingly long spin dephasing times¹², as well as the controlled positioning of single centres^{13,14}. These properties have led to a variety of applications of the NV centre, ranging from quantum science¹⁵ and precision magnetic-field sensing^{16–24} to biolabelling^{25,26}. It is the aim of the present work to explore the interplay between the Zeeman shift, local strain effects and the Stark shift of the ground state spin manifold and use the improved understanding of this interplay for the sensing of electric fields. We will show that the decoupling of the electric sensing

transitions from magnetic fluctuations through careful alignment of the magnetic field provides a means to switch the sensor from ‘magnetic’ to ‘electric’ modes and plays a positive role in improving the spin decoherence time in a ‘dirty’ sensing environment. The rotation of the magnetic bias field provides the means to determine both the magnitude and three-dimensional orientation (up to a four-fold symmetry) of the electric field in the vicinity of single NV spins.

The NV centre is a well-studied defect in diamond, consisting of a substitutional nitrogen atom adjacent to a carbon vacancy (see Fig. 1a). The ground state spin triplet exhibits a zero-field splitting between the $m_s = 0$ and degenerate $m_s = \pm 1$ spin sub-levels of $D_{\text{gs}} \approx 2.87 \text{ GHz}$. The spin state of the triplet can be polarized and read out via optical excitation to the excited triplet state, thereby enabling the implementation of optically detected magnetic resonance (ODMR) techniques using microwave sources tuned to the ground state zero-field splitting¹¹. Stark shifts at low temperature have been demonstrated in the excited triplet states of single defect centres²⁷ and the ground state of NV ensembles²⁸. In our experiments, the electric field was generated by the application of a controlled voltage to a gold microstructure fabricated by lithography and electroplating directly on a bulk diamond sample containing NV centres. A particular NV centre close to the gold microstructure was identified and used for all of our measurements. The electric field at the location of the NV centre was calculated numerically for the given electrode geometry, taking into account the dielectric constant ($\epsilon = 5.7$) of the diamond (see Fig. 1b). To measure electric-field-induced shifts of spin sub-levels, we optically detected the electron spin-resonance transition between the $m_s = 0$ and $m_s = \pm 1$ sub-levels in the triplet ground state of the centre. On application of an electric field of about $3,000 \text{ V cm}^{-1}$, resonance line shifts of 28.4 kHz were observed (the expected value is between 1 kHz for axial and 51 kHz for non-axial electric fields respectively). Before proceeding into the detailed description of the Stark effect in the ground state, we first analysed the spin Hamiltonian H_{gs} of the ground triplet state in the presence of magnetic, strain and electric fields

$$H_{\text{gs}} = (hD_{\text{gs}} + d_{\text{gs}}^{\parallel} \Pi_z) \left[S_z^2 - \frac{1}{3} S(S+1) \right] + \mu_B g_e \mathbf{S} \cdot \mathbf{B} - d_{\text{gs}}^{\perp} [\Pi_x (S_x S_y + S_y S_x) + \Pi_y (S_x^2 - S_y^2)] \quad (1)$$

Here $d_{\text{gs}}^{\parallel}/h = 0.35 \pm 0.02 \text{ Hz cm V}^{-1}$ and $d_{\text{gs}}^{\perp}/h = 17 \pm 3 \text{ Hz cm V}^{-1}$ (ref. 28) are the measured axial and non-axial components of the ground triplet state permanent electric dipole moment \mathbf{d}_{gs} , h is the Planck constant, μ_B is the Bohr magneton, g_e is the electron g -factor, \mathbf{B} is the applied magnetic field, and \mathbf{S} is the electron spin operator. Note that the coordinate system is defined as depicted in

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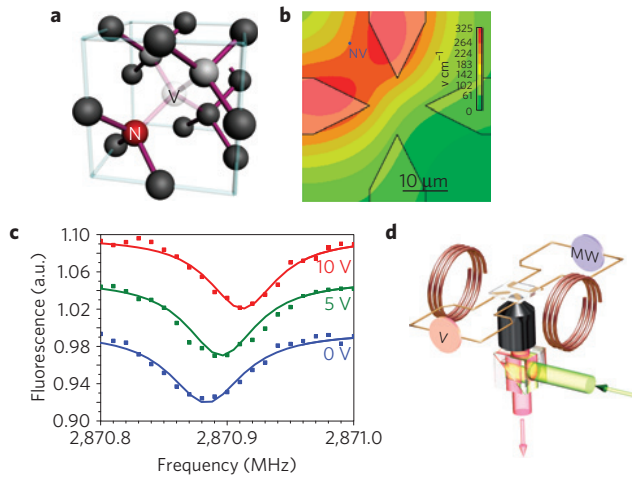


Figure 1 | Schematic of the NV and the measurement scheme.

a, Schematic drawing of the NV centre with one nitrogen at a carbon lattice site and an adjacent vacancy. **b**, Simulated absolute electric field $6 \mu\text{m}$ below the microstructure (depth of the NV) for an applied voltage difference of 1 V. **c**, Observed shift of the ODMR resonance lines for different voltages applied to the electrodes, clearly showing the effect of a Stark shift. **d**, Schematic of the confocal set-up used with Helmholtz coils for magnetic field alignment and a microstructure on the diamond sample to create the electric field and couple in the microwaves

Fig. 2a (that is, the z axis is parallel to the axial symmetry axis of the NV centre which connects the nitrogen and vacancy sites).

It is worth mentioning that \mathbf{d}_{gs} is much smaller than the excited state \mathbf{d}_{es} because of the antisymmetric combination of molecular e_x , e_y type orbitals in the ground state. Consequently, \mathbf{d}_{gs} is non-zero only because of spin orbit coupling between the ground and excited spin triplet states, such that $\mathbf{d}_{\text{gs}} \propto \lambda_{\perp}^2 / E_{\text{es}}^2 \mathbf{d}_{\text{es}}$, where λ_{\perp} is the centre's non-axial spin orbit parameter and E_{es} is the optical energy difference between the triplet states (see Supplementary Information). Given that crystal strain can be treated effectively as a local static electric field $\boldsymbol{\sigma}$ (ref. 27), it combines with the applied electric field \mathbf{E} to give the total effective electric field $\boldsymbol{\Pi} = \mathbf{E} + \boldsymbol{\sigma}$ at the NV centre. In the regime where $D_{\text{gs}} \gg \mu_{\text{B}} g_{\text{e}} B$ and $D_{\text{gs}} \gg d_{\text{gs}} \boldsymbol{\Pi}$, second-order perturbation theory can be applied to obtain the approximate energy solutions of H_{gs} . Considering fixed magnetic and strain fields, the change in the magnetic transition frequency $\Delta\omega_{\pm}$ between the $m_s = 0$ and the $m_s = \pm 1$ spin sub-levels caused by the application of an electric field is

$$\hbar\Delta\omega_{\pm} = d_{\text{gs}}^{\parallel} E_z \pm [F(\mathbf{B}, \mathbf{E}, \boldsymbol{\sigma}) - F(\mathbf{B}, \mathbf{0}, \boldsymbol{\sigma})] \quad (2)$$

where

$$F(\mathbf{B}, \mathbf{E}, \boldsymbol{\sigma}) = \left[\mu_{\text{B}}^2 g_{\text{e}}^2 B_z^2 + d_{\text{gs}}^{\perp 2} \boldsymbol{\Pi}_{\perp}^2 - \frac{\mu_{\text{B}}^2 g_{\text{e}}^2}{D_{\text{gs}}} B_{\perp}^2 d_{\text{gs}}^{\perp} \boldsymbol{\Pi}_{\perp} \right. \\ \left. \times \cos(2\phi_{\text{B}} + \phi_{\boldsymbol{\Pi}}) + \frac{\mu_{\text{B}}^4 g_{\text{e}}^4}{4D_{\text{gs}}^2} B_{\perp}^4 \right]^{1/2}$$

and $\boldsymbol{\Pi}_{\perp}^2 = \Pi_x^2 + \Pi_y^2$, $B_{\perp}^2 = B_x^2 + B_y^2$, $\tan\phi_{\boldsymbol{\Pi}} = \Pi_y / \Pi_x$, and $\tan\phi_{\text{B}} = B_y / B_x$. Given that the Zeeman effect is much stronger than the Stark effect in the ground state, the first-order appearance of $\mu_{\text{B}}^2 g_{\text{e}}^2 B_z^2$ in F indicates that for the expected case, $d_{\text{gs}} \boldsymbol{\Pi} / \mu_{\text{B}} g_{\text{e}} B \ll 1$, careful alignment of the magnetic field in the non-axial plane is required, otherwise the detectable change in the transition frequency caused by an electric field reduces to $\hbar\Delta\omega \approx d_{\text{gs}}^{\parallel} E_z$, which, as $d_{\text{gs}}^{\parallel}$ is small, severely reduces the detectable electric field strength. This argument also indicates that the presence of non-axial strain reduces the

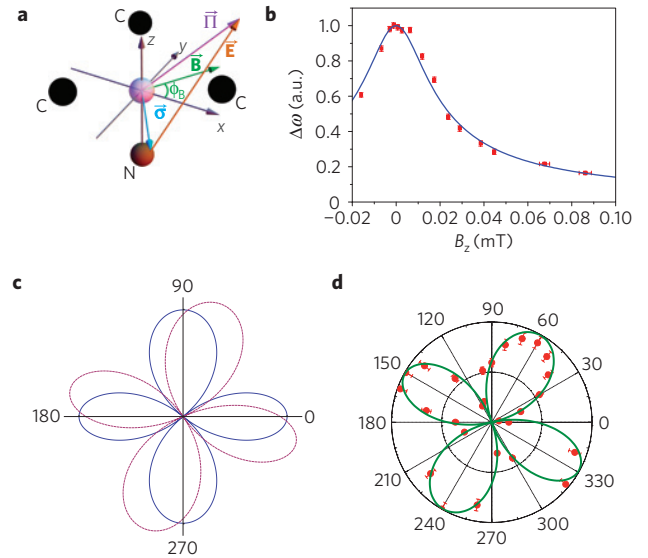


Figure 2 | Theory of NV electric-field sensing and measured results.

a, Schematic of the NV centre, coordinate axes and the magnetic, electric and strain fields defined in the text. The solid spheres represent the nuclei of the respective atoms neighbouring the vacancy (transparent). The coordinate axes are defined such that the z axis coincides with the axis of symmetry connecting the nitrogen and vacancy sites. **b**, The measured normalized magnetic transition frequency change $\Delta\omega$ due to an applied a.c. electric field as a function of the axial magnetic field strength (a.c. voltage of 0–5 V was applied at the electrodes, $\tau = 80 \mu\text{s}$, the maximal interaction was normalized to 1). The blue solid line is the theoretical fit using equation (2). The horizontal error bars are due to the uncertainty in the fit of the ODMR spectra used to calculate B_z , the vertical error bars are the error of the fit of the measured data. **c**, Theoretical change in the magnetic transition frequency $\Delta\omega$ due to an applied electric field as a polar function of the magnetic field orientation ϕ_{B} in the non-axial plane. The blue line corresponds to the case where the applied electric field and the effective strain field are parallel, and the purple dashed line corresponds to a 10° rotation of the external electric field with respect to the strain field. The extremities of the parallel case are defined by $\Delta\omega_{\pm} = \hbar(d_{\text{gs}}^{\parallel} E_z \pm d_{\text{gs}}^{\perp} E_{\perp})$. **d**, Polar plot of the measured detuning $\Delta\omega$ as a function of the magnetic field orientation ϕ_{B} in the non-axial plane. The green solid line is the theoretical fit using equation (2). The error bars in the amplitude are due to magnetic field alignment issues, leading to a non-vanishing B_z and therefore to an error of 7% (see Supplementary Information).

dominating effect of axial magnetic fields on F by increasing the ratio $d_{\text{gs}}^{\perp} \boldsymbol{\Pi}_{\perp} / \mu_{\text{B}} g_{\text{e}} B_z$ (see Supplementary Information). This is important for future sensing applications using nanodiamonds. These typically possess a strain of several tens of MHz, which is larger than the Zeeman shift due to the Earth magnetic field (~ 2 MHz), such that sensing without additional magnetic field alignment seems feasible. Furthermore, a zero magnetic field environment can be reached using a magnetically shielded set-up, which further aids future biological sensing applications.

The dependence of F on the non-axial magnetic field orientation ϕ_{B} indicates that the orientation of the electric field will be determined up to a four-fold symmetry if $\Delta\omega$ is measured for several magnetic field orientations. Figure 2c shows the theoretical polar plot of $\Delta\omega$ as a function of ϕ_{B} for the special case (solid blue line) where the effective strain and applied electric fields are in parallel directions or negligible strain exists. As $\Delta\omega$ depends on both the orientations of the effective strain and applied electric fields, the symmetric 'four-leaf' pattern of the aligned case will distort and rotate if the applied electric field is rotated with respect to the strain field (purple dashed line). If the strain field is characterized for a

given NV centre, the measurement of the $\Delta\omega$ polar pattern and subsequent analysis using equation (2) allows the applied electric field magnitude and orientation to be determined.

Indeed the measured polar plot of $\Delta\omega$ as a function of ϕ_B (Fig. 2d) agrees very well with the theoretical analysis. The small differences between theory and the measurements may be explained by a small axial magnetic field uncertainty of $\pm 5 \mu\text{T}$ that was present. The rotation and distortion of the polar pattern from the symmetric ‘four-leaf’ pattern indicates that the applied electric and effective strain fields are not aligned. A least square fit of the polar pattern yields the field parameters: $B_{\perp} = 23.6 \pm 1.5 \text{ G}$, $d_{\text{gs}}^{\parallel} E_z/h = -4.2 \pm 2.1 \text{ kHz}$, $d_{\text{gs}}^{\perp} E_{\perp}/h = 81.6 \pm 1.7 \text{ kHz}$, $\phi_E = 32^{\circ} \pm 1^{\circ}$, and $\phi_{\sigma} = 22^{\circ} \pm 9^{\circ}$. Note that the non-axial orientations of the electric ϕ_E and strain ϕ_{σ} fields are taken with respect to the laboratory reference frame. The observed strong decay of the electric-field-induced shift $\Delta\omega$ with increasing axial magnetic field strength (depicted in Fig. 2b) also agrees well with the theoretical model and reinforces the requirement for precise alignment of the magnetic field in the non-axial plane. The measurements of Fig. 2b and d and the underpinning theoretical analysis clearly demonstrate how the combination of ODMR techniques and precise magnetic field alignment and manipulation can be used to detect the vector electric field.

As in magnetic-field sensing¹⁸, electric fields are most sensitively detected when a field-induced phase accumulation is used. As an example, Fig. 3c shows the amplitude of a Hahn echo $\propto \cos(\Delta\omega\tau)$ as a function of electric field strength recorded by a two pulse spin echo sequence with a fixed free evolution time τ . The sinusoidal modulation of the measured echo intensity on the increase of the electric field allows a precise determination of the minimally detected electric field, δE_{min} , which can be expressed as the ratio of the standard deviation of a Hahn signal measurement σ_{sn} and the gradient of the oscillation of the Hahn signal $dS = \delta S/\delta E$ (as indicated in Fig. 3c)

$$\delta E_{\text{min}} = \frac{\sigma_{\text{sn}}}{dS}$$

In our measurement, σ_{sn} depends on the photon shot noise, enabling a photon shot-noise limited measurement, as demonstrated in Fig. 3b.

As the amplitude of the Hahn signal decays with τ owing to decoherence, δS likewise decays with τ . τ itself is limited by the dephasing time T_2 . Consequently, an optimal τ exists that maximizes the sensitivity, and this was determined for the Hahn echo (a.c. electric field) and the free induction decay (FID) (d.c. electric field) measurements. The optimal τ for both cases are included with the plot of δE_{min} in Fig. 3b. For a.c. (d.c.) electric-field sensing, a sensitivity of $202 \pm 6 \text{ V cm}^{-1} \text{ Hz}^{-1/2}$ ($891 \pm 21 \text{ V cm}^{-1} \text{ Hz}^{-1/2}$) was achieved, with the smallest detected field being 7.5 V cm^{-1} (173 V cm^{-1}). Here we use the standard definition of the bandwidth as the inverse of twice the measurement time. The intricate combined interaction of strain, electric and magnetic fields that enables this electric-field sensing technique indicates that two different sensing regimes exist, each suited to different sensing applications (see Supplementary Information). One regime is characterized by a non-axial magnetic field that dominates over the strain, that is $g_e \mu_B B_z \ll g_e^2 \mu_B^2 B_{\perp}^2 / D_{\text{gs}}$, $d_{\text{gs}}^{\perp} \Pi_{\perp} \ll g_e^2 \mu_B^2 B_{\perp}^2 / D_{\text{gs}}$ and $d_{\text{gs}}^{\perp} \sigma_{\perp} \ll g_e^2 \mu_B^2 B_{\perp}^2 / D_{\text{gs}}$, and can be engineered by precise magnetic field alignment (as performed in this work) and in which the electric-field sensitivity is independent of the electric, magnetic and strain field strengths. The second regime is characterized by zero magnetic field and a natural strain that is large compared to the electric field shift, such as the strain that occurs in nanodiamonds. In this case, the energy level shift encodes the projection of the electric field onto the major strain direction. Both regimes are suitable for vector electric field measurements. The principal factors that govern the sensitivity of this technique are the

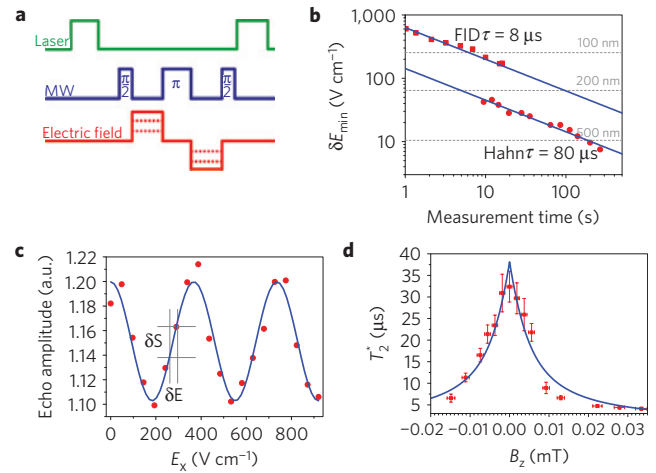


Figure 3 | Sensitivity and coherence time measurements. **a**, Hahn echo pulse scheme with an alternating square electric field for the a.c. measurements (for the d.c. sequence see Supplementary Information). **b**, The measured minimal detectable change in the electric field δE_{min} as a function of the measurement time. The solid blue lines correspond to the fitted shot-noise limit. The grey lines represent the electric field strength of single charges at different distances, taking the dielectric constant of diamond ($\epsilon = 5.7$) into account. **c**, Measured optical Hahn signal as a function of the applied non-axial electric field strength. The solid line is a fit using a cosine function (see Supplementary Information) and a fixed free evolution time ($\tau = 80 \mu\text{s}$). **d**, Measured dependence of the NV centre’s coherence time T_2^* on the axial magnetic field. The solid line shows a fit of the data (see Supplementary Information). The vertical error bars represent the error in the fit of the measured T_2^* data, the horizontal error bars are the uncertainty of the fit of the ODMR transitions used to determine B_z or, for overlapping ODMR transitions, the error in the extrapolation (see Supplementary Information).

T_2^* and T_2 of the NV centre. As the measured T_2 ($304 \pm 36 \mu\text{s}$) of the centre investigated was rather short for an NV centre in bulk diamond, an improvement in the measured sensitivity is expected if an NV centre in a higher purity sample was used. In addition, as T_2 values—similar to the one used here—are now also found for shallow implanted defects²⁹, the method demonstrated here is suitable for charge sensing applications. The sensing scheme presented here exploits the zero axial magnetic field limit of the Hamiltonian where the electrically sensitive transitions are decoupled from magnetic fluctuations (see subsequent paragraph), as is seen most strikingly by the observed narrow line widths in Fig. 1c. Critically, in addition to allowing the nanosensor to be switched from magnetic- to electric-field sensing, it also indicates that decoherence due to impurity spins could be overcome, even in a ‘dirty’ environment, and holds promise for a powerful, yet material-independent route towards quantum metrology under biological conditions.

Figure 3d demonstrates that the observed T_2^* strongly depends on the applied axial magnetic field component and reaches a maximum when the applied axial magnetic field component is zero. This dependence of T_2^* on the magnetic field is best understood by analysing the eigenstates of the spin Hamiltonian (1) in the absence of applied electric and magnetic fields ($B = E = 0$ and $\sigma \neq 0$). In this case, the eigenstates of (1), expressed in terms of the eigenstates of $S_z \{|0\rangle, |+\rangle, |-\rangle\}$, are

$$|S_0\rangle = |0\rangle, |S_{\pm}\rangle = \frac{1}{\sqrt{2}}(e^{-i\phi\sigma/2}|+\rangle \pm e^{i\phi\sigma/2}|-\rangle)$$

and have energies $E_0 = -(2/3)(hD_{\text{gs}} + d_{\text{gs}}^{\parallel}\sigma_z)$ and $E_{\pm} = (1/3)(hD_{\text{gs}} + d_{\text{gs}}^{\parallel}\sigma_z) \pm d_{\text{gs}}^{\perp}\sigma_{\perp}$ respectively. The expectation value

of the spin operator $\langle S \rangle$ is zero for each of these eigenstates, which implies that, as long as $\mu_B g_e B_z \ll d_{gs}^\perp \sigma_\perp$, there will be no first order Zeeman shift of the energies due to a magnetic field. However, the expectation value of the electric dipole operator (d_{gs}) is maximal. Therefore, in this regime, decoherence of the ground state spin will be dominated by electric and strain noise and will be minimally affected by magnetic noise. The opposite is true if $\mu_B g_e B_z \gg d_{gs}^\perp \sigma_\perp$, in which case the eigenstates and energies become approximately $\{|0\rangle, | +1\rangle, | -1\rangle\}$ and $E_0 = -(2/3)D_{gs}$ and $E_\pm = (1/3)D_{gs} \pm \mu_B g_e B_z$ respectively. The application of an axial magnetic field thereby switches the decoherence of the ground state spin from being dominated by electric and strain noise to being dominated by magnetic noise. For the intermediate case, $\mu_B g_e B_z \sim d_{gs}^\perp \sigma_\perp$, it is expected that the decoherence will be influenced by all sources of noise.

In summary, harnessing the interplay between strain, electric and magnetic fields, the ground state spin of single NV centres has been used for vector electric-field sensing on the nanoscale. A photon shot-noise limited a.c. electric-field sensitivity of $202 \pm 6 \text{ V cm}^{-1} \text{ Hz}^{-1/2}$ was achieved, allowing the detection of the electrostatic field produced by a single elementary charge located at a distance of 150 nm from the sensing NV spin within one second of averaging. An electric field strength as small as 14 V cm^{-1} was measured on averaging for about 100 s. This is roughly equivalent to sensing a single electron charge from a distance of 35 nm with a signal to noise ratio of more than 1,000. NVs as close as 40 nm to the surface show coherence times of the order of 100 μs (ref. 29), therefore single external charge detection with the NV centre is within reach (the sensitivity is expected to be $\sqrt{3}$ lower for $T_2 \sim 100 \mu\text{s}$). Tailoring the material aspects of diamond^{12,29}, efficient photon collection³⁰ and multipulse control schemes^{20,21,31} are options available for further improvement.

Benchmarking the achieved sensitivity against other precision charge measuring techniques, such as SET, SCM, EFM and Kelvin probe microscopy, shows that the sensitivity of the method presented here is approximately two orders of magnitude less than the most sensitive electric-field detection technique, this being the SET at a standoff distance of 100 nm. However, the key advantage of the NV centre is the fact that it is an atomic scale sensor and therefore can potentially perform precision sensing at distances as close as a few nanometres under ambient conditions. The first steps towards NV sensing on the nanometre scale under ambient conditions have already been reported³². This regime of applicability is in contrast to all of the above mentioned techniques, in terms of both spatial resolution and operating conditions, and opens up the possibility to image individual charges with nanometre spatial resolution under ambient conditions. In addition, the NV sensor has the unique ability to switch between electric- or magnetic-field detection modes, making it a universal detector system with unprecedented versatility.

Methods

Magnetic field control was realized using two Helmholtz coil pairs for the x and y axes and a single coil for the z axis. The resonant microwave field was generated by a set of waveguides fabricated as part of the gold microstructure. The diamond sample used was a CVD grown diamond with a low nitrogen content and natural abundance of ^{13}C impurity spins (electronic grade Element 6).

To accurately align the magnetic field in the non-axial plane ($B_z = 0$), the orientation-dependent Zeeman splittings of the NV centre's ground state hyperfine structure were observed using CW ODMR techniques. The hyperfine interaction of the NV centre's electronic spin with the ^{14}N nuclear spin results in three observable magnetic transition frequencies separated by 2.2 MHz. Each magnetic transition corresponds to a change in the electronic spin projection $m_s = 0 \leftrightarrow m_s = \pm 1$, but conserves nuclear spin projection, such that the low and high frequency transitions are between hyperfine states with $m_1 = \pm 1$ and the central frequency transition is between hyperfine states with $m_1 = 0$. For magnetic fields applied to NV centres with a crystal strain that satisfies $d_{gs}^\perp / \mu_B g_e B \ll 1$, the hyperfine states with $m_1 = \pm 1$

are not split by the presence of strain and/or a non-axial magnetic field, but are split by the axial component of the magnetic field. Consequently, the magnetic field can be aligned in the non-axial plane by manipulating the field and observing the pulsed CW ODMR spectra such that there is no splitting in either the low or high frequency hyperfine magnetic resonance lines. This alignment technique is limited by the linewidth of these hyperfine lines, but the axial magnetic field component can be determined to a particular uncertainty by interpolating the observed magnetic fields in relation to the coil currents. Once aligned, the magnitude of the non-axial strain σ_\perp can be inferred from the splitting of the central line as long as the non-axial magnetic field strength is known, and for the NV centre studied it was found to be $d_{gs}^\perp \sigma_\perp / h = 0.189 \text{ MHz}$. Given that only the central hyperfine transition, which involves states with $m_1 = 0$, is susceptible to splitting by strain and electric fields, it was this transition that was used in the electric field measurements, reducing the observable ODMR contrast to a third.

Given that the ground triplet state is an orbital singlet and the Stark effect is purely an orbital interaction, the presence of the effect in the ground triplet state is forbidden without some prior mixing of the orbital and spin components of the centre's electronic states. However, the effect is allowed without such mixing in the excited triplet state, as it is an orbital doublet. Indeed, the strong linear splitting of the orbitally degenerate $m_s = 0$ spin sub-levels of the excited triplet has been well documented and attributed to the presence of a permanent electric dipole moment \mathbf{d}_{es} (ref. 27). The application of the well-established molecular model yields $\mathbf{d}_{es} = \langle e_x | x | e_x \rangle + \langle e_x | y | e_y \rangle + (a_1 | z | a_1) + 3 \langle e_x | z | e_x \rangle$, where a_1 , e_x and e_y are molecular orbitals that are constructed from the dangling sp^3 atomic orbitals of the neighbouring carbon atoms. Note that the NV defect has C_{3v} symmetry and the orbitals are of symmetry type A_1 and E , respectively. The charge distributions e_x, e_x and e_x, e_y , responsible for the dominant non-axial components of \mathbf{d}_{es} , are shown in Supplementary Fig. S1. The previous observation of the weak linear splitting of the degenerate $m_s = \pm 1$ spin sub-levels of the ground triplet state indicates that the Stark effect in the ground triplet state is indeed a consequence of a higher-order interaction. Spin-orbit interaction is the immediately obvious higher-order interaction capable of the required mixing, and the application of the molecular model indicates that the $m_s = \pm 1$ spin sub-levels of the ground triplet state are mixed with the degenerate $m_s = 0$ spin sub-levels of the excited triplet state by the non-axial components of spin-orbit interaction. This mixing between the ground and excited triplet states explains the existence of the weaker linear Stark effect in the ground triplet state, as the permanent electric dipole moment of the ground triplet state, \mathbf{d}_{gs} , is related to the dipole moment of the excited triplet state by the square of the non-axial spin-orbit interaction strength λ_\perp , such that $\mathbf{d}_{gs} \propto (\lambda_\perp^2 / E_{es}^2) \mathbf{d}_{es}$, where E_{es} is the energy of the excited triplet state.

Received 14 September 2010; accepted 8 March 2011;
published online 17 April 2011

References

1. Yoo, M. J. *et al.* Scanning single-electron transistor microscopy: Imaging individual charges. *Science* **276**, 579–582 (1997).
2. Martin, J. *et al.* Observation of electron-hole puddles in graphene using a scanning single-electron transistor. *Nature Phys.* **4**, 144–148 (2008).
3. Schonenberger, C. & Alvarado, S. F. Observation of single charge-carriers by force microscopy. *Phys. Rev. Lett.* **65**, 3162–3164 (1990).
4. Schonenberger, C. Charge flow during metal-insulator contact. *Phys. Rev. B* **45**, 3861–3864 (1992).
5. Devoret, M. H. & Schoelkopf, R. J. Amplifying quantum signals with the single-electron transistor. *Nature* **406**, 1039–1046 (2000).
6. Elzerman, J. M. *et al.* Single-shot read-out of an individual electron spin in a quantum dot. *Nature* **430**, 431–435 (2004).
7. Williams, C. C., Slinkman, J., Hough, W. P. & Wickramasinghe, H. K. Lateral dopant profiling with 200 nm resolution by scanning capacitance microscopy. *Appl. Phys. Lett.* **55**, 1662–1664 (1989).
8. Henning, A. K. *et al.* 2-dimensional surface dopant profiling in silicon using scanning Kelvin probe microscopy. *J. Appl. Phys.* **77**, 1888–1896 (1995).
9. Martin, Y., Abraham, D. W. & Wickramasinghe, H. K. High-resolution capacitance measurement and potentiometry by force microscopy. *Appl. Phys. Lett.* **52**, 1103–1105 (1988).
10. Jelezko, F. & Wrachtrup, J. Single defect centres in diamond: A review. *Phys. Status Solidi A* **203**, 3207–3225 (2006).
11. Gruber, A. *et al.* Scanning confocal optical microscopy and magnetic resonance on single defect centres. *Science* **276**, 2012–2014 (1997).
12. Balasubramanian, G. *et al.* Ultralong spin coherence time in isotopically engineered diamond. *Nature Mater.* **8**, 383–387 (2009).
13. Meijer, J. *et al.* Generation of single colour centres by focused nitrogen implantation. *Appl. Phys. Lett.* **87**, 261909 (2005).
14. Toyli, D. M., Weis, C. D., Fuchs, G. D., Schenkel, T. & Awschalom, D. D. Chip-scale nanofabrication of single spins and spin arrays in diamond. *Nano Lett.* **10**, 3168–3172 (2010).
15. Ladd, T. D. *et al.* Quantum computers. *Nature* **464**, 45–53 (2010).
16. Balasubramanian, G. *et al.* Nanoscale imaging magnetometry with diamond spins under ambient conditions. *Nature* **455**, 648–651 (2008).

17. Maze, J. R. *et al.* Nanoscale magnetic sensing with an individual electronic spin in diamond. *Nature* **455**, 644–647 (2008).
18. Taylor, J. M. *et al.* High-sensitivity diamond magnetometer with nanoscale resolution. *Nature Phys.* **4**, 810–816 (2008).
19. Steinert, S. *et al.* High sensitivity magnetic imaging using an array of spins in diamond. *Rev. Sci. Instrum.* **81**, 043705 (2010).
20. Hall, L. T., Hill, C. D., Cole, J. H. & Hollenberg, L. C. L. Ultrasensitive diamond magnetometry using optimal dynamic decoupling. *Phys. Rev. B* **82**, 045208 (2010).
21. Naydenov, B. *et al.* Dynamical decoupling of a single-electron spin at room temperature. *Phys. Rev. B* **83**, 081201 (2011).
22. Cole, J. H. & Hollenberg, L. C. L. Scanning quantum decoherence microscopy. *Nanotechnology* **20**, 495401 (2009).
23. Hall, L. T., Cole, J. H., Hill, C. D. & Hollenberg, L. C. L. Sensing of fluctuating nanoscale magnetic fields using nitrogen-vacancy centers in diamond. *Phys. Rev. Lett.* **103**, 220802 (2009).
24. Hall, L. T. *et al.* Monitoring ion-channel function in real time through quantum decoherence. *Proc. Natl Acad. Sci. USA* **107**, 18777–19782 (2010).
25. Fu, C. C. *et al.* Characterization and application of single fluorescent nanodiamonds as cellular biomarkers. *Proc. Natl Acad. Sci. USA* **104**, 727–732 (2007).
26. Chang, Y. R. *et al.* Mass production and dynamic imaging of fluorescent nanodiamonds. *Nature Nanotech.* **3**, 284–288 (2008).
27. Tamarat, P. *et al.* Stark shift control of single optical centres in diamond. *Phys. Rev. Lett.* **97**, 083002 (2006).
28. Vanoort, E. & Glasbeek, M. Electric-field-induced modulation of spin echoes of N–V centers in diamond. *Chem. Phys. Lett.* **168**, 529–532 (1990).
29. Naydenov, B. *et al.* Increasing the coherence time of single electron spins in diamond by high temperature annealing. *Appl. Phys. Lett.* **97**, 242511 (2010).
30. Babinec, T. M. *et al.* A diamond nanowire single-photon source. *Nature Nanotech.* **5**, 195–199 (2010).
31. de Lange, G., Wang, Z. H., Riste, D., Dobrovitski, V. V. & Hanson, R. Universal dynamical decoupling of a single solid-state spin from a spin bath. *Science* **330**, 60–63 (2010).
32. Hauf, M. V. *et al.* Chemical control of the charge state of nitrogen-vacancy centres in diamond. *Phys. Rev. B* **83**, 081304 (2011).

Acknowledgements

The authors would like to thank P. Neumann, B. Naydenov, R. Kolesov, C. Kim, P. Hemmer and S. Steinert for fruitful discussions and their advice. This work was supported by the EU (QAP, EQUIND, NEDQIT, SOLID), DFG(SFB/TR21, FOR730 and FOR1482), NIH, Baden-Württemberg Stiftung, BMBF (EPHQUAM, KEPHOSI), VolkswagenStiftung, and the Australian Research Council Centre of Excellence Scheme (project ID CE110001027). T.N. wishes to thank Vienna doctoral program CoQuS(Austrian Science Fund (FWF) project W1210).

Author contributions

F.D, H.F., T.N., G.B., T.W. and F.J. carried out the experiments; M.W.D., F. Rempp, F. Reinhard and L.C.L.H developed the theory. All authors discussed the results, analysed the data and commented on the manuscript. J.W. wrote the paper and supervised the project.

Additional information

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