LISA Pathfinder: Understanding DWS noise performance for the LISA mission

Lennart Wissel on behalf of the LPF collaboration
Max Planck Institute for Gravitational Physics (Albert Einstein Institute), Callinstraße 38, 30167 Hannover, Germany
E-mail: lennart.wissel@aei.mpg.de

Abstract. ESA’s L3 Laser Interferometer Space Antenna (LISA) mission contains a mechanism to compensate for out-of-plane angles between the received and emitted beams of the three satellites. Depending on the configuration of this Point-Ahead Angle Mechanism (PAAM) it is expected to contribute readout noise through Differential Wavefront Sensing (DWS). This was investigated with LISA Pathfinder (LPF) through a dedicated investigation. One of the two free-falling test masses was rotated via the on-board electrostatic actuators while the resulting angular noise in the differential interferometer between the two test masses was measured. For angles between $250 \mu$rad to $250 \mu$rad and corresponding contrast in the range of $59.4\%$ to $97.9\%$ an increased spectral density was found. The differential displacement noise remains almost unchanged for these misalignments.

1. Introduction
The performance of LPF’s Optical Metrology System is about two orders of magnitude better than the requirement and is subject to ongoing investigations throughout the mission [1]. Differential Wavefront Sensing (see [2]) as a part of this subsystem is used to control four out of six angular degrees-of-freedom of the two test masses. Conceptually, the segments of Quadrant-Photodiodes (QPD) are demodulated to compare the relative phase difference between the wavefronts of the interfering measurement and reference beams for a group of two complementary quadrants. After processing all four channels using a Single-Bin Discrete Fourier Transformation (SBDFT) the resulting complex values, $F$, contain the encoded phase information which can be retrieved by subtracting left, right and up, down quadrants according to

\[
\begin{align*}
\text{DWS}_\phi &= \arg(F_{\text{left}}) - \arg(F_{\text{right}}), \\
\text{DWS}_\theta &= \arg(F_{\text{up}}) - \arg(F_{\text{down}}),
\end{align*}
\]

(1)
during which the equally distributed longitudinal phase is cancelling and the angular phase difference remains. These raw phase measurements can be expressed as equivalent test mass angles $\phi_i, \eta_i; i \in \{1, 2\}$ over a linear range of at least $-100 \mu$rad to $100 \mu$rad. To calibrate from phase differences to test mass angles, on-ground measurements were performed to determine the coupling coefficients and they are applied as calibration factors in the Data Management Unit (DMU) aboard LPF.
While the digitisation process has a sampling frequency of 50 kHz, further downsampling (to 10 Hz) is applied before transmitting the data to ground. This 10 Hz data is also used to drive the Drag-Free and Attitude Control System (DFACS), keeping the three body system as free from spurious forces as possible.

In the high frequency regime of the DWS data, a quasi-flat noise floor can be observed, as shown in figure 1, allowing a specific noise estimation. In LISA, non-vanishing DWS signals (depending on the point ahead configuration) will originate from motion between the three spacecrafts in combination with their long arm lengths. Beam tilts are magnified by the telescope, causing relatively large DWS phase differences on the quadrants. This distorts the phase readout in a certain way that is investigated here.

2. The DWS step experiment

The DWS step experiment has been designed to measure the DWS noise behaviour and its positional dependence. For this, the electrostatic controllers are used to rotate test mass two around its y and z axes. Motivation for this investigation arises from the following observations: The test mass alignment along $\phi_1$, $\eta_1$, $\phi_2$ and $\eta_2$ does not only couple into the differential length measurement given by the x12 interferometer, it has also shown a different DWS noise floor for each of the angular set points that were commanded during the mission. The experiment is designed to quantify different noise levels and investigate their coupling. It assesses the phase noise in the DWS readout regarding its amplitude and phase (or positional) dependence, estimates possible noise sources and coupling mechanisms, allows to fit contrast models related to test mass slews and helps to draw conclusions for requirements on the LISA point-ahead setup.

Figure 1. DWS spectral density for a specific offset, showing the high frequency flat noise floor. Below 300 mHz real test mass motion is dominating the spectrum.
2.1. Conception
The basic idea consists of commanding a set of angular test mass offsets via the electrostatic controller and calculating the resulting amplitude spectral noise density for each of the steps. LISA Pathfinder has proven to be quiet enough to reach a quasi-flat noise floor within the high frequency regime in the angular test mass readout, where no test mass motion is believed to be happening. For the slews test mass two was chosen because of its closer position to the photodiodes, thus minimizing any induced beam spot offset on the surface of the quadrants. Another benefit is that the differential interferometer is less susceptible to environmental disturbances. The somewhat randomly chosen test mass tilts are shown in figure 2. Larger tilts are not easily possible due to spacecraft safety regulations.

2.2. In-orbit behaviour
The experiment was run on DOY 154 (day-of-year) during the mission. In figure 3 the resulting time series can be found. Shown is the angular readout (DWS) and the differential interferometer readout. Every step with a total duration of 45 min is reached in less than 30 min until the rotational degree of freedom stabilizes. In comparison tilt-to-length coupling in x12 motion, introduced by the commanded torques, experiences a slower impulse response of the suspension.

Figure 2. The commanded test mass two tilts are shown in the $\phi_2, \eta_2$ parameter space. All points are randomly placed such that the maximum radial distance is smaller than $260 \mu\text{rad}$. The middle plot shows the shortest connecting path of all points, calculated by a travelling salesman algorithm (courtesy of G. Heinzel). It reduces test mass trajectories between set points and the risk of larger overshoots.

Figure 3. Time series of the measured slews in the DWS step experiment.
controller. Every set point shows an overshoot of various length, when the test mass rotates further than it should, due to the relatively high slew velocities that the controller can not quickly reduce. The maximal overshoot is just below 30 μrad in η₂. The analysis shows a different amplitude spectral density for every set-point. It increases for larger misalignments, i.e. larger phase differences on the measurement diodes.

3. Outlook
Models are used in the ongoing analysis to find the coupling parameters, which are believed to introduce Relative Intensity Noise (RIN) from the laser. A subsequent investigation was run during the mission extension, incorporating much larger slews while also compensating beamwalk effects with parallel commanded test mass one tilts. A publication with the results is in preparation.

4. Acknowledgments
The Albert-Einstein-Institut acknowledges the support of the German Space Agency, DLR. The work is supported by the Federal Ministry for Economic Affairs and Energy based on a resolution of the German Bundestag (FKZ 50OQ0501 and FKZ 50OQ1601).

References