Chiroptical response of a single plasmonic nanohelix

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Abstract: We investigate the chiroptical response of a single plasmonic nanohelix interacting with a weakly focused circularly polarized Gaussian beam. The optical scattering at the fundamental resonance is characterized experimentally and numerically. The angularly resolved scattering of the excited nanohelix is verified experimentally and it validates the numerical results. We employ a multipole decomposition analysis to study the fundamental and first higher-order resonance of the nanohelix, explaining their chiral properties in terms of the formation of chiral dipoles.

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References and links
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1. Introduction

Chirality in nature is a property of certain molecules which allows them to interact differently with right- and left-handed circularly polarized light. Chiral molecules lack a plane of mirror symmetry in their molecular structure. They may exist in two different forms (enantiomers), which are mirror images of each other. Intuitive examples of chiral molecules are those exhibiting a helical shape in which the sense of twist defines their handedness. Interaction of light with chiral molecules leads to interesting optical phenomena such as optical rotation and circular dichroism [1], and have importance in, e.g., the life sciences and chemical analysis [2–6]. Chiroptical effects of natural compounds are rather weak and typically occur in the ultraviolet which limits their applications.

However, the advances in nanofabrication enabled the manufacture of artificial media of enhanced chiral response over the optical spectral range [7–10]. Such media, typically called chiral metamaterials, consist of chiral metamolecules, which take the form of sub-wavelength chiral particles or particle-clusters. They are engineered to exhibit a strong chiral response by controlling the geometry of the particles [11–13] or clusters [14–18], their spatial arrangement [19–21] or their material composition [22]. Chiral optical phenomena can also occur in anisotropic achiral particles under oblique illumination such that the particle and the wave vector of light form a chiral triad, a phenomenon known as pseudochirality or extrinsic chirality [23–27]. A variety of chiral metamaterials have been proposed and demonstrated to enable strong chiroptical effects [11–13,21,28–30] and unusual optical phenomena such as negative refraction [31–34] and superchiral light [35,36]. Tunable and strongly chiral metamolecules are also desired for the realization of high-efficiency circular-polarization optical elements [13,21] and nanodevices for dynamic light manipulation [27,30,37,38].

As it relates to the lack of mirror symmetry of molecules (or metamolecules), chirality is usually associated with a three-dimensional geometry [1]. Among the various three-dimensional chiral structures which have been investigated, helix-shaped scatterers have received significant attention due to their strong, broadband and tunable chiroptical properties [39–44]. In particular, metallic nanohelices supporting localized surface plasmons at optical frequencies have been used to create metamaterials [39,40,42,43] and metafluids [17,45,46] with enhanced chirality. Despite the intense research on these structures, only few reports have investigated numerically the fundamental chiroptical properties of plasmonic helices [47–49]. To the best of our knowledge, a single plasmonic nanohelix has never been examined experimentally up to now.

In this paper, we study experimentally and numerically the chiroptical response of a right-handed single-loop plasmonic nanohelix excited with circularly polarized light. The investigated structure is much smaller than the wavelength, both in the transverse and longitudinal directions. To this end, the nanohelix is characterized in terms of its optical scattering and its chiral signature is explained based on a multipole decomposition. The extracted spectra of the electric and magnetic dipole moments allow further to determine their contributions to the far-field scattering. Our results show that the optical response of the fundamental resonance has contributions from dipole and quadrupole moments, but it is dominated by the dipolar response.

2. Chiroptical response of a single-loop nanohelix

We investigate a right-handed nanohelix fabricated on a glass substrate using electron-beam-induced deposition and coated with gold (see Appendix I). The nanohelix is depicted schematically in Fig. 1(a). The structure exhibits nanoscopic dimensions with the radius of 60 nm, the pitch of 230 nm and the wire diameter of 70 nm. We characterize the chiroptical response of the nanohelix by measuring its reflectance and transmittance spectra, as well as its far-field forward-scattering using a custom-built confocal-microscope setup (see simplified sketch Fig. 1(b)). The helix is excited with a weakly focused circularly polarized Gaussian beam (effective focusing numerical aperture $NA_{eff} = 0.5$). For that purpose, the incoming beam partially fills the back focal plane of
Fig. 1. Investigated nanostructure and experimental set-up. (a) Schematic illustration and 
scanning-electron micrograph (inset) of the investigated gold-coated nanohelix on a glass 
substrate. (b) Simplified sketch of the experimental set-up utilized for the measurement 
of the nanohelix. A circularly polarized Gaussian beam is focused onto the nanohelix by 
a microscope objective with NA of 0.9. The incoming beam only partially fills the back 
focal plane of the focusing lens and decreases the effective focusing 
NA\text{eff} down to 0.5. 
The same objective collects the reflected and the back-scattered light within a large solid 
angle equivalent to the NA of 0.9. Implementation of a 3D-piezo-stage allows for precise 
positioning of the structure on the optical axis in the focal plane. The transmitted and 
forward-scattered light is collected by a second immersion-type microscope objective with 
an NA of 1.3 which is located below the sample. In both directions, the total power is 
measured with photo-diodes.

Throughout this study we define right-handed circularly polarized light (RCP) as 
\( E^- = E_0(\hat{x}, -i\hat{y})/\sqrt{2} \) and left-handed circularly polarized light (LCP) as 
\( E^+ = E_0(\hat{x}, i\hat{y})/\sqrt{2} \), where \( E_0 \) is the magnitude of the electric field, and \( \hat{x} \) and \( \hat{y} \) are the unit vectors in the directions 
of the \( x \) and \( y \) coordinates, respectively. The reflectance \( R \) and transmittance \( T \) spectra for 
RCP and LCP Gaussian excitation are measured wavelength-by-wavelength in the spectral range 
from 1300 nm to 1650 nm around the fundamental resonance of the investigated nanohelix. From 
this data, the absorbance \( A \) can be calculated as \( A = 1 - R - T \). Subsequently, the differential 
absorption, or equivalently, the circular dichroism \( CD \) can be estimated as:

\[
CD = A_{\text{RCP}} - A_{\text{LCP}}.
\]

The corresponding datasets for \( R, T, A \) and \( CD \) are shown in Fig. 2. Both the experimental and 
numerical data show a resonance around 1450 nm for excitation with RCP light, matching the 
handedness of the nanohelix (relating to the Born-Kuhn model of a helical geometry \[47,52,53\]). 
The simulations were based on the finite-difference time-domain (FDTD) method. They were 
designed carefully to resemble the experimental illumination and measurement schemes, and the 
values of \( A \) and \( CD \) were determined from the retrieved values of \( R \) and \( T \) (see Appendix I). For 
the incoming light of opposite handedness, however, there is no obvious fingerprint of resonant 
excitation. Likewise, the intensity of scattered light in the forward direction is higher for RCP 
than LCP, leading to a non-zero differential scattering (see Appendix II). Thus, the resulting \( CD \) 
spectrum presented in Fig. 2 (bottom) exhibits a broad peak centered at the wavelength of 1450 
mm which is a clear sign of the optical activity of the nanohelix. The experimental and numerical 
spectra are in a good agreement with each other. Moreover, the FDTD simulations over a broader
Fig. 2. Measurements and numerical simulations of the chiroptical response of a single plasmonic nanohelix. Reflectance and transmittance spectra are shown at the top. The corresponding absorbance spectra for both polarization states of the incoming light are shown at the bottom. The resulting differential absorption \((CD)\) is presented in the same graph.

Spectral range confirm that the observed \(CD\) peak corresponds to the fundamental resonance of the structure (see Fig. 7). Hence, at \(\lambda = 1450\) nm the helix pitch (the largest dimension of the structure) is over six times smaller than the wavelength. The experimentally retrieved \(CD\) reaches a maximum value of approximately 2.5 %. It should be emphasized that this value is recorded for a single nanohelix, in contrast to most of the studies reporting on \(CD\) values for large arrays of chiral nanostructures \([13, 41, 44, 47–49, 54]\). In the case discussed here, a single nanohelix with an approximate diameter of only 120 nm is excited by a Gaussian beam focused weakly down to a spot with diameter of around 1.2 \(\mu\)m (full width at half maximum at \(\lambda = 1450\) nm).

3. Multipolar decomposition of the fundamental resonance

To better understand the chiroptical response of the nanohelix, we extract the polarization density provided by the FDTD simulations and expand it into multipoles up to order 3 (dipoles, quadrupoles, and octupoles; see Appendix I). Because the nanohelix interacts effectively only with RCP, only this interaction is further investigated. Figure 3 presents the spectra of the electric \((\mathbf{p})\) and magnetic \((\mathbf{m})\) complex dipole moments obtained with RCP excitation. The FDTD calculations were extended over the wavelengths between 450 nm and 1900 nm and show that, in the entire simulated spectral range, the optical response of the nanohelix is dominated by the two dipoles. Our multipolar analysis indicates also the presence of electric and magnetic...
Fig. 3. FDTD-retrieved dipolar response of the nanohelix. Magnitudes and phases of the components of the electric $\mathbf{p}$ and magnetic $\mathbf{m}$ dipole moments for the right-handed helix under RCP illumination. The blue-shaded range spans over the spectral range of the experiment.

quadrupoles (see Appendix II). However, their contribution and the contribution of other higher order multipoles can be neglected because their strength is several orders of magnitude smaller than the dipoles. A similar dipole-dominated chiroptical response of a two-loop helix was recently reported by Fruhnert et al. in [55].

For a more intuitive understanding of the dipolar composition, it is instructive to analyze the resonant charge and current distributions (see Fig. 4(b)). At a certain point in time, the charges are well separated and accumulated at both ends of the helix. Such a dipolar distribution can be described as an electric dipole $\mathbf{p}$, pointing from the center of the charge accumulation at one end of the helix to the other one. Hence, $\mathbf{p}$ is aligned predominantly along the helix axis having a small tilt from the $z$-axis which results from the finite length of the structure. The time-harmonic excitation, however, requires that after a certain time the charges migrate to the other side, giving rise to a current. Since the resonantly excited charges flow along a curved path, they induce a resonant magnetic field perpendicular to the current, resulting in a magnetic dipole moment $\mathbf{m}$.

It can be further assumed that the charges move in a plane with its normal vector tilted by an angle (defined by the helix radius and the pitch) with respect to the $z$-axis. Therefore, the induced magnetic dipole moment must be tilted respectively. Furthermore, we note that the electric dipole is elliptically polarized (see amplitude and phase spectra in Fig. 3). When the electric current is largest at $\omega t = \pi/2$, the electric charge is separated predominantly along the $x$-direction. Yet, the charges oscillate not along a straight path, but along the curved path defined by the helix wire. As a result, the electric and magnetic dipole moments are not linear but show a non-zero ellipticity. Accordingly, at the resonance wavelength of 1450 nm, the two dipoles are elliptically polarized and oscillate predominantly along the helix axis ($z$-axis, see Fig. 4(a)). The ellipticity $\epsilon$ was estimated to be 0.9965 and 0.9995 for the electric and magnetic dipoles, respectively.

It is clear now that both electric and magnetic dipoles have components in all directions. In
Fig. 4. Optical response of a single nanohelix at the fundamental resonance, excited with right-handed circularly polarized light. (a) The helix can be described as a system of coupled electric and magnetic dipoles of ellipticities $\epsilon$ and oscillating with a phase delay of $\pi/2$. Both dipoles have a strong component along the z-axis (the inset shows the projections of the retrieved dipoles on the xy-, xz- and yz-planes). (b) Distributions of the charge and current densities on the helix surface for two different snapshots in time. Effectively, the structure acts as a nanoLC-circuit accessible for only one handedness of the incoming light (here RCP) depending on its own geometrical twist.

In particular, we note here that transverse components are necessary to excite the fundamental resonance with the incoming plane-wave-like (transverse) RCP field at normal incidence. For a fixed orientation of the nanohelix in space, the two dipoles do not change. As an intrinsically chiral three-dimensional structure, the nanohelix has to exhibit the same handedness even for the reversed propagation direction of the light and, hence, it should be time-invariant (see Appendix II and [1,56]). Thus, the resonance can be excited regardless of the propagation direction of RCP. Importantly, both dipoles are driven by the same source, which is $\pi/2$ delayed for each dipole (see phase spectra in Fig. 3), namely the electric charge harmonically oscillating along a finite helical wire. At the wavelength of the fundamental resonance, the nanohelix can be equivalently described as a point-like scatterer driven by coupled electric and magnetic dipoles $p = -im$. In addition, the structure can also be described as a nanoLC-circuit accessible for only one handedness of the incoming light (here RCP) with regard to its own geometrical twist [57].

Although the geometry does not allow the scatterer to support electric and magnetic dipoles being entirely parallel to each other, the two moments share predominantly a common direction of oscillation (see Figs. 3 and 4(a)). Therefore, the intrinsic cross polarizability $G'' \sim -3 \langle p \cdot m \rangle$ [58] is non-zero. Note that the demanded non-zero projection of the electric and magnetic dipoles onto each other fulfills the condition of a true chiral entity according to Barron’s definition [1]. In our system, the value of $G''$ can be approximated using only the longitudinal components, $p_z$ and $m_z$. Such a system of coupled electric and magnetic dipoles, which we call a chiral dipole, is parity-odd and time-even (see Appendix II). The time delay of $\pi/2$ between the electric and magnetic dipoles ($p_z - im_z$) resembles the relation between the electric and magnetic fields of the eigenwaves of a chiral medium (circularly polarized plane-waves) $H^\pm = \mp i \sqrt{\epsilon/\mu} E^\pm$ [59], with $\epsilon$ and $\mu$ being the permittivity and permeability of the medium, respectively. Further, we note that sets of other dipole components of significant strength which oscillate along perpendicular directions (e.g., $(p_y, m_z)$ or $(p_z, m_y)$) do not contribute to the optical activity as they are parity-invariant. Such a dipolar system can be found in a split-ring resonator under normal illumination for which the structure stays optically inactive [23,26] (see Appendix II and Fig. 11).

To complete the analysis of the chiroptical response of the nanohelix at its fundamental resonance, we investigate the far-field scattered light at $\lambda = 1450$ nm. The emission of a dipole placed near a dielectric interface, regardless of its type and orientation, is predominantly directed into the optically denser medium. In the chosen scheme of an air-glass interface, the scattered light peaks at the angle of $\text{NA} = 1.0$ in the glass substrate [60,61]. Hence, for experimental observation,
we image the back focal plane of the microscope objective in transmission, where the scattered light is angularly separated from the transmitted beam (see Appendix I and Refs. [51, 62] for more details). Figure 5 shows the acquired distribution of the light emitted by the nanohelix excited with RCP light (under LCP excitation the light scattered by the nanohelix is very faint, representing a non-zero differential scattering, see Appendix II). The total intensity exhibits a ring-like distribution. Polarization analysis of the scattered light further reveals that it is predominantly radially polarized and, hence, dominated by the radiation of the electric dipole [51], which is slightly tilted with respect to the z-axis. The emission of the induced magnetic dipole moment, thus, contributes extremely weakly to the intensity of the far-field scattered light. This is caused not only by the lower power radiated by the magnetic dipole but also by its lower transmissivity through the air-glass interface in comparison to the electric dipole [60]. Nonetheless, the magnetic dipole is of utmost importance for the chiral response of the nanohelix as discussed above. The experimental data is in very good agreement with the analytical calculations of the far-field emission of electric and magnetic dipoles above a plane dielectric interface. To this end, the amplitudes and phases of the FDTD-retrieved dipoles at $\lambda = 1450$ nm and RCP light are used. The good overlap confirms again that the contribution of higher-order multipoles can be neglected for the investigated resonance.

4. First higher-order resonance

The dipole decomposition presented in Fig. 3 indicates the first higher-order resonance of the nanohelix at $\lambda = 840$ nm. Similar to the fundamental resonance, the exited mode responds more strongly to RCP illumination (see Appendix II). Figure 6 shows the corresponding distributions of the charge and current densities retrieved from the FDTD simulations at two different points in time delayed by $\pi/2$. Because at a certain point in time the positive or negative charges accumulate at the ends of the nanohelix and the corresponding opposite charge in its middle, the excited electric dipole oscillates predominantly along the $x$-axis. Such charge distribution will produce two curl-like currents flowing from and towards the two ends of the structure. Accordingly, both half-loops will produce two magnetic dipole moments with components along the same
transverse direction but pointing in the opposite \( z \)-direction. While the anti-parallel longitudinal components will cancel each other, the transverse components will interfere constructively. Effectively, the running charges will produce a predominantly \( x \)-polarized magnetic dipole. The dipolar decomposition (see Fig. 3) allows for describing the first higher-order resonance as a point-like system of coupled electric and magnetic dipoles of ellipticities of 0.9998 and 0.9991, respectively. Due to the different charge and current distributions in comparison to the fundamental resonance (see Figs. 4(a) and 6(a)), the cross polarizability of the first higher-order resonance can be estimated using \( p_x \) and \( m_x \) (see amplitude and phase spectra in Fig. 3). The transverse \( x \)-polarized components can be treated, hence, as the chiral dipole of the resonance and have a better coupling overlap with the transverse RCP at normal incidence.

5. Conclusion

In summary, we have studied the optical response of an intrinsically chiral plasmonic nanostructure exhibiting sub-wavelength dimensions. In contrast to the current literature, we study the chiroptical response of an individual single-loop nanohelix to understand its interaction with circularly polarized light on the single-particle level. The discussion focuses on the fundamental and first higher-order resonances of the nanohelix. We investigated the chiroptical response by measuring and numerically calculating its differential absorption of right- and left-handed circularly polarized light. From the numerical data, we retrieve the multipolar response and determined the structure of the dominating electric and magnetic dipole moments. We found that the chiroptical response of the nanohelix is fundamentally different for each of the two resonances, as the charge distributions define chiral dipoles oriented in the \( z \)- and \( x \)-directions for the fundamental and first-higher order resonances, respectively. The non-zero projection of the two dipoles onto each other is parity-odd and time-even and, hence, responsible for the chirality of the structure and determine its strength. The experimentally observed far-field scattering at the fundamental resonance is in a very good agreement with the one found analytically. Our findings contribute to the understanding of chiral light-matter interactions based on the multipolar response of a point-like chiral entity.

Appendix I: Methods

Helix fabrication

A helix of nanometric dimensions was fabricated using electron-beam-induced deposition (EBID) [63]. For that purpose, a 170 \( \mu \)m thick borosilicate glass cover slip with a thin layer (46 nm) of indium tin oxide (ITO) for sufficient surface conductivity was used as a substrate. The EBID process took place in a vacuum chamber of a dual-beam instrument FEI Strata DB 235. The metal-organic precursor dimethyl-gold(III)-acetylacetonate (Me\(_2\)Au(acac)) was heated up to 34°C and introduced to the chamber by a gas-injection system, placing the inlet needle...
approximately 0.5 mm above the sample. Deposition process was carried out under pressure of 0.2 - 0.5 mPa at an acceleration voltage of 15 kV and a current below 100 pA. In the proximity of a focused electron beam, the injected precursor molecules are dissociated and their non-volatile parts formed a deposit while the volatile parts were pumped out. By changing the relative position of the focus with respect to the substrate, a single-loop helix was produced. For the chosen dimensions, a pixel spacing of 1 nm and a dwell time of 1.2 ms led to the vertical pitch height of 230 nm, the helix diameter of 120 nm, and the helix wire of diameter of 20 nm. As EBID process does not allow to fabricate purely metallic structures [64], the helix was subsequently coated with gold using electron beam evaporation under a pressure of 0.1 mPa. Conformity of the coat was achieved by glancing angle deposition under 87° tilt and rotating the sample. The resulting core-shell helix (similar to structures reported recently by Kosters et al. in [40]) had a diameter of approximately 70 nm. Additional FDTD simulations (not shown here) reveal that a 25-nm thick shell is thick enough to ignore the effect of the EBID core of the nanohelix, since the spectral position and strength of the resonances are independent of the core properties. Those simulations included helix-cores made of carbon and gold, both being the main elements of the EBID composite [65]. Therefore, the 25 nm thick Au-coating allows for modeling the nanohelix as a solid-gold structure [66] as it was done for the FDTD simulations. Lastly, the thin gold and ITO layers around the helix were removed by an Ga focused ion-beam operating at a voltage of 30 kV and a beam current of 10 pA.

**Experimental setup and measurement scheme**

The custom-build measurement system (similar to the one used in Refs. [22, 50, 51, 62]) was equipped with a broadband light source (Koheras SuperK Extreme Supercontinuum Laser), which covers the spectral range of interest between 1300 nm and 1650 nm. To provide equal illumination condition at each wavelength, the measurements were performed wavelength-by-wavelength with a spectral step of 10 nm (effectively the experimentally measured spectra consist of data points for 36 wavelength). To this end, the laser Gaussian beam was filtered spectrally by an acousto-optical tunable filter down to approximately 5 nm spectral width. The quasi-monochromatic beam was further polarized with a linear polarizer and an achromatic quarter-wave plate, and subsequently focused with a microscope objective with a high NA of 0.9 (Leica HCX PL FLUOTAR x100/0.90 POL 0/D). The incoming beam only partially filled the back focal plane of the microscope lens, reducing the effective focusing NA to 0.5 (NAeff = f0/NA, with f0 being the filling factor and NA the nominal numerical aperture of the microscope objective (0.9); f0 = w0/a = 0.555, where w0 is the beam waist and a is the aperture radius of the lens [67]), and preventing the formation of strong longitudinal field components across the focal plane (see Appendix II). The focus diameter changed slightly for individual wavelengths, leading to an insignificant increase of the energy density on the optical axis for shorter wavelengths. During the measurement the nanohelix was positioned on the optical axis in the focal plane. The glass substrate with the investigated nanohelix on top was placed on a three-dimensional piezo-stage. This enabled precise positioning of the sub-wavelength structure on the optical axis in the focal plane. The actual on-axis position was found by raster-scanning the nanohelix across the focused beam, and by a subsequent analysis of the scans. The reflected and the back-scattered light was collected by the focusing lens. The smaller waist of the incoming beam with regard to the diameter of the back focal plane aperture resulted in a plane-wave-like illumination of the structure at normal incidence. On the other hand, the back-scattered and reflected light could be collected within the full angular range provided by the numerical aperture (0.9) of the objective. For separation of the incident and the reflected light, a circular-polarization-preserving beam-splitter-system [68] was inserted between the source and the focusing lens. The transmitted and the forward-scattered light was collected by a second immersion-type objective of higher NA, equal to 1.3 (Leica HCX PL FLUOTAR x100/1.30 OIL), which was aligned confocally with respect to the focusing
lens. In both directions, the total power was measured with photo-diodes. The acquired data was normalized to the power of the impinging light onto the sample by measuring a reference signal for the air-glass interface and by calculating the corresponding power Fresnel coefficients for each wavelength for the chosen illumination scheme. For experimental observation of the forward-scattered light in the far-field, the photo-diode in transmission was replaced by a lens and a camera to image the back focal plane of the objective. Due to the very high NA of 1.3 of the microscope lens, the scattered light could be clearly distinguished from the transmitted beam within the angular range of \( \text{NA} \in [0.9, 1.3] \). For details see Refs. [51,62].

**Numerical modeling**

The theoretical transmittance and reflectance spectra were obtained using a Maxwell’s-equations solver based on the finite-difference time-domain method (Lumerical FDTD Solutions). All simulations were carried out using a Gaussian-beam source (the source plane was placed 600 nm away from the air-glass interface) with the same characteristics as those used in the experiments. The permittivity dispersion of gold was taken from [69]. Based on ellipsometry measurements, the refractive index of the glass substrate was set to 1.51, and its dispersion was neglected. For equal illumination conditions, the circularly polarized Gaussian beam was set to be monochromatic. The simulations were run in the spectral range between 450 nm and 1900 nm with a spectral step size of 10 nm (see Appendix II). The focusing scheme was chosen in accordance with the experiment (\( \text{NA}_{\text{eff}} = 0.5 \) for all wavelengths) and, hence, the size of the focal spot changed slightly as explained above. The simulation provided the densities of charge and current as well as the polarization density \( \mathbf{P} \) for the subsequent spectral multipole decomposition of the investigated nanohelix.

**Multipolar decomposition**

The FDTD-retrieved spatial distributions of the polarization density \( \mathbf{P}(\mathbf{r}) \) in close proximity of the nanohelix was further evaluated to determine the spectral multipolar response using [70,71]:

\[
\begin{align*}
\mathbf{p} &= \int \mathbf{P}(\mathbf{r}) \, d\mathbf{r}, \\
\mathbf{m} &= \frac{i \omega}{2} \int \left[ \mathbf{r} \times \mathbf{P}(\mathbf{r}) \right] \, d\mathbf{r}, \\
Q^e &= 3 \int \left[ \mathbf{r} \mathbf{P}(\mathbf{r}) + \mathbf{P}(\mathbf{r}) \mathbf{r} - \frac{2}{3} [\mathbf{r} \cdot \mathbf{P}(\mathbf{r})] \mathbf{U} \right] \, d\mathbf{r}, \\
Q^m &= \frac{\omega}{3i} \int \left( \mathbf{r} \times \mathbf{P}(\mathbf{r})\right) \left[ \mathbf{r} + \mathbf{r} \left( \mathbf{r} \times \mathbf{P}(\mathbf{r}) \right) \right] \, d\mathbf{r},
\end{align*}
\]

where \( \mathbf{p}, \mathbf{m}, Q^e \) and \( Q^m \) represent the electric and magnetic dipole and quadrupole moments, respectively, \( \mathbf{r} = (x,y,z) \) is a position in space and \( \mathbf{U} \) is the 3 x 3 unit tensor. It shall be noted that the equations above are valid for a scatterer of very small dimensions compared to the excitation wavelength. The helix presented in Fig. 1 fulfills the condition as the pitch (the largest dimension of the structure) is over six times smaller and almost four times smaller than the wavelength of the fundamental resonance and the first higher-order resonance, respectively. For scatterers of larger dimensions, the exact solution, which takes into account the so-called toroidal moments, has been recently presented by Alaee et al. in [72].
**Far-field scattering into substrate**

For a point (dipolar) emitter in air close to a dielectric interface, the far-field intensity distribution into the substrate reads $I = |E_{TM}|^2 + |E_{TE}|^2$ with \[67\]:

$$
E_{TM} = E_{TM}^p + E_{TM}^m,
$$
$$
E_{TE} = E_{TE}^p + E_{TE}^m,
$$

where $E_{TM}$ and $E_{TE}$ represent two polarizations of the scattered light for which the electric field oscillates parallelly and perpendicularly with respect to the meridional plane, respectively. The contribution of the electric dipole $p = (p_x, p_y, p_z)$ to the far-field intensity can be determined from:

$$
\begin{pmatrix}
E_{TM}^p \\
E_{TE}^p
\end{pmatrix}
= CF_p M_p
\begin{pmatrix}
p_x \\
p_y \\
p_z
\end{pmatrix}
$$

and the contribution of the magnetic dipole $m = (m_x, m_y, m_z)$ reads:

$$
\begin{pmatrix}
E_{TM}^m \\
E_{TE}^m
\end{pmatrix}
= \frac{C}{c_0} F_m M_m
\begin{pmatrix}
m_x \\
m_y \\
m_z
\end{pmatrix}
$$

with

$$
C = e^{i|k|r} \frac{|k|^2}{\sqrt{|k|^2 n^2 - k_\perp^2}} \frac{1}{4\pi \epsilon_0 \omega \kappa_z} e^{i \kappa_z d}.
$$

Here, $k = (k_x, k_y, k_z)$ represents the wave vector in free space ($|k| = 2\pi / \lambda$), $k_\perp = \sqrt{|k|^2 - k_z^2}$ is the transverse wave number in free space, $\kappa_z = \sqrt{|k|^2 - k_\perp^2}$ and $n, \epsilon_0, c_0, d$ and $r$ are the refractive index of the glass substrate, the vacuum permittivity, the speed of light, the distance between the point emitter and the substrate, and the distance to the observer, respectively. In the equations above $F_f$ stands in for the transmission matrix defined as:

$$
F_f = \begin{pmatrix}
t_{TM} & 0 \\
0 & t_{TE}
\end{pmatrix}
$$

with $t_{TM}$ and $t_{TE}$ being the Fresnel transmission coefficients for TM- and TE-polarized light. The two matrices $M_p$ and $M_m$ are the rotation matrices which project the electric field of the light emitted by the dipoles onto the plane-waves of the angular spectrum of the back focal plane and are defined as:

$$
M_p = \begin{pmatrix}
\frac{k_x}{k_z} & \frac{k_y}{k_z} & \frac{k_z}{k_z} \\
\frac{k_x}{k_z} & \frac{k_y}{k_z} & \frac{k_z}{k_z} \\
0 & 0 & 0
\end{pmatrix},
$$
$$
M_m = \begin{pmatrix}
-\frac{k_x}{k_z} & \frac{k_y}{k_z} & 0 \\
\frac{k_x}{k_z} & \frac{k_y}{k_z} & \frac{k_z}{k_z} \\
0 & 0 & 0
\end{pmatrix}.
$$

Accordingly, the $x$- and $y$-polarized components of the electric field in the far-field read $E_x = E_{TM} \cos \phi - E_{TE} \sin \phi$ and $E_y = E_{TM} \sin \phi + E_{TE} \cos \phi$, where the angle $\phi$ is the azimuth coordinate measured from the $x$-axis towards $y$-axis of the coordinate system whose center coincides with the point emitter (see Fig. 4).
Appendix II: Supplementary information

Spectral multipole expansion of an individual single-loop plasmonic helix

The FDTD simulations were performed for a spectral range between 450 nm and 1900 nm with a step size of 10 nm. The nanohelix was excited with a weakly focused (NA_{eff} = 0.5) circularly polarized Gaussian beam following the illumination scheme in the experiment. Fig. 7 presents the reflectance, transmittance, absorbance, and differential absorption spectra for RCP and LCP light. The reflectance and the transmittance spectra are normalized to the input power and the two other quantities are calculated as explained in the main text. Accordingly, the experimentally investigated resonance at 1450 nm is identified to be the fundamental mode of the structure and the first higher-order resonance is expected at the wavelength of 840 nm. Furthermore, using the FDTD-recorded polarization density \( P \), the spectral multipolar decomposition was done as described in Methods. The optical response of the helix was expanded into electric and magnetic multipoles up to order 3 (dipole, quadrupole, and octupole). The investigated structure can be effectively described with dispersive electric and magnetic dipoles as depicted in Figs. 8-10. Due to the very weak strength of the octupoles (~11-12 orders of magnitude weaker than the retrieved quadrupoles), only the spectra for the dipoles and quadrupoles are presented.

PT-symmetries of a system of coupled electric and magnetic dipoles

Figure 11(a) presents the chiral dipole of the fundamental resonance \( p_z - im_z \) under a parity transformation \( P \) and time inversion \( T \). This can be seen as a test for chirality of the \( z \)-polarized coupled electric and magnetic dipoles [1, 56]. While an electric dipole has an odd parity, a magnetic dipole, in contrast, exhibits even parity. A \( P \) transformation hence results in a dipole system defined by \( -p_z - im_z \) which does not coincide with the original set of dipoles under any isometric transformation except \( P^{-1} \). Effectively, the \( P \) transformed dipole system describes a left-handed structure, which does not coincide with the investigated right-handed nanohelix. Moreover, a true three-dimensional chiral system is time \( T \) irreversible. The sense of rotation of the eddy current (at \( \omega t = \pi/2 \)) changes under a \( T \) transformation \( (t \rightarrow -t) \) and the magnetic dipole moment alters its orientation respectively. If \( p_z \) and \( m_z \) were not coupled via the geometry of the nanohelix, the longitudinal electric dipole moment would stay unaffected. Nevertheless, the time-harmonic oscillation of charge forces \( p_z \) to reorient with \( m_z \), and the resulting state is again indistinguishable from the initial one \( (P(p_z - im_z) \neq p_z - im_z = T(p_z - im_z)) \). The simultaneous change of both dipole moments under \( T \) inversion is a consequence of the magnetoelectric coupling induced by the geometry of the nanostructure.

On the contrary, a point-like system of coupled electric and magnetic dipoles oscillating along two orthogonal directions does not fulfill the argument of the \( PT \)-symmetries. Figure 11(b) shows another set of dipole components \( p_z - im_y \) at \( \lambda = 1450 \) nm presented in Fig. 3 in the main text. Under \( P \) transformation the resulting system can be easily superimposed with the initial pair of dipoles by a rotation about the \( y \)-axis \( (R_y(\pi)) \). Also, a rotation about the \( x \)-axis \( (R_x(\pi)) \) of the \( T \)-transformed dipoles can be overlapped with the input set of dipoles. Since \( P(p_z - im_y) = T(p_z - im_y) = p_z - im_y \), a point-like system based on coupled orthogonal electric and magnetic dipoles is not chiral.

A point-like system of coupled electric and magnetic orthogonal dipoles is supported by a planar and solid split-ring resonator (SRR). Excited at normal incidence with, e.g., linearly or azimuthally polarized beam [50, 73–75], the structure can be represented similarly as depicted in Fig. 11(b) and, hence, a planar SRR does not exhibit optical activity. The excited dipoles can, however, be forced to have a common direction of oscillation, if the structure will be excited at oblique incidence. For tilted illumination, the wave vector of the incoming light and the SRR will create a chiral triad [23]. Effectively the structure will appear to be a three-dimensional figure and exhibit so-called extrinsic chirality; hence extrinsic \( G'' \neq 0 \).
Far-field scattering of the nanohelix under RCP and LCP illumination

The experimental and numerical spectra depicted in Fig. 2 presents non-zero differential absorption of RCP and LCP light and show that only RCP field effectively excite the right-handed nanohelix. The absorbed light is used up to drive back and forth the surface charges along the helix wire (Section 3). The selective excitation of oscillating electric and magnetic dipoles under RCP illumination shall, therefore, result in a non-zero differential scattering in the far-field. Figure 12 presents the experimentally acquired far-field scattering by the nanohelix illuminated with RCP and LCP light at the wavelength of the fundamental resonance. The intensity maps are normalized to the maximum value of forward-scattered light for RCP excitation. The far-field scattered light under LCP excitation is extremely faint. Hence, it is clear that the nanohelix not being able to absorb LCP cannot also scatter under left-handed excitation.

Here, we would like to note that a dipolar emitter placed near a dielectric interface emits predominantly into the optically denser medium. In the presented scheme, the far-field scattered light peaks at the angle of NA = 1.0 in the forward direction [60,61]. Therefore, the distributions of the far-field scattering by the nanohelix under RCP and LCP illumination shown in Fig. 12 present a non-zero differential scattering.

Weakly focused circularly polarized Gaussian beam illumination in presence of a glass substrate

In the experiment and the corresponding simulations, we illuminated a nanohelix standing on a glass substrate with a weakly focused circularly polarized Gaussian beams. Here we show calculations of such a weakly focused beam in presence of a glass substrate (in the absence of the nanohelix) to verify that the nanohelix is indeed exposed to a planewave-like circularly polarized field. Figure 13 shows the distribution of the focal fields of weakly focused (NAeff = 0.5) right-handed circularly polarized Gaussian beam (λ = 1450 nm) which is reflected at the focal plane by a glass substrate of refractive index 1.51. The plane of observation is 125 nm (half of the helix pitch) above the air-glass interface. The focal fields are calculated using vectorial diffraction theory [67] and the electric intensity distributions are normalized to the maximum value of total electric energy density (ε₀/2)|E|². In addition, we outline the position of the nanohelix during measurements. According to the presented field maps, the nanohelix was exposed to a locally circularly polarized and transverse field.
Fig. 8. Magnitudes and phases of the components of the electric $p$ and magnetic $m$ dipole moments of the helix under LCP illumination.

Fig. 9. Magnitudes of the components of the magnetic $Q^m$ and electric $Q^e$ quadrupoles of the helix under RCP illumination.
quadrupole moments for LCP

Fig. 10. The same as Fig. 9, but for an LCP excitation.

for RCP at $\lambda = 1450$ nm

Fig. 11. Parity ($P$) and time ($T$) inversions of a point-like system of coupled electric and magnetic dipoles of (a) parallel and (b) perpendicular orientations.
far-field forward-scattering at $\lambda = 1450$ nm

**Fig. 12.** Far-field forward-scattering of the nanohelix at the wavelength of its fundamental resonance under RCP and LCP illumination.

**Fig. 13.** Distributions of the focal electric energy densities (top) and the relative phases (bottom) of a weakly focused ($\text{NA}_{\text{eff}} = 0.5$) RCP Gaussian beam ($\lambda = 1450$ nm). The individual electric field intensity maps are normalized to the maximum value of total electric energy density ($\epsilon_0/2 |E|^2$). The dashed circle outlines the outer contour of the nanohelix.
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Disclosures
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