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Using Shape Diversity on the Way to Structure-Function Designs for Magnetic Micropropellers

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Synthetic microswimmers mimicking biological movements at the microscale have been developed in recent years. Actuating helical magnetic materials with a homogeneous rotating magnetic field is one of the most widespread techniques for propulsion at the microscale, partly because the actuation strategy revolves around a simple linear relationship between the actuating field frequency and the propeller velocity. However, full control of the swimmers' motion has remained a challenge. Increasing the controllability of micropellers is crucial to achieve complex actuation schemes that, in turn, are directly relevant for numerous applications. However, the simplicity of the linear relationship limits the possibilities and flexibilities of swarm control. Using a pool of randomly shaped magnetic microswimmers, we show that the complexity of shape can advantageously be translated into enhanced control. In particular, directional reversal of sorted micropellers is controlled by the frequency of the actuating field. This directionality change is linked to the balance between magnetic and hydrodynamic forces. We further show an example of how this behavior can experimentally lead to simple and effective sorting of individual swimmers from a group. The ability of these propellers to reverse swimming direction solely by frequency increases the control possibilities and is an example for propeller designs, where the complexity needed for many applications is embedded directly in the propeller geometry rather than external factors such as actuation sequences.

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I. INTRODUCTION

Microswimmers are envisioned for a multitude of applications ranging from solving environmental problems to being used for microsurgery [1–4]. Precise, versatile, and noninvasive controllability is necessary to cover this broad scope of applications. These requirements are mostly matched by magnetic microswimmers. The fuel-free actuation by weak and homogeneous magnetic fields allows remote controlling in many environments and the synthesis via nanofabrication makes them accessible even on a submicrometer scale [5–8]. In addition, the ability to functionalize their surface and the limited toxicity of the mostly iron-based propellers makes them appealing for medical applications [2,9]. Many of the current magnetic microswimmers use a helical shape with a fixed magnetic moment to rotate in an externally applied magnetic field,

which enables stable propulsion. In this case, a simple linear relationship between the frequency of the actuating magnetic field and the velocity of micropellers is used to precisely control the propeller [6,10–13]. This leaves the sign of the swimming direction of the propeller to be determined by the rotation direction of the applied magnetic field, which limits the versatility of their actuation capability: when controlling two or more geometrically identical propellers, it is not possible to let them swim in a common propulsion mode in the same direction and, if needed, in opposite directions, simply because they identically react to the same rotation and/or rotation reversal of the field such that they eventually always all swim in the same direction. This does not change even when using nonlinear propeller behavior after the so-called step-out frequency.

Joining and splitting of swarms of microswimmers in three dimensions plays an important role for multitargeting tasks from micromanipulation to self-organization and drug delivery. With the helical swimmers, this is only

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possible with complex actuation sequences [14] that have remained theoretical. Recent studies have now shown that nonlinear propelling behaviors can be obtained for particular devices [15–18]. The general theory describing linear and nonlinear cases depicts a change of the propeller's axis of rotation as a function of the externally applied frequency for many geometries [19]. So far, this behavior has only been appreciated as a nonswimming (tumbling) or a swimming (wobbling) regime [15,17].

Here, we take advantage of a synthetic route to randomly shaped micropropellers [9,20] to test alternative actuation schemes in this context. Screening a pool of randomly shaped micropropellers, we select those reversing their swimming direction based on the applied actuation frequency. Comparing this frequency-induced reversal with recent progresses in their theoretical description, we make an argument for expanding the degree of controllability of micropropellers. In particular, we demonstrate the isolation of a single propeller from a swarm. This structure function relationship can lead to an alternative method for designing magnetic micropellers, where controllability is not embedded into actuation sequences, but is already included in the geometry of the microswimmer.

II. EXPERIMENTAL DETAILS

The magnetic microswimmers used here are randomly shaped microparticles that were previously synthesized [9]. Their general swimming capability is shown elsewhere [9,21]. They consist of iron(III)-nanoparticles (20–40 nm, NanoArc®, Alfa Aesar) that are connected via hydrothermal carbonization [20] to rigid structures with a magnetic moment fixed to their body [9]. Stored in a dilute suspension in deionized water, some propellers are put into a glass capillary ($0.2 \times 2 \times 50 \text{ mm}^3$) by capillary forces and the open ends are sealed with petroleum jelly to hinder evaporation and unwanted flows of the fluid. The capillary is fixed on an objective slide, which is, in turn, put on the stage of a custom made three-dimensional (3D) Helmholtz-Coil setup [22]. The capillary hangs upside-down on the objective slide and is illuminated from the top by a light-emitting diode (LED) light source (either 400 nm or 635 nm, CoolLED Ltd.). Below the capillary, a $60\times$ Plan Apochromat 1.20 WI Nikon® objective is placed in the optical path, which is led by a mirror system to high-speed cameras (Andor Zyla 5.5 scientific Complementary Metal-Oxide-Semiconductor with a maximum resolution of 2560×2160 pixels or an Optronis CR3000X2 with 1710×1696 pixels, respectively). The sedimented propellers are brought to bulk fluid far away from surfaces by a rotating magnetic field $B(\omega, t) = [B_0 \sin(\omega, t), B_0 \cos(\omega, t), 0]'$ with the rotational angular frequency $\omega = 2\pi f$. Subsequently, the axis of the rotating magnetic field is changed to be along the y direction $\{B(\omega, t) = [B_0 \sin(\omega, t), 0, B_0 \cos(\omega, t)]'\}$ to measure the

velocity along this axis in the bulk fluid. The magnetic field strength is typically chosen to be between 1 and 3 mT and the frequency between 1 and 150 Hz depending on the characteristics observed during the measurement. Testing different frequencies (usually in 10-Hz steps) shows candidates for propellers with frequency-dependent swimming direction. Such propellers are then brought in approximately the same orientation by applying a constant magnetic field along the x direction until the rotating field starts. The rotating magnetic field is applied for 10 s for each frequency and the propulsion of the propeller is imaged and recorded. After another constant field, the rotational frequency is increased in 1-Hz steps. The propeller velocity in dependence of the applied external frequency is determined from the propeller position along the axis of rotation. More details can be found in the Supplementary Material [23].

III. RESULTS AND DISCUSSION

A. Direction reversal and correlation with propeller orientation

Randomly shaped magnetic micropropellers are observed in an inverted custom-designed optical microscope [9,22] and are actuated in water far away from surfaces by a rotating magnetic field $B(\omega, t) = [B_0 \sin(\omega, t), 0, B_0 \cos(\omega, t)]'$. Some of them show a behavior we call frequency-induced reversal of swimming direction (FIRSD). In other words, the propeller swims in two opposing directions for two different field frequencies of the external actuating magnetic field, while no other parameter is changed. This stands in contrast to direction inversions used before, where the magnetic field rotation needed to be inverted to reverse the swimming direction. The velocity-frequency relationship of propellers exhibiting FIRSD is presented in Figs 1(a) and 1(d) for two exemplary propellers. An inverse radon transformation provides 3D reconstructions of the propeller shapes from the recorded two-dimensional (2D) images using the projections of the rotating propellers [Figs. 1(b) and 1(e), more information in the Supplemental Material [23] including Figs. S7 and S8, and Refs. [24,25]]. Figures 1(c) and 1(f) show shape specific velocity landscapes that reflect all coupling possibilities of the respective propellers because more than one possibility can be obtained for a given shape due to the variety of different magnetic properties possible (cf. see Sec. VI in the Supplemental Material [23]). Additionally, microscope image snapshots of the propeller configuration to the horizontal axis of rotation are put in the according frequency regime at the bottom. A theoretical fit (Appendix, [26]) is added to the experimental results of the frequency-dependent velocity measurements in Figs. 1(a) and 1(d). Typically, the curves exhibit a linear regime at low frequencies where the propellers rotate around their short axis (tumbling, region I in Fig. 1; propeller 1: $f = 0\text{--}25$ Hz;

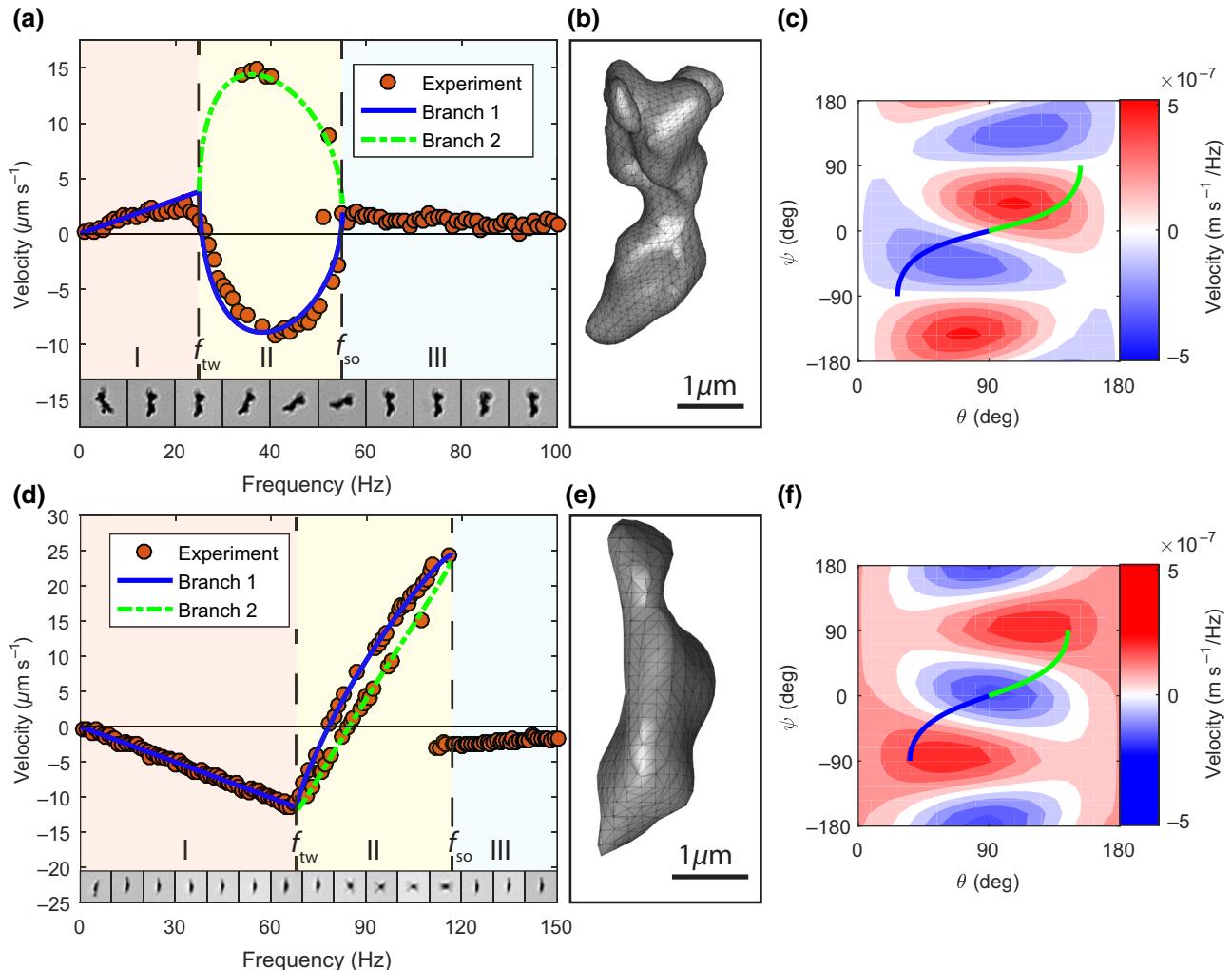


FIG. 1. Velocity-frequency relationship. The measured velocity (red dots) dependent on the applied frequency of the actuating magnetic field is shown in (a) and (d) for propellers 1 and 2, respectively. The theoretic fit on those data points is shown in blue (solid line) and green (dashed line), which also describes the observed branching (corresponding to different propeller configurations at the respective frequencies). The 3D reconstruction of the propellers is depicted in (b) and (e). To visualize the change in propeller configuration to the horizontal axis of rotation dependent on the frequency, microscope images are shown in the measured frequency regime for one respective branch ((a) and (d) on the bottom). The far most left image corresponds to the orientation for a constant field in between the measurements. Both propellers show a reversal of the velocity direction in the first branch (blue), when increasing the frequency: after a linear tumble regime (I, swimming in one direction) until f_{tw} , a nonlinear wobbling regime [II happens up to the step-out frequency f_{so} (III)]. During the wobbling, the long axis of the propeller starts to tilt more and more toward the horizontal axis of rotation and at a certain frequency, the propeller velocity reverses its sign – the propeller swims in the opposing direction. The respective velocity landscapes are shown in (c) and (f) as contour plots (red for positive velocities, blue for negative ones, and white for zero). They reflect the velocity possibilities (in $\text{m s}^{-1}/\text{Hz}$) of the respective propeller shapes. The green and blue lines are again the branches, since the propellers are restricted to certain rotation axes for increasing frequency. The rotational similarity of propeller 2 is reflected in its velocity landscape. As a result, the branches pass similar values for increasing frequency (in contrast to propeller 1).

propeller 2: $f = 0\text{--}68 \text{ Hz}$). At a transition frequency f_{tw} , the behavior changes, and the propellers tilt their long axis toward the horizontal axis of rotation of the actuating field [wobbling, cf. Fig. 2(a)] (propeller 1: $\approx 25 \text{ Hz}$; propeller 2: $\approx 68 \text{ Hz}$). In this frequency regime (region II in Fig. 1), the fit as well as the experimental data imply the existence of two solution branches (blue solid line and green dashed line). These correspond to different orientations

of the propeller during its actuation in an external rotating field. First, we focus on one branch (solid blue) and will discuss the implications of the branching in the next section. The change in the axis of rotation with respect to the propeller geometries alters the rotation-translation coupling of the propellers at each frequency step. In general, this leads to a nonlinear relationship between the actuating field frequency and the propeller velocity. Here, the sign of

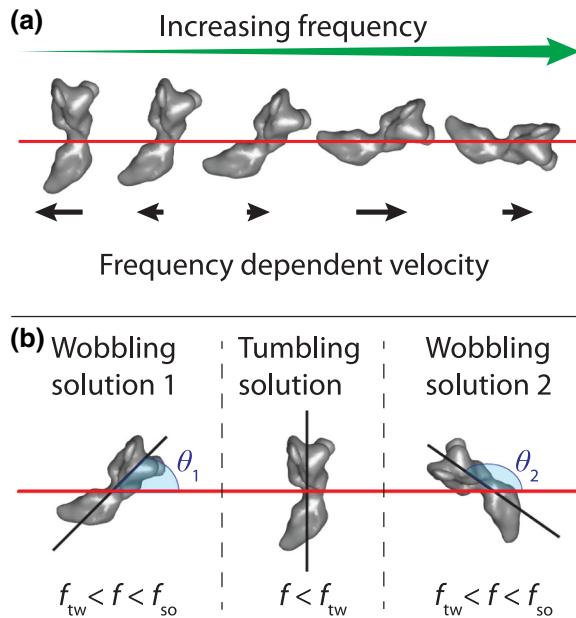


FIG. 2. Frequency dependent axis of rotation (a). The orientation of a propeller toward its axis of rotation (red horizontal line) changes with increasing frequency for some geometries to balance the magnetic and hydrodynamic torques. As a result, the coupling, and therefore, the velocity changes with frequency, which can lead to an inversion of the propulsion direction. Branching schematic (b). Coming from the tumbling configuration at low frequencies (middle), two wobbling configurations are possible for higher frequencies between the transition frequency f_{tw} and the step-out frequency f_{so} . Here, the two possibilities of Propeller 1 are depicted (cf. Movies S7 and S8 in the Supplemental Material [23]): the first wobbling solution with an angle of θ_1 between the long axis of the propeller and the axis of rotation (red horizontal line) and the second solution/configuration (right side) with $\theta_2 = 180^\circ - \theta_1$.

the coupling, and therefore, the velocity changes with frequency: both propellers slow down after f_{tw} and eventually reverse their swimming direction (propeller 1: ≈ 27 Hz; propeller 2: ≈ 77 Hz). Due to the different orientation of the propeller toward the axis of rotation, the behavior deviates from the single linear behavior seen for other magnetic micropropellers [6,11,12,27]: while still turning in the same sense of rotation, the swimming direction reverses. Finally, the velocity breaks down at the frequency f_{so} (propeller 1: ≈ 55 Hz; propeller 2: ≈ 117 Hz), reminiscent to what is seen for the behavior after the step-out frequency of linear propellers. Here, the propellers, with their magnetic moment m fixed in their geometry, can no longer follow the frequency of the magnetic field rotation and apparently return to a rotation around their short axis (microscope images panels A and D, asynchronous regime, region III in Fig. 1). The maximum velocities (Table I) for propeller 1 for the two opposing swimming directions are $v = 3 \mu\text{m s}^{-1}$ at $f = 22$ Hz and $v = -9 \mu\text{m s}^{-1}$ at $f = 41$ Hz. Propeller 2 swims at $v = -11 \mu\text{m s}^{-1}$ for $f = 66$ Hz and up to

$24 \mu\text{m s}^{-1}$ for $f = 117$ Hz. The respective minimal and maximal dimensionless velocities $U = 1000 \cdot v/(l \cdot f)$ of the two propellers are also shown in Table I, where f is the frequency of the actuating external field and l is the characteristic length of a propeller. The lowest and highest dimensionless speeds for propeller 1 are about 36 and -52 , respectively, for propeller 2, they are 51 and -41 , respectively. In summary, both propellers reorient themselves depending on the frequency and are able to effectively swim in two opposing directions by only changing the applied external frequency of the magnetic field.

B. Torque balance determines propeller reorientation and branching

The reorientation of the propeller with changing frequency can be explained by a balance of the acting magnetic and hydrodynamic torques [16,17] and was recently expanded to arbitrarily shaped particles [19]. When applied to our system, this leads to the following qualitative physical description: at low frequencies, the magnetic moment of the propeller is in the plane of the rotating magnetic field but lags behind with a constant angle/phase as result of the torque balance. With increasing frequency, this phase is also increasing. This results in a linear regime (region I in Fig. 1, tumbling). Depending on the geometry of the propeller and the associated magnetic moment, a certain transition frequency f_{tw} exists, where it is favorable to change the propeller orientation and to no longer rotate around the (hydrodynamically worse) short propeller axis [17]. At this point, the magnetic moment is moved out of the magnetic field plane (nonlinear regime, region II in Fig. 1, wobbling), the hydrodynamic drag is decreased by rotating around an axis with a lower hydrodynamic viscous drag, and the torque balance is restored. This balance (synchronous regime, regions I + II in Fig. 1) can only be maintained up to a certain step-out frequency f_{so} , where neither the phase lag can be increased nor the hydrodynamic drag can be decreased by reconfiguration – the propeller can no longer follow the magnetic field and the velocity breaks down (asynchronous regime, region III in Fig. 1) [17]. A detailed theoretical description of this process using the rotational mobility matrix F and coupling mobility matrix G together with the Euler angles ϕ , θ , and ψ to calculate swimming velocities can be found elsewhere [19], but is additionally shortly summarized in Secs I and II in the Supplemental Material [23]. Figures 1(e) and 1(f) illustrate the geometrical possibilities given through F and G and how the magnetic moment orientation restricts the propellers on certain orientations and rotation axes.

Looking back at the measured data in Fig. 1, between f_{tw} and f_{so} , another mutual but unequally spread feature occurs, with some measuring points not following the general curve (also called branching). This branching,

TABLE I. Propeller/measurement characteristics.

Property	Propeller 1	Propeller 2
Magnetic field B_0 (mT)	2	1
Propeller length l (μm)	4.34	4.13
Propeller diameter d (μm)	1.59	1.28
Approx. magnetic moment ^a m (Am^2)	1.08×10^{-14}	3.84×10^{-14}
Magnetic Saturation ^b m/m_{sat}	0.003	0.02
f_{tw} (Hz)	25	68
f_{so} (Hz)	55	117
v_{\min} ($\mu\text{m s}^{-1}$)	-9	-11
v_{\max} ($\mu\text{m s}^{-1}$)	3 and 15 ^c	24
U_{\min}	-52	-41
U_{\max}	36 and 98 ^c	51

^aCalculation from cylindrical approximation [16,28].

^bWith saturation magnetization of maghemite [29].

^cSecond branch values.

which was theoretically predicted [19], is not necessary for the above described frequency-induced reversal of swimming direction, but can offer further possibilities, but also challenges (Supplemental Material [23]). Branching is explained by the fact that two solutions are possible between the two characteristic frequencies f_{tw} and f_{so} for the corresponding Euler angles when applying a frequency above f_{tw} : θ_1 corresponds to the blue solid line in Figs. 1(a/c) and 1(d/f) and $\theta_2 = 180^\circ - \theta_1$ to the green dashed line. These two configurations can be seen in Movie S7 in the Supplemental Material [23]. Figure 2(b) schematically illustrates the two possible solutions at frequencies above f_{tw} when originating from a rotation around the short propeller axis for frequencies below f_{tw} . The two different solutions can result in two rather different velocity responses (propeller 1) dependent on the geometry [velocity landscape in Fig. 1(c)] and the associated magnetic moment (line plots in Fig. 1(c) and [19]). Alternatively, propeller 2 shows a configuration where they are very similar [relatively symmetric velocity landscape in Fig. 1(f)]. It is noteworthy that even identical velocity responses were predicted for the two orientations ([19], point symmetric velocity landscape around tumble configuration), which would avoid nonunique velocities' responses in this frequency regime. This complex behavior can be envisioned to obtain up to three different velocity responses (e.g., negative, positive, zero) for a narrow regime of the applied frequencies by providing the right initial conditions.

C. Changing propeller direction by varying the applied field strength

An additional alternative to achieve a reversal of the swimming direction is to change the strength of the applied magnetic field instead of its frequency, as shown for propeller 1 at three different field strengths [0.5, 1, and 2 mT, Fig. 3(a)]. The magnetic torque determining the propeller configuration scales linearly with the magnetic moment

of the propeller, but also with the applied magnetic field strength ($\tau_m = B \times m$). Therefore, the characteristic frequency-velocity curves scale with the applied magnetic field as can be seen in the inset of Fig. 3, where the frequencies and the velocities of the three measurements at the different magnetic fields are normalized on the respective magnetic field – the curves fall onto each other. This can be used to reverse the swimming direction by only changing the applied magnetic field strength at a constant frequency as illustrated in the theoretical plot of the propeller velocity as a function of the applied magnetic field strength and frequency [Fig. 3(b)]. This can be achieved because the different regimes (and therefore, different swimming directions) can either be reached by changing the applied frequency (horizontally) or the magnetic field strength (vertically). Exemplarily, the propeller has a velocity $v \approx -5 \mu\text{m s}^{-1}$ at an external frequency of 20 Hz and a field of 1 mT. At the same frequency but at 2 mT, the velocity of the same propeller is $v \approx 2.5 \mu\text{m s}^{-1}$.

D. Implication of FIRSD for swarm control

The rather basic question is why this behavior offers any benefit when comparing it to a simple reversal of the sense of rotation of the external field that would also lead to a reversal of the swimming direction. The differences between both methods can be best seen when considering multiple microswimmers actuated by the same external field. Future applications will include tasks like isolating one specific propeller from a swarm of microswimmers. Using previous methods, this is rather complicated but possible by applying a sequence of different actuating field frequencies and directions and using, for example, the step-out behavior after the linear frequency-velocity relationship. However, this currently has mostly remained theoretical or was performed on or close to surfaces in two quasidimensions [14,30,31]. A propeller with frequency-induced reversal of swimming direction allows

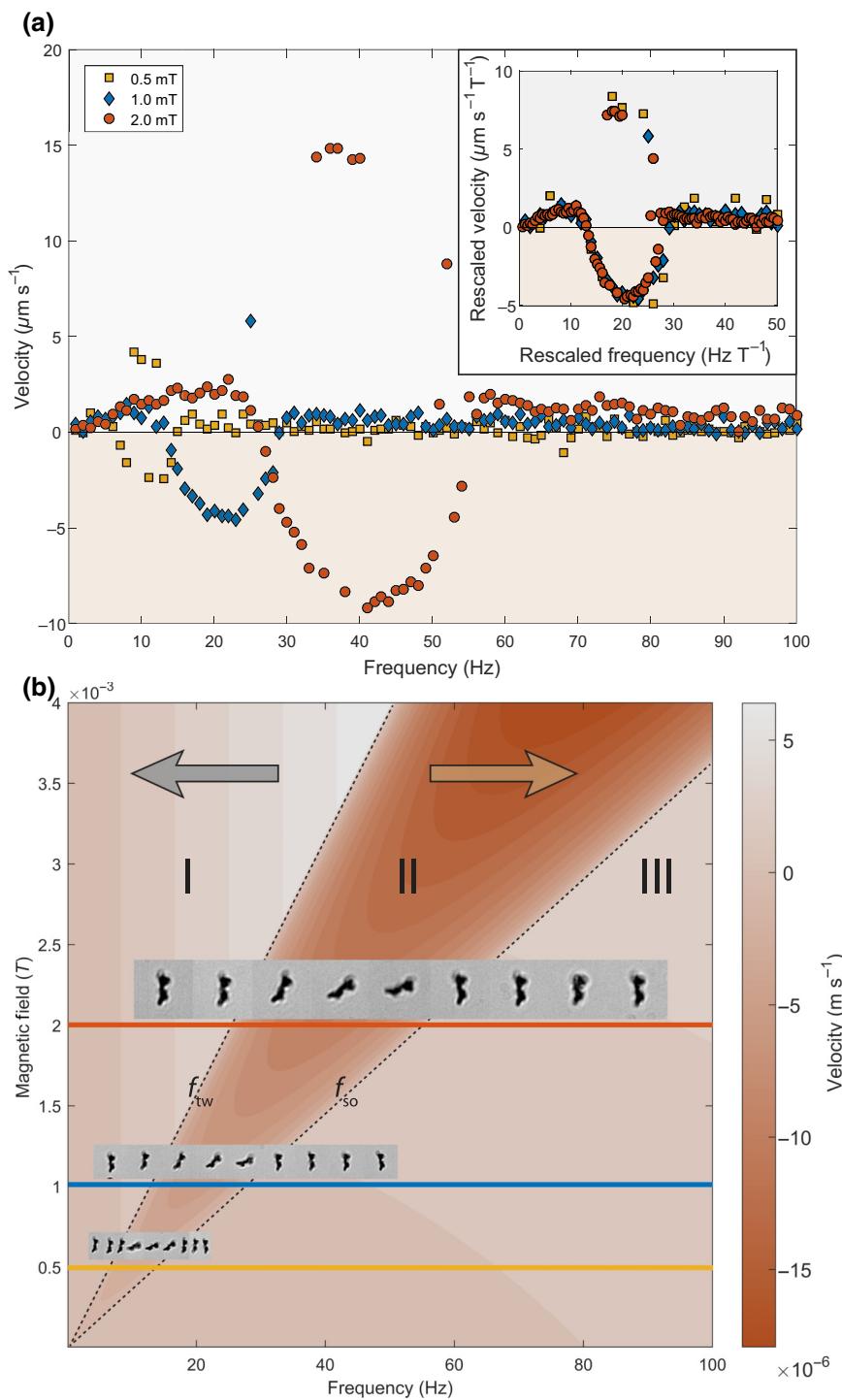


FIG. 3. Scaling with the magnetic field. (a) Velocity-frequency dependence of propeller 1 at three different magnetic field strengths (0.5, 1, and 2 mT). Depending on the magnetic field, the propeller can swim in opposing directions for the same frequency, for example, at $f = 20$ Hz for 1 mT (blue diamonds) and 2 mT (red dots). This is possible since the frequency characteristics scale with the strength of the magnetic field. In the inset, the three curves are normalized on the respective field strength, and therefore, fall onto each other. (b) Theoretical velocity as function of the applied magnetic field strength and frequency. The characteristic frequencies (f_{tw} and f_{so} , dashed lines), and therefore, the propeller behavior scales linearly with the magnetic field strength. The three measurements at 0.5, 1, and 2 mT are depicted through the yellow, blue, and red lines, respectively. Additionally, microscope images of the propeller configuration are shown to illustrate the three different regions and the two arrows indicate the respective swimming direction: the linear regime (I), the wobble regime (II), and the regime after the step-out frequency (III, not included in theory, set to 0).

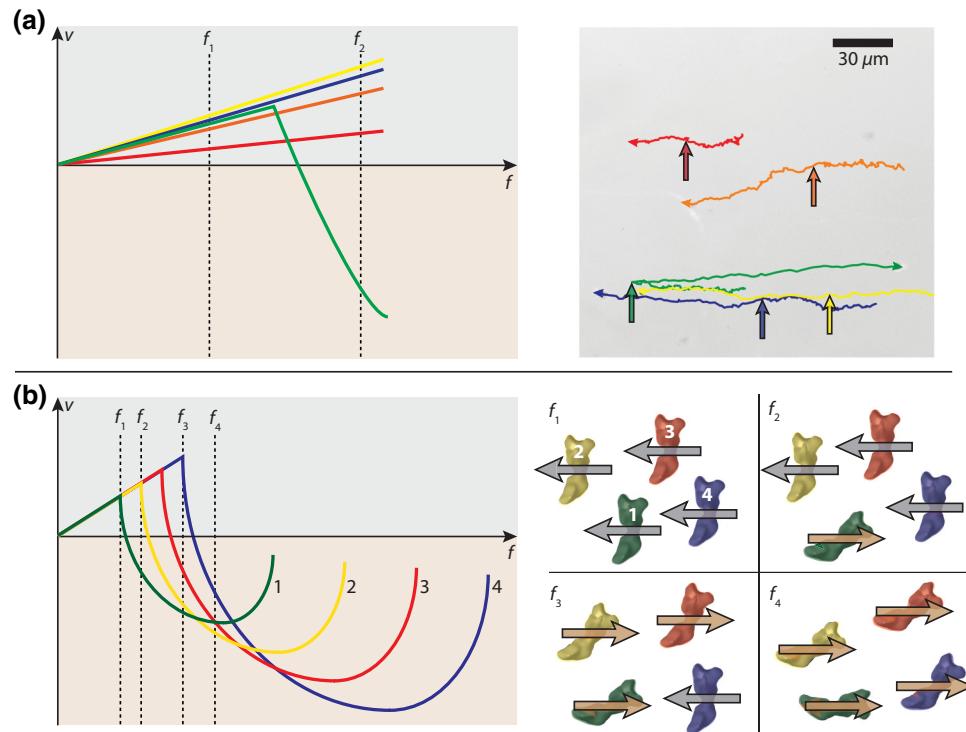


FIG. 4. Propeller isolation for randomly shaped propellers (a). Tracks of a group of randomly shaped propellers. They all swim to the left for the initially applied magnetic field frequency of $f_1 = 20$ Hz. The arrows mark the location when the frequency is increased to $f_2 = 40$ Hz. One propeller (green track) shows a reversal of swimming direction at this frequency and swims in the opposing direction, while the rest of the swarm propellers are still in their linear regime and continue to swim to the left. This allows a joint propulsion for one frequency and an isolation of a single propeller for another as can be seen in the Supplemental movie S11 [23]. The according v - f diagram is schematically shown on the left. Propeller selection schematic for identically shaped propellers (b). Isolation of a single propeller from a swarm of identical propellers that only differ in their magnetic moment modulus (increases from 1 to 4). At a frequency f_1 , all propellers swim in the same direction. At frequency f_2 , the propeller with the smallest magnetic moment (green, 1) has already changed its axis of rotation and has a negative velocity, while the rest of the swarm continues swimming in the original direction (positive velocity). At frequency f_3 , all propellers except for the one with the highest magnetic moment (blue, 4) have reversed their swimming direction. At frequency f_4 , all propellers swim in the opposing direction compared to f_1 . This offers new possibilities for controlling swarms of propellers and single propellers at the same time.

direct targeting of this propeller at a certain frequency. Such a behavior is shown for a swarm of randomly shaped micropropellers in Fig. 4(a) and Movie S11 in the Supplemental Material [23] in three dimensions far away from surfaces: at a frequency of 20 Hz, the whole swarm swims in one direction (here, left) until the frequency is increased to 40 Hz, where all but one propeller continue swimming in the initial direction, the final one reversing its swimming direction. This proof-of-principle motivates a more sophisticated and reliable way, which is schematically depicted in Fig. 4(b): four geometrically identical propellers that show FIRSD only differ in the modulus of their magnetic moment, for example, swimmers prepared by 3D printing with varying amounts of magnetic materials. While at low frequencies, the propeller with the smallest magnetic moment (and therefore, the smallest characteristic frequencies) still swims in the same direction as the rest of the swarm and applying a frequency that is characteristic for this propeller directly reverses

its swimming direction, while the rest of the swarm still moves in the original direction (with a slightly different velocity). The individually addressed propeller is separated from the rest. This behavior might be expanded to more propellers in the swarm so that for different propeller-specific frequencies, they reverse their swimming behavior compared to the rest of the propellers. This allows joint movement for certain frequencies, agglomeration in a certain point, and splitting into groups for other frequencies. Alternatively, this method can be used to collect propellers with a certain desired behavior at selected actuation frequencies from the pool of synthesized random particles, separating them locally.

IV. CONCLUSION

We show that it is possible to reverse the swimming direction of magnetic micropropellers by only changing the applied actuating frequency. This behavior offers an

alternative to the traditional reversing of the actuating magnetic field and enables simple execution of previously more complicated tasks as it can help in shifting the complexity of actuation to the details of the propeller geometry. In swarm control, a group of (nonidentical) propellers swims together at a certain frequency. Although the common linear micropropellers are easily reversed with a rotating field turning in the opposite direction, and therefore, offer great possibilities to globally manipulate swarms of microswimmers, they need a sequence of at least two magnetic field steps to join or separate subgroups of those propellers [14,31,32]. FIRSD propellers are usually able to do those basic tasks in one step (Sec. VII in the Supplemental Material [23]). For more complicated applications with longer actuation sequences and more tasks, a factor of two can rapidly add up. Although FIRSD will not be the optimal solution to all future challenges, it offers additional avenues to master them. Recently, there have been other microswimmer systems enabling direction reversal. Gomez-Solano *et al.* reported on thermally induced direction and motility change of self-propelled colloids, mimicking the run-and-reverse behavior of some bacteria [33]. However, the dependency on the surrounding fuel and the activation through laser light makes *in vivo* applications hard to realize. Khalil *et al.* produced two-tailed microbots that showed frequency-dependent back and forth movement through flagellar propulsion [34]. These microbots are still several hundreds of micrometer and might face micromechanical problems when scaling them down, similar to the theoretically proposed equivalent for joint helices [35]. An interesting system was presented by Garcí Torres *et al.* with frequency-induced reversal based on an interplay of magnetic, hydrodynamic, and gravitational interactions [36]. However, their system is a self-assembled swimmer that requires nearby surfaces to break symmetry and is, therefore, rather complementary than alternative to our propellers swimming far away from surfaces. Our proposed system uses penetrable remote control through weak homogenous magnetic fields together with the intrinsic rich interplay between a fixed geometry and magnetism in magnetic micropropellers. This enables a defined change of axis of rotation in dependence of the applied external frequency or magnetic field strength and can, therefore, be envisioned as an alternative to the common field reversal in some applications. However, there will always be a trade off between a certain functionality or application a propeller can be used for and its effective propulsion. This is the case for the propellers reported here: more efficient, constant stable propulsion over a large frequency regime is traded with the ability to control the sign of the swimming direction and the propeller speed by applying the right frequency beyond the usual linear relationship. This feature is currently underused, but can add to the controllability of the propellers apart from the currently considered options (field orientation/shape

deformation/soft magnetic materials). Especially with the current urgent need of automatization for the control of microrobots [3,37], this offers a simple and continuous method to change the swimming behavior drastically by only changing one parameter (frequency) in the system. Path and time optimization algorithms can benefit from micropropellers with frequency-induced reversal of swimming direction, since it facilitates addressing single propellers in a swarm of microswimmers. In this context, one must keep in mind that with actual practical applications, the requirements on the magnetic fields will increase and set limits to available frequencies and field strengths that could drastically differ from the conditions currently used in labs (e.g., by magnetic coil systems big enough for human limbs). FIRSD and, in general, nonlinear propellers can, therefore, be of some advantage for certain challenges. Another challenging task in this regard is to implement a feedback control/visualization of the microswimmers to make automatization possible in the first place. There have been studies using the fields of magnetic resonance imaging (MRI) to power magnetic microswimmers [38,39]. And with magnetic particle imaging (MPI) [40], another visualization method is on the horizon that might facilitate this for medical applications. In those systems, the magnetic fields possibilities are limited in the sense that they are optimized for the imaging rather than the propulsion. It will, therefore, be necessary to provide the needed complexity and flexibility for navigation in biological environments by introducing different actuation modes such as reversing the swimming direction and changing speed rather by the design of the magnetic micropropellers than by the limited accessible magnetic fields.

For expanding the range of possible applications, it is crucial to acquire a more substantial knowledge about arbitrarily shaped propellers to be able to systematically design micropropellers for specific tasks. Analytically, a direct link between shape and swimming behavior is missing, but with more experimental studies and simulations, this connection will become clearer (a few remarks on this are in Sec. VI in the Supplemental Material [23]). In addition to the two examples shown here, more propellers with frequency-induced reversal of propeller direction were found during the measurements (see the movies in the Supplemental Material [23]). While it might not be a surprise that randomly shaped micropropellers show deviations from the linear frequency-velocity relationship, those are often very small and negligible [21]. With this, we can already formulate some basic requirements for FIRSD (cf. Supplemental Material [23]): (i) the magnetic moment of such propellers has to be nonparallel and nonperpendicular to the principle axis of rotation [19]; (ii) the coupling matrix has to have nonvanishing elements of opposite sign for at least two directions, which are determined by the frequency-dependent axis of rotations. However, looking at more nonlinear cases and their mobility matrices might

enable us to draw a clearer map, which geometric features give contributions to such coupling, and therefore, to the reversal in swimming direction.

Recent progress in material synthesis, especially in 3D printing, already provides tools to potentially realize the production of experimentally found propeller geometries, and therefore, access to those alternative actuation strategies, without relying on filtering more randomly shaped propellers. Additionally, 3D printing may provide the possibility to structurally search the geometrical requirements for FIRSD. However, not every detail of the observed behavior is currently fully understood. In particular, the Euler angles, which describe the frequency-dependent orientation of the propellers, become time dependent after f_{so} and even though some suggestions have been proposed [17] to describe the interactions in this regime, it cannot explain the experimental data measured here. The option for future applications to be able to design propellers with distinct geometry that actively makes use of the changing axis of rotation or even the observed branching by actively determining it can be beneficial. They could either swim in the opposing direction and use the nonlinear regime to increase or decrease the effective coupling, and therefore, speed up or slow down the velocity, or simply overcome certain setup limitations in regard to the magnetic field. This will help to facilitate and speed up envisioned tasks and is a step toward user- and application-friendly micropropellers.

APENDIX A: ESTIMATION OF ROTATIONAL DRAG COEFFICIENTS AND MAGNETIC MOMENT

The magnitude of the magnetic moment and its angle toward the long axis of the chosen propeller coordinate system can be estimated with the experimentally measured characteristic frequencies f_{tw} and f_{so} (or the corresponding angular velocities ω_{tw} and ω_{so}) from the relevant drag or friction coefficients [16,17]. Therefore, an approximation of the propellers of either a cylinder [16,28] or an ellipsoid [17] is needed to analytically calculate the rotational drag coefficients. We chose to follow Ortega and de la Torre [28] and Ghosh *et al.* [16] since the cylindrical approximation seems rather fitting for our propeller shapes (cf. microscope images and the 3D reconstruction of the exemplary propellers in Fig. 1). The according drag coefficients for rotations around the short (γ_s) and long (γ_l) cylinder axes are as follows:

$$\gamma_s = \frac{\pi \eta l^3}{3 (\ln p + C_r^\perp)}, \quad (\text{A1})$$

$$\gamma_l = \frac{\pi \eta l^3 (1 + C_r^\parallel)}{0.96 p^2}, \quad (\text{A2})$$

with

$$C_r^\perp = -0.662 + \frac{0.917}{p} - \frac{0.100}{p^2}, \quad (\text{A3})$$

$$C_r^\parallel = \frac{0.677}{p} - \frac{0.183}{p^2}, \quad (\text{A4})$$

where $\eta = 8.9 \cdot 10^{-4}$ Pa s is the viscosity of water at 25°C and $p = l/d$ the ratio of the cylinder length l and its diameter d . Then the component of the magnetic moment fixed in the propeller along the long axis of the cylindrical approximation is

$$m_\parallel = \frac{\omega_{\text{tw}} \gamma_s}{B_0}, \quad (\text{A5})$$

and along the short axis

$$m_\perp = \gamma_l / B_0 \sqrt{\omega_{\text{so}}^2 - \omega_{\text{tw}}^2}. \quad (\text{A6})$$

The magnitude of the magnetization and its angle toward the long axis is

$$m = \sqrt{m_\parallel^2 + m_\perp^2}, \quad (\text{A7})$$

$$\Phi = \arctan m_\perp / m_\parallel. \quad (\text{A8})$$

Details on the reference frame of the cylindrical approximations and the azimuthal angle can be found in Fig. S5 in the Supplementary Material [23]. The values for the magnitude of the calculated magnetic moments of propellers 1 and 2 based on this approximation are shown in Table SI in the Supplemental Material [23], together with the quantities required for the calculation (magnetic field strength B_0 , characteristic propeller length l and diameter d , characteristic frequencies f_{tw} and f_{so}). The magnetic moment can additionally be compared with the magnetization saturation of the respective propeller assuming the same volume of ordered material (Table SI in the Supplemental Material [23]). To calculate the relative magnetization of the propellers, the saturation magnetization of maghemite [29] is needed ($M_s = 380$ kA m⁻¹)

$$m_{\text{sat}} = \pi L \frac{d^2}{4} M_s. \quad (\text{A9})$$

The relatively low magnetization values of 0.3% and 2% for propeller 1 and propeller 2, respectively, can be explained since the randomly shaped propellers consist of unordered maghemite nanoparticles.

APPENDIX: B. THEORETICAL FRAMEWORK FOR ARBITRARILY SHAPED MAGNETIC MICROPROPELLERS

Below the step-out frequency f_{so} , it is possible to describe the orientation of a propeller by the Euler angles

ϕ , θ , and ψ [41]. Their dependency on the frequency is determined by the propeller shape and the orientation of the magnetic moment with respect to this shape. The propeller geometry determines the mobility matrices: the rotational mobility matrix F , the translational mobility matrix G , and the coupling mobility matrix G [19]. A so-called center of hydrodynamic mobility can be found for every propeller geometry, where F is diagonal and G is symmetric, [19] similar to the center of the hydrodynamic reaction described by Happel and Brenner [42]. Together with the magnetic moment (magnitude, orientation) and the magnetic field strength, F determines the Euler angles, and therefore, the orientation of the propeller, depending on the applied frequency (cf. next paragraph on mobility matrices and Ref. [19]), whereas G couples the forced rotation to an effective translation of the propeller. According to Morozov *et al.*, [19] the resulting velocity $v = v^{(I)} + v^{(II)}$ along the axis of rotation can be written as the sum of the velocities coming from the diagonal and off-diagonal elements of G , v^I , and v^{II} , respectively,

$$\frac{v^{(I)}}{\omega l} = Ch_1 \sin^2 \psi \sin^2 \theta + Ch_2 \cos^2 \psi \sin^2 \theta + Ch_3 \cos^2 \theta, \quad (\text{B1})$$

$$\begin{aligned} \frac{v^{(II)}}{\omega l} &= Ch_{12} \sin 2\psi \sin^2 \theta + Ch_{13} \sin \psi \sin \theta \\ &\quad + Ch_{23} \cos \psi \sin 2\theta, \end{aligned} \quad (\text{B2})$$

with the length l of the propeller, the frequency of the external field $\omega = 2\pi f$, $Ch_i = G_{ii}/F_i$, and

$$Ch_{ij} = (1/2l) (G_{ij}/F_j + G_{ji}/F_i)$$

when $i \neq j$.

The advantage of the cylindrical approximation is that it also simplifies the calculation of the frequency-dependent Euler angles (see next paragraph). The transverse rotational isotropy of the propellers [19] basically implies a similar magnitude of the rotational mobility coefficients in the nonelongated directions, as it is given for an approximated cylinder: $F_1 = F_2 < F_3 = F_{\parallel}$. Therefore, using this approximation leaves only the elements of the mobility coupling matrix G_{ij} as unknown parameters [cf. Eqs. (B1) and (B2)], which are used as fitting parameters on the experimental data. However, the more ideal way would be to have access to the geometrical parameters G and F (e.g., through simulation of the reconstructed shape) and only use the magnetic moment and the characteristic frequencies as fit parameters, which is a work in progress. The fits were done with the NonlinearModelFit function of *Mathematica* [26].

1. Mobility matrices and Euler angles

The mobility matrices, determined by the geometry of the propeller, relate forces (\mathbf{F}) and torques (\mathbf{L}) with

velocities (\mathbf{U}) and rotation rates (Ω) for the low Reynolds number

$$\begin{pmatrix} \mathbf{U} \\ \Omega \end{pmatrix} = \begin{pmatrix} \varepsilon & G \\ G^\dagger & F \end{pmatrix} \begin{pmatrix} \mathbf{F} \\ \mathbf{L} \end{pmatrix}. \quad (\text{B3})$$

They have the following form in the center of hydrodynamic mobility [19], in which the axes are chosen here to be along the long and short axes of the approximated cylinder

$$\begin{pmatrix} F_1 & 0 & 0 \\ 0 & F_2 & 0 \\ 0 & 0 & F_3 \end{pmatrix}, \quad (\text{B4})$$

$$\begin{pmatrix} G_{11} & G_{12} & G_{13} \\ G_{12} & G_{22} & G_{23} \\ G_{13} & G_{23} & G_{33} \end{pmatrix}. \quad (\text{B5})$$

With the Euler angles ϕ , θ , and ψ describing the orientation of the propeller in the lab system (cf. Fig. S3.) [41] and the two angles α and Φ that describe the orientation of the magnetic moment in the propeller, the transverse rotational isotropy solution is accessible for the cylindrical approximation. $F_\perp = F_1 = F_2 < F_3 = F_{\parallel}$ then applies for the three diagonal elements of F , with F_1 and F_2 being the inverse rotational drag coefficients (γ_s^{-1}) of the cylinder rotating around the short axis and F_3 the inverse rotational drag coefficient around the long axis (γ_1^{-1}), respectively. In this case, the solution for the frequency dependent Euler angles can be given for the two synchronous regimes: tumbling solution before ω_{tw} [19]

$$\theta = \frac{\pi}{2}, \quad \psi = -\alpha, \quad \tilde{\phi} = -\Phi + \arccos \tilde{\omega}, \quad (\text{B6})$$

wobbling solution between ω_{tw} and ω_{so} [19]

$$\begin{aligned} \theta_1 &= \arcsin \frac{\cos \Phi}{\tilde{\omega}}, \quad \psi_1 = -\alpha - \arcsin \frac{\cos \theta_1 \tilde{\omega} F_\perp}{\sin \Phi F_{\parallel}}, \\ \tilde{\phi}_1 &= 0, \end{aligned} \quad (\text{B7})$$

$$\theta_2 = \pi - \theta_1, \quad \psi_2 = -2\alpha - \psi_1, \quad \tilde{\phi}_2 = 0, \quad (\text{B8})$$

with $\tilde{\omega} = \omega/m B_0 F_\perp$ and $\phi = \tilde{\phi} - \omega t$.

The second values for the wobbling solution correspond to the second-branch solution. Together with Eqs. (B1) and (B2), the frequency dependent velocity for the transverse rotational isotropic approximations is accessible [19].

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- [1] J. Liu, S. Z. Qiao, Q. H. Hu, and G. Q. Lu, Magnetic nanocomposites with mesoporous structures: Synthesis and applications, *Small* **7**, 425 (2011).
- [2] M. Colombo, S. Carregal-Romero, M. F. Casula, L. Gutierrez, M. P. Morales, I. B. Bohm, J. T. Heverhagen, D. Prosperti, and W. J. Parak, Biological applications of magnetic nanoparticles, *Chem. Soc. Rev.* **41**, 4306 (2012).
- [3] F. Qiu and B. J. Nelson, Magnetic helical micro- and nanorobots: Toward their biomedical applications, *Engineering* **1**, 21 (2015).
- [4] C. Bechinger, R. Di Leonardo, H. Lowen, C. Reichhardt, G. Volpe, and G. Volpe, Active particles in complex and crowded environments, *Rev. Mod. Phys.* **88**, 045006 (2016).
- [5] A. Ghosh and P. Fischer, Controlled propulsion of artificial magnetic nanostructured propellers, *Nano Lett.* **9**, 2243 (2009).
- [6] S. Tottori, L. Zhang, F. Qiu, K. K. Krawczyk, A. Franco-Obregon, and B. J. Nelson, Magnetic helical micromachines: Fabrication, controlled swimming, and cargo transport, *Adv. Mater.* **24**, 811 (2012).
- [7] D. Schamel, A. G. Mark, J. G. Gibbs, C. Miksch, K. I. Morozov, A. M. Leshansky, and P. Fischer, Nanopropellers and their actuation in complex viscoelastic media, *ACS Nano* **8**, 8794 (2014).
- [8] T. Li, J. Li, H. Zhang, X. Chang, W. Song, Y. Hu, G. Shao, E. Sandraz, G. Zhang, L. Li, and J. Wang, Magnetically propelled fish-like nanoswimmers, *Small* **12**, 6098 (2016).
- [9] P. J. Vach, N. Brun, M. Bennet, L. Bertinetti, M. Widdrat, J. Baumgartner, S. Klumpp, P. Fratzl, and D. Faivre, Selecting for function: Solution synthesis of magnetic nanopropellers, *Nano Lett.* **13**, 5373 (2013).
- [10] P. Fischer and A. Ghosh, Magnetically actuated propulsion at low Reynolds numbers: Towards nanoscale control, *Nanoscale* **3**, 557 (2011).
- [11] W. Gao, X. Feng, A. Pei, C. R. Kane, R. Tam, C. Hennessy, and J. Wang, Bioinspired helical microswimmers based on vascular plants, *Nano Lett.* **14**, 305 (2014).
- [12] J. Li, S. Sattayasamitsathit, R. Dong, W. Gao, R. Tam, X. Feng, S. Ai, and J. Wang, Template electrosynthesis of tailored-made helical nanoswimmers, *Nanoscale* **6**, 9415 (2014).
- [13] H. C. Fu, M. Jabbarzadeh, and F. Meshkati, Magnetization directions and geometries of helical microswimmers for linear velocity-frequency response, *Phys. Rev. E: Stat. Nonlin. Soft Matter Phys.* **91**, 043011 (2015).
- [14] P. J. Vach, S. Klumpp, and D. Faivre, Steering magnetic micropellers along independent trajectories, *J. Phys. D: Appl. Phys.* **49**, 065003 (2016).
- [15] A. Ghosh, D. Paria, H. J. Singh, P. L. Venugopalan, and A. Ghosh, Dynamical configurations and bistability of helical nanostructures under external torque, *Phys. Rev. E: Stat. Nonlin. Soft Matter Phys.* **86**, 031401 (2012).
- [16] A. Ghosh, P. Mandal, S. Karmakar, and A. Ghosh, Analytical theory and stability analysis of an elongated nanoscale object under external torque, *Phys. Chem. Chem. Phys.* **15**, 10817 (2013).
- [17] K. I. Morozov and A. M. Leshansky, The chiral magnetic nanomotors, *Nanoscale* **6**, 1580 (2014).
- [18] U. K. Cheang, F. Meshkati, D. Kim, M. J. Kim, and H. C. Fu, Minimal geometric requirements for micropropulsion via magnetic rotation, *Phys. Rev. E: Stat. Nonlin. Soft Matter Phys.* **90**, 033007 (2014).
- [19] K. I. Morozov, Y. Mirzae, O. Kenneth, and A. M. Leshansky, Dynamics of arbitrary shaped propellers driven by a rotating magnetic field, *Phys. Rev. Fluids* **2**, 044202 (2017).
- [20] Z. Zhang, H. Duan, S. Li, and Y. Lin, Assembly of magnetic nanospheres into one-dimensional nanostructured carbon hybrid materials, *Langmuir* **26**, 6676 (2010).
- [21] P. J. Vach, P. Fratzl, S. Klumpp, and D. Faivre, Fast magnetic micropellers with random shapes, *Nano Lett.* **15**, 7064 (2015).
- [22] M. Bennet, A. McCarthy, D. Fix, M. R. Edwards, F. Repp, P. Vach, J. W. Dunlop, M. Sitti, G. S. Buller, S. Klumpp, and D. Faivre, Influence of magnetic fields on magneto-aerotaxis, *PLoS ONE* **9**, e101150 (2014).
- [23] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevApplied.11.034039> for measurement details, further discussion of implications and more examples of FIRSD-propellers including video material showing this behavior.
- [24] A. C. Kak and M. Slaney, *Principles of Computerized Tomographic Imaging* (IEEE Press, New York, 1988).
- [25] J. Radon, *Berichte über die Verhandlungen der Königlich-Sächsischen Gesellschaft der Wissenschaften zu Leipzig*, (Mathematisch-Physische Klasse, Leipzig, 1917), Vol. 69, p. 262.
- [26] Mathematica, (Wolfram Research, Inc.) (2017).
- [27] L. Zhang, J. J. Abbott, L. Dong, K. E. Peyer, B. E. Kratochvil, H. Zhang, C. Bergeles, and B. J. Nelson, Characterizing the swimming properties of artificial bacterial flagella, *Nano Lett.* **9**, 3663 (2009).
- [28] A. Ortega and J. G. de la Torre, Hydrodynamic properties of rodlike and disklike particles in dilute solution, *J. Chem. Phys.* **119**, 9914 (2003).
- [29] C. J. Serna and M. P. Morales, *Maghemite (γ -Fe₂O₃): A Versatile Magnetic Colloidal Material* (Springer US, Boston, MA, 2004), Surface and Colloid Science.
- [30] A. W. Mahoney, N. D. Nelson, K. E. Peyer, B. J. Nelson, and J. J. Abbott, Behavior of rotating magnetic microrobots above the step-out frequency with application to control of multi-microrobot systems, *Appl. Phys. Lett.* **104**, 144101 (2014).
- [31] X. Wang, C. Hu, L. Schurz, C. De Marco, X. Chen, S. Pané, and B. J. Nelson, *Surface-Chemistry-Mediated Control of Individual Magnetic Helical Microswimmers in a Swarm* (ACS Nano, 2018), Vol. 12, p. 6210.
- [32] T. A. Howell, B. Osting, and J. J. Abbott, Sorting Rotating Micromachines by Variations in Their Magnetic Properties, *Phys. Rev. Appl.* **9**, 054021 (2018).
- [33] J. R. Gomez-Solano, S. Samin, C. Lozano, P. Ruedas-Batuecas, R. van Roij, and C. Bechinger, Tuning the motility and directionality of self-propelled colloids, *Sci. Rep.* **7**, 14891 (2017).

- [34] I. S. M. Khalil, A. F. Tabak, Y. Hamed, M. E. Mitwally, M. Tawakol, A. Klingner, and M. Sitti, Swimming back and forth using planar flagellar propulsion at low reynolds numbers, *Adv. Sci.* **5**, 1700461 (2017).
- [35] P. Katsamba and E. Lauga, Micro-Tug-of-War: A Selective Control Mechanism for Magnetic Swimmers, *Phys. Rev. Appl.* **5**, 064019 (2016).
- [36] J. Garcia-Torres, C. Calero, F. Sagues, I. Pagonabarraga, and P. Tierno, Magnetically tunable bidirectional locomotion of a self-assembled nanorod-sphere propeller, *Nat. Commun.* **9**, 1663 (2018).
- [37] M. Medina-Sanchez and O. G. Schmidt, Medical microbots need better imaging and control, *Nature* **545**, 406 (2017).
- [38] G. Kosa, P. Jakab, G. Szekely, and N. Hata, MRI driven magnetic microswimmers, *Biomed. Microdevices* **14**, 165 (2012).
- [39] N. Kumar, V. Verma, and L. Behera, Magnetic navigation and tracking of multiple ferromagnetic microrobots inside an arterial phantom setup for MRI guided drug therapy, *Biocybern. Biomed. Eng.* **37**, 347 (2017).
- [40] K. Bente, M. Weber, M. Graeser, T. F. Sattel, M. Erbe, and T. M. Buzug, Electronic field free line rotation and relaxation deconvolution in magnetic particle imaging, *IEEE Trans. Med. Imaging* **34**, 644 (2015).
- [41] L. D. Landau and E. M. Lifschitz, *Mechanik* (Akademie-Verlag GmbH, Berlin, 1970), Vol. 7.
- [42] J. Happel and H. Brenner, *Low Reynolds Number Hydrodynamics : With Special Applications to Particulate Media* (M. Nijhoff; Distributed by Kluwer Boston, The Hague; Boston Hingham, MA, USA, 1983), 1st ed., Mechanics of fluids and transport processes, 1.